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# Technical Note: Higher-order statistical moments and a procedure that detects potentially anomalous years as two alternative methods describing alterations in continuous environmental data

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Abstract. Statistics of central tendency and dispersion may not capture relevant or desired characteristics of the distribution of continuous phenomena and, thus, they may not adequately describe temporal patterns of change. Here, we present two methodological approaches that can help to identify temporal changes in environmental regimes. First, we use higher-order statistical moments (skewness and kurtosis) to examine potential changes of empirical distributions at decadal extents. Second, we adapt a statistical procedure combining a non-metric multidimensional scaling technique and higher density region plots to detect potentially anomalous years. We illustrate the use of these approaches by examining long-term stream temperature data from minimally and highly human-influenced streams. In particular, we contrast predictions about thermal regime responses to changing climates and human-related water uses. Using these methods, we effectively diagnose years with unusual thermal variability and patterns in variability through time, as well as spatial variability linked to regional and local factors that influence stream temperature. Our findings highlight the complexity of responses of thermal regimes of streams and reveal their differential vulnerability to climate warming and human-related water uses. The two approaches presented here can be applied with a variety of other continuous phenomena to address historical changes, extreme events, and their associated ecological responses.

## 1 Introduction

Environmental fluctuation is a fundamental feature that shapes ecological and evolutionary processes. Although empirical distributions of environmental data can be characterized in terms of the central tendency (or location), dispersion, and shape, most traditional statistical approaches are based on detecting changes in location and dispersion, and tend to oversimplify assumptions about temporal variation and shape. This issue is particularly troublesome for understanding the stationarity of temporally continuous phenomena and, thus, the detection of potential shifts in distributional properties beyond the location and dispersion. For instance, descriptors of location, such as mean, median or mode, may not be the most informative when extreme hydrological events are of primary attention (e.g., Chebana et al., 2012). In many regions, the future climate is expected to be characterized by increasing the frequency of extreme events (e.g., Jentsch et al., 2007; IPCC, 2012). Hence, the detection of changes in the shape of empirical distributions could be more informative than only using traditional descriptors of central tendency and dispersion (e.g., Shen et al., 2011; Donat and Alexander, 2012). More importantly, factors associated with changes in the shape of empirical distributions may have greater effects on species and ecosystems than do simple changes in location and dispersion (e.g., Colwell, 1974; Gaines and Denny, 1993; Thompson et al., 2013; Vasseur et al., 2014).

Here, we explore two approaches that identify and visualize temporal alterations in continuous environmental vari-



**Figure 1.** Conceptual diagram showing hypothesized shifts of distribution of water temperatures at both seasonal (upper panels) and annual (lower panels) scales in regulated (left panels) and unregulated (right panels) streams. In the upper panels examples of changes in skewness and kurtosis are shown for temperature distributions affected by stream regulation and a warming climate in a given season. For instance, in regulated streams the influence of the reservoir may reduce both extreme cold and warm temperatures confounding the effect from the climate (**a**) whereas less cold temperatures and an overall shift toward warming values may occur in unregulated streams (**b**). In the lower panels, we illustrate the use of N-MDS and HDR plots for detecting potentially anomalous years in regulated and unregulated streams (the shaded area represents a given coverage probability). Points located in the outer or the confidence region represent potentially anomalous years. For instance, in regulated streams individual years are more clustered because the reservoir may homogenize temperatures across years (**c**) whereas in unregulated streams individual years are less clustered due to more heterogeneous responses to the warming climate (**d**).

ables using thermal regimes of streams as an illustrative example. First, applying frequency analysis, we examine patterns of variability and long-term shifts in the shape of the empirical distribution of stream temperature using higherorder statistical moments (skewness and kurtosis) by season across decades. Second, we combine non-metric multidimensional scale ordination technique (N-MDS) and highest density region (HDR) plots to detect potentially anomalous years. To exemplify the utility of these approaches, we employ them to evaluate predictions about long-term responses of thermal regimes of streams to changing terrestrial climates and other human-related water uses (Fig. 1). Our main goal is to identify temporal changes of environmental regimes not captured by lower-order statistical moments. This is particularly relevant in streams because (1) global environmental change may affect water quality beyond the traditional lower-order statistical moments (e.g., Brock and Carpenter, 2012), and (2) ecosystems and organisms have been shown to be sensitive to such changes (e.g., Thompson et al., 2013; Vasseur et al., 2014).

# **1.1** Thermal regime of streams as an illustrative example

Temperature is a fundamental driver of ecosystem processes in freshwaters (Shelford, 1931; Fry, 1947; Magnuson et al., 1979; Vannote and Sweeney, 1980). Short-term (daily/weekly/monthly) descriptors of mean and maximum temperatures during summertime are frequently used for characterizations of thermal habitat availability and quality (McCullough et al., 2009), definitions of regulatory thresholds (Groom et al., 2011), and predictions about possible influences of climate change on streams (Mohseni et al., 2003; Mantua et al., 2010; Arismendi et al., 2013a, b). These simple descriptors can serve as useful first approximations but do not capture the full range of thermal conditions that the aquatic biota experience at daily, seasonal, or annual intervals (see Poole and Berman, 2001; Webb et al., 2008). Both human impacts and climate change have been shown to affect thermal regimes of streams at a variety of temporal scales (e.g., Steel and Lange, 2007; Arismendi et al., 2012, 2013a,

#### I. Arismendi et al.: Statistical moments and outliers

River	Start of water regulation	Gage ID	ID	Lat. N	Long. W	Elevation (m)	Watershed area (km <sup>2</sup> )	% of daily gaps
Fir Creek, OR	unregulated	14138870	site1	45.48	122.02	439	14.1	2.8%
SF Bull Run River, OR	unregulated	14139800	site2	45.45	122.11	302	39.9	2.0%
McRae Creek, OR	unregulated	TSMCRA	site3	44.26	22.17	840	5.9	3.5%
Lookout Creek, OR	unregulated	TSLOOK	site4	44.23	122.12	998	4.9	2.6%
Elk Creek, OR	unregulated	14338000	site5	42.68	122.74	455	334.1	5.2%
Clearwater River, ID	1971	13341050	site6	46.50	116.39	283	20658	4.0%
Bull Run River near Multnomah Falls, OR	1915*	14138850	site7	45.50	122.01	329	124.1	5.3%
NF Bull Run River, OR	1958	14138900	site8	45.49	122.04	323	21.6	2.6%
Rogue River near McLeod, OR	1977	14337600	site9	42.66	122.71	454	2,429	3.7%
Martis Creek near Truckee, CA	1971	10339400	site10	39.33	120.12	1747	103.4	6.5%

**Table 1.** Location and characteristics of unregulated (n = 5) and regulated (n = 5) streams at the gaging sites. Percent of daily gaps in the stream temperature time series from January 1979 to December 2009 used in this study.

\* regulation at times

b). For example, recent climate warming could lead to different responses of streams that may not be well described using average or maximum temperature values (Arismendi et al., 2012). Daily minimum stream temperatures in winter have warmed faster than daily maximum values during summer (Arismendi et al., 2013a; for air temperatures see Donat and Alexander, 2012). In human modified streams, seasonal shifts in stream temperatures and earlier warmer temperatures have been recorded following removal of riparian vegetation (Johnson and Jones, 2000). Simple threshold descriptors of central tendency (location) and dispersion cannot characterize these shifts.

Using higher-order statistical moments, we examine the question of whether the warming climate has led to shifts in the distribution of stream temperatures (Fig. 1a, b) or if all stream temperatures have warmed similarly and moved without any change in distribution or shape. In addition, we compare these potential shifts in the distribution of stream temperature between streams with unregulated and humanregulated streamflows. Using a technique that combines a non-metric multidimensional scaling procedure and higher density region plots, we address the question of whether potentially anomalous years are synoptically detected across streams types (regulated and unregulated) and examine if those potentially anomalous years represent the influence of regional climate or alternatively highlight the importance of local factors. Previous studies have shown that detecting changes in thermal regimes of streams is complex and the use of only traditional statistical approaches may oversimplify characterization of a variety of responses of ecological relevance (Arismendi et al., 2013a, b).

### 2 Material and methods

### 2.1 Study sites and time series

We selected long-term gage stations (US Geological Survey and US Forest Service) that monitored year-round daily stream temperature in Oregon, California, and Idaho (n =10; Table 1). The sites were chosen based on (1) availability of continuous daily records for at least 31 years (1 January 1979-31 December 2009) and (2) complete information for time series of daily minimum (min), mean (mean), and maximum (max) stream temperature for at least 93 % of the period of record. Half of the sites (n = 5) were located in unregulated streams (sites 1-5) and the other half were in regulated streams (sites 6-10). Regulated streams were those with reservoirs constructed before 1978, whereas unregulated streams had no reservoirs upstream during the entire time period of the study (1979-2009). Time series were carefully inspected and the percentage of daily missing records of each time series was less than 7% (Table 1). To ensure enough observations to adequately represent the tails of the respective distributions at a seasonal scale for analyses of higher-order statistical moments (i.e., winter: December-February; spring: March-May; summer: June-August; fall: September-November), we grouped and compared daily stream temperature data at each site among the three decades 1980-1989, 1990-1999, and 2000-2009. For the procedure that detects potentially anomalous years only (see below), we interpolated missing data following Arismendi et al. (2013a).

### 2.1.1 Higher-order statistical moments

To visualize and use a similar scale of stream temperatures across sites, we standardized time series of daily temperature values using a Z transformation as follows:

$$\mathrm{ST}_i = \frac{T_i - \mu}{\sigma},$$

where  $ST_i$  was the standardized temperature at day *i*,  $T_i$  was the actual temperature value at day *i* (°C),  $\mu$  was the mean and  $\sigma$  was the standard deviation of the respective time series considering the entire time period.

Although common estimators of skewness and kurtosis are unbiased only for normal distributions, these moments can be useful to describe changes in the shape of the distribution of environmental variables over long-term periods (see Shen et al., 2011; Donat and Alexander, 2012). Skewness addresses the question of whether or not a certain variable is symmetrically distributed around its mean value. With respect to temperature, positive skewness of the distribution (or skewed right) indicates colder conditions are more common (Fig. 1a) whereas negative skewness (skewed left) represents increasing prevalence of warmer conditions (Fig. 1b). Therefore, increases in the skewness over time could occur with increases in warm conditions, decreases in cold conditions, or both.

Kurtosis describes the structure of the distribution between the center and the tails representing the dispersion around its "shoulders". In other words, as the probability mass decreases the shoulders of a distribution kurtosis it may increase in either the center, the tails, or both, resulting in a rise in the peakedness, the tail weight, or both, and thus the dispersion of the distribution around its shoulders increases. The reference standard is zero, a normal distribution with excess kurtosis equal to kurtosis minus three (mesokurtic). A sharp peak in a distribution that is more extreme than a normal distribution (excess kurtosis exceeding zero) is represented by less dispersion in the observations over the tails (leptokurtic). Distributions with higher kurtosis tend to have "tails" that are more accentuated. Therefore, observations are spread more evenly throughout the tails. A distribution with tails more flattened than the normal distribution (excess kurtosis below zero) is described by higher frequencies spread across the tails (platykurtic). With respect to temperature, a leptokurtic distribution may indicate that average conditions are much more frequent with a lower proportion of both extreme cold and warm values (Fig. 1a). A platykurtic distribution represents a more evenly distributed distribution across all values with a higher proportion of both extreme cold and warm values (Fig. 1b). Therefore, increases in the kurtosis over time would occur with decreases in extreme conditions, increases of average conditions, or both.

Time series of environmental data are generally large data sets that often have missing values and errors (see Table 1). Although the data we selected had no more than 7 % of missing values, we accounted for potential bias inherent to incomplete time series or small sample sizes by using sample skewness (adjusted Fisher–Pearson standardized moment coefficient) and sample excess kurtosis (Joanes and Gill, 1998). The sample skewness and sample excess kurtosis are dimensionless and were estimated as follows:

Skewness = 
$$\frac{n}{(n-1)(n-2)} \sum_{i=1}^{n} \left(\frac{T_i - \mu}{\sigma}\right)^3$$
,

Kurtosis = 
$$\left[\frac{n(n+1)}{(n-1)(n-2)(n-3)}\sum_{i=1}^{n} \left(\frac{T_i - \mu}{\sigma}\right)^4\right] - \frac{3(n-1)^2}{(n-2)(n-3)},$$

where *n* represented the number of records of the time series,  $T_i$  was the temperature of the day *i*,  $\mu$  and  $\sigma$  the mean and standard deviation of the time series.

To define the status of the skewness for the stream temperature distribution in a particular season and decade, we followed Bulmer (1979) in defining three categories as follows: "highly skewed" (if skewness was < -1 or > 1), "moderately skewed" (if skewness was between -1 and -0.5 or between 0.5 and 1), and "symmetric" (if skewness was between -0.5 and 0.5). We used similar procedures to define the status of excess kurtosis. We defined five categories that included "negative kurtosis or platykurtic" (if kurtosis was < -1), "moderately platykurtic" (if kurtosis was between -0.5 and -1), "positive kurtosis or leptokurtic" (if kurtosis was < 1), and "moderately leptokurtic" (if kurtosis was between 0.5 and 1). Finally, if kurtosis was between -0.5 and 0.5, we considered the distribution as "mesokurtic".

There are some caveats inherent to time series analyses of environmental data that should be considered. First, error terms for sequential time periods may be influenced by serial correlation affecting the independence of data. For hypothesis testing, when serial correlation occurs, the goodness of fit is inflated and the estimated standard error is smaller than the true standard error. Serial correlation often occurs on short-term scales (hourly, daily, weekly) in analyses of environmental water quality (Helsel and Hirsch, 1992). In this study, we reduced the potential for serial correlation by using higher-order statistical moments aggregated over longer time periods that allowed for a contrast among decades. Second, it is important to note that temporal changes in skewness and kurtosis could be influenced by several factors. Because skewness and kurtosis are ratios based on lower-order moments, their temporal changes may be the result of changes in only the lower-order moments, changes in the higher-order moments, or both. Thus, we recommend the use of highermoment ratios in conjunction to the lower-order moments of central tendency and dispersion.

# 2.1.2 Statistical procedure to detect potentially anomalous years

We considered an entire year as one finite-dimensional observation (365 days of daily minimum stream temperature;



**Figure 2.** Density plots of standardized temperatures (1979–2009) by season (winter – blue line; spring – green line; summer – red line; fall – black line) in unregulated (left panel) and regulated (right panel) streams using time series of daily minimum.

see Sect. 2.1 above). Using N-MDS unconstrained ordination technique (Kruskal, 1964), we compared the similarity among years of the Euclidean distance of standardized temperatures for each day within a year across all years. The N-MDS analysis places each year in multivariate space in the most parsimonious arrangement (relative to each other) with no a priori hypotheses. Based on an iterative optimization procedure, we minimized a measure of disagreement or stress between their distances in 2-D using 999 random starts following the original MDSCAL algorithm (Kruskal, 1964; Clarke, 1993; Clarke and Gorley, 2006). The algorithm started with a random 2-D ordination of the years and it regressed the inter-year 2-D distances to the actual multidimensional distances (365-D). The distance between the *j*th and the *k*th year of the random 2-D ordination is denoted as  $d_{jk}$  whereas the corresponding multidimensional distance is denoted as  $D_{jk}$ . The algorithm performed a non-parametric rank-order regression using all the *j*th and the *k*th pairs of values. The goodness of fit of the regression was estimated using the Kruskal stress as follows:

Stress = 
$$\sqrt{\frac{\sum_{j} \sum_{k} \left( d_{jk} - \hat{d}_{jk} \right)^2}{\sum_{j} \sum_{k} d_{jk}^2}},$$

where  $\hat{d}_{jk}$  represented the predicted distance from the fitted regression between  $d_{jk}$  and  $D_{jk}$ . If  $d_{jk} = \hat{d}_{jk}$  for all the distances, the stress is zero. The algorithm used a steepest descent numerical optimization method to evaluate the stress of the proposed ordination and it stops when the stress converges to a minimum. Clarke (1993) suggests the following benchmarks: stress < 0.05 - excellent ordination; stress < 0.1- good ordination; stress < 0.2 - acceptable ordination; stress >0.2 – poor ordination. The resulting coordinates 1 and 2 from the resulted optimized 2-D plot provided a collective index of how unique a given year was (Fig. 1c, d). In N-MDS the order of the axes was arbitrary and the coordinates represented no meaningful absolute scales for the axis. Fundamental to this method was the relative distances between points; those with greater proximity indicated a higher degree of similarity, whereas more dissimilar points were positioned further apart. We performed the N-MDS analyses using the software Primer version 6.1.15 (Clarke, 1993; Clarke and Gorley, 2006).

We created a bivariate highly dimensional region (HDR) boxplot using the two coordinates of each point (year) from the 2-D plot from the N-MDS ordination (Hyndman, 1996). The HDR plot has been typically produced using the two main principal component scores from a traditional principal component analysis (PCA; Hyndman, 1996; Chebana et al., 2012). However, in this study, we modified this procedure taking the advantage of the higher flexibility and lack of assumptions of the N-MDS analysis (Everitt, 1978; Kenkel and Orloci, 1986) to provide the two coordinates needed to create the HDR plot. In the HDR plot, there are regions defined based on a probability coverage (e.g., 50, 90, or 95 %) where all points (years) within the probability coverage region have higher density estimates than any of the points outside the region (Fig. 1c, d). The outer region of the probability coverage region (Fig. 1c, d) is bounded by points representing potentially anomalous years. We created the HDR plots using the package hdrcde (Hyndman et al., 2012) in R version 2.15.1 (R Development Core Team, 2012).

Similarly to the higher-order statistical moments, there are some caveats that should be considered when using the procedure that detects potentially anomalous years. First, it is important to note that this procedure identified years outside of a confidence region, in other words, those years that fall in the tails of the distribution. Because the confidence region represented an overall pattern extracted from the available data, it was constrained by the length of the time series. Thus, potentially anomalous years located outside of the confidence region may not necessarily represent true outliers. In addition, when the ordination is poor (stress >0.2), interpreting the regularity/irregularity of the geometry of the confidence region should be done with caution. In our illustrative example, the regularity of the confidence region seen for regulated streams (Fig. 1c), when contrasted to unregulated sites, could be interpreted as influence of the reservoir in dampening the inter-annual variability of downstream water temperature.

### 3 Results and discussion

Empirical distributions of stream temperature were distinctive among seasons, and seasons were relatively similar across sites (Fig. 2). Temperature distributions during winter had high overlap with those during spring. Winter had the narrowest range and, as would be expected, the highest frequency of observations occurring at colder standardized temperature categories (-1.3, -0.7). The second highest proportion of observations occurred in different seasons for regulated and unregulated sites: during spring in unregulated streams and during summer at four of the five regulated sites. This shift of frequency could be due to warming and release of the warmer water from the upstream reservoirs. Fall distributions showed the broadest range, with a similar proportion for a number of temperature values.

Changes in the shape of empirical distributions among seasons over decades were not immediately evident. However, the values of skewness or types of kurtosis captured these decadal changes in cases when lower-order statistical moments (average and standard deviation) did not show marked differences (e.g., site1 during fall and spring in Fig. 3; Tables 2 and 3; see also differences among decades at site1 during summer in Fig. S1 in the Supplement). The utility of combining skewness and kurtosis to detect changes in distributional shapes over time can be illustrated using site3 during winter and spring (Tables 2 and 3 and S1–S6). At this site, there was a shift across decades from symmetric towards a negatively skewed distribution in winter and from symmetric towards positively skewed in spring (Table 2), as well as from mesokurtic towards a leptokurtic distribution in both winter and spring (Table 3). Overall, in most unregulated sites, the type of kurtosis differed among decades during winter and summer (Tables 3 and S4-S6). Winter and summer frequently had negatively skewed distributions whereas spring generally had positively skewed distributions or those with little change across decades, except for site3 (Tables 2 and S1-S3).

Decadal changes in both skewness and kurtosis during winter and summer at unregulated sites suggest that the probability mass moved from its shoulders into warmer values at its center, but maintained the tail weight of the extreme cold temperature values (Figs. 3 and S1; Tables 2, 3 and S1–S6). However, in spring the probability mass diminished around its shoulders, likely due to decreases in the frequency of extreme cold temperature values. Hence, higher-order statistical moments may help in describing the complexity of temporal changes in stream temperature among seasons and highlight how shifts may occur at different portions of the distribution (e.g., extreme cold, average, or warm conditions) or among streams.



**Figure 3.** Examples of (a) density plots of standardized temperatures by decade (period 1980–1989 dashed line; period 1990–1999 grey line; period 2000–2009 solid color line) and season using time series of daily minimum in an unregulated (site1) and a regulated (site6) stream. In the lower panel (b) central tendency statistics (average  $\pm$  SD) for each decade and season (winter – blue; spring – green; summer – red; fall – black) are also included. See results for all sites in Figs. S1 and S2.

In regulated sites, we observed shifts toward colder temperatures (e.g., site6 and site9 during summer and fall in Figs. 3 and S2), suggesting local influences of water regulation may dominate the impacts from warming climate. This is illustrated by the mixed patterns of skewness and kurtosis due to climate and water regulation, especially during spring, winter, and summer (Tables 2 and 3; Figs. 3 and S2). In particular, in spring, patterns of skewness in regulated sites were similar to unregulated sites, whereas patterns of kurtosis were in opposite directions (more platykurtic in regulated sites). This can be explained by the water discharged from reservoirs in spring that could be a mix of the cool inflows to the reservoir, the deep, colder water stored in the reservoir over the winter, and the accelerated warming of the exposed surface of the reservoir. Patterns of skewness and kurtosis seen in regulated sites also highlight the influences of site-dependent water management coupled with climatic influences. This is exemplified by the skewness of site7 and site8 compared to site9 and site10 in fall, winter, and spring (Table 2) and the high variability of the value of skewness among sites in summer.

Increased understanding of the shape of empirical distributions by season or by year will help researchers and resource managers evaluate potential impacts of shifting environmental regimes on organisms and processes across a range of disturbance types. Empirical distributions are a simple, but comprehensive way to examine high-frequency measurements that include the full range of values. Higher-order statistical moments provide useful information to characterize and compare environmental regimes and can show which seasons are most responsive to disturbances. The use of higher-order moments could help improve predictive models of climate change impacts in streams by incorporating full environmental regimes into scenarios rather than only using descriptors of central tendency and dispersion from summertime.

The technique for detection of potentially anomalous years used here was able to incorporate all daily data to provide a simple but comprehensive comparison of environmental regimes among years. We were able to characterize whole

**Table 2.** Magnitude and direction of the value of skewness in probability distributions of daily minimum stream temperature by season and decade at unregulated (sites 1-5) and regulated (sites 6-10) streams. Symmetric distributions are not shown. m: moderately skewed; h: highly skewed; (–): negatively skewed; (+): positively skewed (see Tables S1–S3 for more details).

		Season/time period											
		fall			winter			spring			summer		
Site type	Site ID	1980– 1989	1990– 1999	2000– 2009	1980– 1989	1990– 1999	2000– 2009	1980– 1989	1990– 1999	2000– 2009	1980– 1989	1990– 1999	2000– 2009
unregulated (1-5)	site1 site2 site3 site4 site5				m(-)	m(-) m(-)	m(-) m(-) m(-)	m(+) m(+) h(+) m(+)	m(+) m(+) m(+) m(+) h(+)	m(+) m(+) h(+) h(+) m(+)	m(-) m(-) m(-)	m(-) m(-)	m(-) m(-) m(-)
regulated (6-10)	site6 site7 site8 site9 site10	m(-) m(+)	m(-) m(+)	m(+)	m(+)	m(-) m(+) m(+)		m(+) m(+) m(+)	m(+)	m(+) m(+)	h()	m(-)	m(+) m(-) h(-) m(+)

**Table 3.** Types of kurtosis of probability distributions of daily minimum stream temperature by season and decade at unregulated and regulated sites.  $\leftrightarrow \leftrightarrow$ : platykurtic;  $\leftrightarrow$ : moderately platykurtic;  $\uparrow$ : leptokurtic, and  $\uparrow$ : moderately leptokurtic. Mesokurtic distributions are not shown (see Tables S4–S6 for more details).

		Season/time period											
		fall			winter			spring			summer		
Site type	Site ID	1980– 1989	1990– 1999	2000– 2009	1980– 1989	1990– 1999	2000– 2009	1980– 1989	1990– 1999	2000– 2009	1980– 1989	1990– 1999	2000– 2009
unregulated (1-5)	site1 site2 site3 site4	$\leftrightarrow$	$\leftrightarrow$	$ \begin{array}{c} \leftrightarrow \\ \leftrightarrow \\ \leftrightarrow \\ \leftrightarrow \\ \leftrightarrow \end{array} $	\$	\$	\$ \$ \$\$	\$\$ \$\$		\$ ^^	$\leftrightarrow$	$\leftrightarrow$	\$
	site5	$\leftrightarrow$	$\leftrightarrow$	$\overleftrightarrow$	$\leftrightarrow$			**	\$	** \$\$		\$	*
regulated (6-10)	site6	$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$								$\leftrightarrow$	\$
	site7	$\leftrightarrow$		$\leftrightarrow$				\$\$					
	site8	\$		$\leftrightarrow$	\$		\$		$\leftrightarrow$			\$	\$\$
	site9			$\leftrightarrow$	\$			$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$	
	site10	$\leftrightarrow \leftrightarrow$	$\leftrightarrow \leftrightarrow$	$\leftrightarrow \leftrightarrow$	$\leftrightarrow$	\$\$		$\leftrightarrow \leftrightarrow$	$\leftrightarrow$	$\leftrightarrow$	\$\$	\$	\$

year responses and identify where regional climatic or hydrologic trends dominated versus where local influences distinctively influenced stream temperature. For example, year 1992 was identified as potentially anomalous at three unregulated sites (or four at 90 % CI) and at two regulated sites (or four at 90 % CI), and identified that across the region, the majority of stream temperatures were being influenced (Figs. 4 and 5; Table S7). Stream temperatures in years 1987 and 2008 were less synchronous across the region, but regulated and unregulated sites located in the same watershed (site2, site7, and site8 in Tables 1 and S7; Figs. 4 and 5) shared similar potentially anomalous years. We also observed site-specific anomalous years, suggesting that more local conditions of watersheds influenced stream temperature (e.g., Arismendi et al., 2012). Indeed, sites located close to one another (site3 and site4 in Tables 1 and S7; Fig. 4) did not necessarily share all potentially anomalous years, suggesting that local drivers were more influential than regional climate forces during those years. Hence, the procedure for detection of potentially anomalous years used here may be useful to evaluate and contrast the vulnerability of streams to regional or local climate changes by characterizing years with anomalous conditions.

The technique that detects potentially anomalous years identified years with differences in either magnitude or timing of events (Figs. 4 and 5) and mapped these differences



**Figure 4.** Bivariate HDR boxplots (left panel) and standardized daily temperature distribution (right panel) in unregulated streams using annual time series of daily minimum. The dark and light grey regions show the 50, 90, and 95 % coverage probabilities. The symbols outside the grey regions and darker lines represent potentially anomalous years. Examples of years between 90 and 95 % of the coverage probability were italicized.

within the ordination plot. For example, years 1992 and 1987 were potentially anomalous likely due the magnitude of warming throughout the year. At other sites, such as site3, site4 and site5 (Fig. 4), the potentially anomalous years were most likely due to increased temperatures in seasons other than summertime, and not related to higher summertime temperatures. Years 1992 and 2008 plotted at the opposite extremes of the ordination plot for site1, site2 and site7 (Figs. 4 and 5); see also years 1982–1983 and 1986–1987 for site3. These years contained warm and cold conditions, respectively, and likely influenced the shape of the confidence region (Figs. 4 and 5; Table S7). Interestingly, we observed that the confidence region for unregulated sites (Fig. 4) appeared

to be more irregularly shaped than regulated sites (Fig. 5), which suggests that stream regulation may tightly cluster and homogenize temperature values across years (e.g., Fig. 1c, d). Further attention on the interpretation of the geometry of a confidence region may be useful to contrast purely climatic from human influences on streams.

There are some considerations when detecting potential changes in continuous environmental phenomena that are inherent to time series analysis, including the length, timing, and quality of the time series as well as the type of the driver that is investigated as responsible for such change. Often, the detection of shifts in time series of environmental data is affected by the amount of censored data that lim-



**Figure 5.** Bivariate HDR boxplots (left panel) and standardized daily temperature distribution (right panel) in regulated streams using annual time series of daily minimum. The dark and light grey regions show the 50, 90, and 95% coverage probabilities. The symbols outside the grey regions and darker lines represent potentially anomalous years. Examples of years between 90 and 95% of the coverage probability were italicized.

its the length and timing of the time series (e.g., Arismendi et al., 2012). There are uncertainties regarding the importance of regional drivers and the representativeness of sites (e.g., complex mountain terrain) and periods of record (e.g., ENSO, and PDO climatic oscillations). Lastly, the type of climatic influences may affect the magnitude and duration of the responses resulting in short-term abrupt shifts (e.g., extreme climatic events), persistent long-term shifts (e.g., climate change), or a more complex combination of them (e.g., regime shifts; Brock and Carpenter, 2012).

#### 4 Summary and conclusions

Here we show the utility of using higher-order statistical moments and a procedure that detects potentially anomalous years as complementary approaches to identify temporal changes in environmental regimes and evaluate whether these changes are consistent across years and sites. Stream ecosystems are exposed to multiple climatic and nonclimatic forces which may differentially affect their hydrological regimes (e.g., temperature and streamflow). In particular, we show that potential timing and magnitude of responses of stream temperature to recent climate warming and other human-related impacts may vary among seasons,

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years, and across sites. Statistics of central tendency and dispersion may or may not distinguish between thermal regimes or characterize changes to thermal regimes, which could be relevant to understanding their ecological and management implications. In addition, when only single metrics are used to describe environmental regimes, they have to be selected carefully. Often, selection involves simplification resulting in the compression or loss of information (e.g., Arismendi et al., 2013a). By examining the whole empirical distribution and multiple moments, we can provide a better characterization of shifts over time or following disturbances than simple thresholds or descriptors.

In conclusion, our two approaches complement traditional summary statistics by helping to characterize continuous environmental regimes across seasons and years, which we illustrate using stream temperatures in unregulated and regulated sites as an example. Although we did not include a broad range of stream types, they were sufficiently different to demonstrate the utility of the two approaches. These two approaches are transferable to many types of continuous environmental variables and regions and suitable for examining seasonal and annual responses as well as climate or humanrelated influences (e.g., for streamflow see Chebana et al., 2012; for air temperature see Shen et al., 2011). These analyses will be useful to characterize the strength of the resilience of regimes and to identify how regimes of continuous phenomena have changed in the past and may respond in the future.

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