

## AN ABSTRACT OF THE THESIS OF

Enrique Arriola for the degree of Doctor of Philosophy in Chemical Engineering  
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Title: Residence Time Distribution of Solids in Staged Spouted Beds.

Redacted for privacy

Abstract approved: \_\_\_\_\_

 Goran Jovanovic

A new type of multistage spouted bed is developed for a counterflow of gas and solids. A one-stage and a three-stage units are studied, the RTD's of solids therein are measured, and a solids flow compartment model is developed to represent obtained family of RTD curves.

Colored particles, identical to those used as a bed material ( $D_{ave} = 1.78$  mm,  $\rho_s = 2.64$  grams/cm<sup>3</sup>), are adopted as tracer particles in impulse-response experiments. The RTD of solids is measured in both one-stage and three-stage columns of spouted beds with draft tubes. The hold-up of particles in each stage is self controlled by a specially designed feature of the bed. The recirculation of solids within each stage is controlled by the flow of gas (air) through the draft tube. The solids are continuously withdrawn from the system through a modified "L-valve" which operates with oscillating air pressure for a more uniform throughflow of solid material.

A simple compartment model consisting of a plug-flow vessel, with dead space, in series with a continuous-stirred-tank vessel is developed to represent the flow of solids through a single spouted bed vessel:

$$E(t) = \begin{cases} 0 & \text{for } t < \tau_p \\ \frac{1}{\tau_M} \exp\left[\frac{-(t - \tau_p)}{\tau_M}\right] & \text{for } t \geq \tau_p \end{cases}$$

A self-convolution of the above model/equation yields the residence time distribution expression for the three-stage column,

$$E(t) = \begin{cases} 0 & \text{for } t < 3\tau_{pi} \\ \frac{(t - 3\tau_{pi})^2}{2\tau_{Mi}^3} \exp\left[\frac{-(t - 3\tau_{pi})}{\tau_{Mi}}\right] & \text{for } t \geq 3\tau_{pi} \end{cases}$$

System parameters  $\tau_p$  and  $\tau_M$  (or  $\tau_{pi}$  and  $\tau_{Mi}$ ) are correlated to operating variables (solid flow rate,  $S_o$ , gas flow rate, GFR, and recirculation time,  $t_R$ ) by,

$$\frac{\tau_p}{\tau} = \alpha \exp[-\beta(t_{Ro} - t_R)]$$

where  $\alpha$  and  $\beta$  are functions of the solid flow rate,  $S_o$ . This correlation is tested with an independent set of data. The correlation represents data well in the solid flow range of 6.0 to 17.0 g/sec, and in the gas flow range of 3.5 to 3.7 lit/sec.

This particular multistage spouted bed design has clear operating and scale-up advantages over previous reported designs. It can tolerate a wide range of solid flow, it starts operating without difficulties, and when shut down it empties readily. The countercurrent system, also can be easily transformed in a cross-current multistage system.

# Residence Time Distribution of Solids in Staged Spouted Beds

by

Enrique Arriola

A THESIS

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degree of

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Doctor of Philosophy thesis of Enrique Arriola presented on September 15, 1997

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Major Professor, representing Chemical Engineering

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Chair of Chemical Engineering Department

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Dean of Graduate School //

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Enrique Arriola, Author

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**Enrique Arriola Guevara**

# TABLE OF CONTENTS

|                                                      | <u>Page</u> |
|------------------------------------------------------|-------------|
| <b>1. INTRODUCTION</b>                               | <b>1</b>    |
| <b>2. BACKGROUND AND LITERATURE SURVEY</b>           | <b>5</b>    |
| 2.1 The Spouted Bed                                  | 5           |
| 2.2 Spouting And Fluidization                        | 7           |
| 2.3 Multistage Spouting                              | 11          |
| 2.4 Modifications To The Spouting Technique          | 13          |
| 2.5 The RTD Approach To Modeling Flow In Mobile Beds | 14          |
| 2.5.1 Tanks-In-Series Model                          | 15          |
| 2.5.2 Compartment Models                             | 16          |
| 2.6 Research With Multistage Units In Series         | 17          |
| <b>3. MODEL DEVELOPMENT</b>                          | <b>23</b>   |
| 3.1 Introduction                                     | 23          |
| 3.2 Tank-In-Series Model                             | 23          |
| 3.3 Compartment Model                                | 26          |
| <b>4. EXPERIMENTAL EQUIPMENT DESIGN</b>              | <b>32</b>   |
| 4.1 Geometry Of The Vessels                          | 32          |
| 4.2 Interconnection Of The Stages                    | 34          |
| 4.3 Feeding/Discharging. L-valve                     | 36          |

## TABLE OF CONTENTS (Continued)

|                                                        | <u>Page</u> |
|--------------------------------------------------------|-------------|
| <b>5. EXPERIMENTAL MEASUREMENTS AND PROCEDURES</b>     | <b>39</b>   |
| 5.1 Spouted Bed Material                               | 39          |
| 5.2 Tracer                                             | 39          |
| 5.3 Experimental procedures                            | 40          |
| 5.3.1 Preliminary Steps                                | 41          |
| 5.3.2 Running The RTD Experiment                       | 42          |
| 5.3.3 Analytical Steps                                 | 42          |
| 5.4 Experimental Plan                                  | 43          |
| 5.5 Results                                            | 51          |
| <b>6. ANALYSIS AND DISCUSSION OF EXPERIMENTAL DATA</b> | <b>64</b>   |
| 6.1 Introduction                                       | 64          |
| 6.2 Single-Stage Unit                                  | 66          |
| 6.3 Three-Stage Column                                 | 80          |
| 6.4 Discussion                                         | 93          |
| <b>7. CONCLUSIONS AND RECOMMENDATIONS</b>              | <b>94</b>   |
| <b>BIBLIOGRAPHY</b>                                    | <b>96</b>   |
| <b>APPENDICES</b>                                      | <b>106</b>  |
| APPENDIX A Documentation For Single-stage Unit Model   | 107         |
| APPENDIX B Documentation For Multistage Unit Model     | 109         |
| APPENDIX C Optimization Routine                        | 111         |
| APPENDIX D Experimental Data                           | 114         |
| APPENDIX E Identical Stages Test                       | 158         |

## **LIST OF FIGURES**

| <b><u>Figure</u></b>                                                                                                       | <b><u>Page</u></b> |
|----------------------------------------------------------------------------------------------------------------------------|--------------------|
| 2.1      Schematic diagram of a spouted bed                                                                                | 5                  |
| 2.2      Phase diagram for semicoke (particle diameter range from 1mm to 5mm). Adapted from Dumitrescu and Ionescu (1967)  | 6                  |
| 2.3      The Geldart classification of particles for air at ambient conditions. Adapted from Levenspiel (1991)             | 8                  |
| 2.4      Long contacting time spouted bed                                                                                  | 10                 |
| 2.5      Flow of spouting gas in parallel                                                                                  | 11                 |
| 2.6      Flow of spouting gas in series                                                                                    | 12                 |
| 2.7      Modifications and variations to the spouting technique<br>(a) Spouted bed with draft tube<br>(b) Slot spouted bed | 14                 |
| 2.8      (a) Twin continuous stirred tank model by Chatterje (1970)<br>(b) Circulation models by Mann and Crosby (1972)    | 16                 |
| 2.9      Parallel spouted beds in a batch process. Adapted from Paterson, Grace and Watkinson (1983)                       | 18                 |
| 2.10     The multistage column used by Malek and Walsh (1966)                                                              | 20                 |
| 2.11     Multistage spouted bed test facility as used by Van Weert and Van Hasselt (1997)                                  | 21                 |
| 3.1      Graphical representation of the tank-in-series model                                                              | 24                 |
| 3.2      Tank-in-series responses to a pulse tracer input for different numbers of tanks. Adapted from Levenspiel (1993)   | 25                 |
| 3.3 $E(\theta)$ curve obtained from measured concentrations                                                                | 26                 |
| 3.4 $E(t)$ curve for plug flow and ideal mixed tank in series. Adapted from Levenspiel (1993)                              | 27                 |

## **LIST OF FIGURES (Continued)**

| <b><u>Figure</u></b> |                                                                                                                                       | <b><u>Page</u></b> |
|----------------------|---------------------------------------------------------------------------------------------------------------------------------------|--------------------|
| 3.5                  | E(t) curve for plug flow, with dead space, and ideal mixed tank in series. Adapted from Levenspiel (1993)                             | 28                 |
| 3.6                  | E(t) curve for plug flow, with dead space, followed by ideal mixed tank in series, with recirculation. Adapted from Levenspiel (1993) | 28                 |
| 3.7                  | Observed flow regions                                                                                                                 | 30                 |
| 3.8                  | A possible model for the data shown on Figure 3.3                                                                                     | 30                 |
| 3.9                  | A possible model for a three-stage column of spouted beds.                                                                            | 31                 |
| 4.1                  | Diagram of the designed vessel showing input/output streams of air and solids                                                         | 33                 |
| 4.2                  | Diagram of the designed vessel showing important measurements in cm                                                                   | 34                 |
| 4.3                  | Three-stage spouted bed configuration                                                                                                 | 35                 |
| 4.4                  | Observed solid circulation in a single-stage unit                                                                                     | 37                 |
| 4.5                  | Diagram of the modified L-valve                                                                                                       | 38                 |
| 5.1                  | Experimental set up for the RTD of solids in a single-stage unit                                                                      | 41                 |
| 5.2                  | Diagram showing how tracer particles are introduced into the system                                                                   | 43                 |
| 5.3                  | Pressure drop for an empty column                                                                                                     | 44                 |
| 5.4                  | Pressure drop for a SFR = 2 g/s                                                                                                       | 44                 |
| 5.5                  | Pressure drop for a SFR = 7 g/s                                                                                                       | 45                 |
| 5.6                  | Pressure drop for a SFR = 17 g/s                                                                                                      | 45                 |
| 5.7                  | Total pressure drop for different solid flow rates                                                                                    | 46                 |
| 5.8                  | Modified L-valve behavior for flow rate of 0.55 lit/sec of pushing gas                                                                | 47                 |

## **LIST OF FIGURES (Continued)**

| <b><u>Figure</u></b> |                                                     | <b><u>Page</u></b> |
|----------------------|-----------------------------------------------------|--------------------|
| 5.9                  | Recirculation rate of solids                        | 48                 |
| 5.10                 | C(t) curve of experiment #1030 (single-stage unit)  | 51                 |
| 5.11                 | C(t) curve of experiment #1031 (single-stage unit)  | 52                 |
| 5.12                 | C(t) curve of experiment #1032 (single-stage unit)  | 52                 |
| 5.13                 | C(t) curve of experiment #1033 (single-stage unit)  | 53                 |
| 5.14                 | C(t) curve of experiment #1034 (single-stage unit)  | 53                 |
| 5.15                 | C(t) curve of experiment #1035 (single-stage unit)  | 54                 |
| 5.16                 | C(t) curve of experiment #1036 (single-stage unit)  | 54                 |
| 5.17                 | C(t) curve of experiment #1037 (single-stage unit)  | 55                 |
| 5.18                 | C(t) curve of experiment #1038 (single-stage unit)  | 55                 |
| 5.19                 | C(t) curve of experiment #1039 (single-stage unit)  | 56                 |
| 5.20                 | C(t) curve of experiment #1040 (single-stage unit)  | 56                 |
| 5.21                 | C(t) curve of experiment #1041 (single-stage unit)  | 57                 |
| 5.22                 | C(t) curve of experiment #1042 (single-stage unit)  | 57                 |
| 5.23                 | C(t) curve of experiment #1043 (single-stage unit)  | 58                 |
| 5.24                 | C(t) curve of experiment #2000 (three-stage column) | 58                 |
| 5.25                 | C(t) curve of experiment #2001 (three-stage column) | 59                 |
| 5.26                 | C(t) curve of experiment #2002 (three-stage column) | 59                 |
| 5.27                 | C(t) curve of experiment #2003 (three-stage column) | 60                 |
| 5.28                 | C(t) curve of experiment #2004 (three-stage column) | 60                 |



## **LIST OF FIGURES (Continued)**

| <b><u>Figure</u></b> |                                                       | <b><u>Page</u></b> |
|----------------------|-------------------------------------------------------|--------------------|
| 5.29                 | C(t) curve of experiment #2005 (three-stage column)   | 61                 |
| 5.30                 | C(t) curve of experiment #2006 (three-stage column)   | 61                 |
| 5.31                 | C(t) curve of experiment #2007 (three-stage column)   | 62                 |
| 5.32                 | C(t) curve of experiment #2008 (three-stage column)   | 62                 |
| 5.33                 | C(t) curve of experiment #2009 (three-stage column)   | 63                 |
| 6.1                  | Compartment model for the single-stage unit           | 67                 |
| 6.2                  | E(t) modeling of experiment #1030 (single-stage unit) | 68                 |
| 6.3                  | E(t) modeling of experiment #1031 (single-stage unit) | 68                 |
| 6.4                  | E(t) modeling of experiment #1032 (single-stage unit) | 69                 |
| 6.5                  | E(t) modeling of experiment #1033 (single-stage unit) | 69                 |
| 6.6                  | E(t) modeling of experiment #1034 (single-stage unit) | 70                 |
| 6.7                  | E(t) modeling of experiment #1035 (single-stage unit) | 70                 |
| 6.8                  | E(t) modeling of experiment #1036 (single-stage unit) | 71                 |
| 6.9                  | E(t) modeling of experiment #1037 (single-stage unit) | 71                 |
| 6.10                 | E(t) modeling of experiment #1038 (single-stage unit) | 72                 |
| 6.11                 | E(t) modeling of experiment #1039 (single-stage unit) | 72                 |
| 6.12                 | E(t) modeling of experiment #1040 (single-stage unit) | 73                 |
| 6.13                 | E(t) modeling of experiment #1041 (single-stage unit) | 73                 |
| 6.14                 | E(t) modeling of experiment #1042 (single-stage unit) | 74                 |
| 6.15                 | E(t) modeling of experiment #1043 (single-stage unit) | 74                 |

## **LIST OF FIGURES (Continued)**

| <b><u>Figure</u></b> |                                                                         | <b><u>Page</u></b> |
|----------------------|-------------------------------------------------------------------------|--------------------|
| 6.16                 | Plug and mixed flow behavior for the single-stage unit                  | 75                 |
| 6.17                 | Plug, mixed flow and dead space for the single-stage unit               | 75                 |
| 6.18                 | Recirculation time of solids                                            | 76                 |
| 6.19                 | Correlation for $\tau_p/\tau$ , “m” dependency on solid flow rate $S_o$ | 78                 |
| 6.20                 | Correlation for $\tau_p/\tau$ , “b” dependency on solid flow rate $S_o$ | 79                 |
| 6.21                 | Compartment model for the three-stage column                            | 80                 |
| 6.22                 | E(t) modeling of experiment #2000 (Three-stage column)                  | 81                 |
| 6.23                 | E(t) modeling of experiment #2001 (Three-stage column)                  | 81                 |
| 6.24                 | E(t) modeling of experiment #2002 (Three-stage column)                  | 82                 |
| 6.25                 | E(t) modeling of experiment #2003 (Three-stage column)                  | 82                 |
| 6.26                 | E(t) modeling of experiment #2004 (Three-stage column)                  | 83                 |
| 6.27                 | E(t) modeling of experiment #2005 (Three-stage column)                  | 83                 |
| 6.28                 | E(t) modeling of experiment #2006 (Three-stage column)                  | 84                 |
| 6.29                 | E(t) modeling of experiment #2007 (Three-stage column)                  | 84                 |
| 6.30                 | E(t) modeling of experiment #2008 (Three-stage column)                  | 85                 |
| 6.31                 | E(t) modeling of experiment #2009 (Three-stage column)                  | 85                 |
| 6.32                 | Plug and mixed flow behavior for the three-stage column                 | 86                 |
| 6.33                 | Plug, mixed flow and dead space for the three-stage column              | 86                 |
| 6.34                 | Model-parameters. Experimental and model predictions                    | 87                 |
| 6.35                 | Model-parameters. Experimental and model predictions                    | 88                 |

## **LIST OF FIGURES (Continued)**

| <b><u>Figure</u></b> |                                                        | <b><u>Page</u></b> |
|----------------------|--------------------------------------------------------|--------------------|
| 6.36                 | Measured versus predicted parameters                   | 88                 |
| 6.37                 | E(t) modeling of experiment #2000 (three-stage column) | 89                 |
| 6.38                 | E(t) modeling of experiment #2001 (three-stage column) | 89                 |
| 6.39                 | E(t) modeling of experiment #2002 (three-stage column) | 90                 |
| 6.40                 | E(t) modeling of experiment #2003 (three-stage column) | 90                 |
| 6.41                 | E(t) modeling of experiment #2004 (three-stage column) | 91                 |
| 6.42                 | E(t) modeling of experiment #2005 (three-stage column) | 91                 |
| 6.43                 | E(t) modeling of experiment #2006 (three-stage column) | 92                 |
| 6.44                 | E(t) modeling of experiment #2007 (three-stage column) | 92                 |
| 6.45                 | E(t) modeling of experiment #2009 (three-stage column) | 93                 |

## **LIST OF TABLES**

| <b><u>Table</u></b> |                                                                               | <b><u>Page</u></b> |
|---------------------|-------------------------------------------------------------------------------|--------------------|
| 2.1                 | Comparison between spouting and fluidization characteristics                  | 9                  |
| 5.1                 | Combinations of gas and solids flow rates used in the single-stage bed unit.  | 49                 |
| 5.2                 | Combinations of gas and solids flow rates used in the three-stage bed column. | 50                 |
| 6.1                 | Correlations to predict $\tau_p/\tau$ in the single-stage unit                | 77                 |

## **LIST OF APPENDIX FIGURES**

| <b><u>Figure</u></b> |                                                             | <b><u>Page</u></b> |
|----------------------|-------------------------------------------------------------|--------------------|
| C.1                  | Newton's method applied to solution of $f'(x) = 0$          | 112                |
| E.1                  | Diagram of the designed vessels                             | 158                |
| E.2                  | C(t) curves of experiments to test identical stage behavior | 160                |
| E.3                  | E(t) curves of experiments to test identical stage behavior | 160                |

## **LIST OF APPENDIX TABLES**

| <b><u>Table</u></b>    | <b><u>Page</u></b> |
|------------------------|--------------------|
| D.1      Data Run#1030 | 114                |
| D.2      Data Run#1031 | 116                |
| D.3      Data Run#1032 | 118                |
| D.4      Data Run#1033 | 120                |
| D.5      Data Run#1034 | 122                |
| D.6      Data Run#1035 | 123                |
| D.7      Data Run#1036 | 124                |
| D.8      Data Run#1037 | 125                |
| D.9      Data Run#1038 | 127                |
| D.10     Data Run#1039 | 128                |
| D.11     Data Run#1040 | 131                |
| D.12     Data Run#1041 | 133                |
| D.13     Data Run#1042 | 134                |
| D.14     Data Run#1043 | 135                |
| D.15     Data Run#2000 | 137                |
| D.16     Data Run#2001 | 140                |
| D.17     Data Run#2002 | 143                |
| D.18     Data Run#2003 | 146                |
| D.19     Data Run#2004 | 147                |
| D.20     Data Run#2005 | 149                |

## **LIST OF APPENDIX TABLES (Continued)**

| <b><u>Table</u></b>                                         | <b><u>Page</u></b> |
|-------------------------------------------------------------|--------------------|
| D.21     Data Run#2006                                      | 151                |
| D.22     Data Run#2007                                      | 153                |
| D.23     Data Run#2008                                      | 155                |
| D.24     Data Run#2009                                      | 156                |
| E.1     Construction data. Experimental measurements in cm. | 159                |
| E.2     Operating data used/obtained in testing the vessels | 159                |

## NOMENCLATURE

|              |                                                                                    |
|--------------|------------------------------------------------------------------------------------|
| $b$          | Area under the curve (Figure 3.5)                                                  |
| $C(t)$       | Tracer concentration                                                               |
| $C_{in}(t)$  | Tracer concentration at vessel inlet                                               |
| $C_{out}(t)$ | Tracer concentration at vessel outlet                                              |
| $C_{in}(s)$  | Tracer concentration at vessel inlet (Laplace domain)                              |
| $C_{out}(s)$ | Tracer concentration at vessel outlet (Laplace domain)                             |
| $D_{ave}$    | Average particle diameter                                                          |
| $d_p$        | Particle diameter                                                                  |
| $E(t)$       | Residence time distribution function                                               |
| $E_1(t)$     | Residence time distribution function for plug flow                                 |
| $E_2(t)$     | Residence time distribution function for mixed flow                                |
| $E_3(t)$     | Residence time distribution function for mixed flow                                |
| $E_4(t)$     | Residence time distribution function for mixed flow                                |
| $E_1(s)$     | Residence time distribution function for plug flow (Laplace domain)                |
| $E_2(s)$     | Residence time distribution function for mixed flow (Laplace domain)               |
| $E_3(s)$     | Residence time distribution function for mixed flow (Laplace domain)               |
| $E_4(s)$     | Residence time distribution function for mixed flow (Laplace domain)               |
| $E(\theta)$  | Dimensionless residence time distribution                                          |
| $GFR$        | Gas flow rate                                                                      |
| $(GFR)_o$    | Minimum gas flow rate to spout the solid particles over the edge of the draft tube |



|                 |                                                     |
|-----------------|-----------------------------------------------------|
| $h$             | Height of solids in bed                             |
| $H_s$           | Separation between draft tube and bottoms of bed    |
| $L$             | Draft tube length                                   |
| $N$             | Number of stages                                    |
| RTD             | Residence Time Distribution                         |
| $R_v$           | Volume recirculated                                 |
| SFR             | Solids flow rate                                    |
| $S_o$           | Mass flow rate of solids                            |
| $S_R$           | Mass flow rate of solids in the spout               |
| $t$             | Time                                                |
| $t_R$           | Recirculation time                                  |
| $t_{Ro}$        | Recirculation time at $(GFR)_o$                     |
| $\bar{t}_{obs}$ | Mean residence time (observed) in Levenspiel (1993) |
| $v$             | Flow rate                                           |
| $V_d$           | Dead volume                                         |
| $V_M$           | Mixed flow volume                                   |
| $V_p$           | Plug flow volume                                    |
| $W$             | Bed Weight                                          |
| $W_0$           | Total amount of tracer material                     |
| $W_d$           | Dead weight                                         |
| $W_p$           | Plug flow weight                                    |
| $W_M$           | Mixed flow weight                                   |
| $\Delta P$      | Pressure drop across the spouted bed                |

|            |                                                                                  |
|------------|----------------------------------------------------------------------------------|
| $\Delta t$ | Time interval                                                                    |
| $\Delta W$ | Amount of tracer material leaving the vessel between time $t$ and $t + \Delta t$ |

### Greek letters

|               |                                                                                                        |
|---------------|--------------------------------------------------------------------------------------------------------|
| $\rho_g$      | Gas density                                                                                            |
| $\rho_s$      | Density of solids                                                                                      |
| $\theta$      | Dimensionless time                                                                                     |
| $\theta_i$    | Dimensionless time for stage “i”                                                                       |
| $\tau$        | Mean residence time = $W/S_o$                                                                          |
| $\tau_d$      | Mean residence time of the dead space = $W_d/S_o = \tau - \tau_{obs}$                                  |
| $\tau_i$      | Mean residence time for stage “i”                                                                      |
| $\tau_M$      | Mixed flow time                                                                                        |
| $\tau_{Mi}$   | Mixed flow time for the “i” vessel                                                                     |
| $\tau_{obs}$  | Mean residence time (observed) = $\frac{\sum_{i=1}^n t_i C_i \Delta t_i}{\sum_{i=1}^n C_i \Delta t_i}$ |
| $\tau_p$      | Plug flow time                                                                                         |
| $\tau_{pi}$   | Plug flow time for the “i” vessel                                                                      |
| $\tau_R$      | Solids recirculation time                                                                              |
| $\tau_\theta$ | Mean residence time of the curve $E(\theta)$ curve (equal to 1)                                        |
| $\sigma^2$    | Variance                                                                                               |

$\sigma_t^2$  Variance of the E(t) curve

$\sigma_\theta^2$  Dimensionless variance of the E( $\theta$ ) curve

$\sigma_{\theta i}^2$  Variance of the E( $\theta$ )<sub>i</sub> curve

To the memory of

Francisco Arriola Adame, my father

and

Luis F. Cervantes Jauregui, my lifetime friend

whose standards and lifelong achievements

serve to inspire me

# **RESIDENCE TIME DISTRIBUTION OF SOLIDS IN STAGED SPOUTED BEDS**

## **CHAPTER 1**

### **INTRODUCTION**

Spouting is a gas-solid contact operation in which a high velocity jet of fluid moves through a bed of solids forcing them up to the center of the vessel until they reach the top of the bed, where particles then drop back around the spout. The flow of solids is circulatory, and if a cylindrical column is used, the flow is symmetrical, on average, about the axis. One of the major advantages claimed by the originators (Mathur and Gishler, 1955) of these gas-solid contactors, is that they can handle particles that are in a size range ( $> 10^{-3}$  m) which are too coarse to fluidize. The technical terms relating to the fields of fluidization and fluid flow will be used in this thesis as defined by Levenspiel (1972, 1991).

According to Mathur and Epstein (1974), "the operations for which the use of a spouted bed attract attention are remarkably varied". Applications, ranging from drying (Peterson, 1962), heating and cooling of granular solids (Fisons Ltd., 1969), blending (Bowers *et al*, 1960), to coating and granulating all type of coarse particles (Siginser *et al*, 1966; Berquin, 1964; Nichols, 1966), are now commercially used. Even though it is still possible to affirm that spouting serves the same purpose for coarse particles as fluidization does for fine solid materials (with the additional advantage, for some cases, of the regular cyclic motion of solids and low pressure drop), spouted beds have lately been used for processing micron-size particles, which otherwise would be difficult to fluidize (Hattori and Takeda, 1978; Littman *et al*, 1990; Jovanovic, 1994).

The addition of a tubular insert as a draft tube in a spouted bed, changes some of the operational and design characteristics of an ordinary spouted bed, as previously shown by Buchanan and Wilson (1965), Ishida and Shirai (1975), Yang and Keairns (1978,

1988), and Tsutsumi and Yoshida (1996) among others. The big advantages in using draft tubes is that there is practically no limitation on the maximum spoutable bed height, the solid circulation rate in the bed can be easily controlled, and pressure drop and minimum gas flow rates, are both lower compared to a bed without a draft tube.

Most of the previous studies (Quinlan and Ratcliffe, 1970; Chatterjee, 1970; Mann and Crosby, 1972; Pallai and Nemeth, 1972) are done with a batch of solids rather than in a truly throughflow operation. One of the challenges presently faced by the spouted bed technique is that of designing a suitable, simple, continuous solid-flow operation. The solids in a continuous solid-flow single spouted beds behave very similarly to a *continuous stirred tank reactor* (CSTR) (Mathur and Epstein, 1974). Some solid particles entering the bed leave almost immediately since material is being continuously withdrawn from the vessel, while other particles remain in the vessel for a very long time because all solid particles are never entirely removed from the vessel at one time. Some particles, however, leave the vessel after spending a period of time approximating the mean residence time. Consequently, in a single spouted bed there is a wide solid *residence time distribution* (RTD), which can be a serious disadvantage if, as in many commercial applications, uniform treatment of solids is desired.

The idealized plug-flow vessel is the only class of continuous flow vessels in which all particles in the vessel have the same residence time. However, the plug flow of solids through the vessel, in which all particles have the same residence time, is difficult to accomplish in practice. It has been shown that for CSTR's in series, when the number of tanks becomes large ( $N > 20$ ), the behavior of the system approaches that of an idealized plug-flow vessel. (Levenspiel and Bischoff, 1963). Accordingly, if enough stages are provided, one would expect that a multistage spouted bed should approach the behavior of an idealized plug-flow vessel.

Some experimental work has been done involving multistage spouted beds: Madonna et al (1961) used a batch system to demonstrate savings in spouting air; Malek and Walsh (1966) tried a multistage continuous system of spouted beds, but their system had operational disadvantages as will be shown later in this thesis; and Van Weert and

Van Hasselt (1997) recently tested a countercurrent flow of dissimilar solids in a vertical, multistage, spouting-bed configuration, in a semi-continuous operation.

This investigation directly addresses the problem of determining the RTD of solids in a new, much simpler design of a continuous multistage spouted system with draft tubes. We believe that our design, does not have problems of hydrodynamic instabilities, and improves operational characteristics and controllability of the bed. To prove these claims we used solid tracer technique and RTD analysis. Even though the RTD does not carry complete information about the flow and structure of a particular bed, it is possible to affirm that the RTD is a characteristic of the mixing that occurs in that bed (Fogler, 1992; Levenspiel, 1991; Bischoff, 1966).

Our goal is to extend our basic understanding of the motion of solid phase (particles) in a multistage spouted bed through the study of the *residence time distribution* (RTD) of solids in this operation. With some exceptions, all previous investigations on spouted beds have been conducted in either cylindrical or semicylindrical batch columns. Furthermore, none of the previous work in this field was done using “two-dimensional”, half-rectangular, continuous, multistage spouted beds with draft tube, which we believe is a better design in terms of operation, control, and scale-up criteria. The approach used in this study is based on meeting four specific objectives:

- i) **Design, construction and operation of a single stage-spouted bed.**- This required the appropriate use of related previous experience in general design criteria, followed by preliminary laboratory tests with some suitable solid material. A single-stage bed with the geometric characteristics mentioned above is designed and tested. Since there is no available information for this specific geometry, the "best" design is chosen in terms of experimental observation. Parameters depending on solid and fluid properties, bed size, and geometry are obtained.

Two specific design details are of particular interest and importance: feeding and discharging of solids, and application of a draft tube. The objective is to design a possible feeding/discharge device with no moving parts which “automatically” maintains particles in the bed, and provides stable mass flow of solids. As far as the

draft tube is concerned, the objective is to establish its operational characteristics visually, i.e.: location, geometry, size, and pressure drop in the bed.

- ii) **Design, construction and operation of a multistage column.-** Based upon the experience acquired with a single-stage spouted bed, a multistage column system is designed and tested. Hydrodynamic stability of bed operation, which is a typical problem for multistage operations, is resolved without compromising the overall simplicity of the operation.

Two specific problems that are not properly solved in any of the known multistage spouted bed designs are addressed: (a) start-up procedure/conditions, and (b) shut-down procedure/conditions. Both operations should be easy to perform and should not demand special procedures and devices with moving parts.

- iii) **RTD studies for both single and multistage operation.-** In the absence of known theoretical models applicable to the operation of multistage spouted bed, information concerning gross mixing behavior of solids come from stimulus-response experiments where the residence time distribution of particles fed into and discharged from the bed at a steady rate are measured. Again, simplicity in choosing both the tracer and the appropriate method of detection is a major goal. Data from these experiments are properly manipulated and analyzed.

- iv) **Modeling.-** From the analysis of the experimental data, an appropriate solids circulation model is proposed and tested.



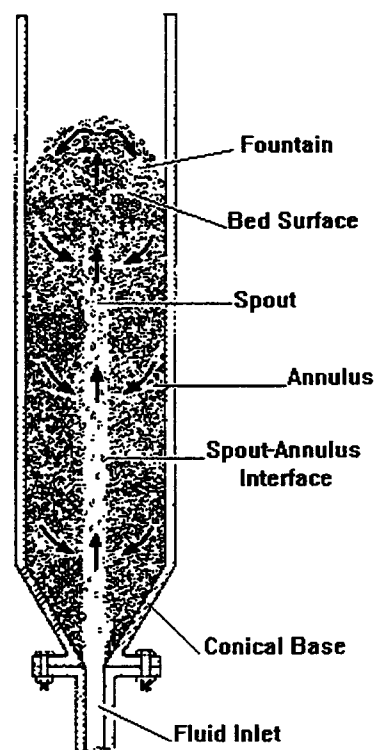
## CHAPTER 2

### BACKGROUND AND LITERATURE SURVEY

#### 2.1 The Spouted Bed

Spouting is a technique for contacting fluids with solid particles. Initially developed as a method for drying grains and peas (Peterson, 1962; Sevilla and Pinder, 1970; Clary *et al*, 1970), spouted beds are used now in many other processes, such as solid separation (Van Weert and Van Hasselt, 1997), granulation (Tsvik, 1966 and 1967), catalytic reactions (Uemaki, 1968), and heat and mass transfer operations in general (Uemaki and Kugo, 1967 and 1968).

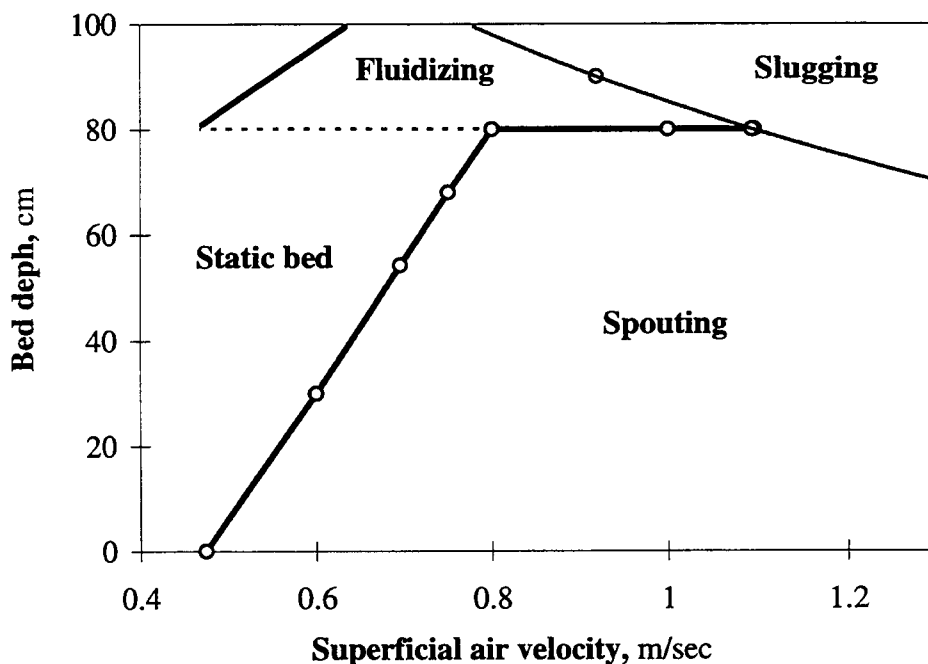
We may consider a spouted bed as a combination of a dilute, fluidized phase and a coexistent moving bed of solids. Figure 2.1 shows a schematic diagram of a typical spouted bed: a vessel, open at the top, is filled with solid particles. A fluid enters coaxially through a small opening in the apex of the conical base. Since the injection rate of the fluid is very high, it produces a high velocity jet causing a stream of solid particles to rise rapidly and form a central channel within the bed of solids. At the upper end of this channel, the solids spill over and rain back as a fountain onto an annulus that defines the column of descending solids in the moving bed. Coexistence of the two phases (fluid and



**Figure 2.1** Schematic diagram of a spouted bed

solids) produces a characteristic solids circulation pattern: the solid material is carried upward by a cocurrent flow of fluid in the central core and it descends by gravity, through the surrounding dense phase annular region, with countercurrent percolation of fluid.

Spouting is a visually observable phenomenon which occurs over a certain range of fluid velocity for a given combination of fluid, solids, and geometry of the vessel. Figure 2.2, represents an example of a phase diagram which shows, in general, the range of conditions for transitions from a static, to a fluidizing, to a slugging, and to a spouting bed. From this type of diagram one may conclude that spouting is a phenomenon that usually occurs at high fluid velocities and small bed depths.



**Figure 2.2** Phase diagram for semicoke (particle diameter range from 1mm to 5mm).  
Adapted from Dumitrescu and Ionescu (1967).

## 2.2 Spouting And Fluidization

It seems obvious to compare a spouting bed with an "ordinary" fluidized bed during channel formation. In this respect, according to several authors -Zenz and Othmer (1960), Leva (1959), Zabrodsky (1966), Davidson and Harrison (1963)- a spouted bed is qualitatively similar to a channeling, fluidized bed; however, in a spouting bed, the agitation of the entire bed is achieved by means of the fluid jet causing the intimate and desired contact in both dilute and dense phases. Channeling is an undesirable phenomenon in a fluidized bed. Madonna *et al* (1961) propose that "channeling is an accidental by-passing of gas in the fluidized bed while spouting is an intentional by-passing in a packed bed system". They present a comparison between channeling and spouting pressure drop curves to support their statement.

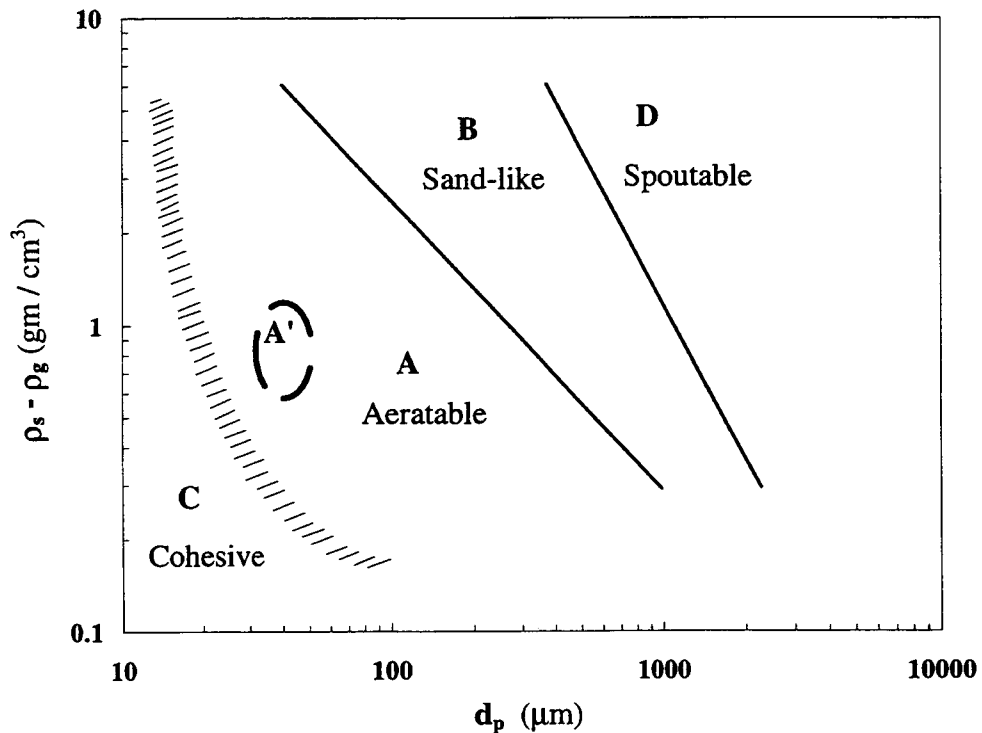
Another parallel between spouting beds and fluidized beds is the *jetting* region located on the bottom of the fluidized bed. This region is nothing more than a miniature spouted bed with considerably finer particles using a very small gas inlet. Indeed, according to Lefroy and Davidson (1969), and Fakhimi and Harrison (1970), the use of sieve plates distributors for fluidized beds gives rise to spout formation above each hole, and the spouts breaking into bubbles further up the bed. If, however, a single small hole is used to spout fine particles, Vainberg *et al* (1967) show that the allowable holdup and capacity of the bed would also be small, and any attempt at scale-up by enlarging the inlet hole would give rise to nonhomogeneous fluidization rather than spouting.

While the original statement by Mathur (1955) that "spouting appears to achieve the same purpose for particles as fluidization does for fine materials" remains true, it is clear now that for certain applications (granulation and particle coating processes) the cyclic movement of solids in a spouted bed is an important and unique feature. As Mathur later explained, "spouted beds allowed a very systematic cyclic movement of particles which are too coarse (millimeter size) for good fluidization. An overall circulatory movement of particles could, no doubt, be achieved in a fluidized bed with draft tube, but it would not be as systematic as in a spouted bed" (Mathur and Ratcliffe, 1974). Beside achieving gas-solid contact spouted beds provide a very good way of agitation of coarse

particles. They can be applied for mechanical operations like grinding, blending, and dehusking.

We may attempt to establish a comparison between spouting and fluidization by observing differences and similarities of their characteristics. Table 2.1 summarizes all these characteristics. Those observations include:

- a) **Particle Size.**- Spouting seems to be a practical operation for coarse particles with a minimum diameter of about 1 mm. This particle size is about the maximum above which the "ordinary" fluidized bed gas-solid contacting effectiveness is clearly affected by formation of big bubbles (Davidson and Harrison, 1963). Moreover, according to Geldart's classification (Geldart, 1973), particles suitable for the spouting operation are "Geldart D solids" while those for fluidization fall into the region of "Geldart A and B solids". For particles in air at ambient conditions, Levenspiel (1991) adapted the Geldart classification that is shown in Figure 2.3.



**Figure 2.3** The Geldart Classification of particles for air at ambient conditions. Adapted from Levenspiel (1991).

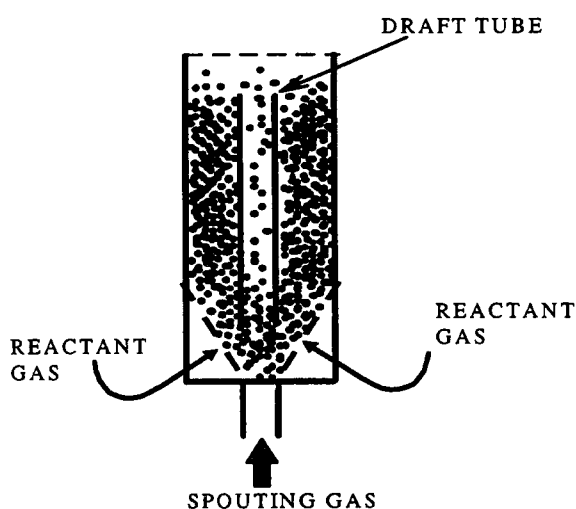
|                                        | <b>SPOUTING</b>                                                | <b>FLUIDIZATION</b>                                          |
|----------------------------------------|----------------------------------------------------------------|--------------------------------------------------------------|
| Particle Size                          | coarse particles<br>( > 1mm )<br>Geldart D                     | fine particles<br>( 40 - 500 $\mu\text{m}$ )<br>Geldart A, B |
| Pressure Drop                          | low                                                            | high                                                         |
| Motion Of Solids                       | systematic cyclic movement                                     | almost random motion                                         |
| Heat and Mass<br>Transfer Coefficients | large                                                          | large                                                        |
| Fluid Velocity                         | very high                                                      | low-high                                                     |
| Fluid-Solid<br>Contact Time            | short to large<br>( greater flexibility in<br>controlling it ) | larger than in<br>conventional spouted bed                   |

**Table 2.1** Comparison Between Spouting and Fluidization Characteristics

- b) Pressure Drop.-** Epstein and Mathur (1974) established that “the total pressure drop across a fully spouting bed is always lower by at least 20% than that required to support the weight of the bed”.
- c) Motion of Solids.-** The previously mentioned systematic cyclic movement of solid particles is a unique characteristic of spouted beds and can be a very important feature valuable for certain applications such as: particle coating (Heiser *et al*, 1960; Singinser and Lowenthal, 1961; and Siginser, Heiser, and Prillig, 1966), and many

different chemical processes (Ratcliffe and Rigby, 1969, Berti, 1968; Vavilov *et al*, 1967 and Uemaki *et al*, 1970)

- d) Heat and Mass Transfer Coefficients.-** For gas-solid systems, the wall-to-bed heat transfer coefficient  $h_w$ , exhibits a sharp increase once a spouting state is reached (Uemaki and Kugo, 1967). This is also true for fluidization; but for spouting, the coefficient increases with increasing particle diameter, a characteristic which is the opposite of that observed in fluidization of the same particles.
- e) Contact Time.-** Spouted beds have more flexibility in gas-solid contacting (Uemaki *et al*, 1970). Nominal values for contact times may be obtained by dividing the packed height of the solids in the bed by the *superficial velocity* of the spouting gas. One can easily control the length of contact time by changing the bed depth, by varying the diameter of the gas inlet, or by changing the draft tube operating characteristics. Uemaki further note that for a given solid material, there is only one way to control the contact time in a fluidized bed and that is to reduce the depth of the bed. This cannot be done beyond a certain limit since a sizable depth is required to keep isothermal conditions. On the other hand, the contact time in a spouted bed remains short even in relatively deep beds. Some specially designed spouted beds may have very long contacting times between reacting gas and solids. (see Figure 2.4.).



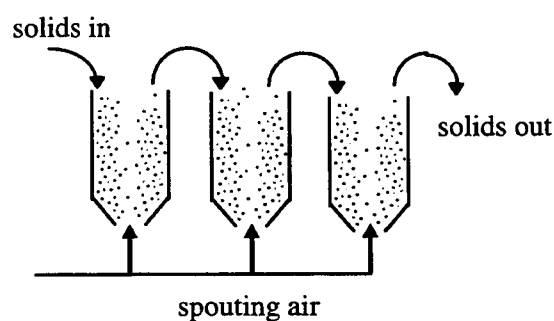
**Figure 2.4.** Long contacting time spouted bed.

The idea behind these designs (Johnston *et al*, 1961; Vukovic *et al*, 1973; Jovanovic, 1995) is to superimpose two entirely different mechanisms for gas-solid contacting: a very effective, long, contact between solids and reactant gas in the annular region, and a characteristic spouting circulation pattern without the necessity of expensive mechanical agitation.

### 2.3 Multistage Spouting

Multistage operation of spouted beds involving countercurrent flow of solids and spouting fluid has been reported by several researchers: Elperin (1955, 1960 and 1965), Khokhlov (1959 and 1965), Madonna (1961), Malek and Walsh (1966), Rovero and Watkinson (1990). Different types of units of varying design were used. Two different multistage operations involving flow of solids in series through more than one spouted bed were developed:

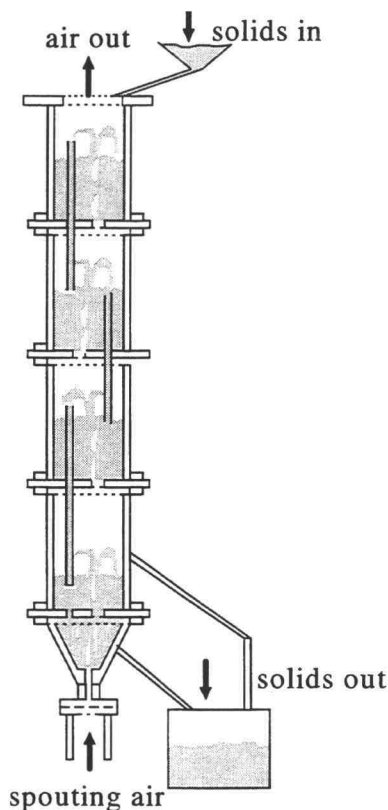
- 1- Flow of spouting gas in parallel (Figure 2.5)
- 2- Flow of spouting gas in series (Figure 2.6)



**Figure 2.5** Flow of spouting gas in parallel.

A good example of flow of spouting gas in parallel is the work done by Paterson *et al* (1983). Works by Elperin and Khokhlov (1965), Madonna *et al* (1961), Malek and Walsh (1966) and, more recently, Rovero and Watkison (1990) may well represent the flow of spouting gas in series. Depending on the purpose of the process, a multistage continuous operation has several advantages over the batch operation; among the most important ones are:

- a) Continuous operation.
- b) Less gas flow rate requirement for a given depth of solids.
- c) Prolonged gas contact time with solids in the bed.
- d) Shorter solid residence time distribution and increase of the uniformity in solids treatment.



**Figure 2.6** Flow of spouting gas in series



## 2.4 Modifications to the Spouting Technique

There are many alternate configurations for the spouted bed operation, such as multiple spouting, pulsed flow spouting, spouting with tubular inserts, slot spouted bed, two-fluid phase spouting, as well as others. (Mathur and Epstein, 1974, Chapter 12). For the present work it is important to examine two of these configurations in more detail:

### a) Spouted Beds with draft tubes

Mathur and Epstein (1974), believe that "as far as solids circulation is concerned, flow of fluids through the annulus region of a normal spouted bed serves little purpose". Bowers *et al* (1960) and Buchanan and Wilson (1965) were among the first to try the use of draft tubes in spouted beds.

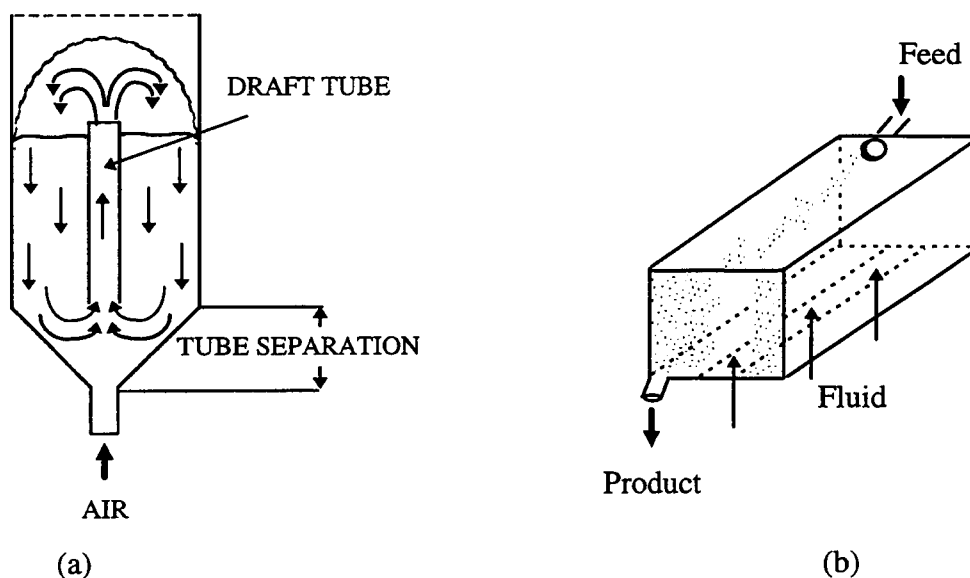
In the draft tube, the spouting gas is forced to go up through the central core without contacting the solids in the bed except for a very short distance between the fluid inlet and the lower end of the draft tube (see Figure 2.7a).

Certain advantages and limitations are observed in the use of draft tubes. The most important to mention are: (1) they allow the spouting of small size particles as shown by Hattori and Takeda (1978); (2) the spouting process can be done with smaller pressure drop and/or higher bed depths, (3) the so-called minimum spouting velocity will also be smaller because the fluid in the draft tube is confined and does not leak out along the spout height as in an ordinary spouted bed, (4) the advent of draft tube spouted beds also eliminated the bubbling problems in gas-particle systems (Hattori and Takeda, 1978), (5) the overall mixing efficiency is reduced. The hydrodynamic behavior of spouted beds with draft tubes is extensively discussed by Yang and Keairns (1983) and Hadzismajlovic *et al* (1992).

### b) Slot Spouted Bed

A modification involving the introduction of the fluid into the base of the bed through a narrow slot running across the longer dimension of a rectangular bed has been widely studied by Mitev (1967), Romankov and Rashkovskaya (1968), and by Volkov (1970). One of the favorable features of the slot spouted beds is the relative ease with which the design can be scaled up: it can be achieved by simple parallel

arrangement of a series of slot units into a multiple system, resulting in a considerable throughput increase. The slot may be either continuous or with spaced openings; in both cases, a stable spouting of solids can be obtained (see Figure 2.7b).



**Figure 2.7** Modifications and variations to the Spouting Technique. (a) Spouted Bed with draft tube, (b) Slot Spouted Bed.

## 2.5 The RTD Approach To Modeling Flow In Mobile Beds

In an idealized plug-flow vessel, all the solid particles leaving the vessel have been inside it for exactly the same amount of time. Similarly, in an batch vessel, all the particles within the vessel have been inside it for an identical length of time. This time is called the residence time of the particles in the vessel. These two vessels are the only two classes of vessels in which all the particles have the same residence time. In all other types of vessels, the solid particles spend different times within the vessel; in other words, there is a *residence time distribution* of these particles inside such vessels.

It can be visually observed that in a continuous single spouted bed there is a wide solids residence time distribution. This fact is inevitably associated with the solids mixing characteristics of the single-stage spouted bed. This can be a serious disadvantage if uniform treatment of particles is desired.

### **2.5.1 Tank-In-Series-Model**

According to Becher and Sallans (1961), Kugo *et al* (1965), Barton *et al* (1968), Quinlan and Ratcliffe (1970), and Pallai and Nemeth (1972), the solid mixing in a single stage spouted bed is close to perfect mixing:

Becher and Sallans (1961) used a pulse of dyed wheat injected at bed top, and the concentration of colored particles in the bed was measured periodically. Kugo *et al* (1965) also experimented with wheat, but they observed the output response to a step change in solids input: the feed was changed to colored particles, and their concentration measured in wheat discharging from the opening in the conical base of the vessel. Barton *et al* (1968) fitted their own experimental concentration-time data by linear regression, and obtained an empirical equation.

Quinlan and Ratcliffe (1970) reached the conclusion that only 8-10 % of the total spouted volume is in plug flow, while the remainder is perfectly mixed. According to them, dead space and bypassing are negligible. Finally, Pallai and Nemeth (1972) arrived at the conclusion that solids mixing in spouted beds is nearly but not quite perfect.

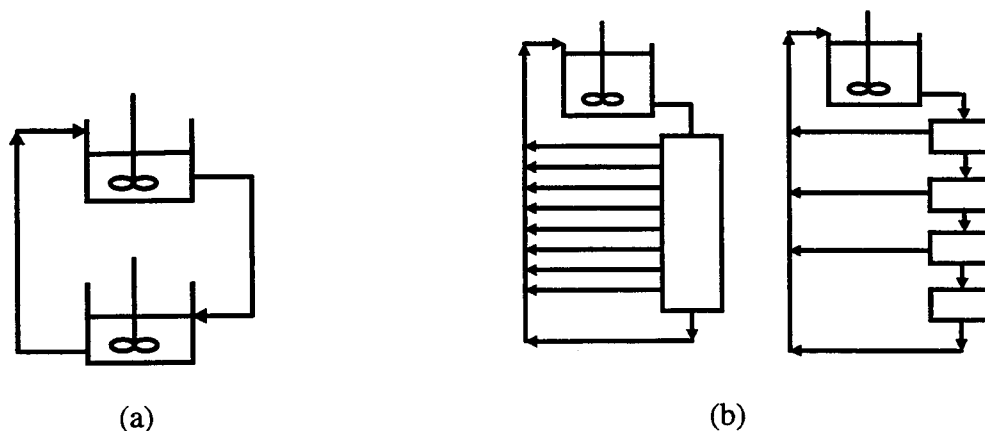
Although all those researchers claim that the assumption of perfect mixing would be a good approximation for most practical purposes, none of them ever adopted the “tank-in-series-model” and/or tested a multistage system. Furthermore, we know of no published work attempting the utilization of tank-in-series-model to describe the multistage spouted bed behavior of solid particles.

### 2.5.2 Compartment Models

According to Levenspiel (1972), “when one-parameter models are unable to account satisfactorily for deviations from the ideals of plug and mixed flow, the more complicated models must be attempted”. One approach is to look at all possible combinations that one can use to model a nonideal vessel using only plug flow, dispersed plug flow, mixed flow, dead volume and bypassing. The rate of transfer between such vessels is one of the model parameters. This approach, however, is not based upon the careful visual observation of the flow patterns.

A second approach is to obtain a compartment model with parameters that are based upon *phenomenological* observation. In this case, an actual flow situation may better be described.

A suitable model carefully checked by appropriate measurements of tracer particle concentration can be quite helpful in estimating the actual solids circulation in a spouted bed. Chatterjee (1970) proposed a model based on measurements of the degree of mixing of tracer particles at the top of the bed as a function of time. The model proposed by Chatterjee describes the spouted bed as two stirred tanks connected in series, as shown in Figure 2.8a, with the output of the second tank recycled to the first tank.



**Figure 2.8** (a) Twin continuous stirred tank model by Chatterjee (1970),  
(b) Circulation models by Mann and Crosby (1972).

According to Mann and Crosby (1972), the model by Chatterjee fails to represent actual movement of solids because: (1) concentrations of tracer particles are assumed uniform in both upper and lower sections of the annulus, (2) there is an actual short-circuiting along the spout which is not included in the model and, (3) the fraction of the particles in the spouting region is not necessarily insignificant. Therefore, Mann and Crosby proposed a more realistic model, shown in Figure 2.8b, which takes into account the cross-flow of solids from the annulus to the spout as well as the holdup in the spout. However, it should be noted that the, Chatterjee and Mann and Crosby analyses, concern the mixing behavior of a *batch* of solids rather than a continuous flow system, and unfortunately they do not present an analytical solution.

## 2.6 Research With Multistage Units In Series

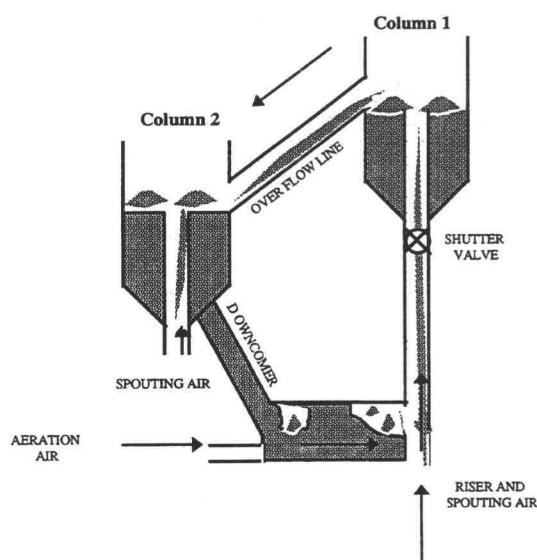
A large volume of information on spouted beds has appeared in technical journals and books showing that their use is becoming extraordinarily popular. There are now hundreds of papers on the subject that initially was referred to as "Canadian Fluidization". Most of the past work has been done using cylindrical beds with no draft tubes, and the operations were performed in a single, batch fashion. Multistage systems, i.e. vertically superimposed spouting beds, have not been well described in the literature, and there are no good commercial designs available. Moreover, there are no known published papers dealing with the experimental determination of the RTD of solids in a multistage spouted bed with draft tubes, and the use of such data for modeling purposes.

Elperin and Khokhov (1965), were among the first to experiment with multistage operation involving countercurrent flow of solids and spouting fluid in a manner characteristic of spouted beds. They constructed units consisting of several retorts vertically superimposed one upon the other. Each retort was connected to the next one via a throat. The fluid velocity in the throat was then higher than in the widest parts of the beds. Pulsating downward flow of solids was caused by pulsations of the upward-flowing gas. Units of that type are hydrodynamically unstable and they have been used for many

different purposes, such as cement clinker production, drying, heating, and gypsum production. More recently, Paterson *et al* (1983) experimented with parallel spouted beds in a batch process (Figure 2.9). Their experiments were conducted with two different types of solids to determine the solids flow rate and the pressure drop through different sections of the loop.

The works by Madonna *et al* (1961) and by Malek and Walsh (1966) are important to us because they are all investigations of multistage units.

Madonna and coworkers used a group of four 6-in diameter Pyrex tubes of equal length stacked one above the other, and separated from each other by septa each with a central orifice. These stages contain spouted batch systems designed simply to show that the air requirement to spout the entire assembly was reduced compared to the air requirement for the accumulated depth of all four beds taken as a unit.



**Figure 2.9** Parallel spouted beds in a batch process. Adapted from Paterson, Grace and Watkinson (1983)

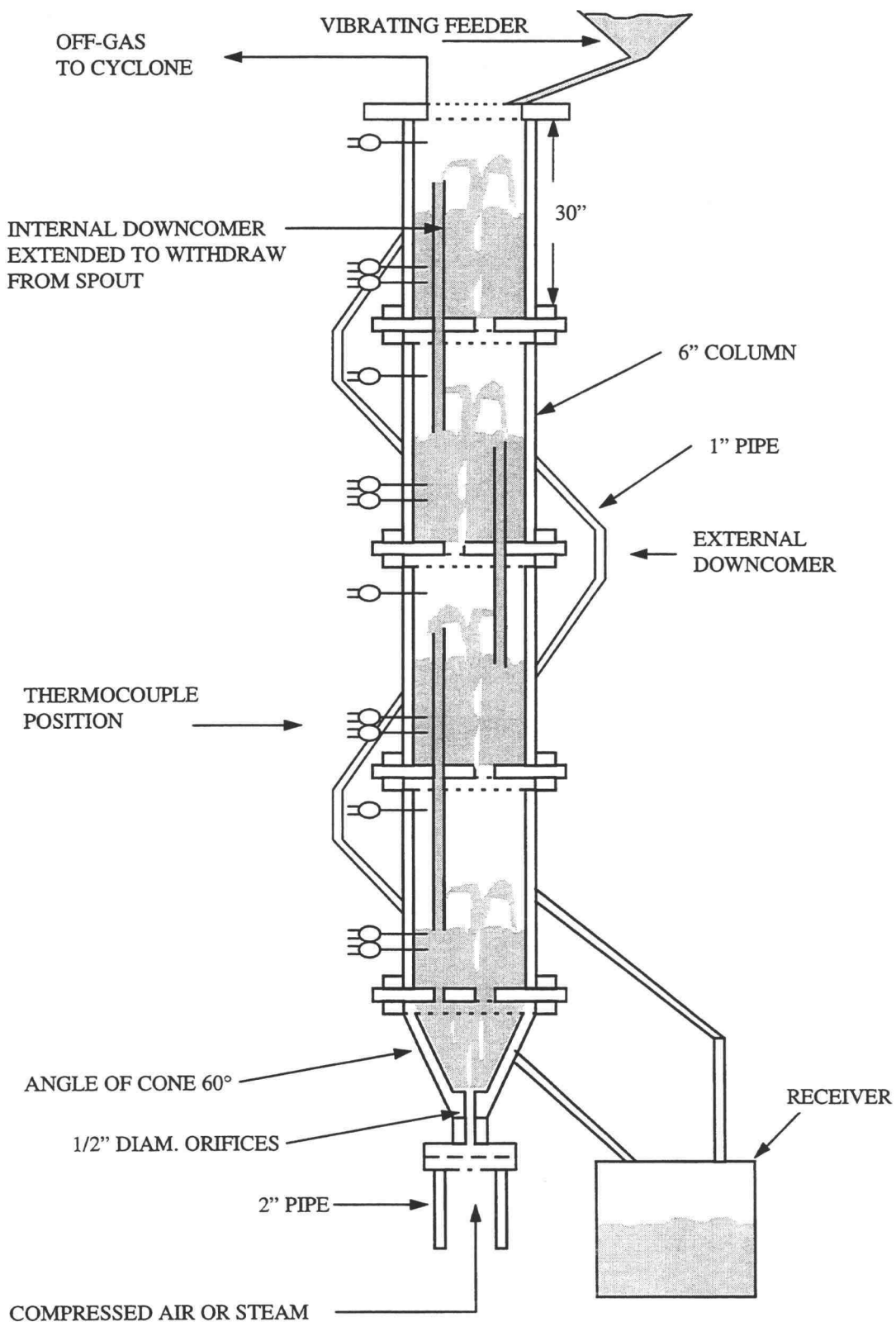
The multistage column used by Malek and Walsh is of the type shown in Figure 2.10 and it deserves special attention since these workers experimented with continuous

multistage units with countercurrent flow of gas-solids in series. Transfer of particles from stage to stage is accomplished by the use of 1-inch internal downcomers. No mechanical device is used, and the solids are taken from the upper stage, either in the moving bed zone or from the dilute phase zone. For the later case, the top end of the internal downcomer is extended above the bed level so that the only material transferred in the tube is solids falling directly from the spout itself. The discharge end is located in the lower moving bed zone. Malek and Walsh agree that the position of this lower end is critical, since a slight displacement upwards changes the flow rate of solids until the end becomes totally exposed and the spouting of the upper bed stops.

Clearly, since the location of the downcomer is very sensitive, Malek and Walsh suggest the possibility of using a “mechanical feeding device that could be superior in practice”. These researchers also attempted the use of external downcomers. According to their own words, “primarily because of the number of bends necessary, it proved impossible to maintain a reliable flow of solids, although a slight improvement was obtained when a smooth liner was installed”. Later investigations used only vertical, internally mounted transfer lines.

At this point, it is very important to realize that, in our opinion, the column used by these workers has other disadvantages besides those mentioned for its possible industrial application. Our first objection has to do with the feeding and discharging procedures for solids. To start the operation of the column, it is necessary first fill up to all stages using “extra” external downcomers (with all the problems mentioned above). On the other hand, at shut-down time, a large fraction of solids remains within the column, and there is no way to clean out the column completely unless it is disassembled. Obviously this amount of solids never was in contact with the gas during the operation, and represent an undesirable dead space.

Our second, and no less important objection has to do with the high peak pressure drop within the column. This is a serious limitation for a continuous, multistage, stable, inexpensive operation. We have found that the use of draft tubes in each stage will certainly solve the problem of high pressure drop, and we will illustrate this later.



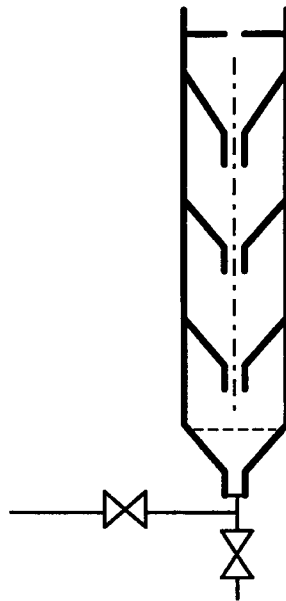
**Figure 2.10** The multistage column used by Malek and Walsh (1966)



Finally, we are persuaded that the column of Malek and Walsh, although it represents an important contribution toward the use of multistage systems of spouted beds for industrial applications, has operating characteristics that place numerous constraints for its possible operation on an industrial scale.

The Himsley column, adopted for uranium extraction, and the NIMCIX column developed in South Africa for the same application, are briefly mentioned in Anon (1990) and in Van Weert and Van Hasselt (1997). According to these authors, very little is published on this equipment, but it is known that these columns have a semi continuous operation with serious hydrodynamic instabilities due to the plugging of their screens that cause gold extraction inefficiencies.

The spouting bed configuration by Van Weert and Van Hasselt, shown in Figure 2.11, was also used to separate dissimilar solid particles.



**Figure 2.11** Multistage spouting bed test facility as used by Van Weert and Van Hasselt (1997).

The vertical multistage spouting bed was investigated as an alternative to mechanical devices, such as screens or cyclone separators to achieve separation of solids. The operation of their column could be characterized as a semicontinuous operation. Periodically the upward velocity of the gas is lowered, allowing the solid particles to settle and be collected in the cone of each stage. At the moment of zero velocity the solid particles slide through the opening in the cone into the lower compartment, after which the regular upward velocity of the gas is resumed. This transport of particles into the next lower compartment happens simultaneously for all stages. Van Weert and Van Hasselt found that their spouting configuration requires “internal modification” to achieve hydrodynamic stability.

## CHAPTER 3

### MODEL DEVELOPMENT

#### 3.1 Introduction

The application of population-balance principles to modeling of non-ideal flow and mixing characteristics in vessels was formally organized by Danckwerts (1953). He was the first to define the distribution functions for the residence time of fluid elements in a vessel. RTD functions give information about the fraction of the fluid that spends a certain time within the vessel. It allows a possible velocity distribution map for the fluid, which frequently is sufficient information to give adequate estimation of the behavior of the vessel.

#### 3.2 Tanks In-Series Model

It has been shown (Levenspiel and Bischoff, 1963) that the residence time distribution of solids in a perfect mixed flow vessel is well described by:

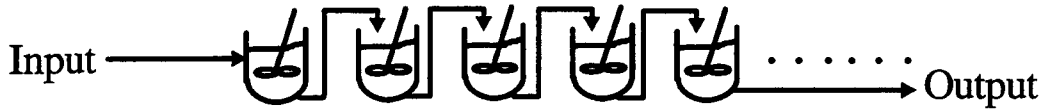
$$E(t) = \frac{1}{\tau} \exp\left(-\frac{t}{\tau}\right) \quad (3.1)$$

where  $E(t)$ , the residence-time distribution function, describes in a quantitative manner how much time different particles have spent in the vessel. Therefore, for the case of a continuous single-spouted bed,  $E(t)dt$  is the fraction of solids staying in the bed between time  $t$  and  $t + dt$ , and  $\tau$  is the mean residence time. Equation (3.1) can be likewise obtained from conceptual considerations in a fairly straightforward manner by a material balance on an inert tracer that has been injected as a pulse into a CSTR. Also,

$$\int_0^{\infty} E(t) dt = 1 \quad (3.2)$$

For an ideal multistage spouted system of  $N$  equal-sized perfectly mixed beds (see Figure 3.1),

$$\tau E(t) = \left(\frac{t}{\tau}\right)^{N-1} \frac{N^N}{(N-1)!} \exp\left(-\frac{tN}{\tau}\right) \quad (3.3)$$



**Figure 3.1** Graphical representation of the tank-in-series model.

Similarly,

$$\tau_i E(t) = \left(\frac{t}{\tau_i}\right)^{N-1} \frac{1}{(N-1)!} \exp\left(-\frac{t}{\tau_i}\right) \quad (3.4)$$

Where  $\tau_i$  is the mean residence time in each stage given by

$$\tau_i = \frac{\tau}{N} \quad (3.5)$$

It can be noted that for  $N=1$ , equation (3.4) reduces to equation (3.1).

Variance for this model is given by

$$\sigma_i^2 = N\tau_i^2 = \frac{\tau^2}{N} \quad (3.6)$$

Frequently, a normalized RTD,  $E(\theta)$ , is used instead of the function  $E(t)$ . The flow performance inside beds of different sizes can be compared directly. Consequently, if the normalized RTD is used,

$$\theta = \frac{t}{\tau} \quad (3.7)$$

then equation (3.1) becomes

$$E(\theta) = e^{-\theta} \quad (3.8)$$

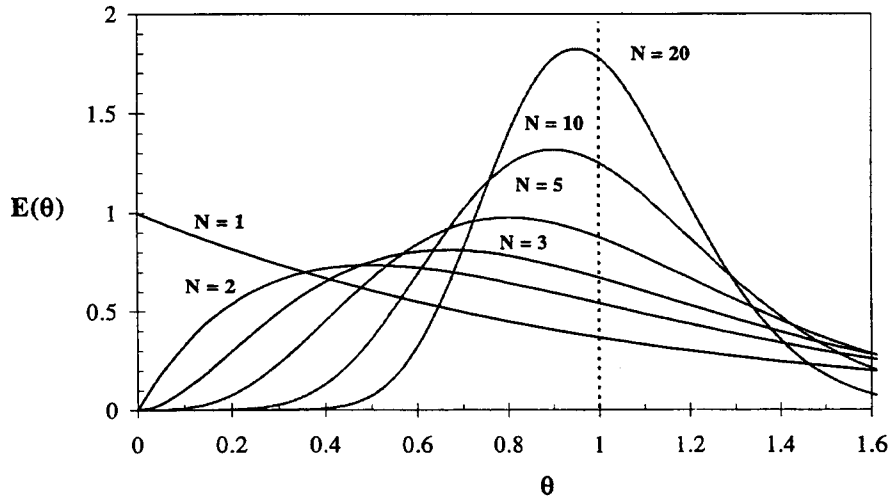
where  $E(\theta) = \tau E(t)$ . Similarly, equation (3.3) can be written as

$$E(\theta) = [N t_i] \cdot E(t) = \frac{N \cdot (N\theta)^{N-1}}{(N-1)!} e^{-N\theta} \quad (3.9)$$

with the mean  $\tau_\theta = 1$  and the variance  $\sigma_\theta^2 = \frac{1}{N}$ ; also, equation (3.4) becomes

$$E(\theta_i) = \tau_i E(t) = \frac{\theta_i^{N-1}}{(N-1)!} e^{-\theta_i} \quad (3.10)$$

with the mean and the variance both equal to  $N$ . The graphical representation of equation (3.9) is shown in Figure 3.2.

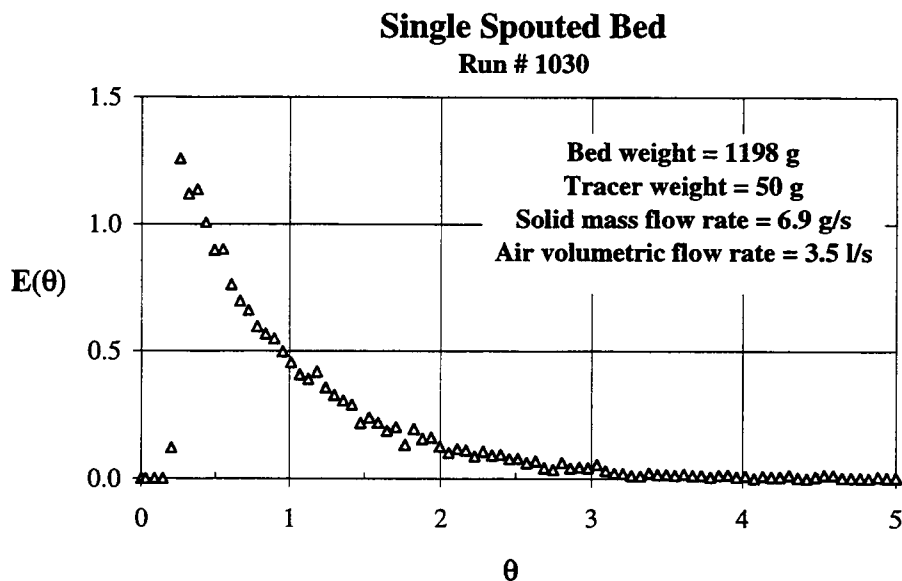


**Figure 3.2** Tank-in-series responses to a pulse tracer input for different numbers of tanks. Adapted from Levenspiel (1993).

Figure 3.2 illustrates the RTD for various numbers of stages. It should be noted that on increasing the number of stages, the uniformity of solids residence time also increases, approaching plug-flow behavior as this number becomes very large.

### 3.3 Compartment Model

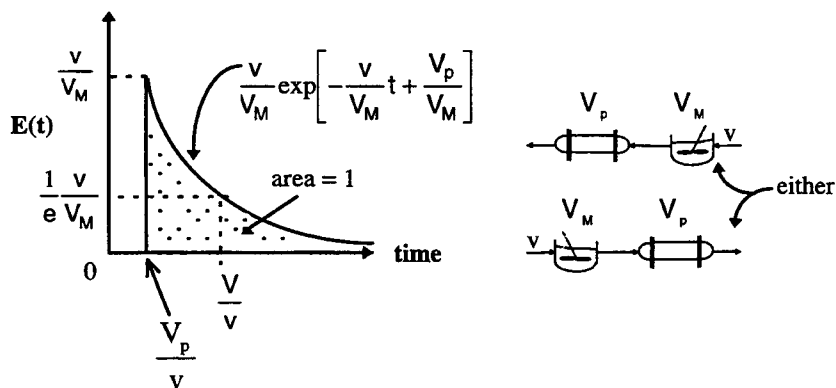
Figure 3.3 shows the actual  $E(\theta)$  curve obtained in one of our stimulus-response experiments with a single-stage spouted bed with draft tube.



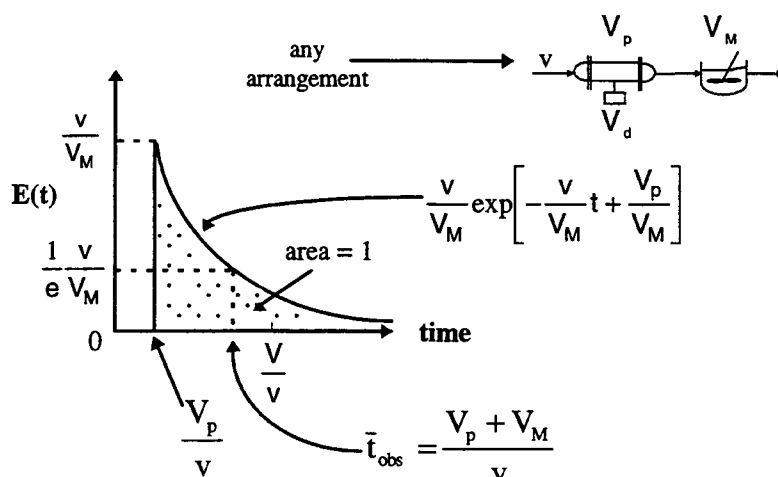
**Figure 3.3**  $E(\theta)$  curve obtained from measured concentrations

Clearly, the shape of this curve suggest that the assumption of a “perfect solid mixing behavior” is not entirely correct for this case. Fortunately, there are several other alternatives to describe what is really happening in this situation. A real vessel might be modeled by different combinations of “ideal” vessels. As was mentioned earlier, two types of ideal flow are commonly used as limiting cases of flow patterns: the “plug” or “piston” flow or the “perfectly mixed” flow. Often, flow patterns found in actual vessels,

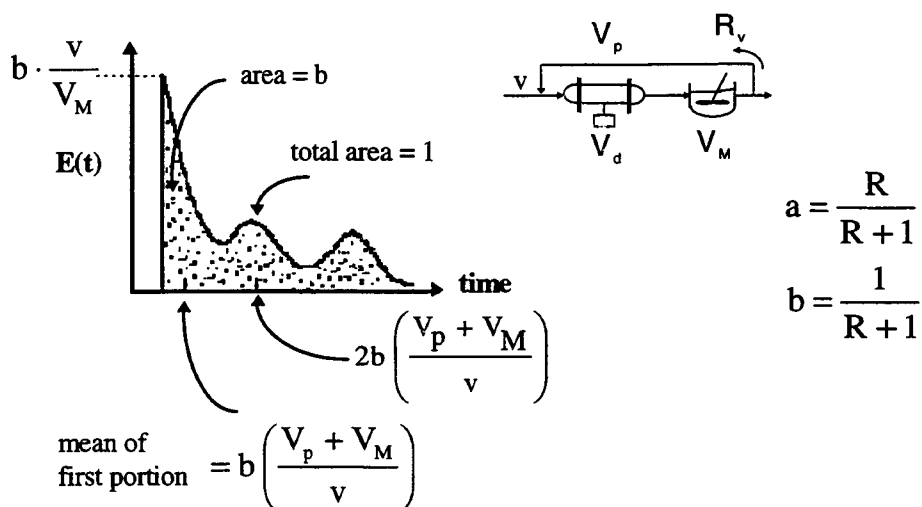
lie between these ideal flow behaviors. According to Levenspiel (1993), the "compartment models" consider an almost unlimited number of combinations that could be made, and as an example, he presents a wide variety of models with their characteristic  $E(\theta)$  curves. Several elements of flow patterns could be included: *channeling* (termed *bypassing*), when part of the solids slip or pass through the vessel considerably faster than others do; *stagnant pockets* of solids (termed *dead space*), representing regions with extremely poor contact between solids and gas (considerable bypassing is an indication of poor design and is not desirable since the stagnant regions reduce the effective or useful volume); and *recycling*, when a certain amount of solids is recirculated (in general a desirable characteristic in dealing with drying operations and/or autocatalytic or autothermal reactions). Figures 3.4, 3.5, and 3.6 show some possible flow models that could give a better explanation or be a base for the good development of a new model that can successfully describe the actual situation depicted in Figure 3.3. Levenspiel (1993) and Fogler (1992) show that for the case of plug flow and ideal mixed tank in series, no matter where the CSTR occurs within the PF/CSTR vessel sequence, the same RTD results as long as the sum of the residence times in the two sections are the same.



**Figure 3.4**  $E(t)$  curve for plug flow and ideal mixed tank in series.  
Adapted from Levenspiel (1993).



**Figure 3.5**  $E(t)$  curve for plug flow, with dead space, and ideal mixed tank in series. Adapted from Levenspiel (1993).



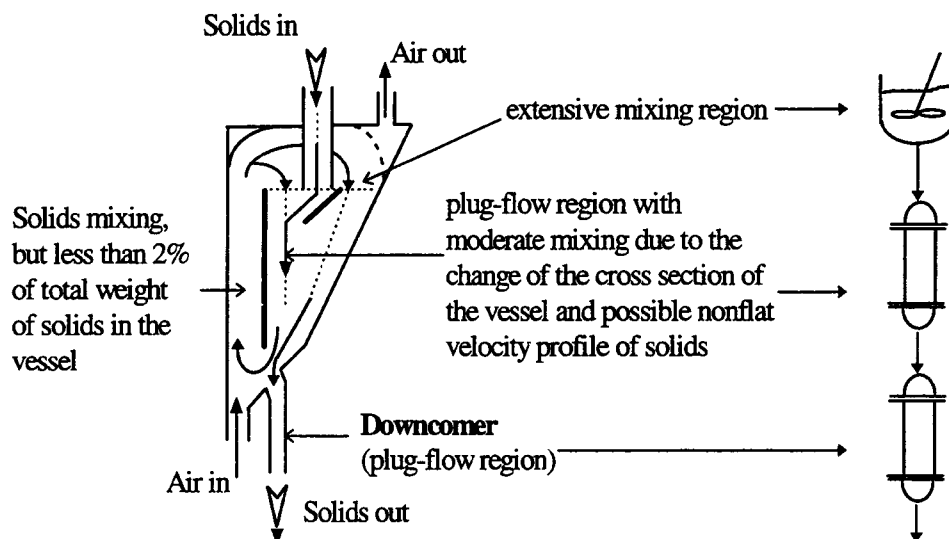
**Figure 3.6**  $E(t)$  curve for plug flow, with dead space, followed by ideal mixed tank in series, with recirculation. Adapted from Levenspiel (1993).



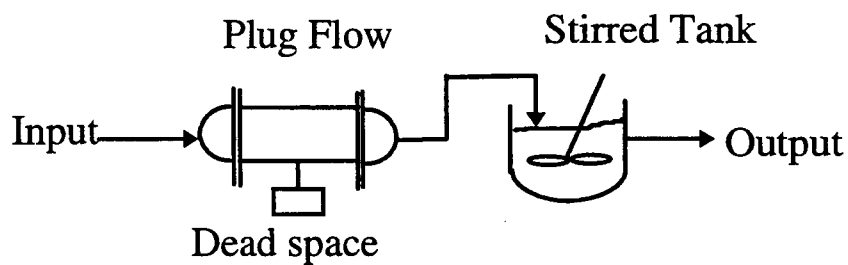
By comparing the  $E(t)$  experimental curves for the actual bed with the theoretical curves for different combinations of ideal vessels or compartments and flows, the “best” model (the one that best fits the data) can be found. According to Fogler (1992) “There appears to be only one almost inviolable rule for a reasonable model of a nonideal vessel: The maximum number of adjustable parameters in the model is two”. If a model with more than two adjustable variables is used then the modeling process probably becomes an exercise in curve fitting.

Our experimental system, as will be shown in Chapter 4, is compounded of vessel(s) and downcomer(s). Figure 3.3 reveals that the first data points are a collection of zero concentration values. This may be modeled as a plug-flow vessel (PFV), a type of flow expected in a downcomer. After these initial points, we recognize that there is a highly agitated zone, occurring within each vessel/stage, which can be modeled as a perfectly (ideal) mixed continuous stirred tank vessel (CSTV). Also, as will be shown later in this thesis, only runs at very low gas flow rates combined with high flow rate of solids, show a difference between the mean residence time, “ $\tau$ “, and “ $\tau_{\text{obs}}$ ” computed from the experimental data. This implies, as was mentioned before, the presence of stagnant pockets of solids for those flow conditions. According to Levenspiel (1963), this dead space can be assigned to either the plug-flow vessel or to the CSTV. Figure 3.7 shows a diagram of the designed single-stage spouted bed and the observed flow regions.

Mixing occurring in the plug-flow region is lumped with mixed region in order to reduce the number of parameters in the model. Similarly, all plug-flow regions (within the vessel and in the downcomer) can be lumped in a single larger plug-flow vessel as shown by Levenspiel (1993). Thus, this type of single-spouted bed may be modeled as a plug-flow vessel, with dead space, in series with a CSTV (see Figure 3.8).



**Figure 3.7** Observed flow regions



**Figure 3.8** A possible model for the data shown on Figure 3.3.

For this situation, it can be shown that

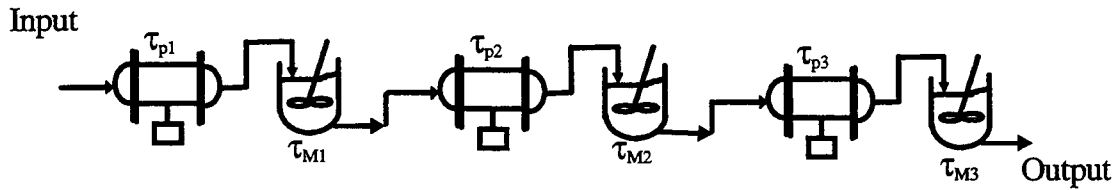
$$\left. \begin{aligned} E(t) &= 0 && \text{for } t < \tau_p \\ E(t) &= \frac{1}{\tau_M} \exp\left[\frac{-(t - \tau_p)}{\tau_M}\right] && \text{for } t \geq \tau_p \end{aligned} \right\} \quad (3.11)$$

where “ $\tau_p$ ” and “ $\tau_M$ ” represent the mean residence time of the plug-flow vessel and the ideal CSTV respectively.

If the assumption of *identical* stages is made, then self-convolution of eq. (3.11) yields the  $E(t)$  expression for the three-stage column,

$$\left. \begin{aligned} E(t) &= 0 && t < 3\tau_{pi} \\ E(t) &= (1/2)(1/\tau_{Mi}^3)(t - 3\tau_{pi})^2 \exp\{-(t - 3\tau_{pi})/\tau_{Mi}\} && t \geq 3\tau_{pi} \end{aligned} \right\} \quad (3.12)$$

where “ $\tau_{Mi}$ ” and “ $\tau_{pi}$ ” represent the mean residence time of each plug-flow vessel and each ideal CSTV respectively (see Figure 3.9).



**Figure 3.9** A possible model for a three-stage column of spouted beds.

## **CHAPTER 4**

### **EXPERIMENTAL EQUIPMENT DESIGN**

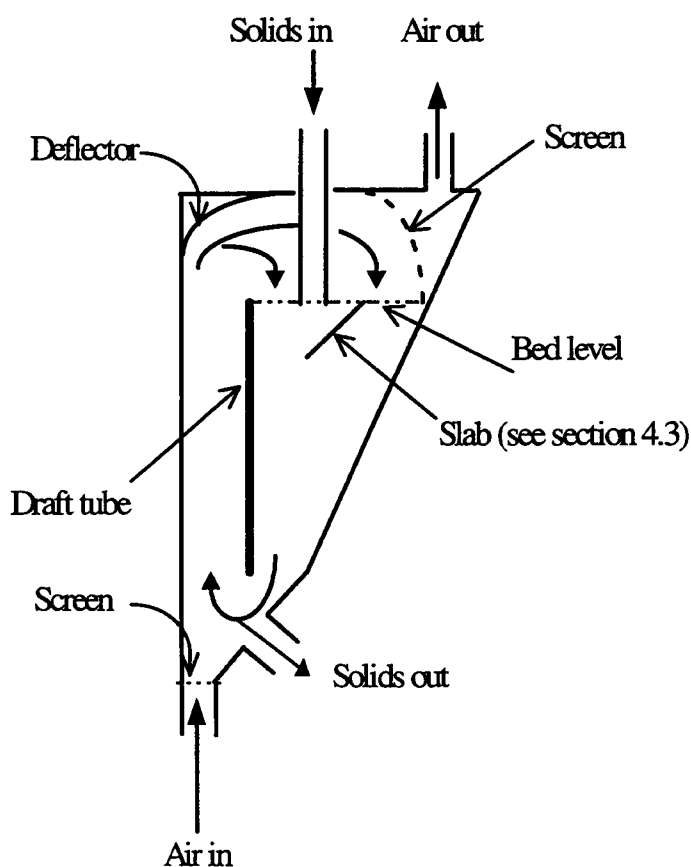
In Chapter 2, few multistage systems of spouted bed designs were presented and discussed. It was shown that all of them have problems of a similar nature, i.e. lack of stability, intermittent operation, improper feeding and discharging of solids, and high pressure drop. Our main objective and a goal is therefore to develop a design for a system of multistage spouted beds, capable of simple, continuous, stable operation, with very low pressure drop. In addition to that, the entire focus of many other experiments with both the single spouted bed and the multistage system is to define a model capable of predicting the behavior of solids in a vessel in a comparable situation.

#### **4.1 Geometry Of The Vessels**

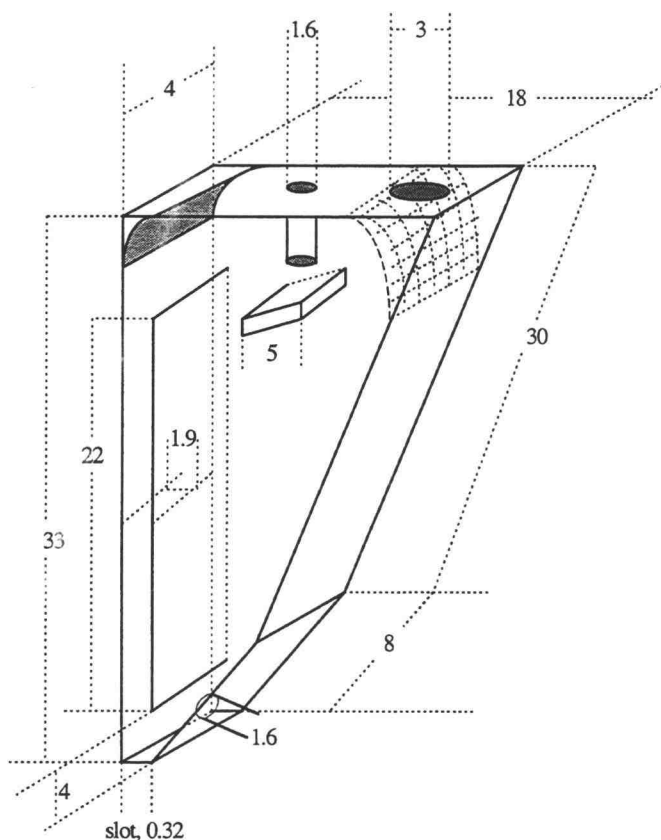
Based on general considerations typically explored in literature, a single spouted bed with draft tube was designed. In the absence of any applicable theoretical and/or deterministic guidance, the objective of an "adequate design" of the spouted bed is to obtain a very intensive particle circulation with no dead zones within the bed. Variables such as "particle attrition", "minimum spouting velocity", "maximum spoutable bed depth", and the like, are not considered here. Consequently, greater emphasis is placed on the geometry of the bed and on the simplicity of its operation. In order to decide which bed design is "better", a series of experiments were conducted changing key parameters such as: height, thickness and "cone angle", size and location of the draft tube, location, shape and dimensions of inlets and outlets, ways of controlling hold up of solid particles, and determination of some operating variables such as: pressure drop, gas velocity, and solid-flow rate.

For construction, operation, control, and simplicity in scale-up, a “two-dimensional”, half-rectangular vessel was preferred. For better scrutiny of the movement of solids in all experiments, the vessels and every connection between them were made of plexiglass. The particular geometry and measurements -shown in Figures 4.1 and 4.2- were determined after analyzing several experiments in which we were looking for an intensive movement of particles, with limited dead zones within the vessel, and stable spouting operation.

A narrow screened slot running across the bottom of the vessel lets the spouting gas (air) enter into the bed. To avoid particles coming into the air pipes, small screens were appropriately installed.



**Figure 4.1** Diagram of the designed vessel showing input/output streams of air and solids.



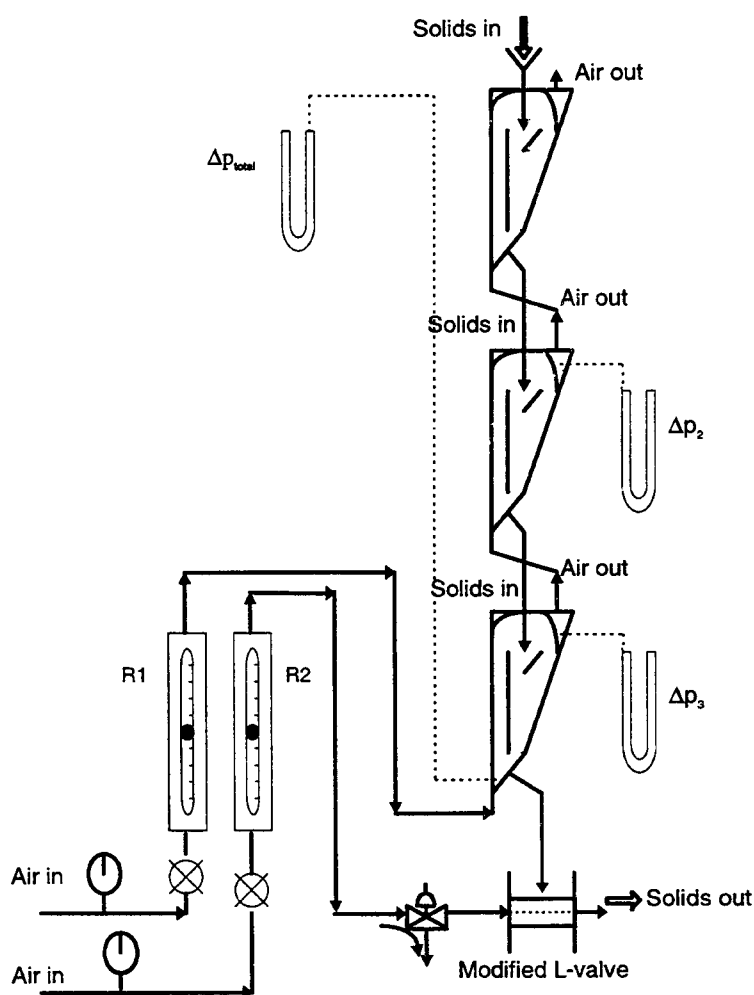
**Figure 4.2** Diagram of the designed vessel showing important measurements in cm.

## 4.2 Interconnection of the Stages

The multistage system was constructed using three *identical* spouted beds (see Appendix E for corresponding test) placed one upon the other, and connected with plexiglass tubes for flow of ascending air and descending solids. The diameter of the air pipes was chosen concurrent to the thickness of the vessel, and with the objective of achieving a low pressure drop. On the other hand, the diameter of the tubes for solids circulation was limited by the necessary free space between the pipe and the walls of the

vessel. The length of the tubes for solids circulation, was determined such that a continuous operation could be achieved at the maximum pressure drop within the system.

Figure 4.3 shows the three-stage spouted bed system used in our experiments. The addition of a draft tube to each stage allows the operation at very low pressure drop per stage ( $\Delta P_{\max} \approx 15$  cm of water/stage). Consequently, there should be practically no limitation in the number of stages that could be used, nor in the maximum spoutable bed height. Also, the recirculation of solids within each stage was improved, as expected.



**Figure 4.3** Three-stage spouted bed configuration

### 4.3 Feeding/Discharging. L-valve.

Special attention in the design was given to self controlled-hold-up of particles within the vessel. Consequently, location of the solids inlet is crucial. If solids are to enter into a “moving bed zone”, they will continuously keep flowing into the bed, no matter how deeply the feeding pipe penetrates; however, if solid particles coming into the vessel find a “packed bed zone”, they will cease to flow through the feeding pipe. In this design, shown in Figures 4.1 and 4.2, the internal configuration allows continuous operation with a uniform level of solids -at fixed operating conditions- within the vessel.

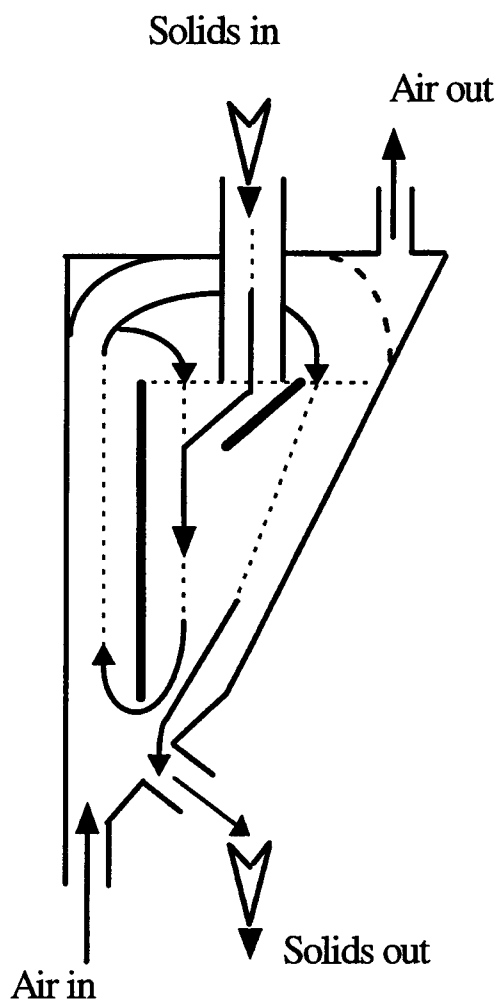
A small (5 x 4 cm) angled slab of plexiglass, located close to the inlet pipe for solids, provides the necessary packed bed zone of solids. This allows a constant level of solids within the bed. The slab angle is such that it forces the incoming solids to follow a path close to the wall of the draft tube. An increase of the probability of recirculation of solids within the vessel is then achieved.

Figure 4.4 shows the typical solid trajectory observed in most experiments. The vessel geometry, the position of the draft tube, and the angled slab, are designed to provide good circulatory movement of solids within the vessel. The size of the dead space is found to be negligible for almost all working conditions, and it can be observed that solids complete at least one full cycle within the vessel before exiting.

Discharging solid particles out of the one stage or three-stage unit is also a very simple and efficient operation. It requires no moving parts and/or complex mechanical devices. In this design, the solids are continuously withdrawn from the vessel (the bottom vessel in the case of the three-stage unit) through a modified “L-valve”. This valve works with compressed air as a “pushing fluid”, and plays an important role since it is a simple way of driving the solids out of the system as shown by Geldart and Jones (1991).

Although it has not yet been thoroughly documented, we recommend a pulsating valve for feeding air to the L-valve. Visual observations show that, compared to constant pressure, a more uniform flow of solids is obtained when oscillating air pressure is used. This modification of the L-valve transforms it into a “spitting valve”, which should be tested in further studies.



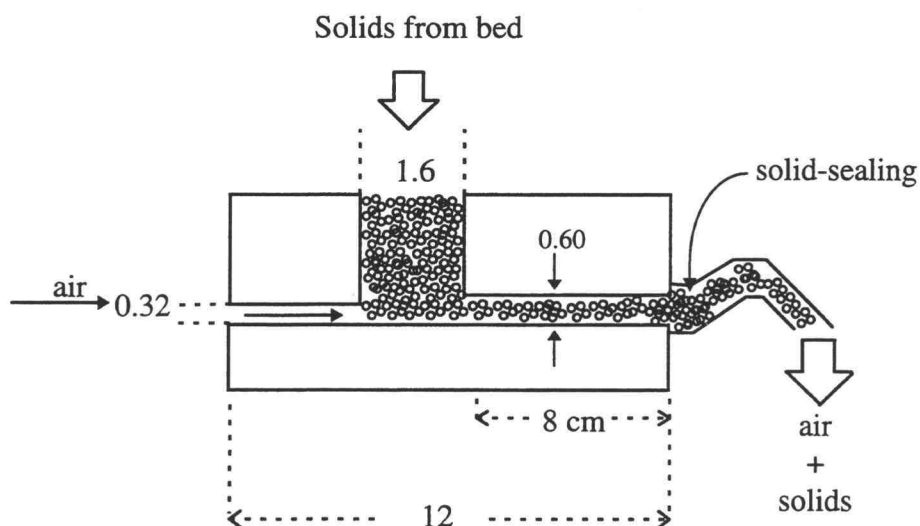


**Figure 4.4** Observed solid circulation in a single-stage unit.

One last adjustment to a typical L-valve configuration was confirmed to be essential. When pressure within the system increases, solid particles are being pushed out by the air *inside* of the vessel. This causes a continuous flow of solids out of the system due to this *extra* force. Moreover, this force could be really important, especially in the case of the three-stage operation. Unless an airtight sealing is provided, the outflow of

particles becomes unpredictable, and control is no longer achieved. We found that just a slight arching of the outlet pipe of the L-valve provided the sealing wanted.

Figure 4.5 shows a schematic diagram of the modified L-valve with all relevant dimensions in centimeters.



**Figure 4.5** Diagram of the modified L-valve.

The mean solids residence time in the valve is negligible small, since the total weight of particles in this device is less than 4 grams. Since no written information was found describing similar devices, more research should be done on this type of modified L-valve (here called “*spitting valve*”), its characteristics, and mathematical modeling.

## CHAPTER 5

### EXPERIMENTAL MEASUREMENTS AND PROCEDURES

In order to meet budget limitations, we adapt for use experimental methods and procedures not requiring expensive and/or sophisticated laboratory equipment and materials. Accordingly, the criteria behind most experimental procedures and selected materials were to acquire reliable results at the lowest possible cost.

#### 5.1 Spouted Bed Material

Glass beads were used as the bed solids throughout all the experiments. To estimate their average size, we first classified them using sieve trays. After this first gross classification, we measured particle diameters using digital calipers. Samples of hundreds of particles, chosen at random, were used for this evaluation. Following this procedure, the average diameter turns out to be,  $D_{ave} = 1.78 \text{ mm}$  ( $\sigma^2 = 0.0140$ ).

The average density of particles was determined with the aid of an appropriate picnometer. The density of the solids obtained in this manner was,  $\rho_s = 2.64 \text{ grams/cm}^3$  ( $\sigma^2 = 0.0176$ ).

#### 5.2 Tracer

The residence time distribution (RTD) for the solids can be determined easily and directly by the so-called “*stimulus-response*” technique. With this method, the RTD is experimentally obtained by injecting an inert particle, called a *tracer*, into the inlet stream of solids at time  $t = 0$ , and then measuring the tracer concentration in the effluent stream of the vessel as a function of time. According to Levenspiel (1972), “any material that can

be detected and which does not disturb the flow pattern in the vessel can be used as tracer". Moreover, the tracer has to meet the following general characteristics:

1. It should be "miscible" in all proportions, and have physical properties similar to all solid particles within the vessel under investigation. If the experiment involves more than one phase, then the tracer should stay in the phase of interest.
2. It has to be nonreactive and perfectly detectable even in very small concentrations.
3. The detection device and the tracer itself have to be unquestionably inexpensive.

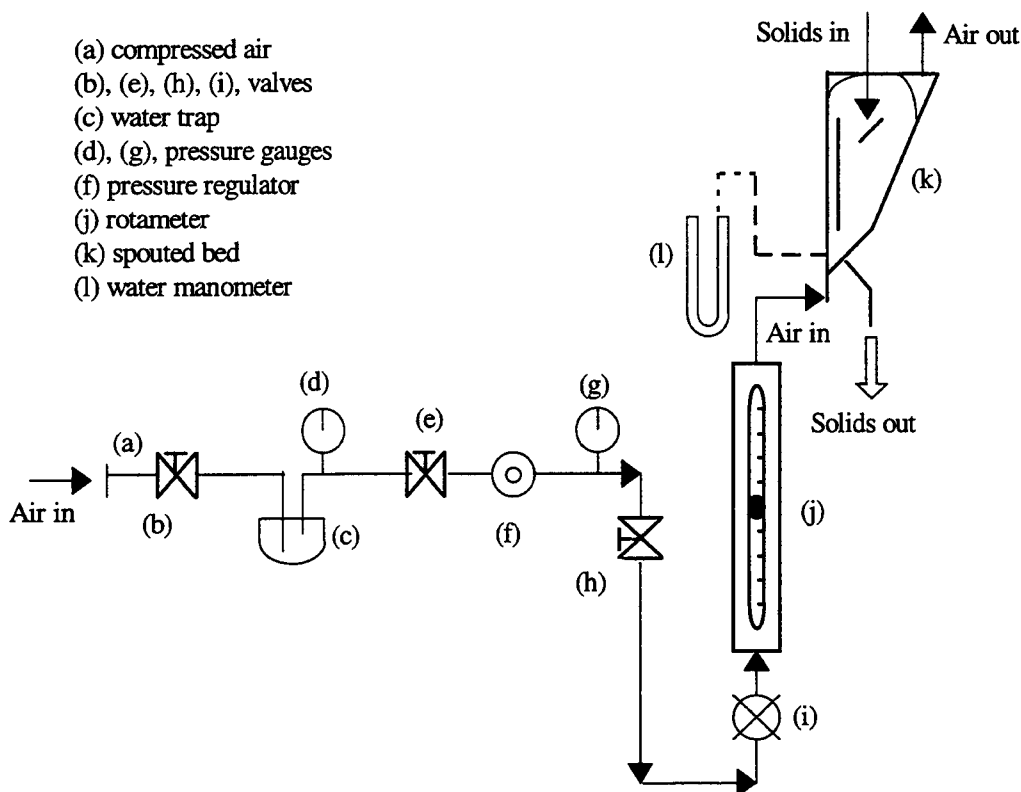
Consequently, the tracer was prepared by using the same glass beads adopted as a bed material. The solid particles were coated with permanent marker red ink.

### 5.3 Experimental Procedures

The experimental setup is shown in Figure 5.1. The spouting fluid (air) is supplied from the high-pressure air system available in the laboratory. Before entering into the spouting vessel, air flows through a pressure regulator, equipped with a water trap and a filter, and a calibrated rotameter. The air inlet to the vessel is a screened, narrow slot (0.32cm x 4cm). Pressure drop for each stage is measured with a U-tube water manometer conveniently installed.

The solid particles -spouted bed material- are continuously fed into the system (one or three stages) by gravity from a hopper located above the system. They may also be continuously withdrawn from the bottom vessel through the modified L-valve.

The air to the modified L-valve also comes from the building high-pressure pipe line. Likewise, it flows through a pressure regulator, filter, water trap, and rotameter assemblage before entering to a *solenoid* valve. The function of this valve is to provide a controlled, pulsating flow of air to the modified L-valve.



**Figure 5.1.** Experimental set up for the RTD of solids in a single-stage unit.

### 5.3.1 Preliminary Steps

For each experiment several preliminary steps were taken:

1. Prepare solid particles (i.e, glass beads) for the experiment. This requires their treatment with fabric softener which instantly eliminates static electricity and prevents the static build-up that otherwise would produce an “extra-resistance” that would keep the solids from flowing through the pipes and/or vessels.
2. Visually inspect the air filter and water trap. Clean them if needed.
3. Pour solid particles into the vessel/column.
4. Weigh precise amount of tracer.

5. Set the solenoid valve for desired flow rate of solids.
6. Let air into the modified L-valve.
7. Let spouting air into the vessel/column. Set required gas flow rate.
8. Adjust, if needed, the ON/OFF percentage in solenoid valve, by taking and weighting several samples of solids coming out of the system to obtain a known flow rate of solids.
9. Allow enough time for the system to reach a steady-state regime.
10. Take necessary readings of all instruments (pressure drops, flow rates, ON/OFF %)
11. Measure level of solids within the vessel(s).
12. Estimate time of solids flowing per 10 cm length in pipes and within the vessel(s).

### **5.3.2 Running The RTD Experiment**

After all preliminary set-up procedures are complete, we proceed as follows:

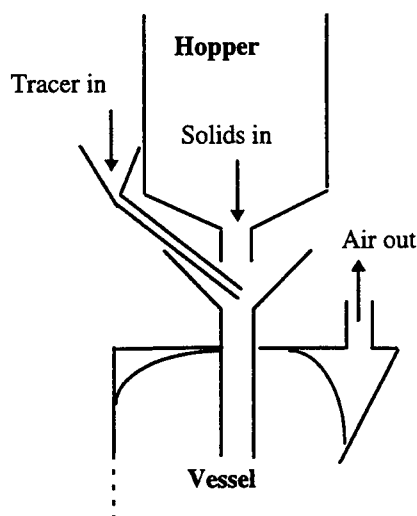
1. At time equal to zero ( $t = 0$ ) instantaneously introduce 50 grams of colored particles (tracer) into the system. Tracer particles enter the vessel together with the solids entering the system (see Figure 5.2). At the same time, start collecting samples at the exit of the modified L-valve .
2. Take samples at prescribed intervals of time.
3. When practically all tracer particles are out of the system, simultaneously stop the in/out flow of solids, and turn off the spouting gas.
4. Using a special container, collect the remainder of the solids by reestablishing only the solids flow out of the system.
5. The column is now empty again, ready for the next experiment.

### **5.3.3 Analytical Steps**

After collecting all samples from each experiment, the following steps are taken:

1. Obtain total weight of each sample and weight of the hold-up of the bed.

2. Colored particles (tracer) are separated from the rest of the particles in each sample.
3. Weigh tracer particles.
4. Separate colored particles in the hold-up of the bed and weigh them.

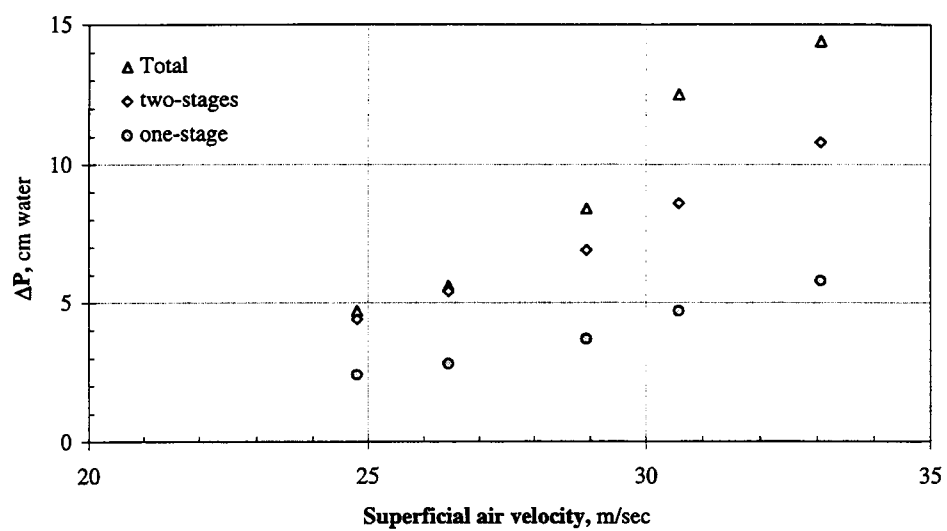


**Figure 5.2** Diagram showing how tracer particles are introduced into the system.

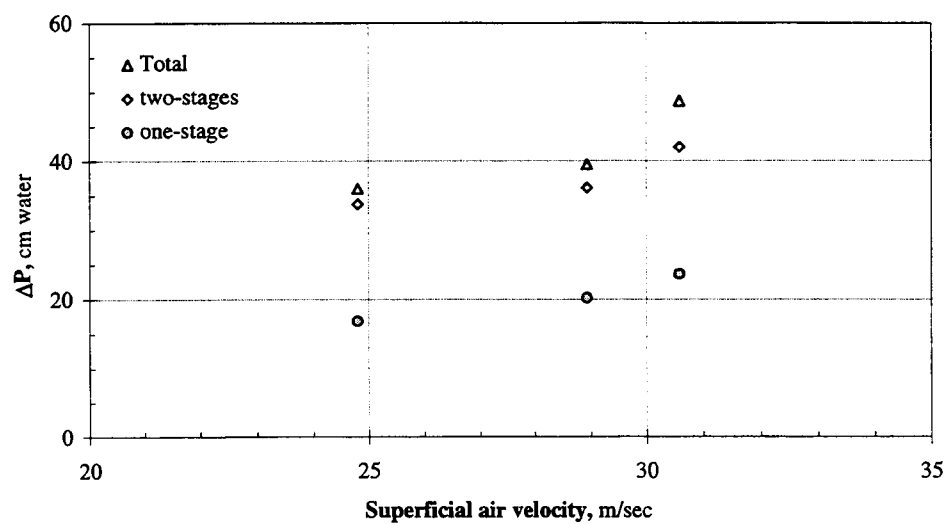
## 5.4 Experimental Plan

Once we were satisfied with the operating characteristics of the designed system (single-stage and three-stage column), in order to achieve all the aforementioned objectives of this research, the following experimental plan was conceived and put into practice:

- A. Determination of operating variables, such as: pressure drops, air superficial velocities, and gas flow rates. Results for a single-stage unit and for the three-stage column are shown in Figures 5.3 to 5.7. It is important to notice, in both cases, the resultant very low pressure drop due to the presence of the draft tube, and the  $\Delta P$  differences due to the location of the pressure ports (see Figure 4.3).

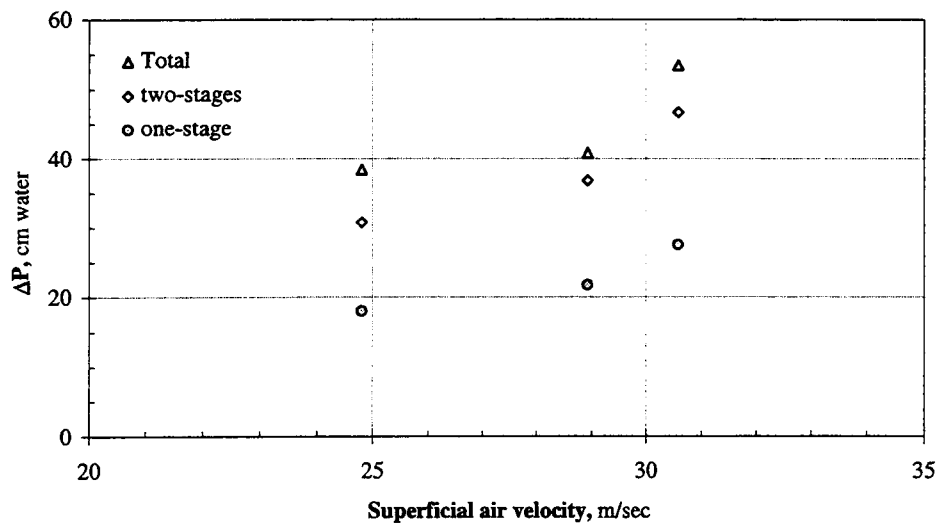


**Figure 5.3** Pressure drop for an empty column.

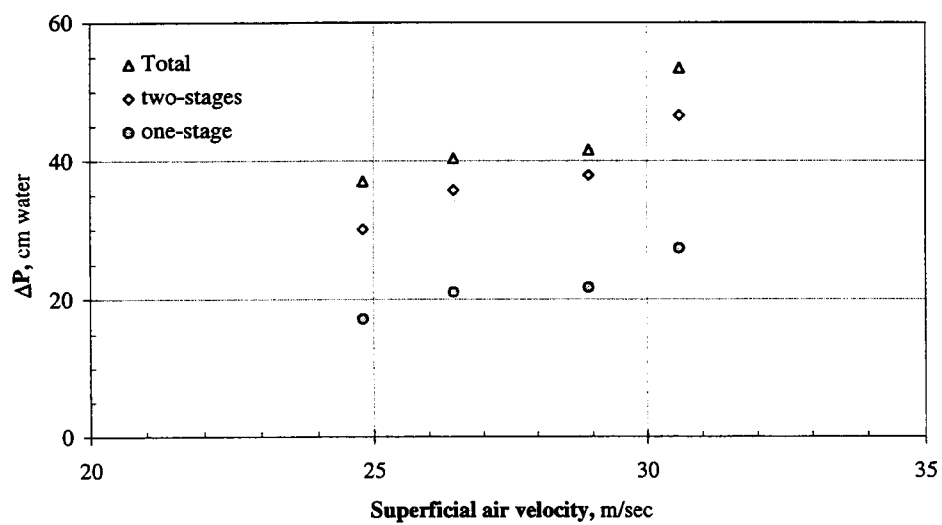


**Figure 5.4** Pressure drop for a SFR = 2 g/s.

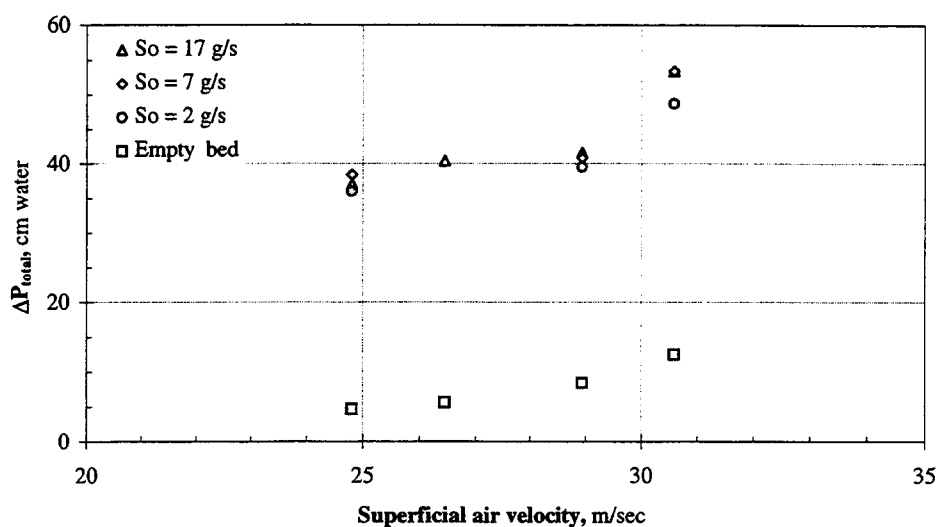




**Figure 5.5** Pressure drop for a SFR = 7 g/s.

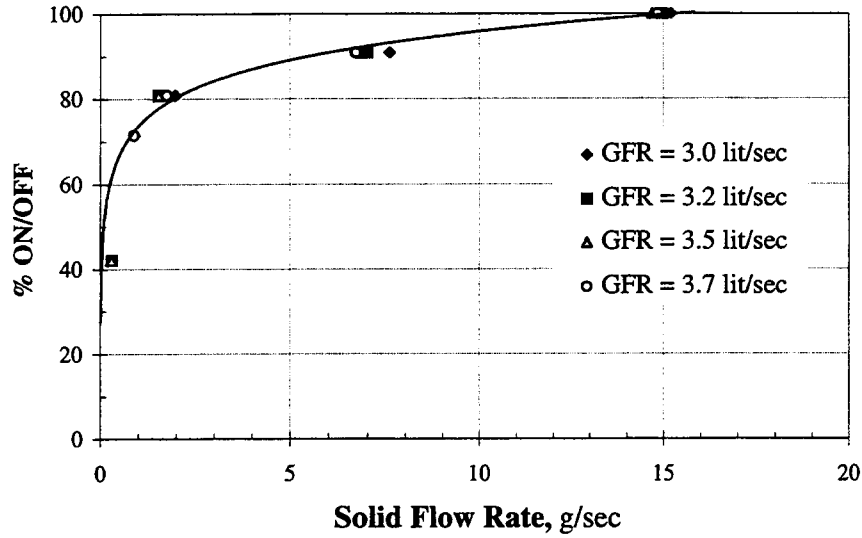


**Figure 5.6** Pressure drop for a SFR = 17 g/s.



**Figure 5.7** Total pressure drop for different solid flow rates.

B. Acquisition of information about the solid flow rate (SFR) for different ON/OFF percentages on the solenoid valve. As was mentioned before, the function of this valve is to provide a controlled, pulsating flow of air to the modified L-valve. Consequently, for a fixed gas flow rate fed to the *solenoid valve*, there is a certain amount of solids per unit time being pushed out of the system. Figure 5.8 shows the solid flow rate obtained for different ON/OFF percentages used at four different gas flow rates (GFR) within the unit. This graph shows that there is a maximum possible flow rate of solids when the air flow rate to the solenoid valve (pushing gas) is fixed. For the particular case of 0.55 liters/second of pushing gas used, the maximum solid flow rate (100 %ON/OFF) turns out to be approximately 15 grams/second for any GFR to the column.



**Figure 5.8** Modified L-valve behavior for a flow rate of 0.55 lit/sec of pushing gas.

C. Determination of the recirculation time of solids within each stage. This time was obtained using a video camera to film the movement of the solids inside the vessels for different gas flow rates. From this time, the solids recirculation rate for each stage, in grams/sec, is computed. Here the solids recirculation rate is defined as

$$\text{solids recirculation rate} = \frac{W_{\text{active}}}{t_R} \quad \left( \frac{\text{grams}}{\text{second}} \right) \quad (5.1)$$

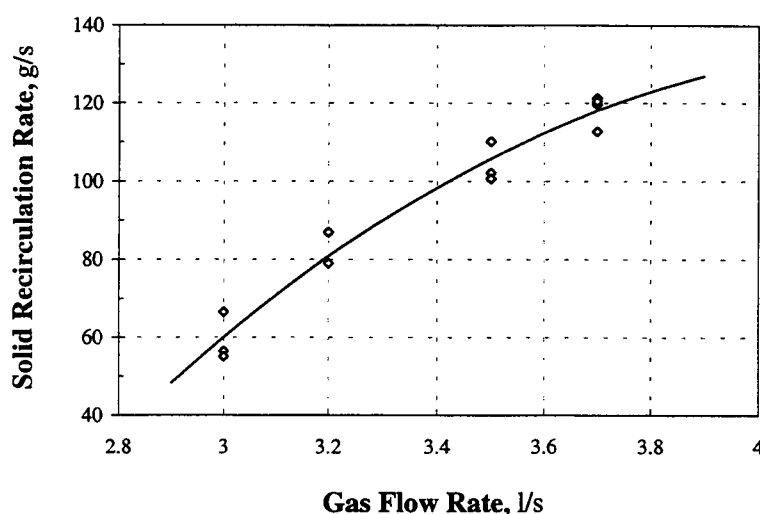
Where  $W_{\text{active}}$  is the weight in grams of solids that are truly recirculated within the vessel, and  $t_R$  is the measured recirculation time in seconds. Since

$$W_{\text{active}} = \tau_{\text{obs}} \times S_o \quad (5.2)$$

then

$$\text{solids recirculation rate} = \frac{\tau_{\text{obs}} \times S_o}{t_R} \quad \left( \frac{\text{grams}}{\text{second}} \right) \quad (5.3)$$

Results are shown in Figure 5.9. According to this figure, increasing the gas flow rate will also cause an increase in the solids recirculation rate within the bed as expected. Also, when the recirculation time is short, we have many recirculations per mean residence time of solids within the vessel and, therefore, a closer approach to CSTR behavior.



**Figure 5.9** Recirculation rate of solids

D. Investigation of the RTD of solids for different solid flow rate and gas flow rate conditions. Table 5.1 and 5.2 show all combinations used of these two variables for the single-stage spouted bed unit and for the three-stage column experiments. Four different gas flow rates and three different solid flow rates were used. The range of these conditions was limited by the size characteristics of the system. Figures 5.10 to 5.23 show the results for the single-stage unit, and Figures 5.24 to 5.33 show the results for the three-stage column.

**Table 5.1** Combinations of gas and solids flow rates used in the single-stage spouted bed unit.

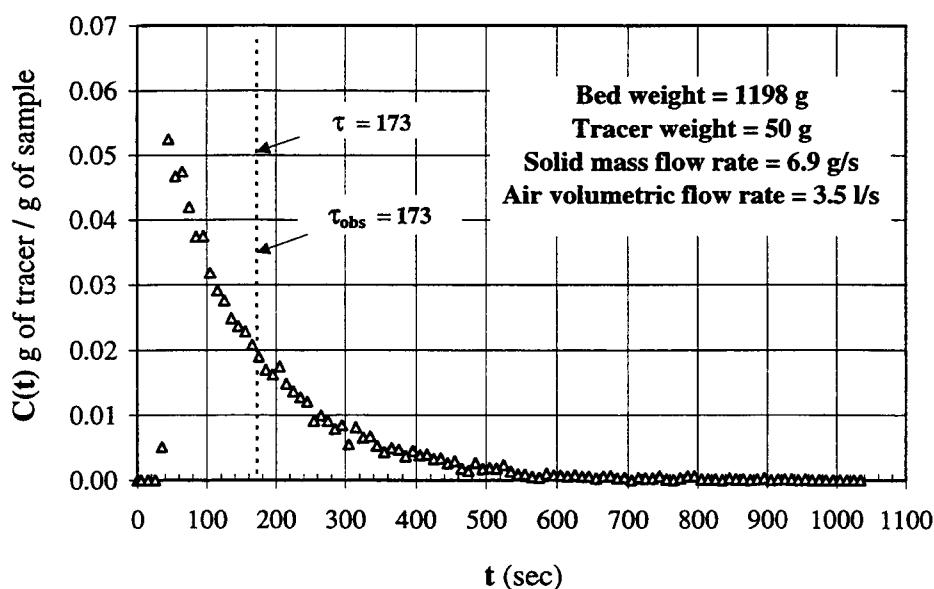
| F<br>L<br>O<br>W<br><br>O<br>F<br><br>S<br>O<br>L<br>I<br>D<br>S<br><br>↓<br><br>(grams/sec) | F L O W   O F   G A S                      →                      (lit/sec) |           |           |           |           |           |
|----------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------|-----------|-----------|-----------|-----------|-----------|
|                                                                                              |                                                                             | 0         | 3.0       | 3.2       | 3.5       | 3.7       |
|                                                                                              |                                                                             |           |           |           |           |           |
|                                                                                              | 2.7                                                                         |           | Run #1035 | Run #1037 | Run #1040 | Run #1041 |
|                                                                                              |                                                                             |           |           |           |           |           |
|                                                                                              | 6.1                                                                         | Run #1034 | Run #1031 | Run #1033 | Run #1030 | Run #1043 |
|                                                                                              |                                                                             |           |           |           |           |           |
|                                                                                              | 17.0                                                                        |           | Run #1036 | Run #1042 | Run #1038 | Run #1032 |
|                                                                                              |                                                                             |           |           |           |           |           |
|                                                                                              |                                                                             |           |           |           |           |           |

**Table 5.2** Combinations of gas and solids flow rates used in the three-stage spouted bed column.

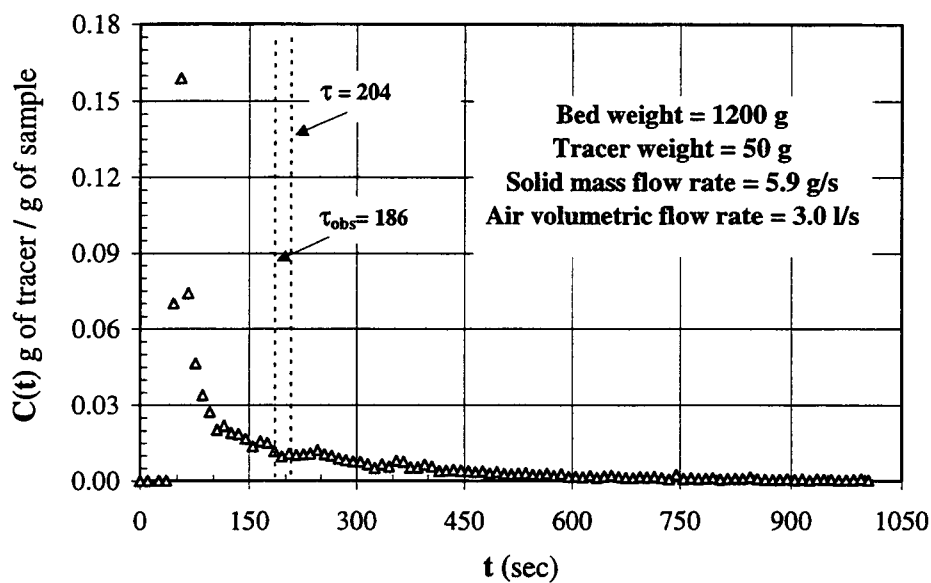
| F<br>L<br>O<br>W<br><br>O<br>F<br><br>S<br>O<br>L<br>I<br>D<br>S<br><br>↓<br><br>(grams/sec) | F L O W   O F   G A S   →   (lit/sec) |           |           |           |           |
|----------------------------------------------------------------------------------------------|---------------------------------------|-----------|-----------|-----------|-----------|
|                                                                                              |                                       | 0         | 3.0       | 3.5       | 3.7       |
|                                                                                              |                                       |           |           |           |           |
|                                                                                              | 2.0                                   |           | Run #2001 | Run #2002 | Run #2000 |
|                                                                                              |                                       |           |           |           |           |
|                                                                                              | 7.2                                   | Run #2008 | Run #2009 | Run #2004 | Run #2006 |
|                                                                                              |                                       |           |           |           |           |
|                                                                                              | 17.0                                  |           | Run #2007 | Run #2003 | Run #2005 |
|                                                                                              |                                       |           |           |           |           |
|                                                                                              |                                       |           |           |           |           |

## 5.5 Results

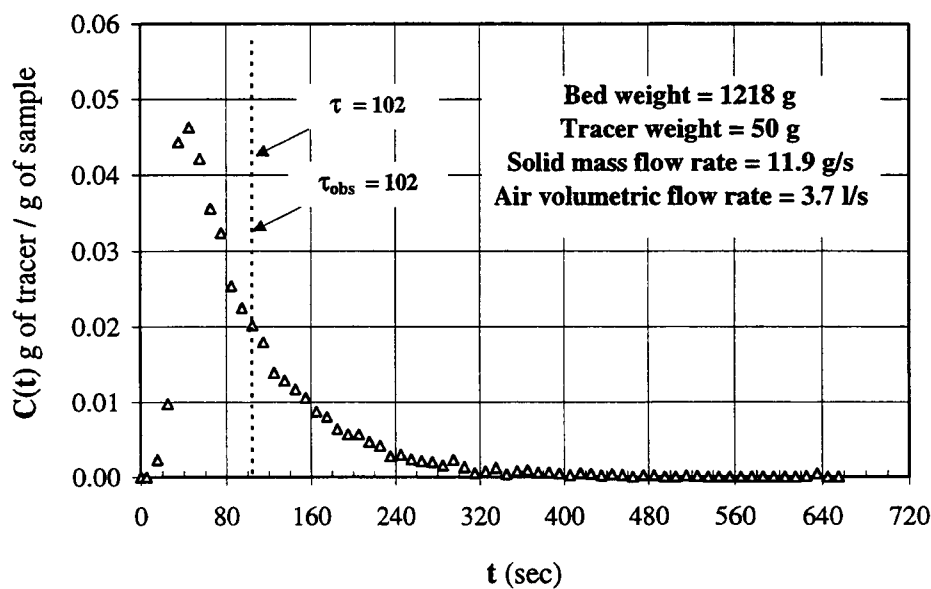
A total of 24 RTD experiments were carried out. Investigated operating variables or parameters were the spouting gas flow rate and the flow rate of solids. A range of gas (0 to 3.7 lit/sec) and solids (0 to 17.0 g/s) flow rates, were used for stimulus-response experiments. Three specific time indicators of solids within each stage were of particular interest: *residence time distribution*,  $E(t)$ , *mean residence time*,  $\tau$ , and *recirculation time*,  $\tau_R$ . Figures 5.10 to 5.33 show concentration-time data obtained from the RTD experiments. From the data of a tracer concentration-time curves for both single-stage unit and three-stage column, nearly all the desired system parameters can be obtained. Specific conclusions are drawn from these data in Chapters 6 and 7.



**Figure 5.10**  $C(t)$  curve of experiment #1030 (single-stage unit)

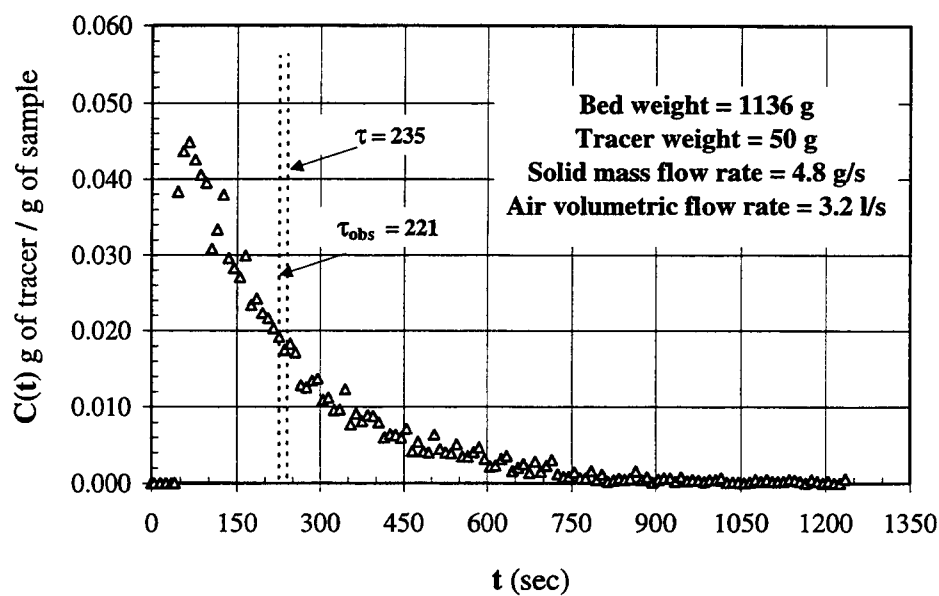


**Figure 5.11**  $C(t)$  curve of experiment #1031 (single-stage unit)

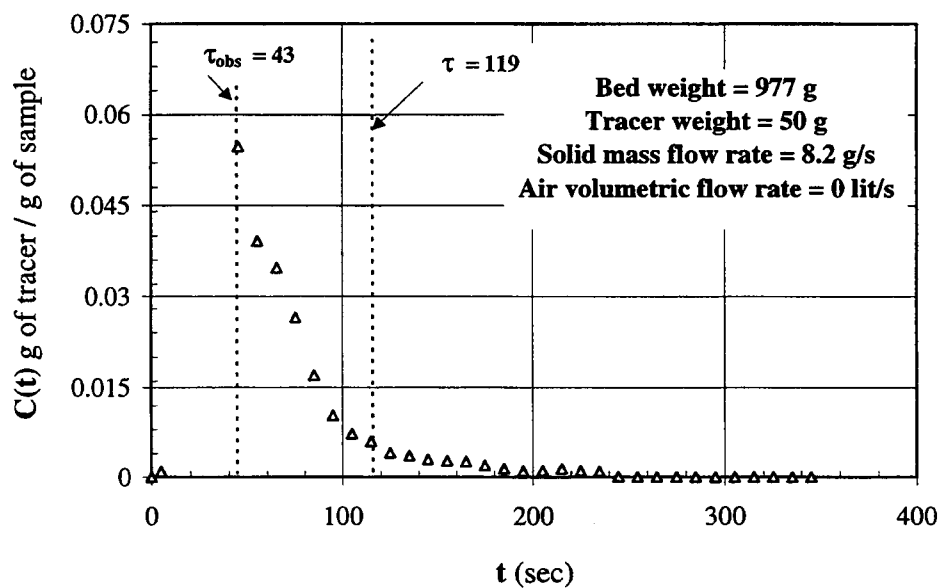


**Figure 5.12**  $C(t)$  curve of experiment #1032 (single-stage unit)

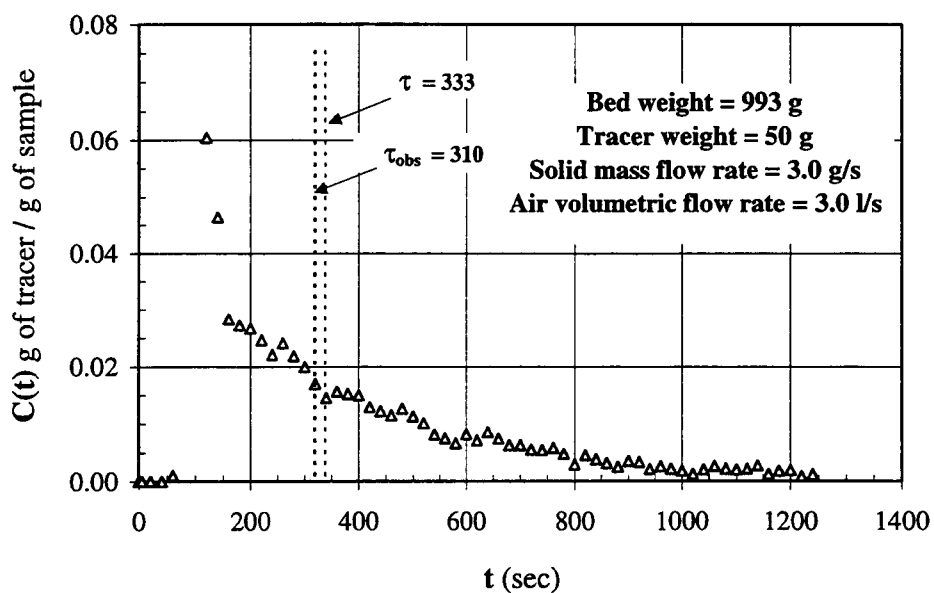




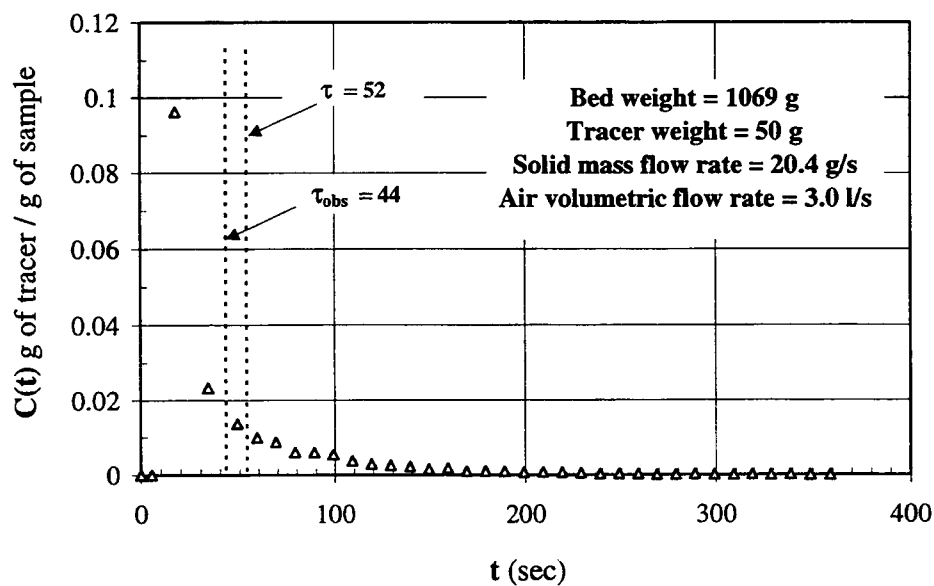
**Figure 5.13**  $C(t)$  curve of experiment #1033 (single-stage unit)



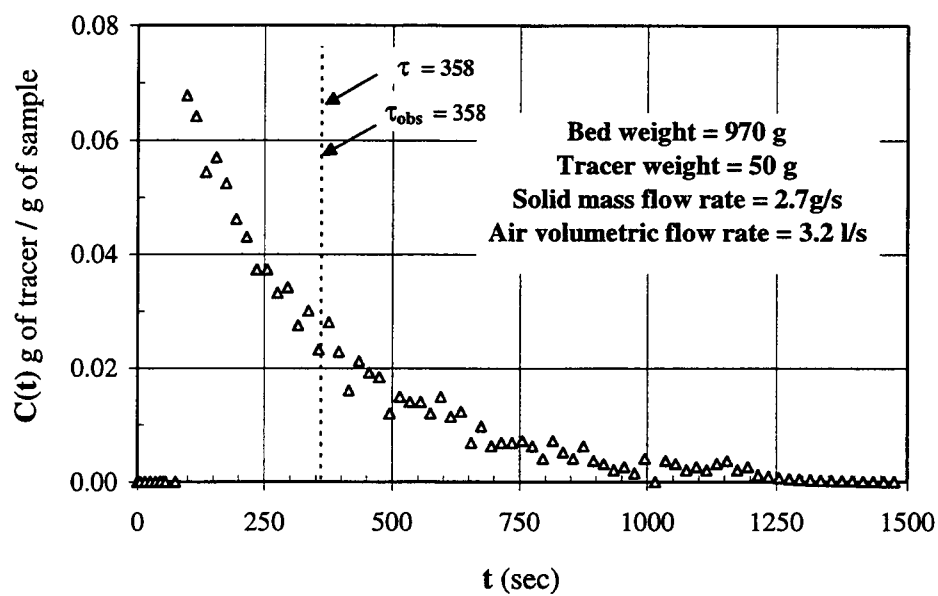
**Figure 5.14**  $C(t)$  curve of experiment #1034 (single-stage unit)



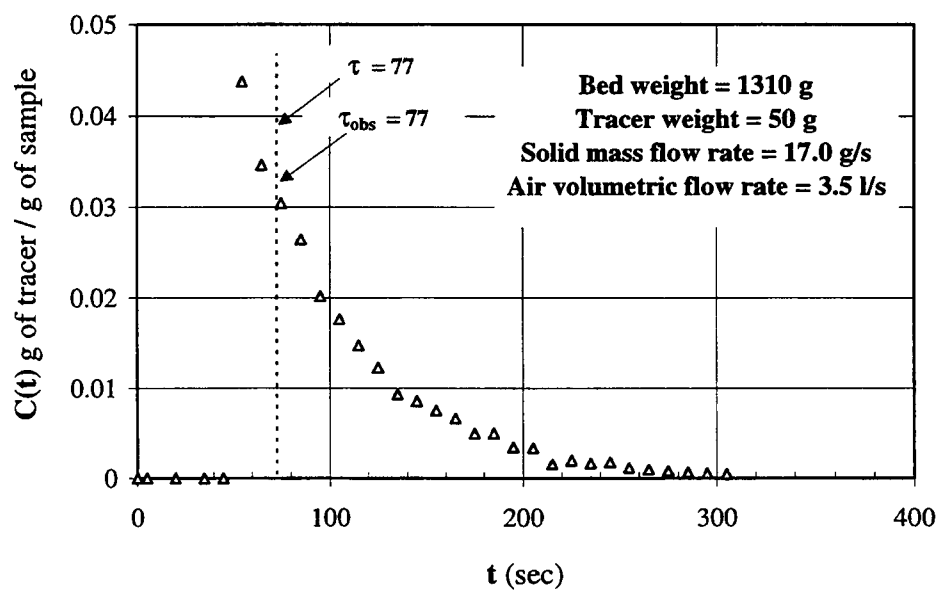
**Figure 5.15**  $C(t)$  curve of experiment #1035 (single-stage unit)



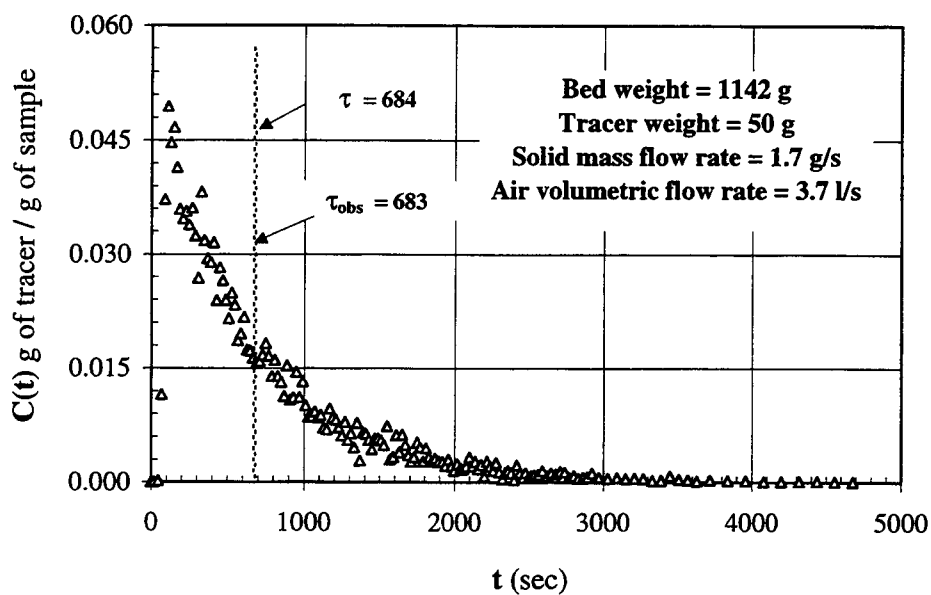
**Figure 5.16**  $C(t)$  curve of experiment #1036 (single-stage unit)



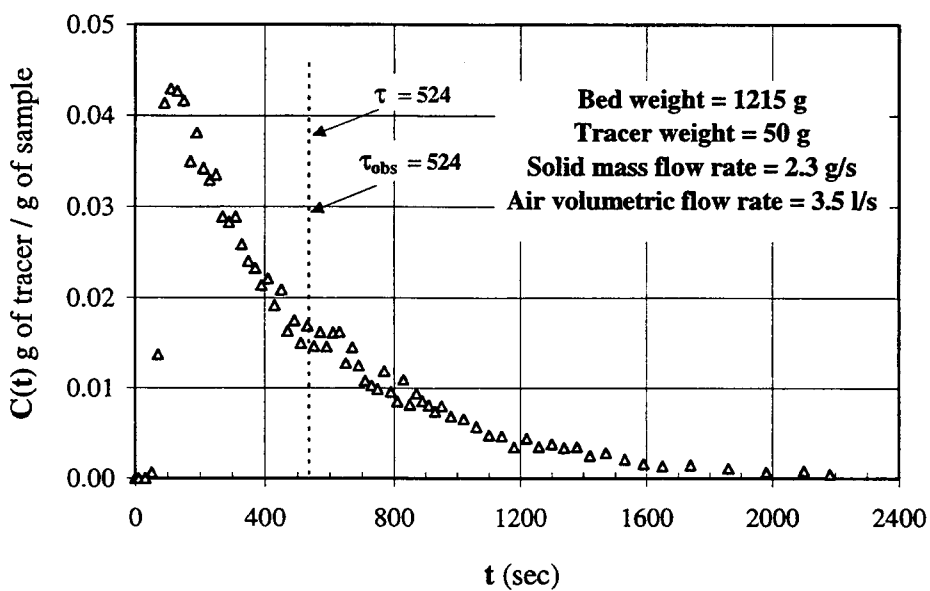
**Figure 5.17**  $C(t)$  curve of experiment #1037 (single-stage unit)



**Figure 5.18**  $C(t)$  curve of experiment #1038 (single-stage unit)



**Figure 5.19**  $C(t)$  curve of experiment #1039 (single-stage unit)



**Figure 5.20**  $C(t)$  curve of experiment #1040 (single-stage unit)

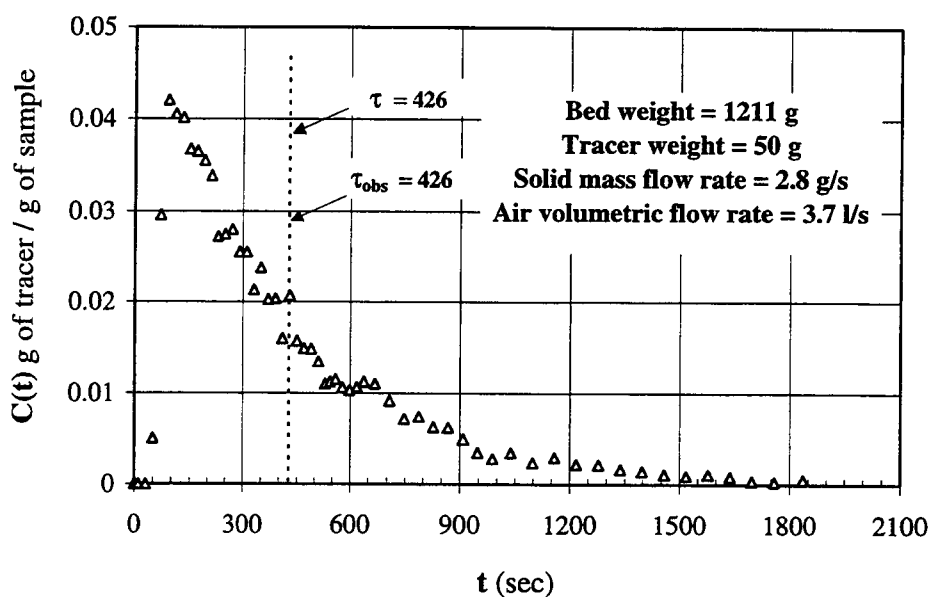


Figure 5.21  $C(t)$  curve of experiment #1041 (single-stage unit)

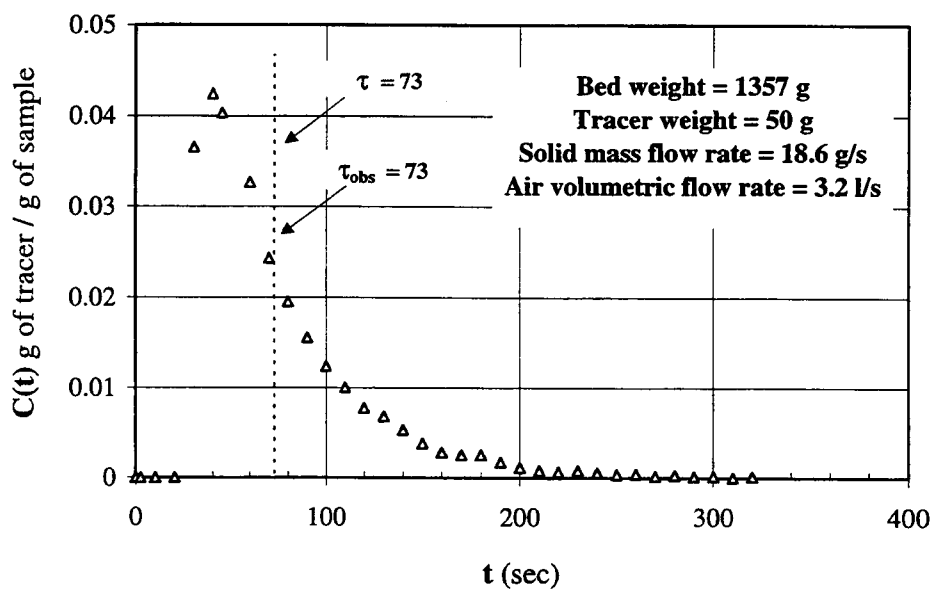
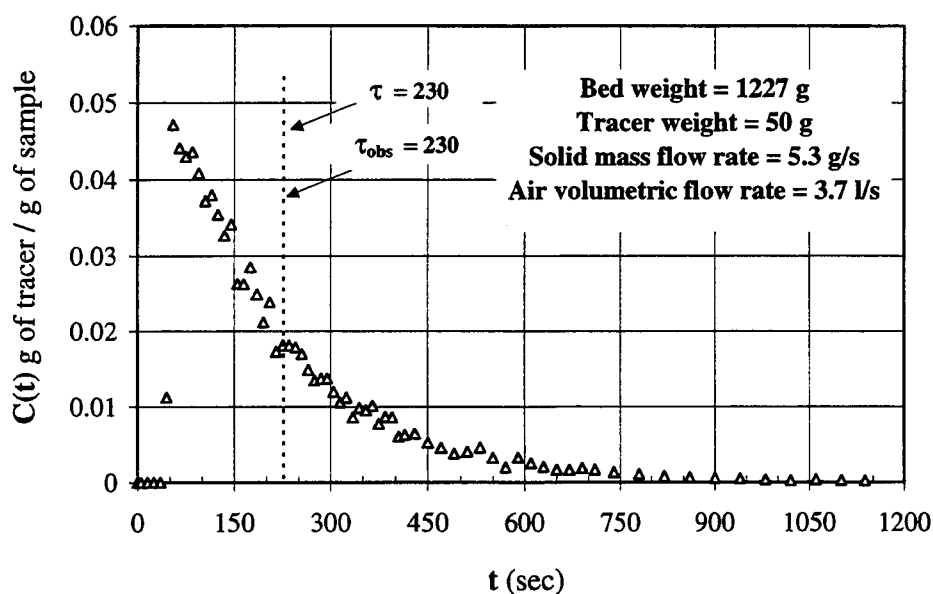
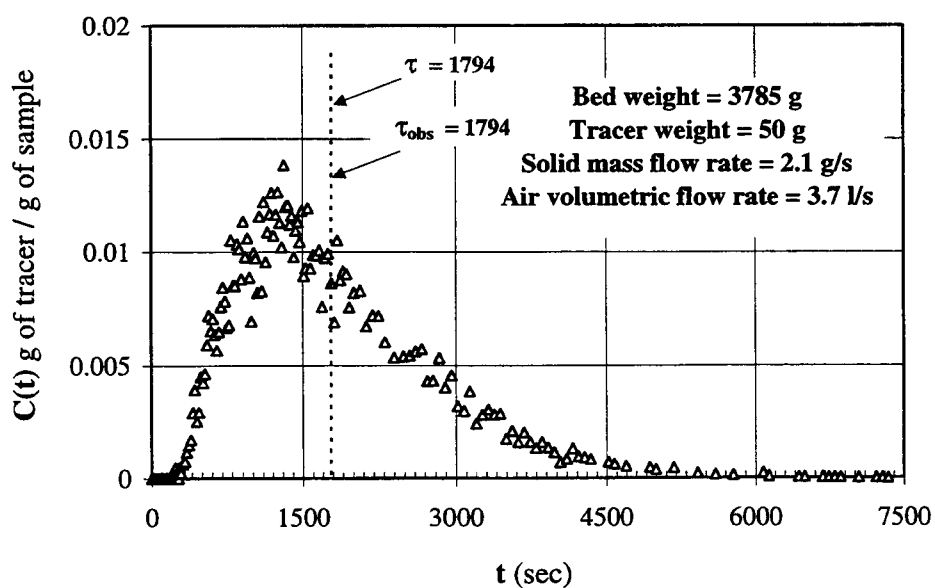


Figure 5.22  $C(t)$  curve of experiment #1042 (single-stage unit)



**Figure 5.23**  $C(t)$  curve of experiment #1043 (single-stage unit)



**Figure 5.24**  $C(t)$  curve of experiment #2000 (three-stage column)

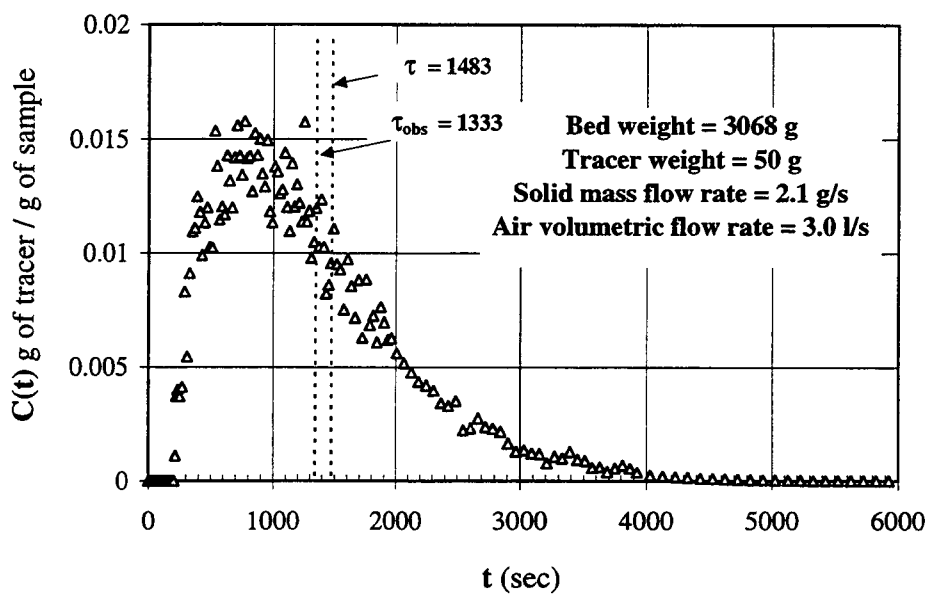


Figure 5.25  $C(t)$  curve of experiment #2001 (three-stage column)

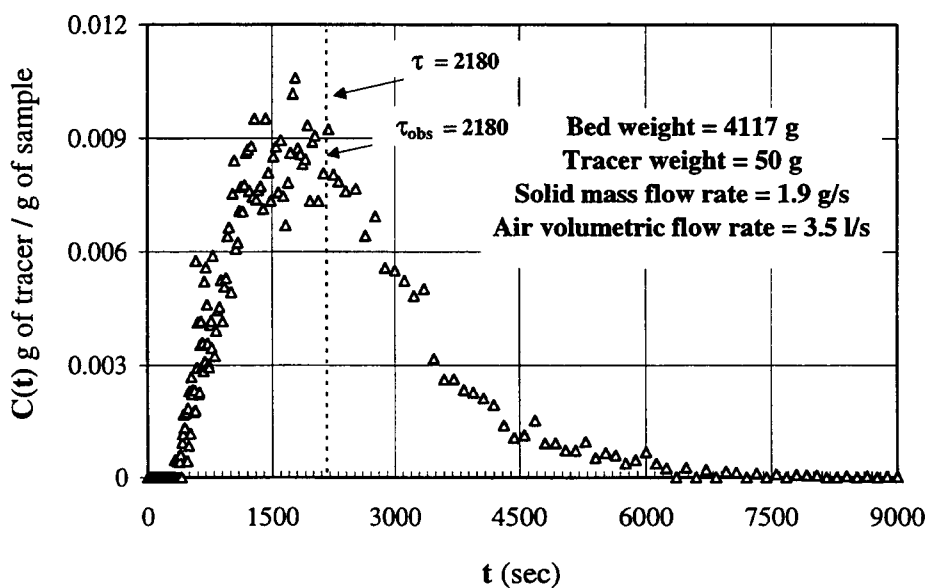
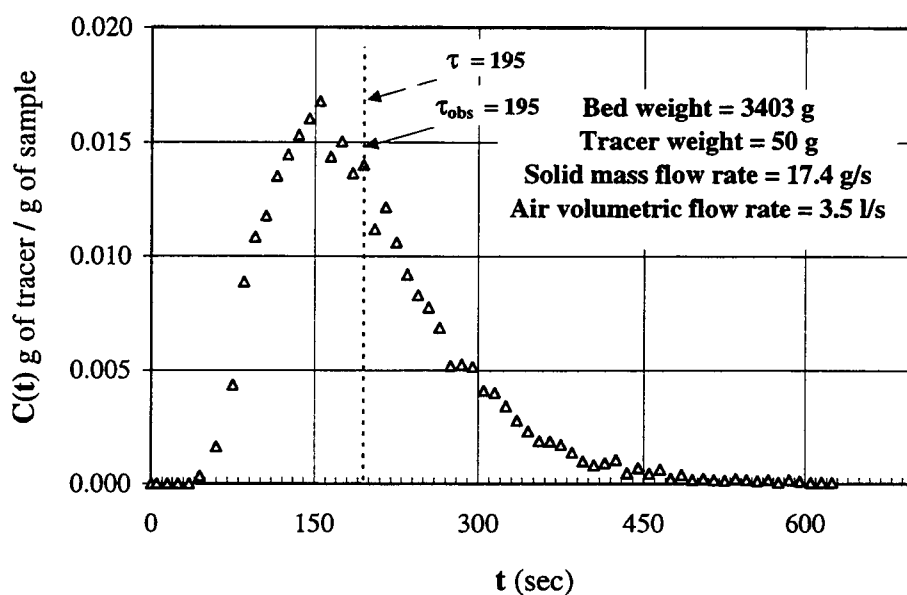
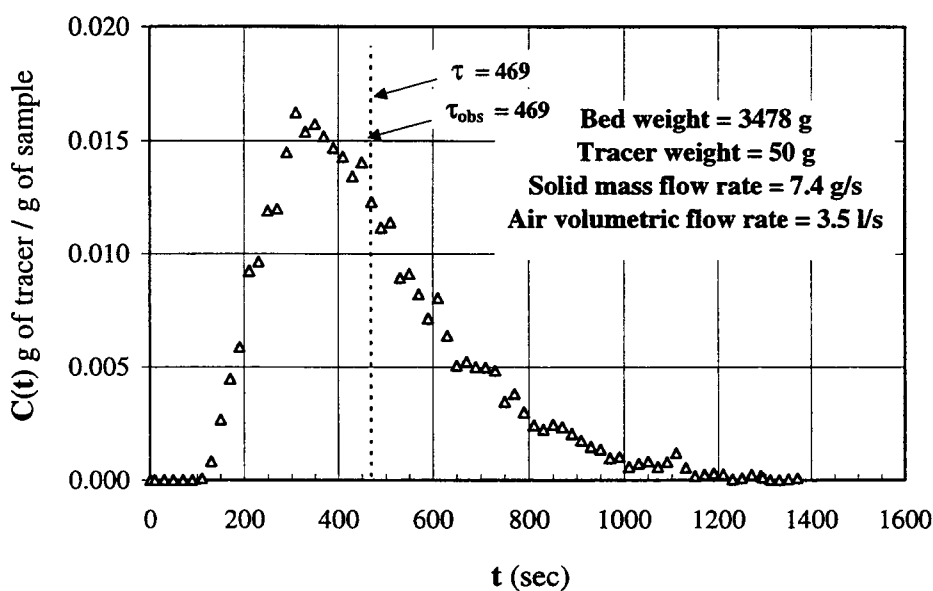


Figure 5.26  $C(t)$  curve of experiment #2002 (three-stage column)

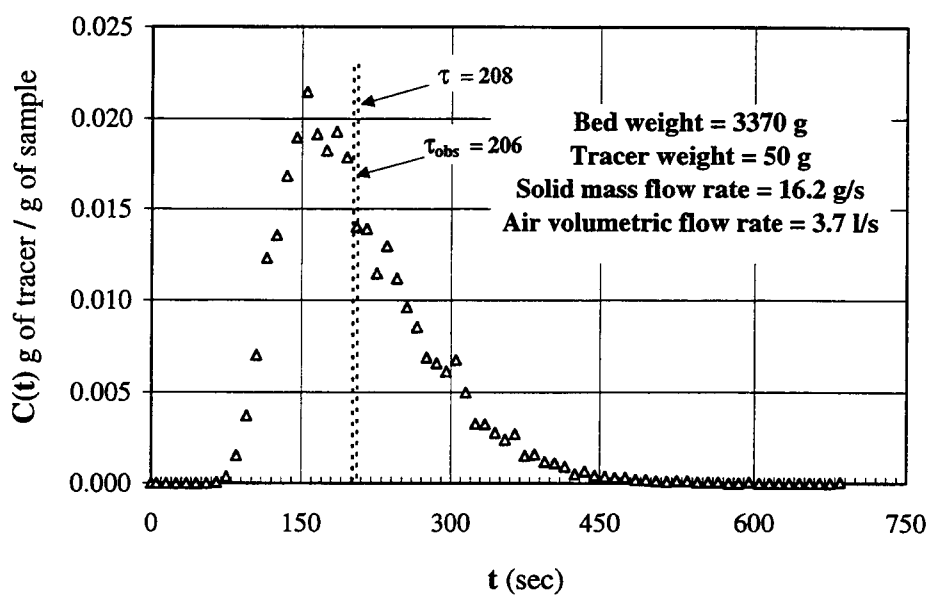


**Figure 5.27**  $C(t)$  curve of experiment #2003 (three-stage column)

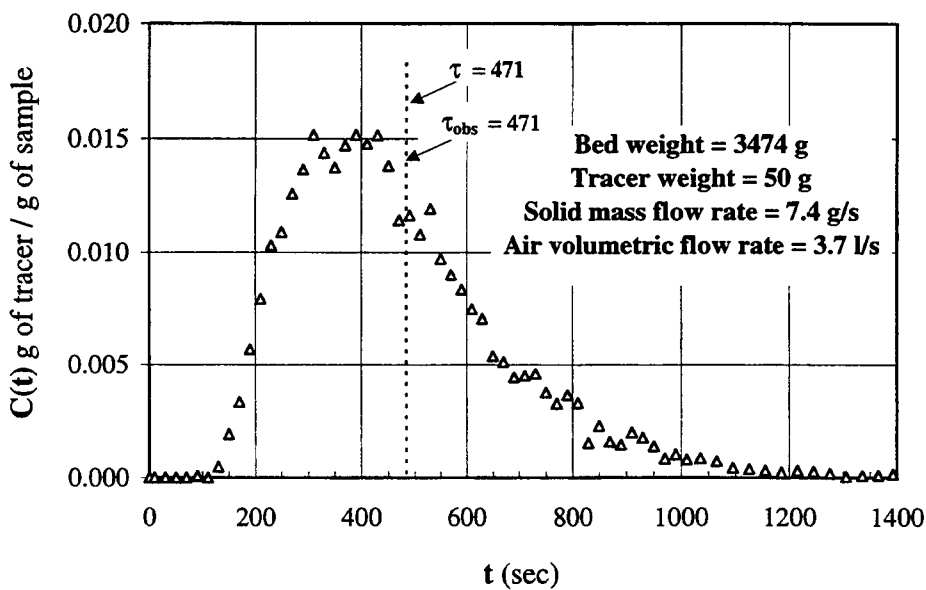


**Figure 5.28**  $C(t)$  curve of experiment #2004 (three-stage column)

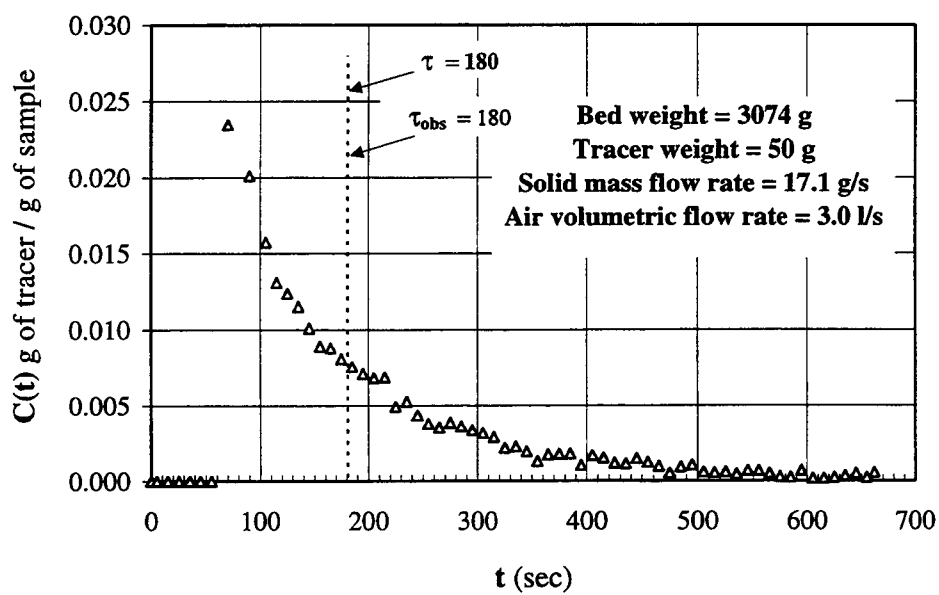




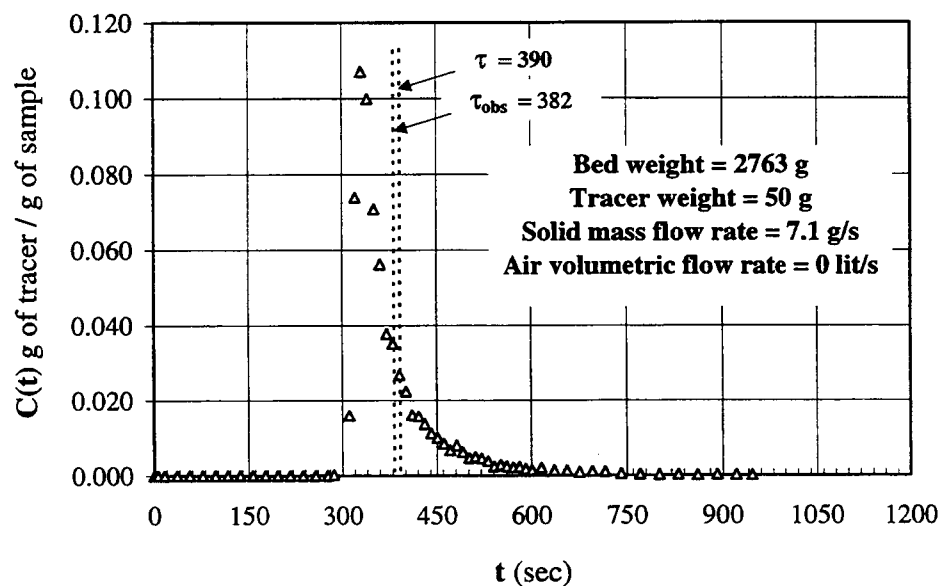
**Figure 5.29**  $C(t)$  curve of experiment #2005 (three-stage column)



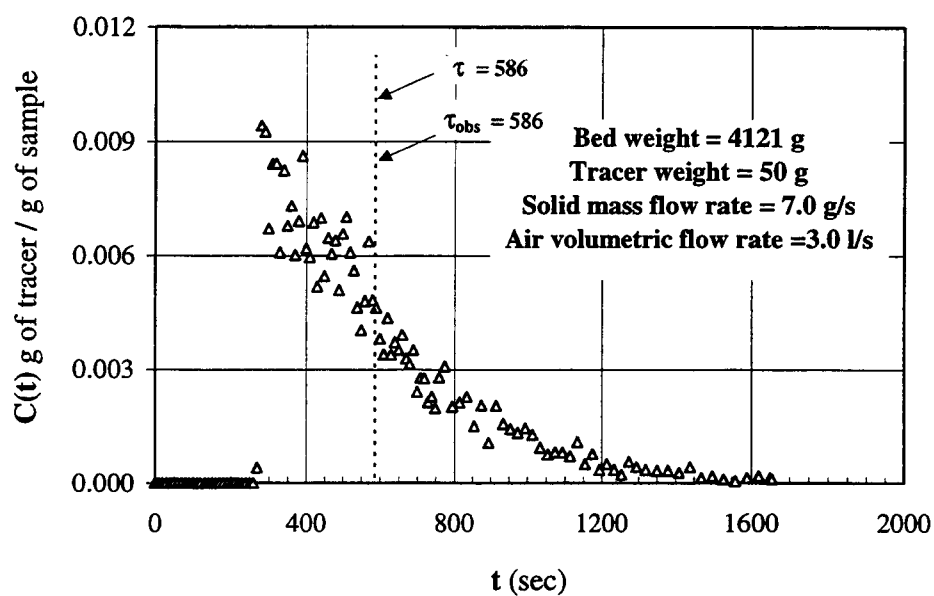
**Figure 5.30**  $C(t)$  curve of experiment #2006 (three-stage column)



**Figure 5.31**  $C(t)$  curve of experiment #2007 (three-stage column)



**Figure 5.32**  $C(t)$  curve of experiment #2008 (three-stage column)



**Figure 5.33**  $C(t)$  curve of experiment #2009 (three-stage column)

## CHAPTER 6

### ANALYSIS AND DISCUSSION OF EXPERIMENTAL DATA

#### 6.1 Introduction

The function of residence time distribution of solids gives information about the fraction of solids that spend a given time interval in the vessel. This information is sufficient to provide a description of the flow of solids through the vessel. Engineers have found that various RTD models, called *macromixing* models (in contrast to extremely detailed microscopic modeling) are very useful in providing adequate estimates of important process characteristics, like reaction conversion and efficiency of unit operations.

According to Hoffmann (1979), Levenspiel (1997) and Jovanovic (1997), the characteristics of a simple, reliable RTD model should be:

1. The model should reflect true nature of the flow characteristics observed in the vessel. The building elements of the compartment model: ideal plug flow compartment, ideal mixed flow compartment, and dead zone compartment, should be experimentally observed and identified before they are incorporated into the model. This leads to a class of compartment models that are truly corresponding to existing flow situation: *phenomenological* compartment models.
2. The model should be as simple as possible in its choice of compartment types for the intended application.
3. The model should contain as few parameters as possible
4. Reliable correlations should exist for the parameters of the selected model
5. If possible, the complexity of the mathematical apparatus involved in determination of model parameters should be reasonably simple.

It is crucial to avoid unnecessary model complexity. Complex models inevitably introduce additional parameters for which high resolution data are required. Once a model has been chosen, the values of the characteristic parameters must be determined.

To obtain the model parameters, the measurements of the tracer concentration at the exit of the system are compared with the prediction of the chosen model. The tracer concentration curve,  $C(t)$ , the response on the impulse tracer stimulus, should be obtained when the system operates at steady-state-flow mode. As for the model, the usual practice is to obtain mathematical representation of the chosen compartment flow model containing pertinent parameters. Furthermore, these parameters are usually expressed as a function of measurable system variables/parameters like: flow rates, volume, hold-up weight, velocity, etc. The model parameters must be picked with the idea of obtaining the closest possible agreement between suggested-model-RTD and real-vessel-RTD. If this agreement is *sufficiently close*, then the model is acceptable. If not, a better model should be found. The quality of the agreement necessary to fulfill the criterion “sufficiently close” depends on engineering judgment.

Most often, the *least square method* is used to find the best set of values for the model parameters. In other words we minimize the function “J”,

$$J = \sum_{i=1}^{i=n} \left[ E_{\text{model}}(t_i, \Phi_1, \Phi_2, \dots, \Phi_n) - \Psi_i E_{\text{exp.}}(t_i) \right]^2 \quad (6.1)$$

by finding appropriate values for the set of parameters  $\Phi_i$ . The weighing function  $\Psi_i$  is in this study set identically to 1. The details of this simple procedure are found in Appendix D. The amount of tracer material,  $\Delta W$ , leaving the vessel between time  $t$  and  $t + \Delta t$  is

$$\Delta W = C(t) S_0 \Delta t \quad (6.2)$$

where  $S_0$  is the solids flow rate. If we now divide by the total amount of tracer material that was injected into the vessel,  $W_0$ , we obtain

$$\frac{\Delta W}{W_0} = \frac{S_0 C(t)}{W_0} \Delta t = \text{fraction of material with residence time between } t + \Delta t \quad (6.3)$$

For pulse injection we define

$$E(t) \equiv \frac{S_0 C(t)}{W_0} \quad (6.4)$$

so that

$$\frac{\Delta W}{W_0} = E(t) \Delta t \quad (6.5)$$

where the quantity  $E(t)$  is the residence-time distribution function.

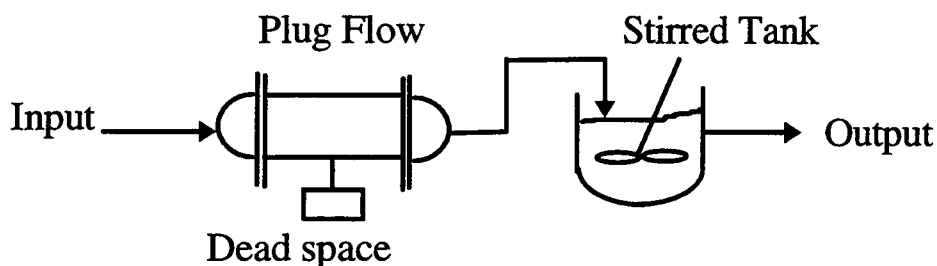
## 6.2 Single-stage Unit

In Section 3.3 we already presented, a model that we believe may well describe the experimental situations depicted in Chapter 5. Visual observation of the spouted bed clearly indicate that the total volume of the bed consist of: a region where particles are vigorously mixed, a region where particles flow in the form of moving bed with insignificant mixing, and a region where there is apparent absence of flow (dead zones).

For the case of a single-stage unit, convolution of the  $E(t)$  equations for plug flow and mixed flow compartments yields the  $E(t)$  equation [equation (3.11)] that is used to represent the experimental data.

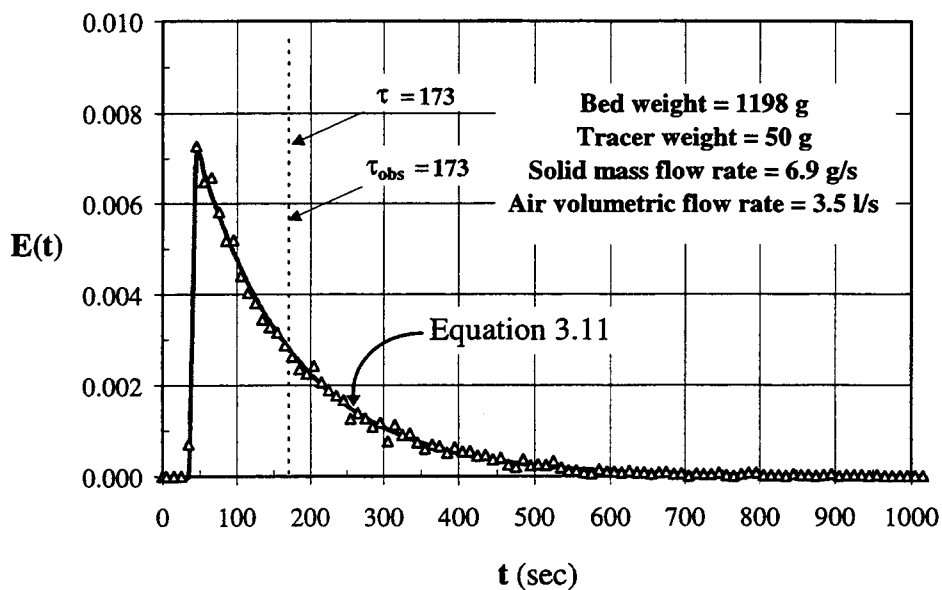
$$\left. \begin{aligned} E(t) &= 0 && \text{for } t < \tau_p \\ E(t) &= \frac{1}{\tau_M} \exp \left[ \frac{-(t - \tau_p)}{\tau_M} \right] && \text{for } t \geq \tau_p \end{aligned} \right\} \quad (3.11)$$

Figure 6.1 represents the actual flow situation observed in the single-stage unit. The RTD of this single-stage compartment model can be represented by convolution of the RTD's for plug flow and mixed flow compartment. The dead space is not an active volume of the single-stage and therefore it does not show up in the overall RTD except for the shift in the observed mean residence time.

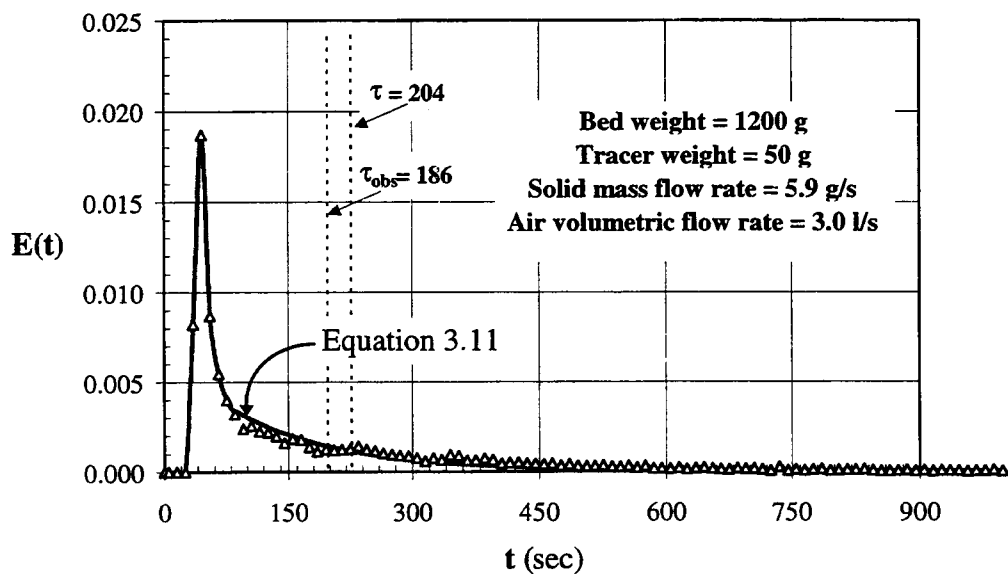


**Figure 6.1** Compartment model for the single-stage unit.

The best-fit optimization procedure, using a quasi-Newton search algorithm, yields satisfactory results for most runs. The outcomes are shown in Figures 6.2 to 6.15. Also Figures 6.16 and 6.17 summarize the results for single-stage unit experiments.

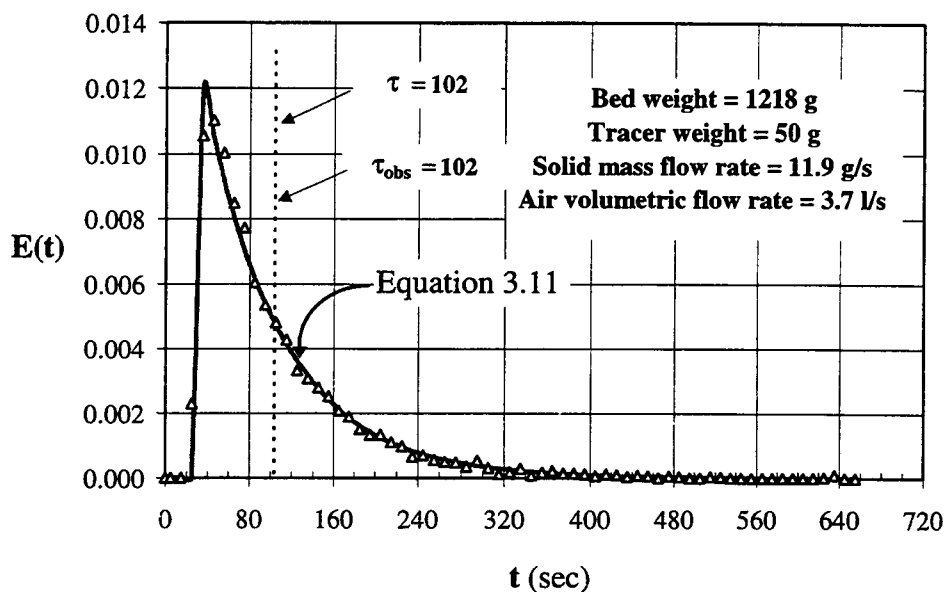


**Figure 6.2**  $E(t)$  modeling of experiment #1030 (single-stage unit)

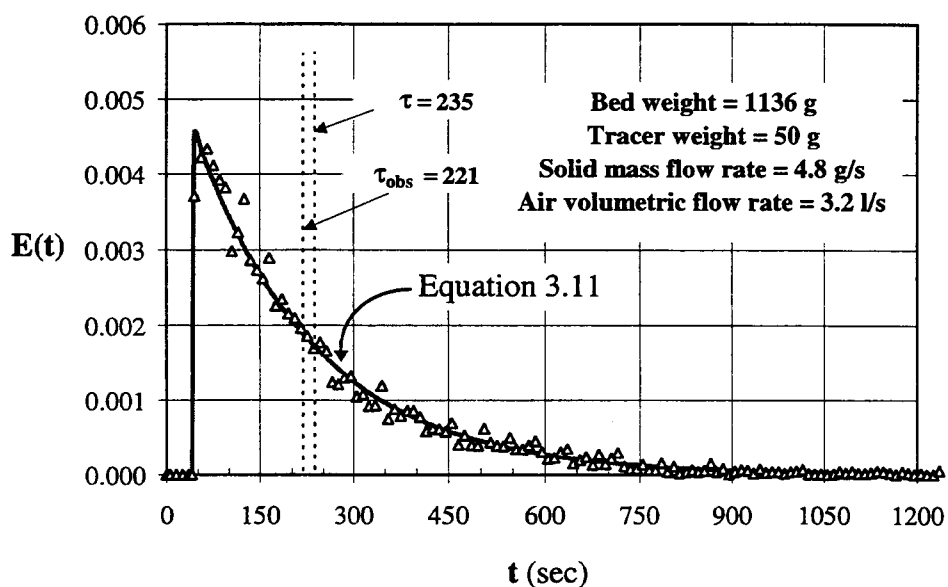


**Figure 6.3**  $E(t)$  modeling of experiment #1031 (single-stage unit)





**Figure 6.4**  $E(t)$  modeling of experiment #1032 (single-stage unit)



**Figure 6.5**  $E(t)$  modeling of experiment #1033 (single-stage unit).

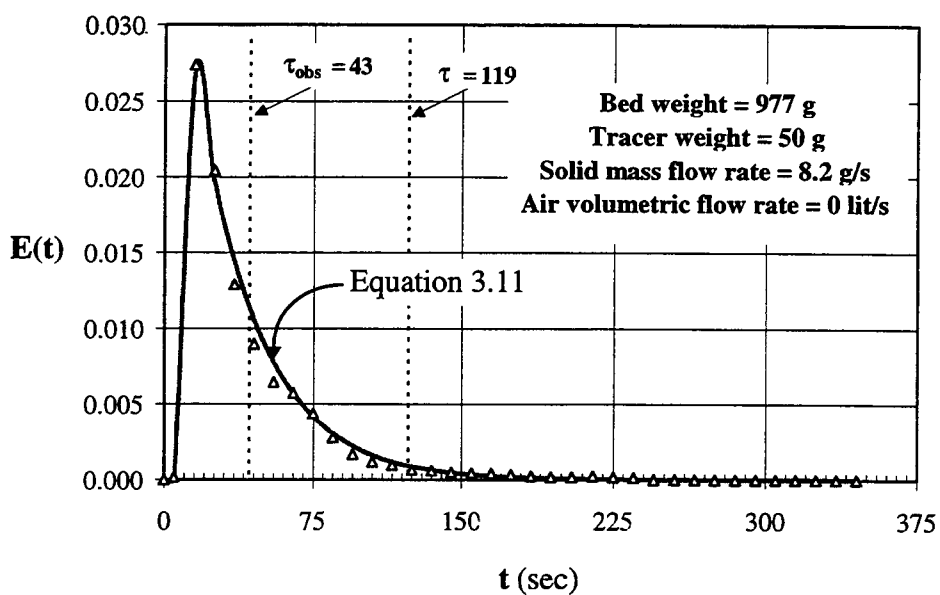


Figure 6.6  $E(t)$  modeling of experiment #1034 (single-stage unit).

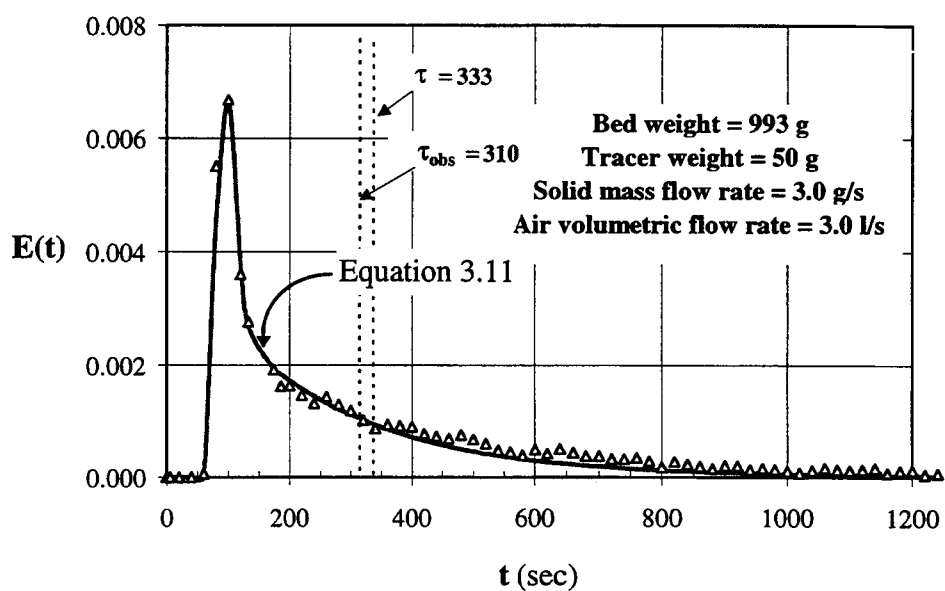
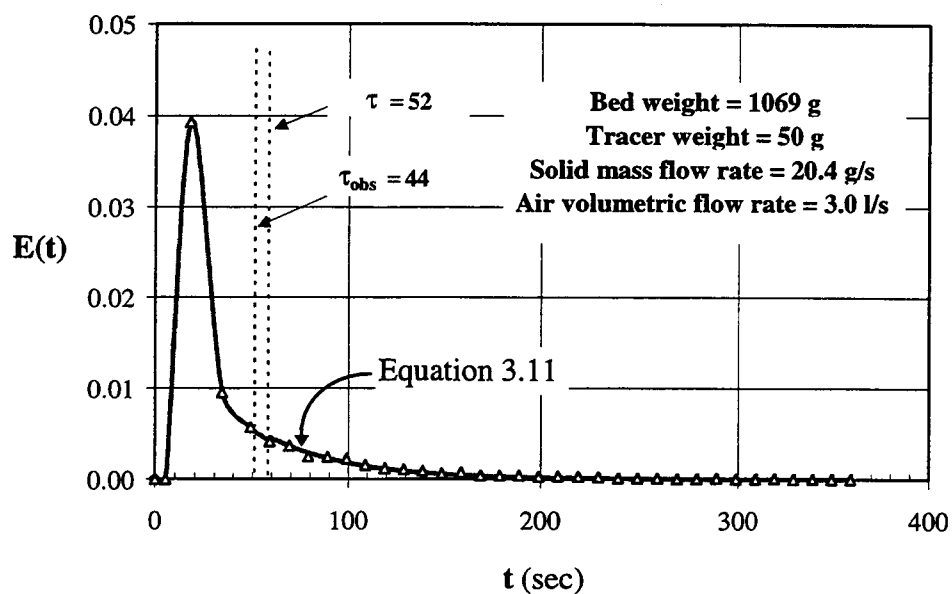
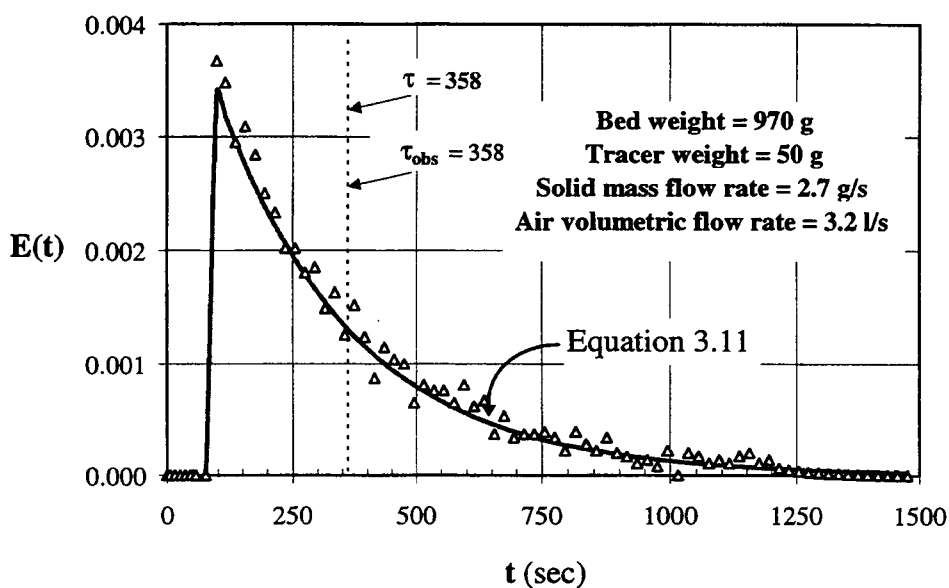


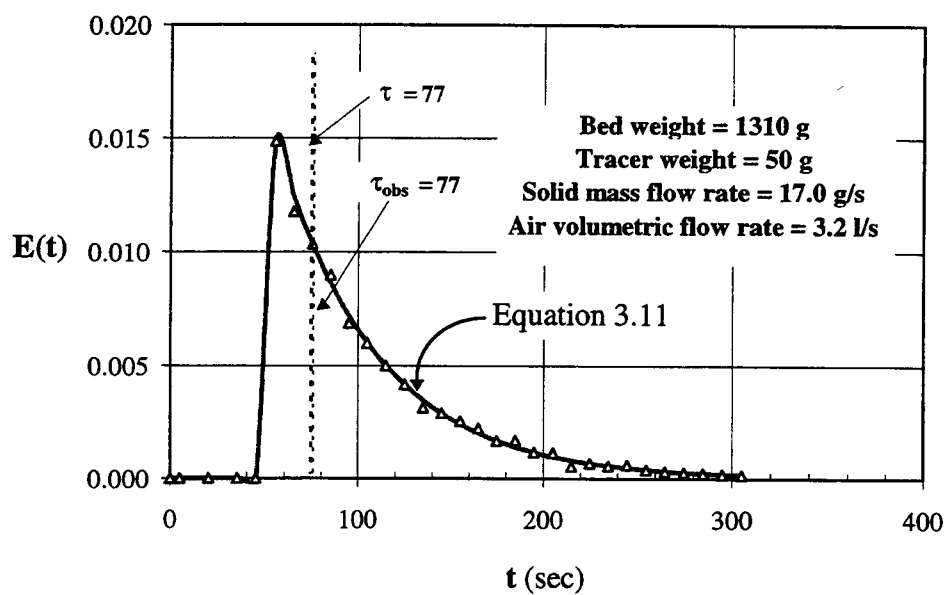
Figure 6.7  $E(t)$  modeling of experiment #1035 (single-stage unit)



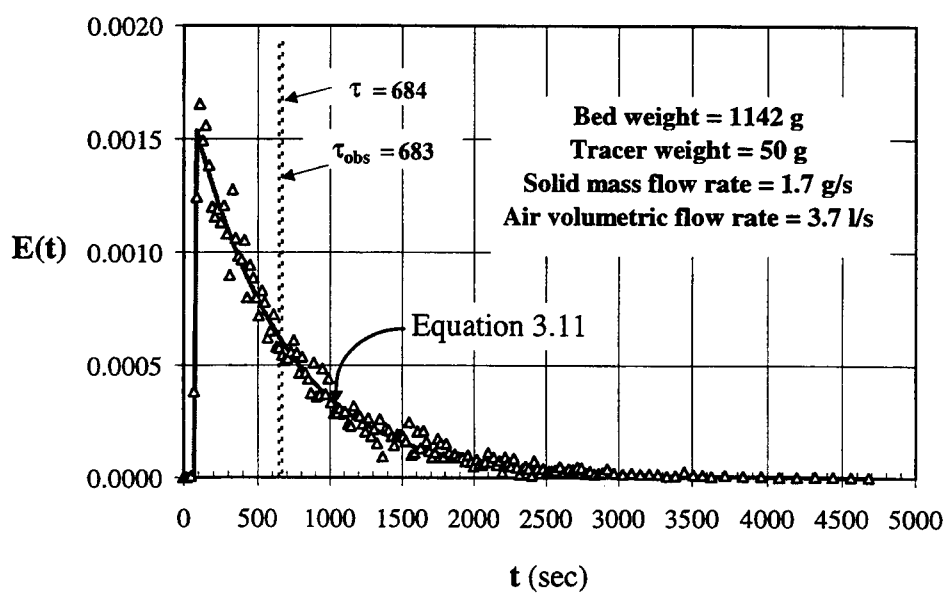
**Figure 6.8**  $E(t)$  modeling of experiment #1036 (single-stage unit)



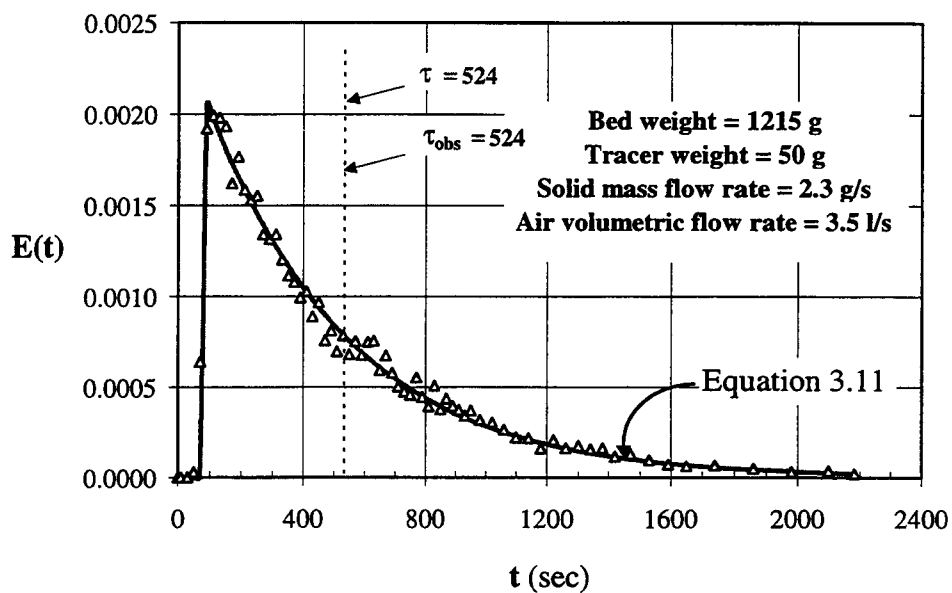
**Figure 6.9**  $E(t)$  modeling of experiment #1037 (single-stage unit)



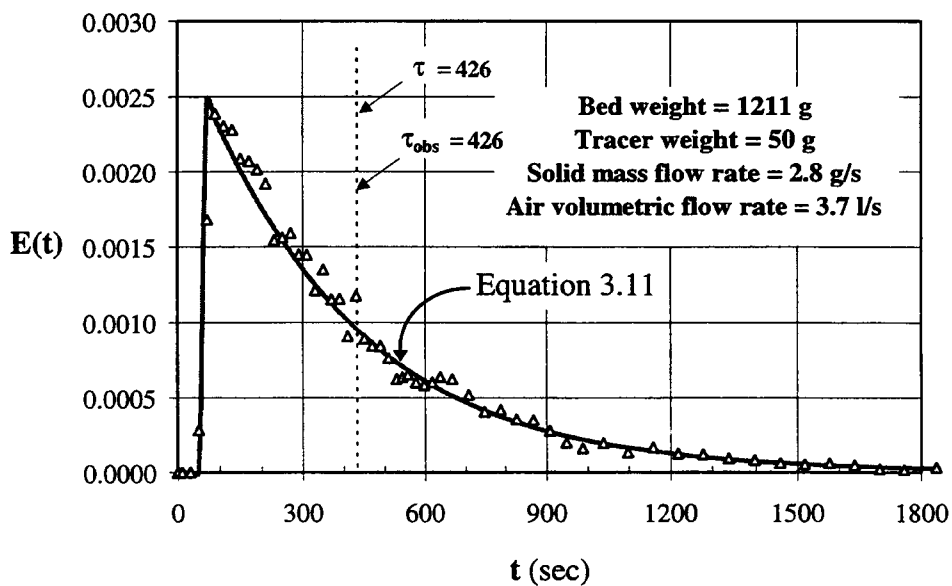
**Figure 6.10**  $E(t)$  modeling of experiment #1038 (single-stage unit)



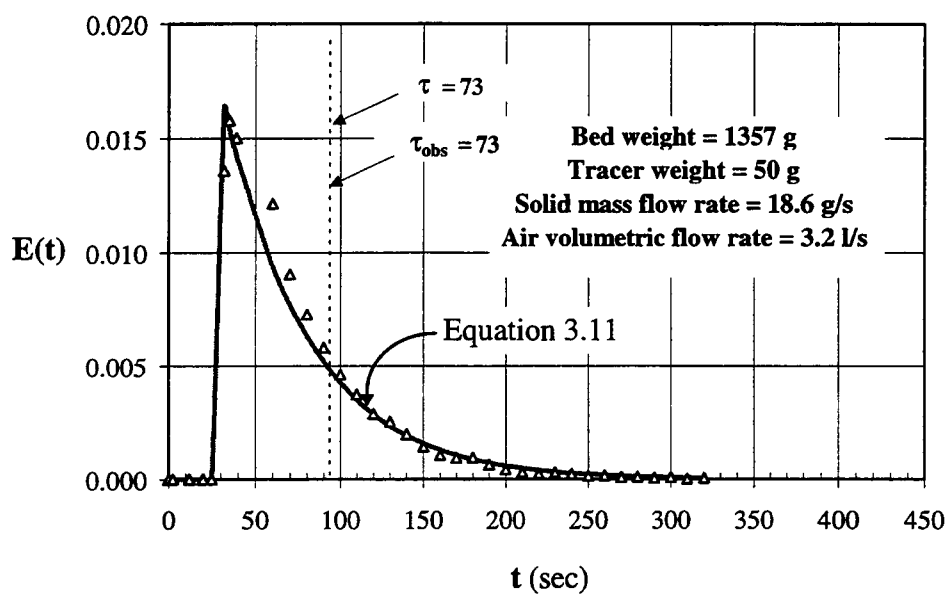
**Figure 6.11**  $E(t)$  modeling of experiment #1039 (single-stage unit)



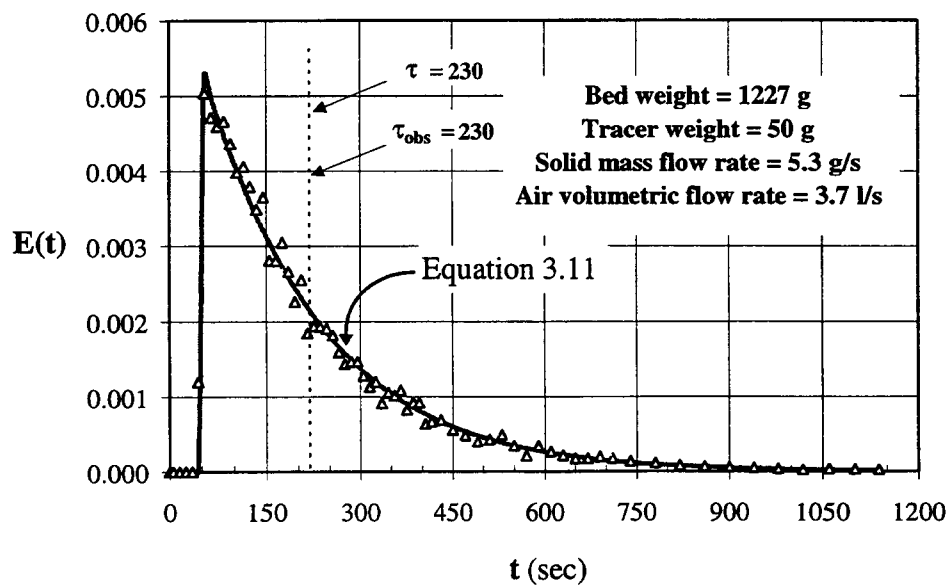
**Figure 6.12**  $E(t)$  modeling of experiment #1040 (single-stage unit)



**Figure 6.13**  $E(t)$  modeling of experiment #1041 (single-stage unit)



**Figure 6.14**  $E(t)$  modeling of experiment #1042 (single-stage unit)



**Figure 6.15**  $E(t)$  modeling of experiment #1043 (single-stage unit)

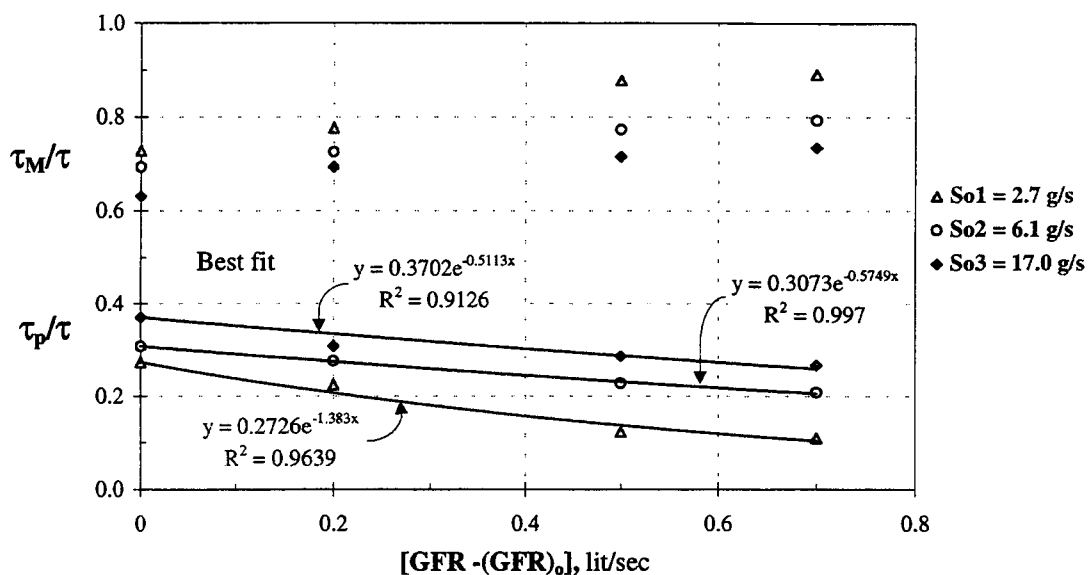


Figure 6.16 Plug and mixed flow behavior for the single-stage unit.

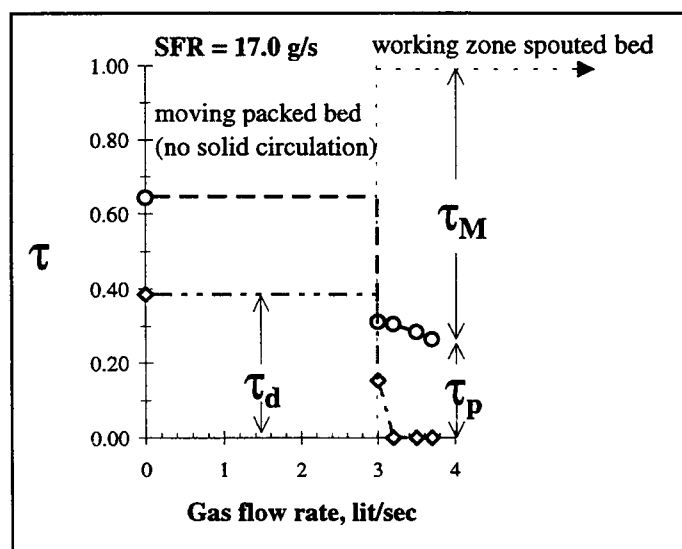
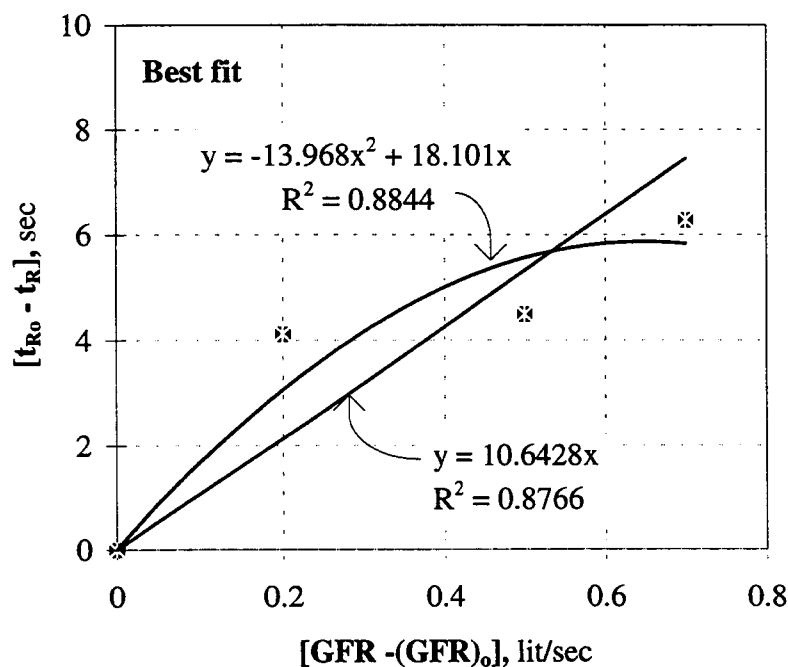


Figure 6.17 Plug, mixed flow and dead space for the single-stage unit.

From the plotted data in Figure 6.16 we observe that for constant solid flow rate, an increase of the gas flow rate causes also an increase in *mixing behavior* ( $\tau_M/\tau$ ). Similarly, for constant solid flow rate, an increase in gas flow rate will reduce the *plug flow behavior* of the vessel ( $\tau_p/\tau$ ) as expected. On the other hand, for constant gas flow rate, it can be observed that an increase of solid flow rate reduces the mixing of solids, since the particles flow faster through the system.

From the analysis of Figure 6.17, it is possible to conclude that the size of the dead volume is practically negligible for almost all working conditions. For low gas flow rate (below 3.0 liters/second) and in absence of reliable data, we assume that plug flow, mixed flow, and dead space remain practically constant, since for that range of gas flow rate, the solid particles cannot jump over the top of the draft tube.

$\tau_p/\tau$  and  $\tau_M/\tau$  can also be plotted in terms of the recirculation time of solids, " $t_R$ ". This time, as it is shown in Figure 6.18, is obtained as a function of the gas flow rate.



**Figure 6.18** Recirculation time of solids.



Out of the proposed model we obtain the two model-parameters  $\tau_M$  and  $\tau_p$ . Figure 6.16 shows how these model-parameters change with the operating conditions, gas flow rate (GFR) and solid flow rate (SFR or “S<sub>o</sub>”).  $\tau_p/\tau$  data are correlated and the resulting equations are shown in Table 6.1. All three correlations are of the general form

$$y = A \exp (-Bx) \quad (6.6)$$

where  $y = \tau_p/\tau$ ,  $x = [\text{GFR} - (\text{GFR})_o]$  and A and B are constants for each SFR. This type of correlation has a physical meaning and it may well represent the actual behavior of the single-stage unit. Accordingly, when “x” goes to zero,

$$y = A = \left( \frac{\tau_p}{\tau} \right)_o = \text{Fraction of plug-flow behavior at the lowest possible GFR}$$

Similarly, when “x” increases, the plug-flow behavior of the stage is reduced ( $y \rightarrow 0$ ) due to the intensive agitation within the vessel.

| SFR (g/s) | Correlation for $\tau_p/\tau$                          | R <sup>2</sup> |
|-----------|--------------------------------------------------------|----------------|
| 2.7       | $0.2726 \exp\{-1.383 [\text{GFR} - (\text{GFR})_o]\}$  | 0.964          |
| 6.1       | $0.3073 \exp\{-0.5749 [\text{GFR} - (\text{GFR})_o]\}$ | 0.997          |
| 17.0      | $0.3702 \exp\{-0.5113 [\text{GFR} - (\text{GFR})_o]\}$ | 0.913          |

**Table 6.1** Correlations to predict  $\tau_p/\tau$  in the single-stage unit

The next step is to obtain a *single* correlation capable of predicting mixing flow behavior and plug flow behavior, as a function of both operating variables. A method, shown by Davis (1962), of correlating three variables “x” (S<sub>o</sub>), “y” (GFR), and “z” ( $\tau_p/\tau$  or  $\tau_M/\tau$ ), considers one variable, for example “x”, as constant, temporarily, and relating “y” and “z” for each value of “x” by equations of the same type, as

$$\phi(z) = mF(y) + b \quad (6.6)$$

Where “m” is the slope of the line, and “b” is the intersection. Then “m” and “b” can be expressed as function of “x” (the third variable involved), as

$$m = \psi(x) \quad (6.7)$$

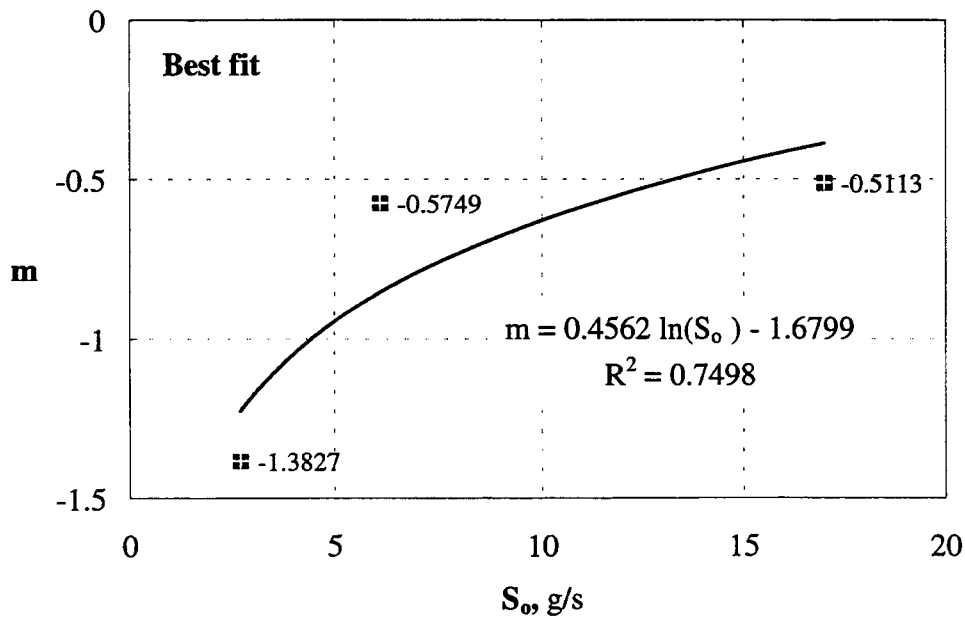
and

$$b = f(x) \quad (6.8)$$

so that the final equation becomes

$$\phi(z) = \psi(x) F(y) + f(x) \quad (6.9)$$

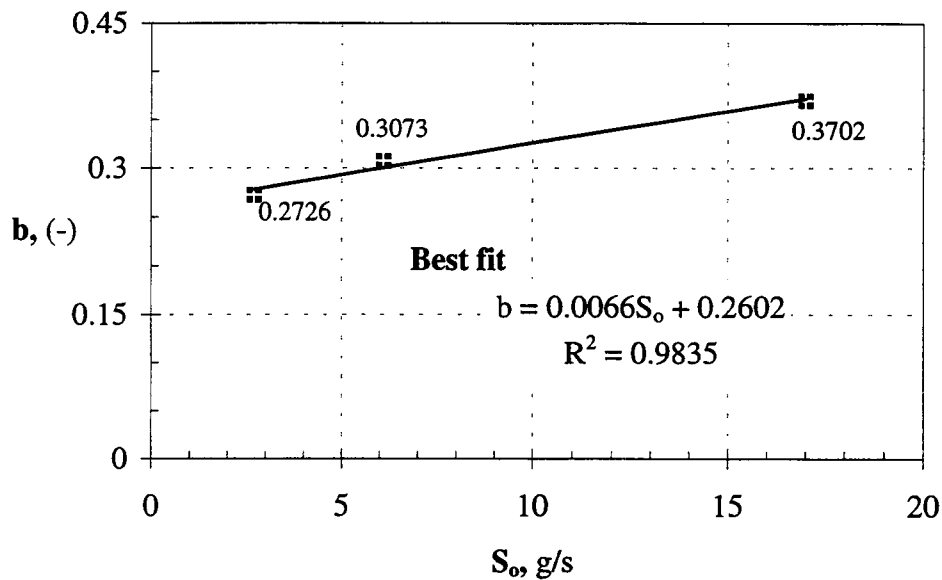
Following this procedure, from the correlations in Table 6.1 we obtain the values of “m” and “b” for constant  $S_o$ . Figures 6.19 and 6.20 show how these parameters change as a function of the solid flow rate  $S_o$ . From this information, the correspondent correlations,  $m = \psi(x)$  and  $b = f(x)$ , also shown in these figures, are determined.



**Figure 6.19** Correlation for  $\tau_p/\tau$ : “m” dependency on solid flow rate  $S_o$ .

Substitution of the correlations from Figures 6.19 and 6.20 in Equation 6.9 yields the desired model correlation:

$$\tau_p/\tau = (0.0066 S_o + 0.26) \text{EXP} \{-(0.46 \ln S_o - 1.68)(\text{GFR} - \text{GFR}_o)\} \quad (6.10)$$



**Figure 6.20** Correlation for  $\tau_p/\tau$ : “b” dependency on solid flow rate  $S_o$ .

If the linear correlation ( $y = 10.6428x$ ) of Figure 6.18 is used, then Equation (6.10) can be written in terms of the *recirculation time* of solids,

$$\tau_p/\tau = (0.0066 S_o + 0.26) \text{EXP} \{-(0.043 \ln S_o - 0.16)(t_{R0} - t_R)\} \quad (6.11)$$

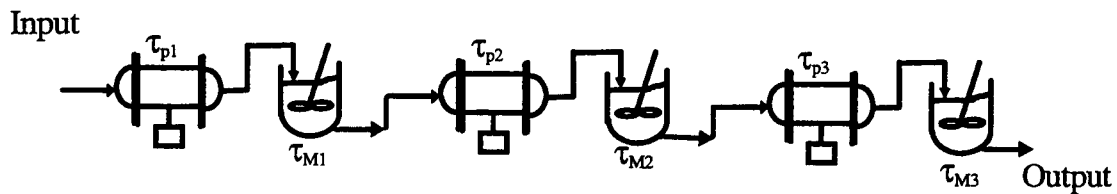
These correlations have to be tested with an independent set of experimental data. The data used for that purpose are from the three-stage column experiments. Results are shown later in Section 6.3 of this thesis.

### 6.3 Three-stage Column

In Section 3.3 of this thesis, the mathematical model for the three-stage column that we believe may well describe the experimental situations depicted in Chapter 5 is presented. For this case, convolution of the  $E(t)$  equations (3.11) yield the  $E(t)$  expression [equation (3.12)] that is used to represent our data.

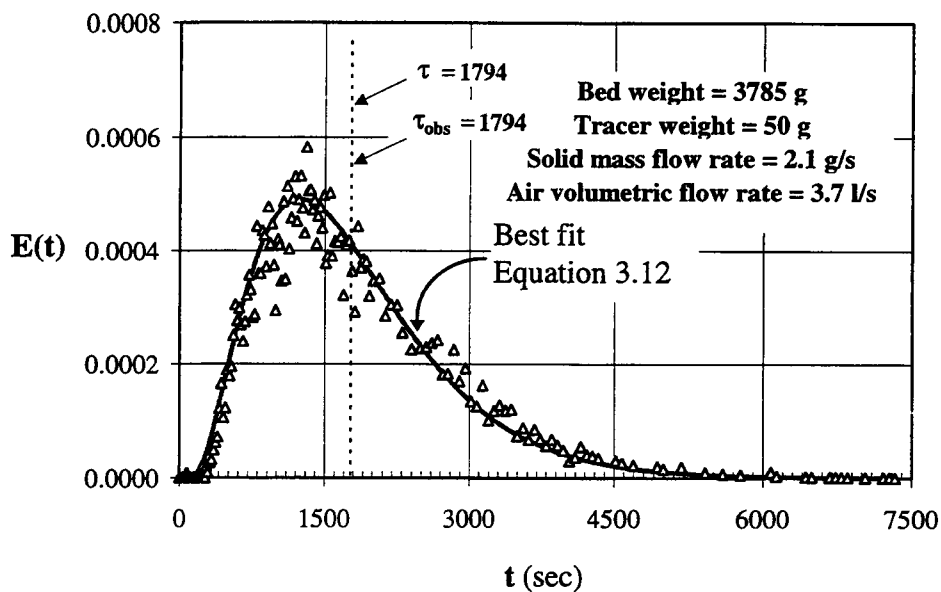
$$\left. \begin{aligned} E(t) &= 0 & t < 3\tau_{pi} \\ E(t) &= (1/2)(1/\tau_{Mi}^3)(t - 3\tau_{pi})^2 \exp\{-(t - 3\tau_{pi})/\tau_{Mi}\} & t \geq 3\tau_{pi} \end{aligned} \right\} \quad (3.12)$$

Figure 6.21 represents this combination of *ideal vessels*.

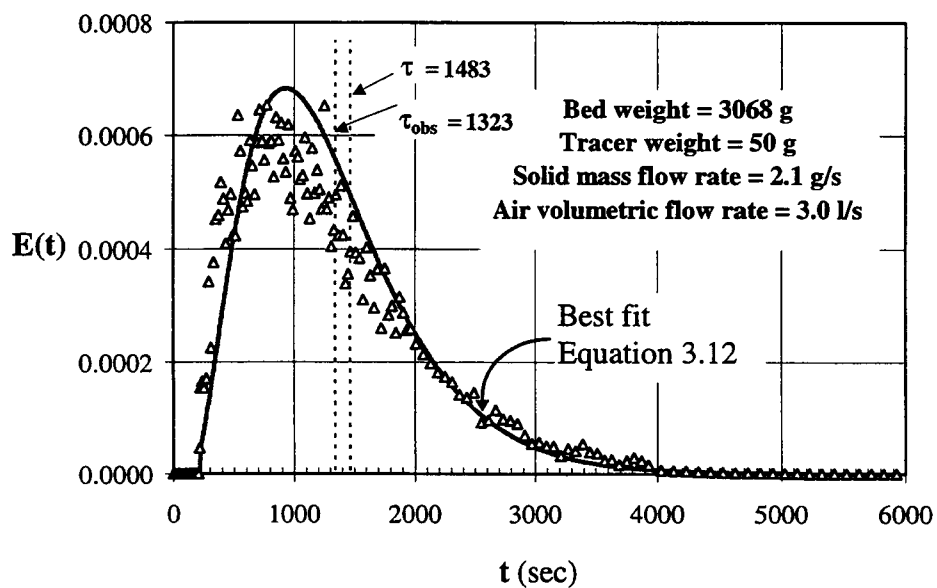


**Figure 6.21** Compartment model for the three-stage column.

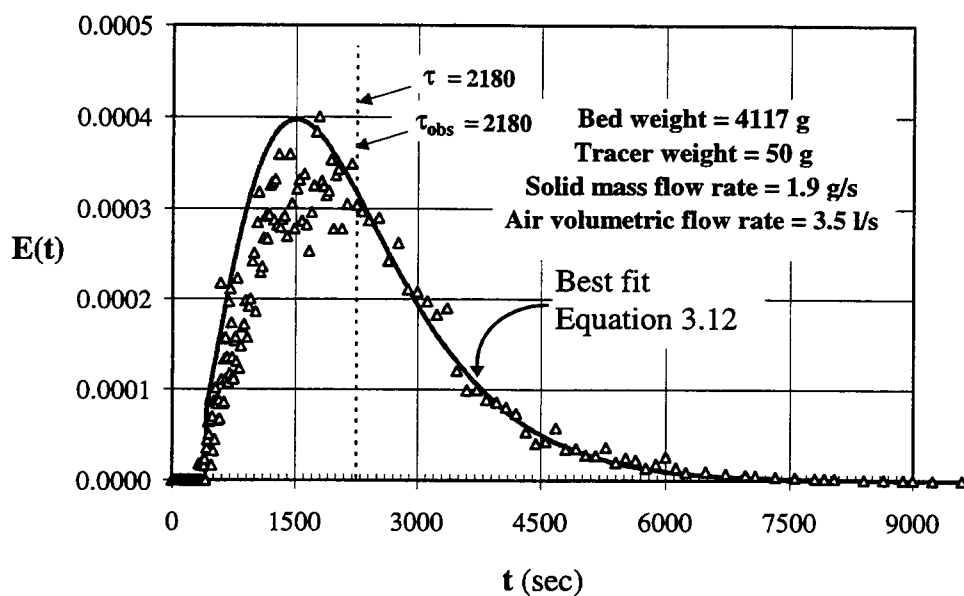
The least-square method is again used to determine model-parameters from the experimental data, and the best-fit optimization procedure, (quasi-Newton search algorithm) also yields satisfactory results for most experiments. Figures 6.22 to 6.33 show the results for the three-stage column.



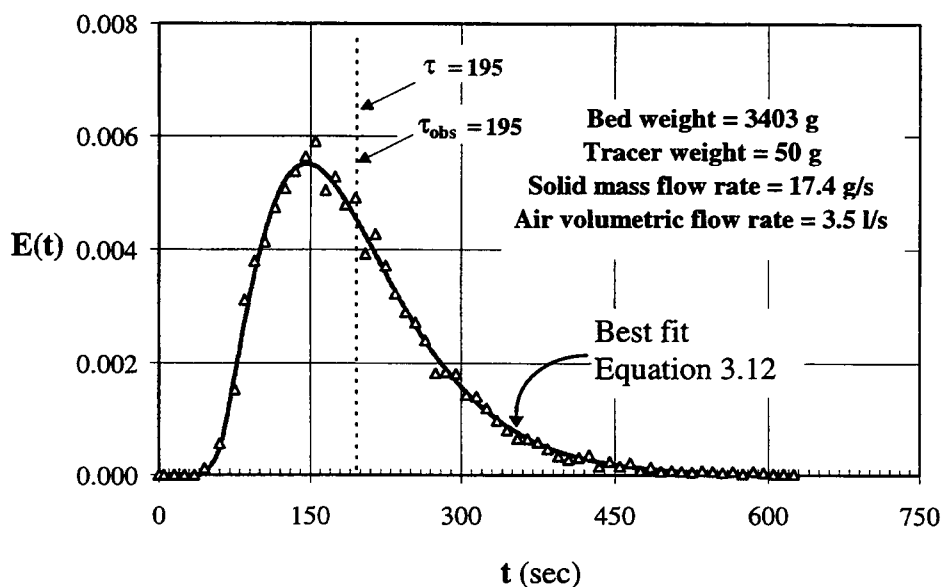
**Figure 6.22**  $E(t)$  modeling of experiment #2000 (three-stage column)



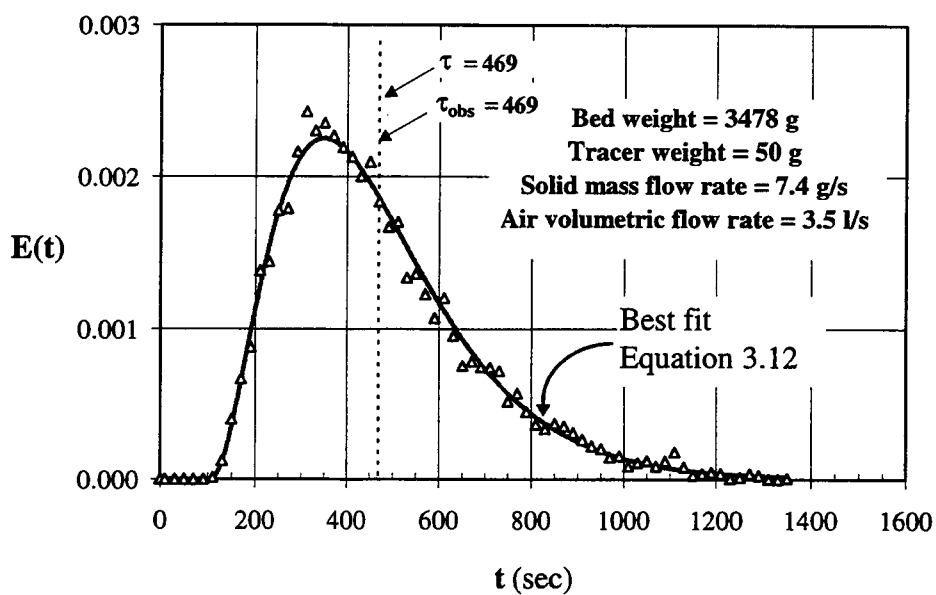
**Figure 6.23**  $E(t)$  modeling of experiment #2001 (three-stage column)



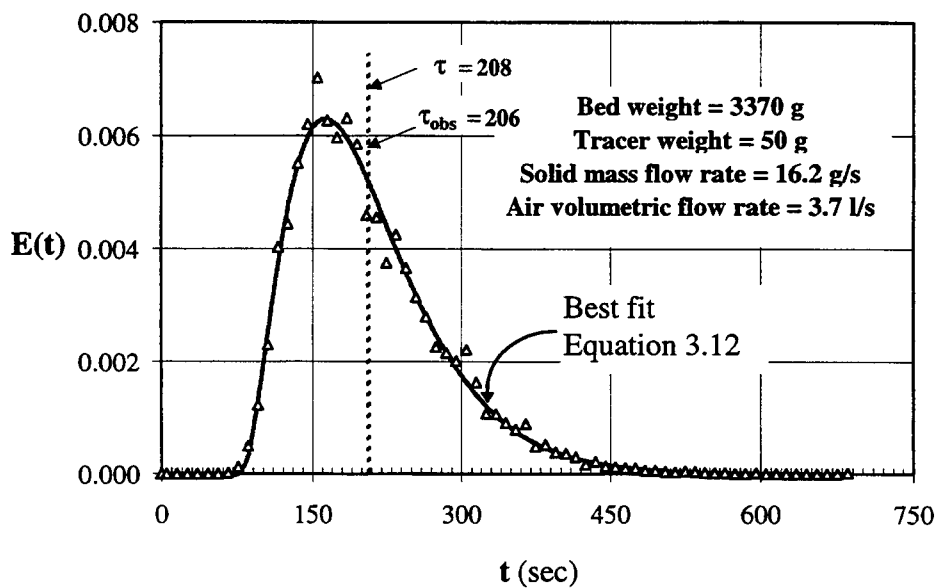
**Figure 6.24**  $E(t)$  modeling of experiment #2002 (three-stage column)



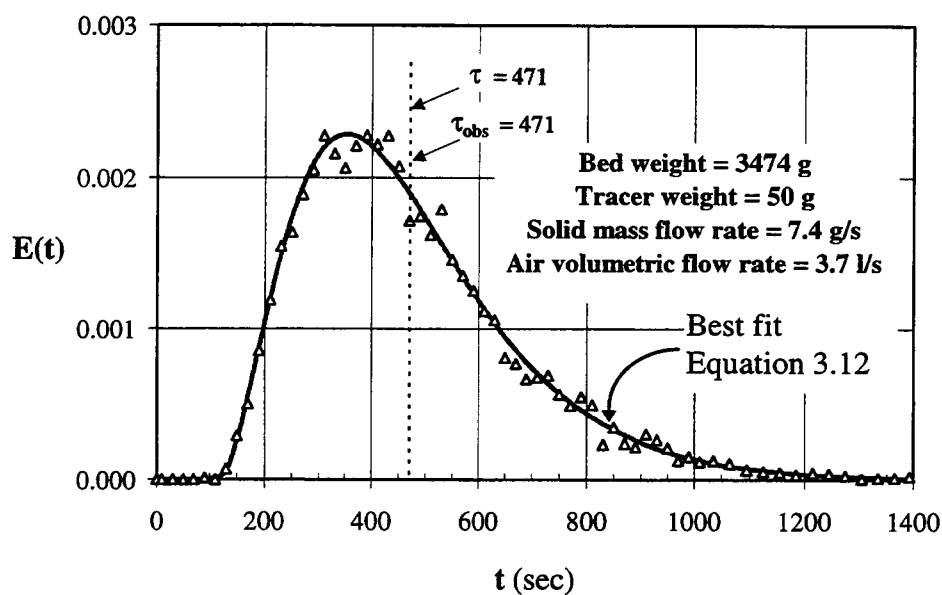
**Figure 6.25**  $E(t)$  modeling of experiment #2003 (three-stage column)



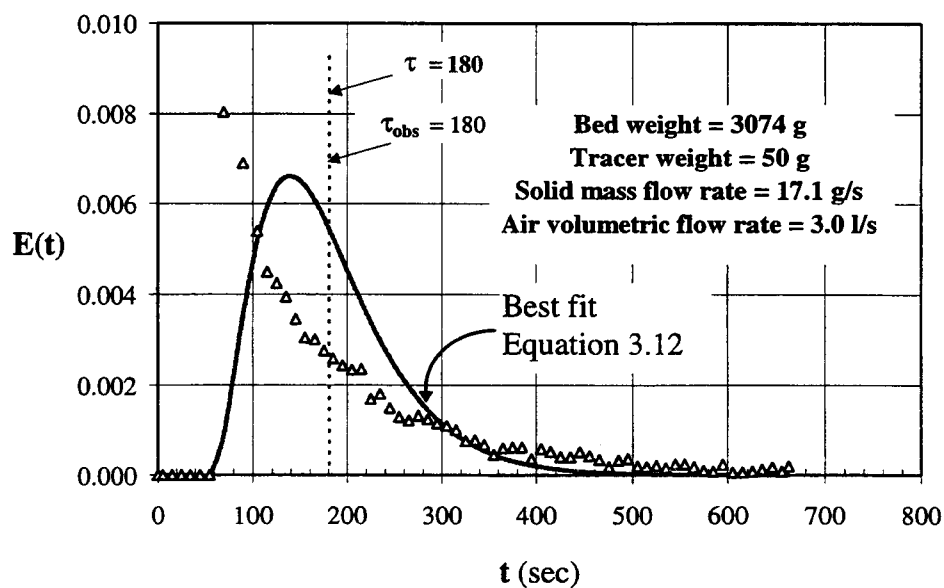
**Figure 6.26**  $E(t)$  modeling of experiment #2004 (three-stage column)



**Figure 6.27**  $E(t)$  modeling of experiment #2005 (three-stage column)

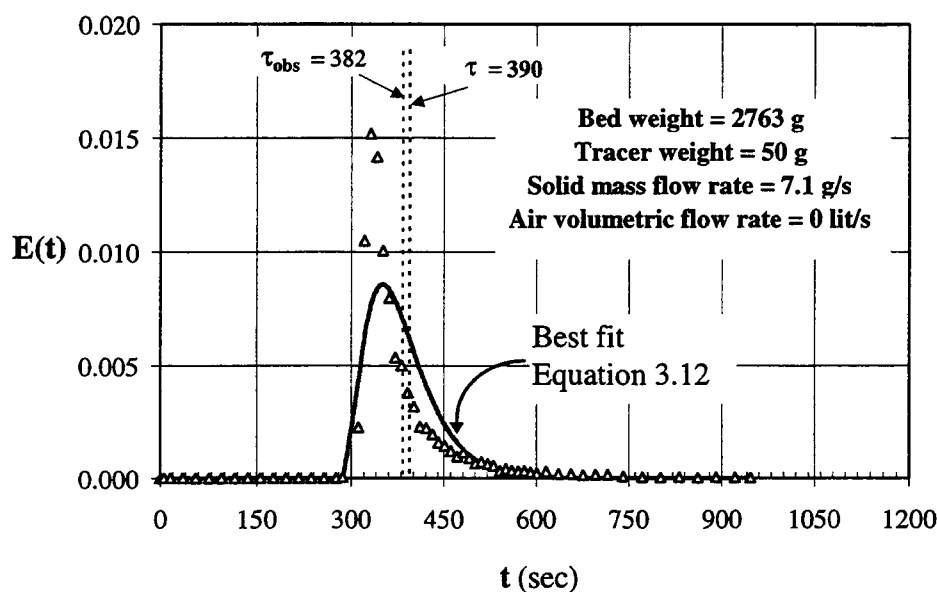


**Figure 6.28**  $E(t)$  modeling of experiment #2006 (three-stage column)

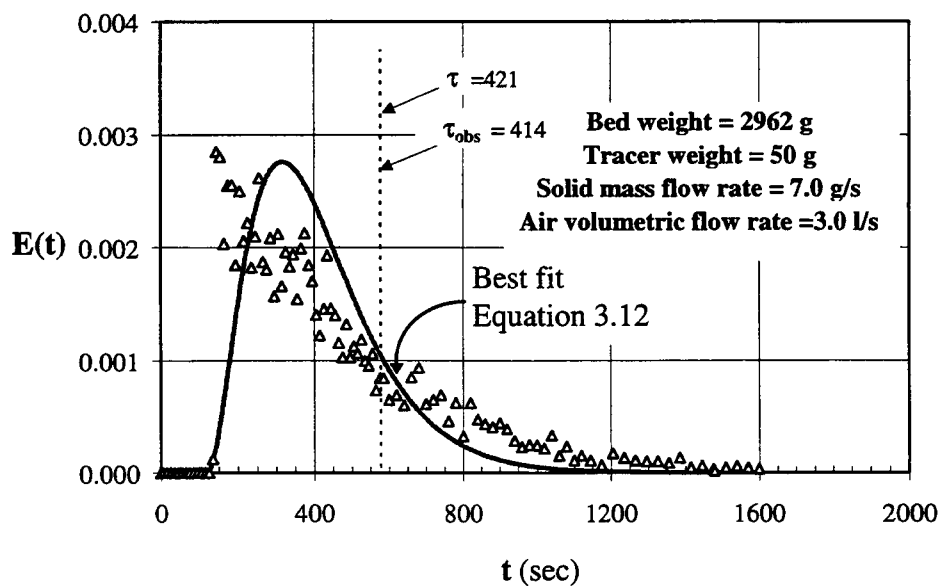


**Figure 6.29**  $E(t)$  modeling of experiment #2007 (three-stage column)





**Figure 6.30**  $E(t)$  modeling of experiment #2008 (three-stage column)



**Figure 6.31**  $E(t)$  modeling of experiment #2009 (three-stage column)

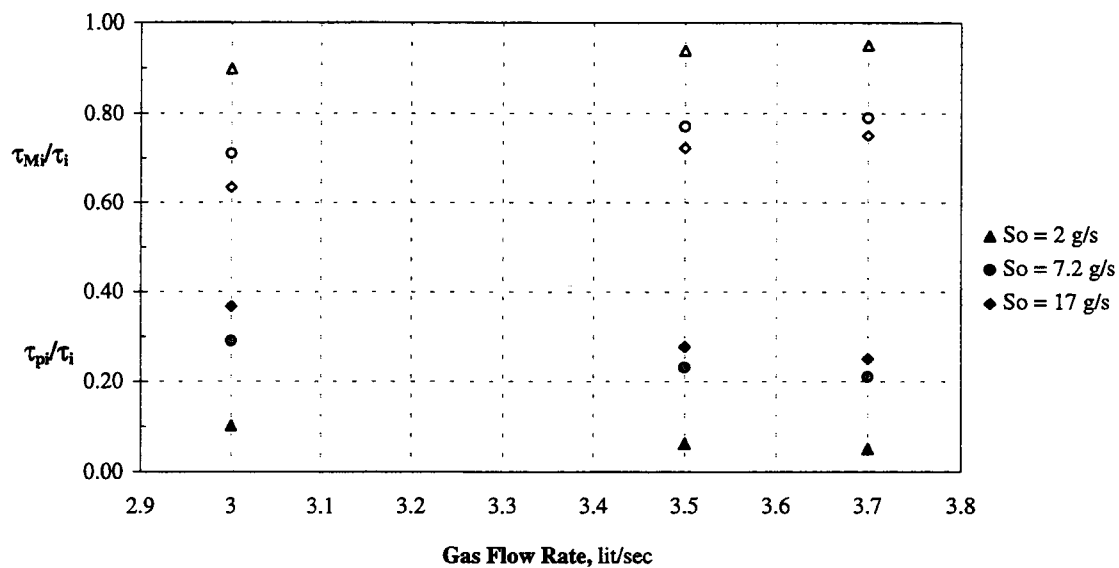


Figure 6.32 Plug and mixed flow behavior for the three-stage column.

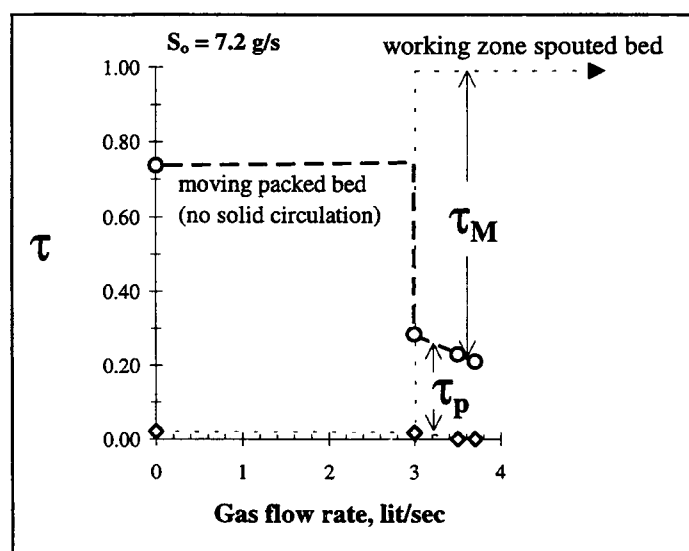
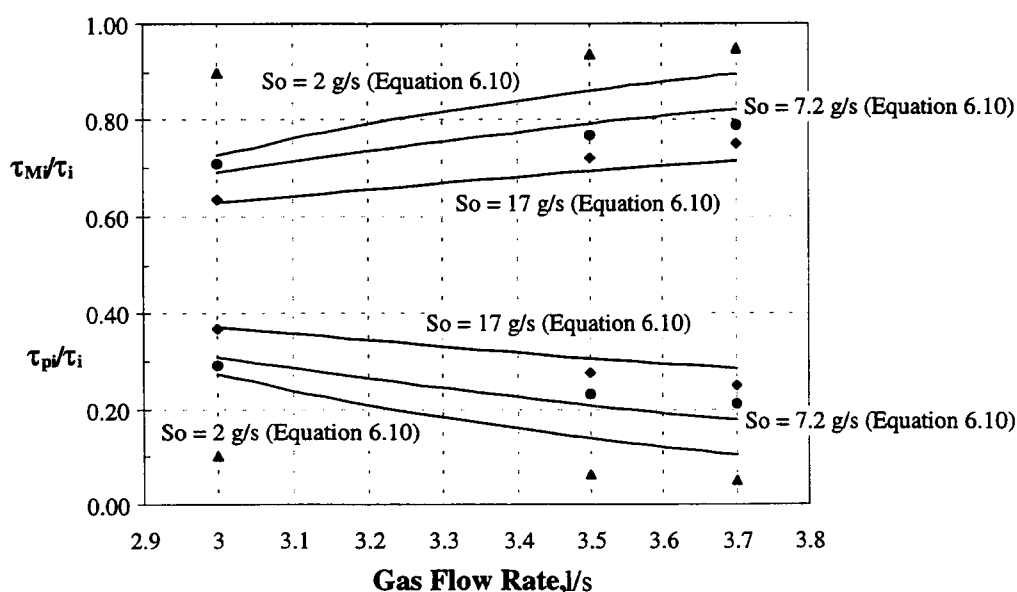


Figure 6.33 Plug, mixed flow and dead space for the three-stage column.

Once again, from the plotted data in Figure 6.32 we may confirm that for constant solid flow rate, an increase of the gas flow rate causes also an increase in *mixing behavior* ( $\tau_M/\tau$ ). Similarly, for constant solid flow rate, an increase in gas flow rate will reduce the *plug flow behavior* of the vessel ( $\tau_p/\tau$ ) as expected. Also in this case, for constant gas flow rate, an increase of solid flow rate reduces the mixing of solids.

Out of Figure 6.33, it is also possible to conclude that the size of the dead volume is practically negligible. Again, for low gas flow rate (below 3.0 liters/second), we assume that plug flow, mixed flow, and dead space remain practically constant, since as it was mentioned before, for that range of gas flow rate the solid particles cannot jump over the top of the draft tube.

Equations 6.10 and 6.11 can now be tested. Data from the three-stage column are used for that purpose since they are independently obtained. Figure 6.34 and 6.35 show the model predictions for the three-stage column. The experimental parameters are plotted against the predicted values in Figure 6.36. The predicted values are calculated using the correlations developed for the single-stage unit. The predictions are shown to be in very satisfactory agreement with the experimental results.



**Figure 6.34** Model-parameters. Experimental and model predictions.

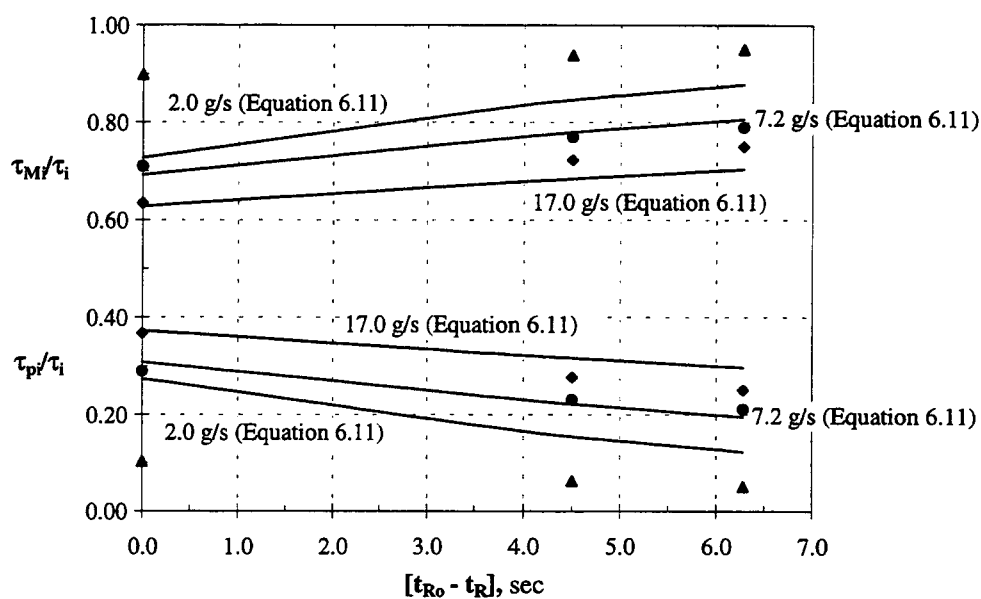


Figure 6.35 Model-parameters. Experimental and model predictions.

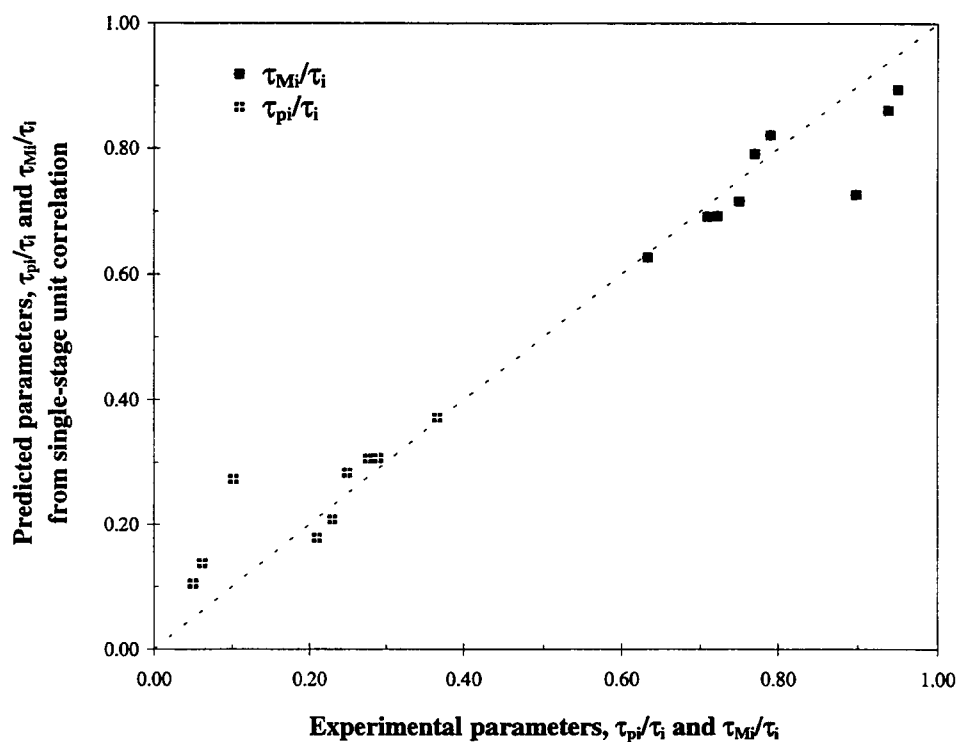
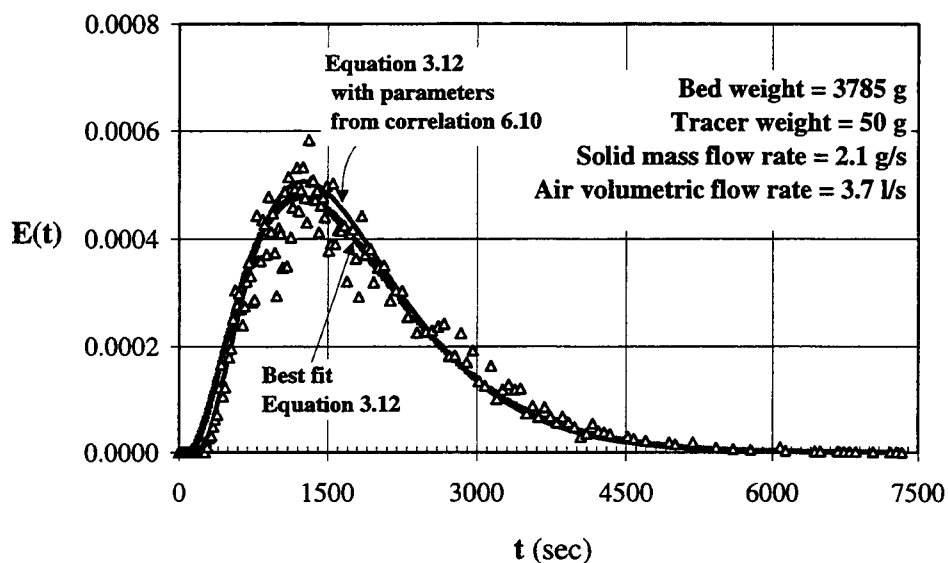
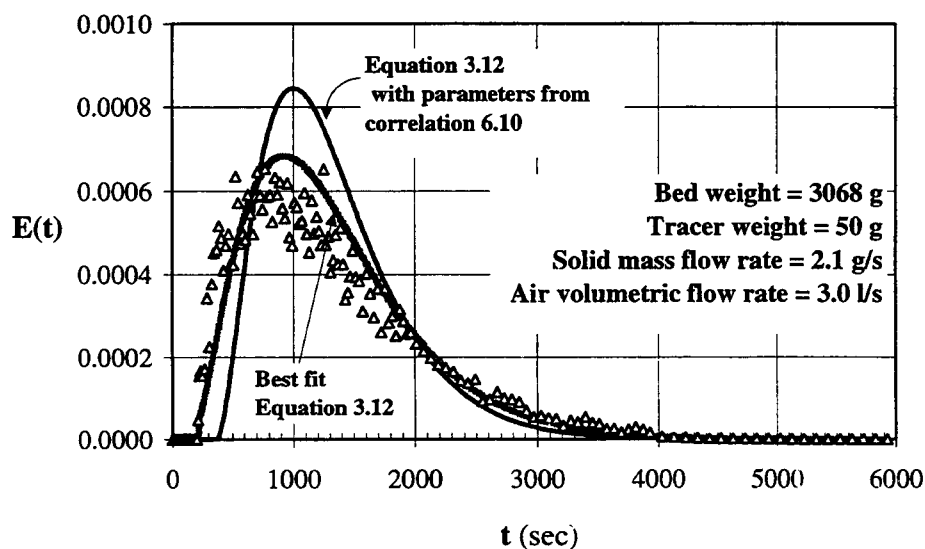


Figure 6.36 Measured versus predicted parameters.

Finally, using the predicted values coming from either Equation 6.10 or Equation 6.11, we generate the  $E(t)$  curves shown in Figures 6.37 to 6.45.



**Figure 6.37**  $E(t)$  modeling of experiment #2000 (three-stage column).



**Figure 6.38**  $E(t)$  modeling of experiment #2001 (three-stage column).

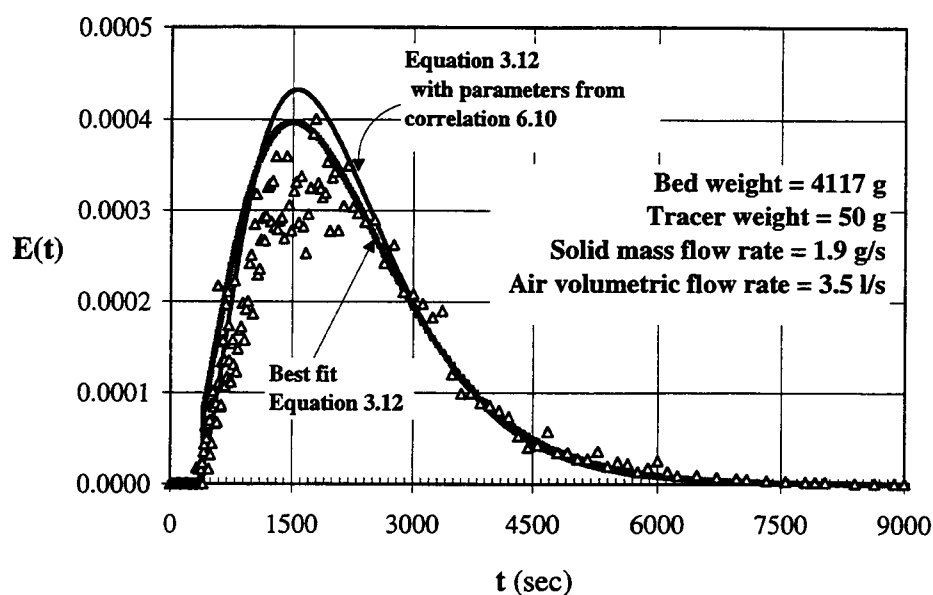


Figure 6.39  $E(t)$  modeling of experiment #2002 (three-stage column).

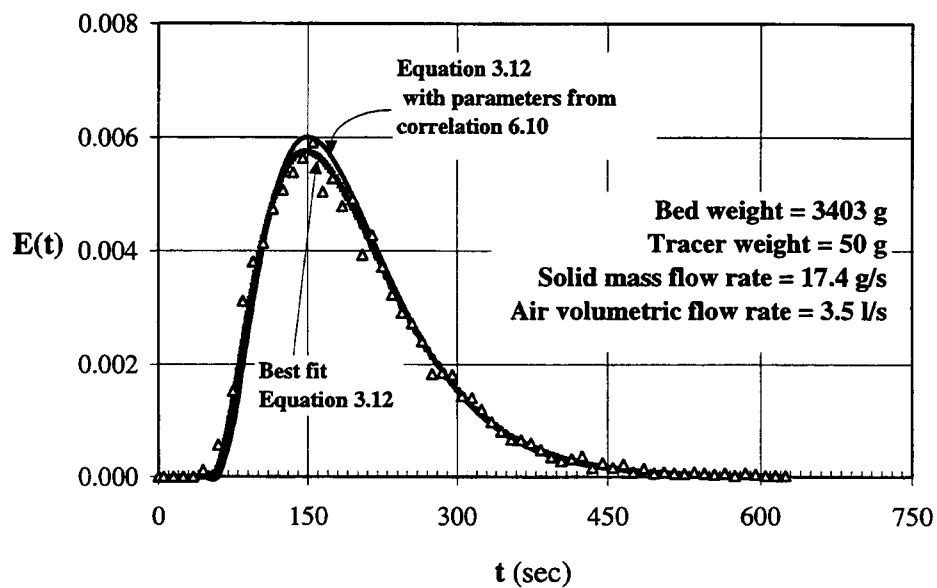
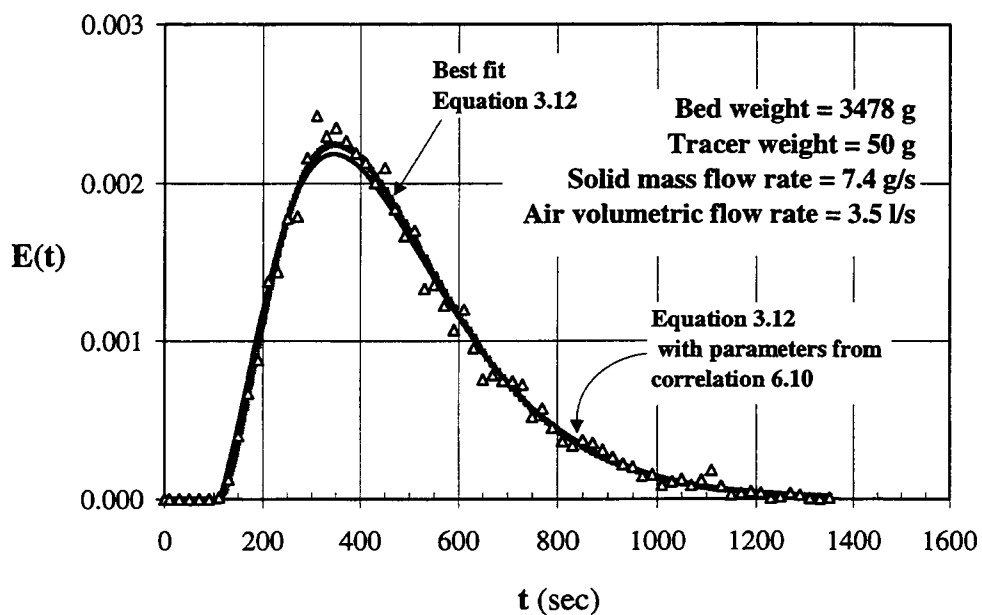
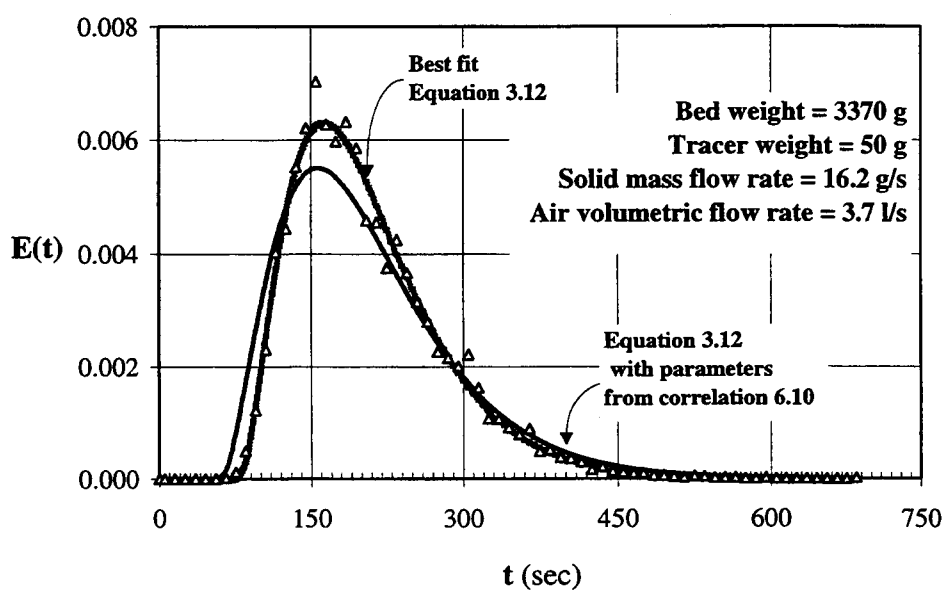


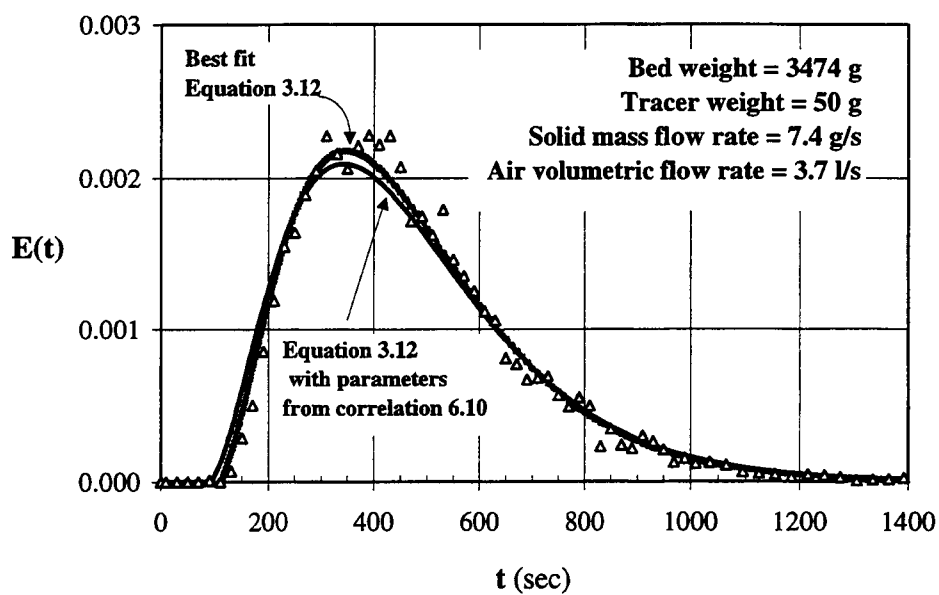
Figure 6.40  $E(t)$  modeling of experiment #2003 (three-stage column).



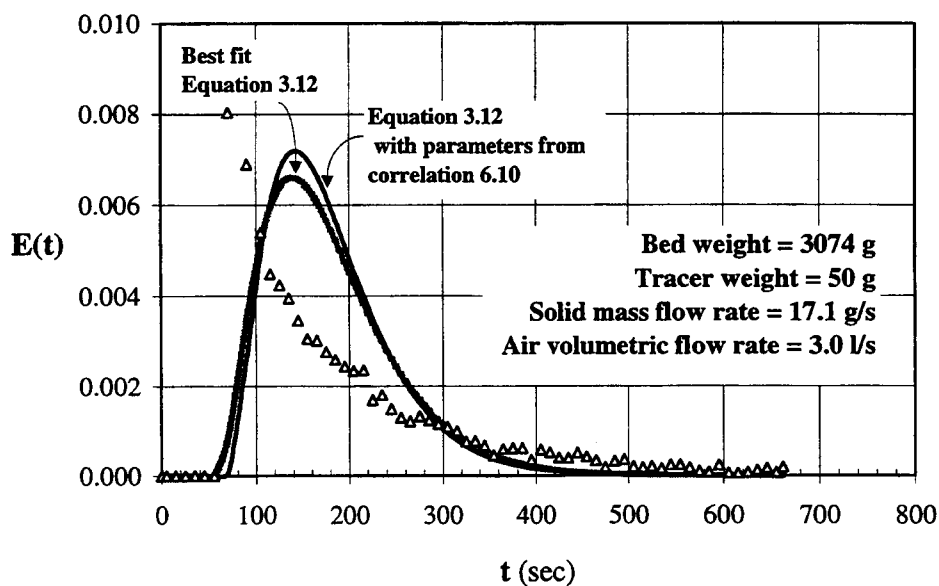
**Figure 6.41**  $E(t)$  modeling of experiment #2004 (three-stage column).



**Figure 6.42**  $E(t)$  modeling of experiment #2005 (three-stage column).

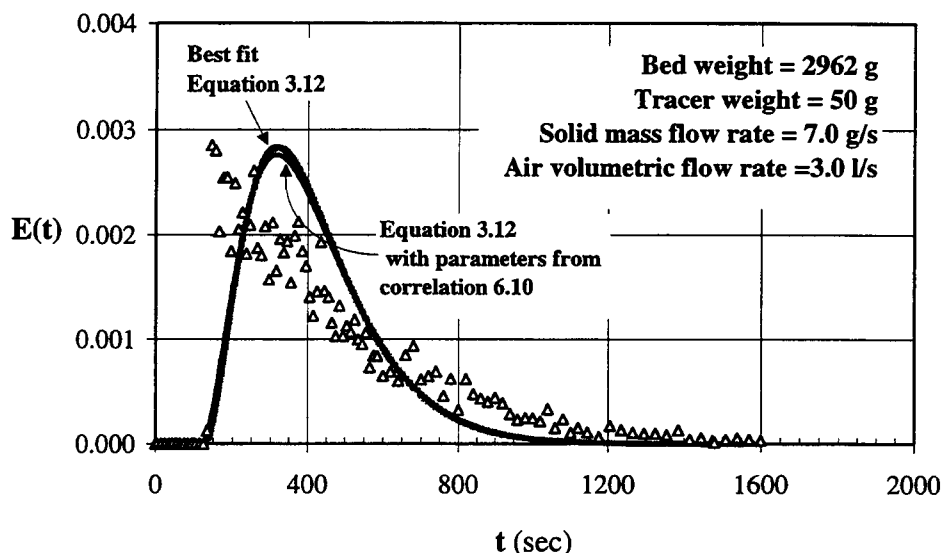


**Figure 6.43**  $E(t)$  modeling of experiment #2006 (three-stage column).



**Figure 6.44**  $E(t)$  modeling of experiment #2007 (three-stage column).





**Figure 6.45**  $E(t)$  modeling of experiment #2009 (three-stage column).

## 6.4 Discussion

After looking all previous results, we conclude that the data corresponding to those experiments in the region of higher gas flow rates, are well modeled by both Equations 3.12 and 6.10. On the other hand, it is obvious that for lower gas flow rates, and any of the tested solid flow rates, both equations fail in predicting the experimental data. When gas flow is low, it seems that the solid circulating pattern does not develop because not all the particles have enough kinetic energy to rise to the top of the draft tube. Therefore, to get mixed flow behavior, we need high recirculation rates.

Certainly, with units of different size and geometry, this low gas flow limit will be different. We must say that we consider these conditions as the limit for bad behavior of the vessel. What causes this bad behavior?. We are not sure and consequently we can not give a satisfactory answer in this preliminary study. Most important is that we were not interested in studying bad behavior, rather we wanted to know the lower flow rate limits and good behavior. We found this limit to be above a GFR of 3.5 lit/sec for our particular design.

## CHAPTER 7

### CONCLUSIONS AND RECOMMENDATIONS

The following conclusions can be drawn based on the results obtained in this study:

1. The design of a staged spouted bed column used in this study has clear operating and scale-up advantages over designs reported in the literature. With the addition of a draft tube to each stage, internal recirculation of solids is improved, allowing operation with less gas and lower pressure drop. Under these conditions, there should be practically no limitation to the number of stages that could be used in such a column.
2. For high gas flow rates (above 3.5 liters/sec), the simple circulation model developed and tested predicts the data well.
  - a) At a constant gas flow rate, an increase in solid flow rate will reduce the mixing of solids since solids spend less time within the vessel.
  - b) Similarly, at a constant solid flow rate, an increase of gas flow rate will reduce the plug flow behavior of the vessel.
  - c) The size of the dead volume is found to be negligible for almost all working conditions.
3. To start up an empty unit: turn on the gas, then pour in the solids. These will fill the bottom stage, then the ones above. To shut down, just let the solids pour out. Hardly any solids will be left behind in the unit. Thus the start-up and shut-down procedures for this column are easy to perform and do not require special devices with moving parts.
4. For low gas flow rates, the developed model is not a good representation of the experimental data. It is not clear in this preliminary study what could be the reasons behind this disagreement. One could speculate that one cause of disagreement may be found in the pressure drop difference. For the single-stage

unit a set of experiments were conducted just to show that the individual vessels, taken *one-by-one*, behave identically. It is proved, and we have no reasons to suspect any difference. But for the three-stage column, besides a possible interaction between the stages, merely a speculation, the actual total pressure is not the same for each stage.

5. A more general, and also probably more complex, circulation model could be developed. This model should include characteristics that allow prediction of all operating conditions such as zero and low spouting gas flow rates. For these situations, the present circulation model fails to represent the data properly. The reason behind this “failure” may be found on the assumption of *identical* stages for this column. Therefore, it can be speculated that a model coming from the convolution of Model 1, representing a single stage, with the assumption that all three stages are different, may produce better results than the model developed here.
6. Although we have not yet thoroughly documented this viewpoint, we believe that a pulsating valve should be used for feeding air to the L-valve. Visual observations show that a more uniform flow of solids is obtained when oscillating air pressure is used. This modification of the L-valve transforms it into a “*spitting valve*”, which should be tested for further studies.
7. In order to have a better flow description of either the single-stage unit or the three-stage column, it would be convenient to obtain information on *gas* RTD.
8. The multistage, countercurrent, gas-solid spouted bed here presented, could be easily transformed in a cross-current multistage system. The various applications for this column become, in that case, even more interesting than the countercurrent system, since different conditions could be easily achieved in each stage.

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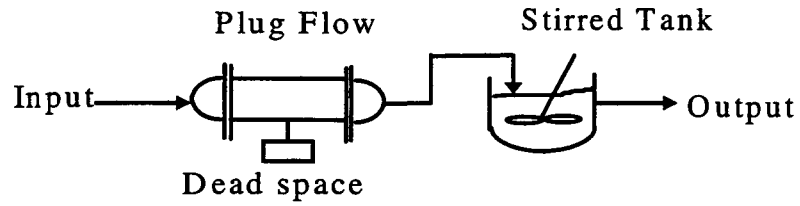
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## **APPENDICES**

## APPENDIX A

### DOCUMENTATION FOR SINGLE-STAGE UNIT MODEL



The mean residence time,  $\tau$ , can be written as

$$\tau = \frac{W}{v} = \frac{W_p}{v} + \frac{W_M}{v} + \frac{W_d}{v} = \tau_p + \tau_M + \tau_d \quad (A1)$$

Since dead zone does not participate in the distribution of the tracer, one can write from a material balance of active vessel volume

$$v \cdot C_{out}(t) = v \cdot C_{in}(t) \cdot E_1(t) \cdot E_2(t) \quad (A2)$$

Taking Laplace transforms in both sides of equation (A2)

$$C_{out}(s) = C_{in}(s) \cdot E_1(s) \cdot E_2(s) \quad (A3)$$

or

$$\frac{C_{out}(s)}{C_{in}(s)} = E_1(s) \cdot E_2(s) \quad (A4)$$

In Laplace domain it can be shown that

$$E_1(s) = e^{-s \tau_p} \quad (A5)$$

similarly

$$E_2(s) = \frac{\frac{1}{\tau_M}}{s + \frac{1}{\tau_M}} \quad (\text{A6})$$

Therefore, equation (A4) can be written as

$$\frac{C_{\text{out}}(s)}{C_{\text{in}}(s)} = \frac{1}{\tau_M} \frac{e^{-s\tau_p}}{s + \frac{1}{\tau_M}} \quad (\text{A7})$$

Taking the inverse of the Laplace transform, we obtain the model equation

$$E(t) = \frac{C_{\text{out}}(t)}{C_{\text{in}}(t)} = \frac{1}{\tau_M} e^{-\frac{(t-\tau_p)}{\tau_M}} \quad (\text{A8})$$

Equation (A1) reduces to

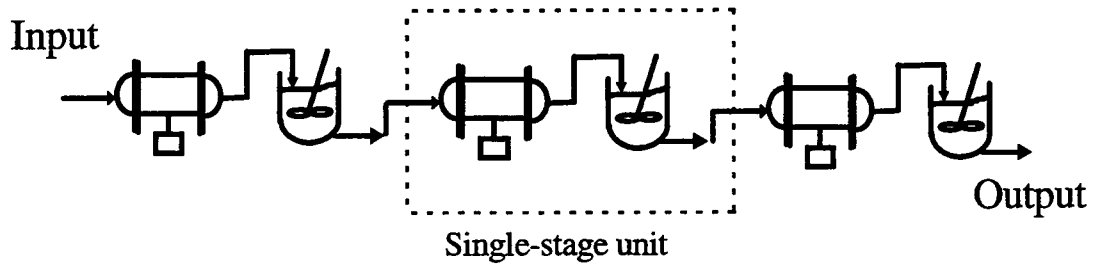
$$\tau = \tau_p + \tau_M \quad (\text{A1}')$$

when there are not dead zones in the vessel. This is often the case when vigorous mixing is provided.



## APPENDIX B

### DOCUMENTATION FOR MULTISTAGE UNIT MODEL



For three-stage column

$$E(t) = E_1(t) * E_2(t) * E_3(t) \quad (B1)$$

where  $E(t)$  is the residence-time distribution of solids in the column, and  $E_i(t)$  represent the residence-time distribution of solids in each single-stage unit.

From a material balance

$$\begin{aligned} v \cdot C_{out}(t) &= v \cdot C_{in}(t) * E(t) \\ &= v \cdot C_{in}(t) * E_1(t) * E_2(t) * E_3(t) \end{aligned} \quad (B2)$$

Taking Laplace transforms in both sides of equation (B2)

$$C_{out}(s) = C_{in}(s) \cdot E_1(s) \cdot E_2(s) \cdot E_3(s)$$

or

$$\frac{C_{out}(s)}{C_{in}(s)} = E_1(s) \cdot E_2(s) \cdot E_3(s) \quad (B3)$$

where

$$E_1(s) = E_2(s) = E_3(s) = \frac{1}{\tau_M} \frac{e^{-s\tau_p}}{s + \frac{1}{\tau_M}} \quad \dots \quad (B4)$$

since we are assuming *identical* stages. Then,

$$\begin{aligned} \frac{C_{out}(s)}{C_{in}(s)} &= \left( \frac{1}{\tau_{Mi}} \frac{e^{-s\tau_{pi}}}{s + \frac{1}{\tau_{Mi}}} \right)^3 \\ &= \frac{1}{\tau_{Mi}^3} \frac{e^{-3s\tau_{pi}}}{\left(s + \frac{1}{\tau_{Mi}}\right)^3} \end{aligned} \quad (B5)$$

Taking the inverse of the Laplace transform, we obtain the residence-time distribution of solids for the entire column

$$E(t) = \frac{C_{out}(t)}{C_{in}(t)} = \frac{1}{2\tau_{Mi}^3} (t - 3\tau_{pi})^2 \exp\left(-\left(t - 3\tau_{pi}\right)/\tau_{Mi}\right) \quad (B6)$$

Using equation (A1'), we finally obtain

$$E(t) = \frac{C_{out}(t)}{C_{in}(t)} = \frac{1}{2} \frac{(t - 3\tau_{pi})^2}{(\tau_i - \tau_{pi})^3} \exp\left(-\left(t - 3\tau_{pi}\right)/(\tau_i - \tau_{pi})\right) \quad (B7)$$

## APPENDIX C

### OPTIMIZATION ROUTINE<sup>1</sup>

#### Newton's Method

The primary necessary condition for  $f(x)$  to have a local minimum is that  $f'(x) = 0$ . Consequently, we can solve the equation  $f'(x) = 0$  by Newton's method to get

$$x^{k+1} = x^k - \frac{f'(x^k)}{f''(x^k)} \quad (\text{C.1})$$

making sure on each  $k$  that  $f(x^{k+1}) < f(x^k)$  for a minimum (see Figure C.1).

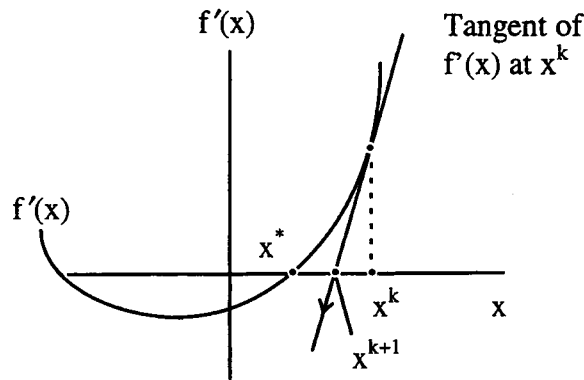
To see what Newton's method implies about  $f(x)$ , suppose  $f(x)$  is approximated by a quadratic function at  $x^k$

$$f(x) = f(x^k) + f'(x^k)(x - x^k) + \frac{1}{2}f''(x^k)(x - x^k)^2 \quad (\text{C.2})$$

Find  $df(x)/dx = 0$ , a stationary point of the quadratic model of the function. The result by differentiating Equation (C.2) is

$$f'(x^k) + \left(\frac{1}{2}\right)(2)f''(x^k)(x - x^k) = 0 \quad (\text{C.3})$$

which can be rearranged to yield Eq.(C.1). Consequently, Newton's method is equivalent to using a quadratic model for a function in minimization (or maximization) and applying the necessary conditions.



**Figure C.1** Newton's method applied to solution of  $f'(x) = 0$ .

The advantages of Newton's method are:

1. The procedure is locally quadratically convergent to the extremum as long as  $f''(x) \neq 0$ .
2. For a quadratic function, the minimum is obtained in one iteration.

The disadvantages of the method are:

1. We have to calculate both  $f'(x)$  and  $f''(x)$ .
2. If  $f'(x) \rightarrow 0$ , the method converges slowly.
3. If more than one extremum exist, the method may not converge to the desired extremum (the global one) and might oscillate.

### Quasi-Newton's Method

A quasi-Newton method in general is one that imitates Newton's method. If  $f(x)$  is not given by a formula, or the formula is so complicated that analytical derivatives cannot be formulated, we can replace Eq.(C.1) with a finite difference approximation

$$x^{k+1} = x^k - \frac{[f(x+h) - f(x-h)] / 2h}{[f(x+h) - 2f(x) + f(x-h)] / h^2} \quad (C.4)$$

Central differences have been used in Eq.(C.4) but forward differences or any other difference scheme would suffice as long as the step size  $h$  is selected to match the difference formula and the computer (machine) precision for the computer on which the calculations are to be executed.

Other than selection of the value of  $h$ , the only additional disadvantage of the quasi-Newton method is that additional function evaluation are needed on each iteration  $k$  [three for formula (C.4) versus two for formula (C.1)].

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<sup>1</sup> Adapted from Edgar, T. F., and Himmelblau, D. M., "Optimization of Chemical Processes", McGraw-Hill, Inc., 1988.

## APPENDIX D

## EXPERIMENTAL DATA

Table D.1 Data Run# 1030

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | C(t)     | E(t)    | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|-------|--------|------------|-------|----------|---------|-------------------|--------------------|--------------------------|
| 0          | 69.3  | 0.00   | 10         | 0     | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 10         | 69.3  | 0.00   | 10         | 5     | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 20         | 69.3  | 0.00   | 10         | 15    | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 30         | 67.2  | 0.00   | 10         | 25    | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 40         | 67.3  | 0.34   | 10         | 35    | 0.005053 | 0.00070 | 0.00700           | 0.0505             | 1.77                     |
| 50         | 69.3  | 3.64   | 10         | 45    | 0.052495 | 0.00727 | 0.07272           | 0.5249             | 23.62                    |
| 60         | 73.2  | 3.42   | 10         | 55    | 0.046731 | 0.00647 | 0.06474           | 0.4673             | 25.70                    |
| 70         | 68.3  | 3.24   | 10         | 65    | 0.047445 | 0.00657 | 0.06573           | 0.4744             | 30.84                    |
| 80         | 67.2  | 2.82   | 10         | 75    | 0.041964 | 0.00581 | 0.05813           | 0.4196             | 31.47                    |
| 90         | 67.1  | 2.51   | 10         | 85    | 0.037401 | 0.00518 | 0.05181           | 0.3740             | 31.79                    |
| 100        | 71.5  | 2.68   | 10         | 95    | 0.037503 | 0.00520 | 0.05195           | 0.3750             | 35.63                    |
| 110        | 72.4  | 2.3    | 10         | 105   | 0.031786 | 0.00440 | 0.04403           | 0.3179             | 33.37                    |
| 120        | 67.0  | 1.95   | 10         | 115   | 0.029087 | 0.00403 | 0.04030           | 0.2909             | 33.45                    |
| 130        | 67.6  | 1.86   | 10         | 125   | 0.027535 | 0.00381 | 0.03815           | 0.2754             | 34.42                    |
| 140        | 68.0  | 1.69   | 10         | 135   | 0.024860 | 0.00344 | 0.03444           | 0.2486             | 33.56                    |
| 150        | 68.1  | 1.61   | 10         | 145   | 0.023656 | 0.00328 | 0.03277           | 0.2366             | 34.30                    |
| 160        | 71.5  | 1.63   | 10         | 155   | 0.022813 | 0.00316 | 0.03160           | 0.2281             | 35.36                    |
| 170        | 71.8  | 1.49   | 10         | 165   | 0.020758 | 0.00288 | 0.02876           | 0.2076             | 34.25                    |
| 180        | 67.5  | 1.28   | 10         | 175   | 0.018957 | 0.00263 | 0.02626           | 0.1896             | 33.18                    |
| 190        | 68.2  | 1.16   | 10         | 185   | 0.017004 | 0.00236 | 0.02356           | 0.1700             | 31.46                    |
| 200        | 72.5  | 1.18   | 10         | 195   | 0.016267 | 0.00225 | 0.02253           | 0.1627             | 31.72                    |
| 210        | 70.5  | 1.23   | 10         | 205   | 0.017458 | 0.00242 | 0.02418           | 0.1746             | 35.79                    |
| 220        | 68.0  | 1.01   | 10         | 215   | 0.014859 | 0.00206 | 0.02059           | 0.1486             | 31.95                    |
| 230        | 67.5  | 0.92   | 10         | 225   | 0.013634 | 0.00189 | 0.01889           | 0.1363             | 30.68                    |
| 240        | 67.4  | 0.86   | 10         | 235   | 0.012769 | 0.00177 | 0.01769           | 0.1277             | 30.01                    |
| 250        | 76.2  | 0.92   | 10         | 245   | 0.012072 | 0.00167 | 0.01672           | 0.1207             | 29.58                    |
| 260        | 63.7  | 0.58   | 10         | 255   | 0.009099 | 0.00126 | 0.01261           | 0.0910             | 23.20                    |
| 270        | 68.2  | 0.68   | 10         | 265   | 0.009972 | 0.00138 | 0.01381           | 0.0997             | 26.43                    |
| 280        | 67.8  | 0.62   | 10         | 275   | 0.009140 | 0.00127 | 0.01266           | 0.0914             | 25.14                    |
| 290        | 67.8  | 0.53   | 10         | 285   | 0.007818 | 0.00108 | 0.01083           | 0.0782             | 22.28                    |
| 300        | 74.7  | 0.63   | 10         | 295   | 0.008434 | 0.00117 | 0.01168           | 0.0843             | 24.88                    |
| 310        | 69.1  | 0.38   | 10         | 305   | 0.005502 | 0.00076 | 0.00762           | 0.0550             | 16.78                    |
| 320        | 67.8  | 0.55   | 10         | 315   | 0.008113 | 0.00112 | 0.01124           | 0.0811             | 25.56                    |
| 330        | 67.7  | 0.44   | 10         | 325   | 0.006504 | 0.00090 | 0.00901           | 0.0650             | 21.14                    |
| 340        | 67.0  | 0.45   | 10         | 335   | 0.006712 | 0.00093 | 0.00930           | 0.0671             | 22.49                    |
| 350        | 73.8  | 0.39   | 10         | 345   | 0.005287 | 0.00073 | 0.00732           | 0.0529             | 18.24                    |
| 360        | 70.1  | 0.3    | 10         | 355   | 0.004278 | 0.00059 | 0.00593           | 0.0428             | 15.19                    |
| 370        | 67.0  | 0.33   | 10         | 365   | 0.004924 | 0.00068 | 0.00682           | 0.0492             | 17.97                    |
| 380        | 68.1  | 0.32   | 10         | 375   | 0.004696 | 0.00065 | 0.00651           | 0.0470             | 17.61                    |
| 390        | 73.0  | 0.27   | 10         | 385   | 0.003700 | 0.00051 | 0.00513           | 0.0370             | 14.25                    |
| 400        | 70.9  | 0.32   | 10         | 395   | 0.004514 | 0.00063 | 0.00625           | 0.0451             | 17.83                    |
| 410        | 67.2  | 0.26   | 10         | 405   | 0.003871 | 0.00054 | 0.00536           | 0.0387             | 15.68                    |
| 420        | 67.1  | 0.265  | 10         | 415   | 0.003952 | 0.00055 | 0.00547           | 0.0395             | 16.40                    |
| 430        | 67.8  | 0.22   | 10         | 425   | 0.003247 | 0.00045 | 0.00450           | 0.0325             | 13.80                    |
| 440        | 69.0  | 0.23   | 10         | 435   | 0.003331 | 0.00046 | 0.00462           | 0.0333             | 14.49                    |
| 450        | 74.7  | 0.195  | 10         | 445   | 0.002610 | 0.00036 | 0.00362           | 0.0261             | 11.62                    |
| 460        | 69.0  | 0.2    | 10         | 455   | 0.002897 | 0.00040 | 0.00401           | 0.0290             | 13.18                    |
| 470        | 67.1  | 0.12   | 10         | 465   | 0.001788 | 0.00025 | 0.00248           | 0.0179             | 8.31                     |
| 480        | 68.5  | 0.1    | 10         | 475   | 0.001460 | 0.00020 | 0.00202           | 0.0146             | 6.94                     |
| 490        | 67.8  | 0.18   | 10         | 485   | 0.002654 | 0.00037 | 0.00368           | 0.0265             | 12.87                    |
| 500        | 75.5  | 0.13   | 10         | 495   | 0.001722 | 0.00024 | 0.00239           | 0.0172             | 8.52                     |
| 510        | 69.3  | 0.13   | 10         | 505   | 0.001876 | 0.00026 | 0.00260           | 0.0188             | 9.47                     |
| 520        | 68.0  | 0.12   | 10         | 515   | 0.001766 | 0.00024 | 0.00245           | 0.0177             | 9.09                     |
| 530        | 68.6  | 0.16   | 10         | 525   | 0.002333 | 0.00032 | 0.00323           | 0.0233             | 12.25                    |

## Run# 1030 (Cont..)

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$   | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|-------|--------|------------|-------|----------|---------|-------------------|--------------------|--------------------------|
| 540        | 75.0  | 0.10   | 10         | 535   | 0.001333 | 0.00018 | 0.00185           | 0.0133             | 7.13                     |
| 550        | 67.5  | 0.06   | 10         | 545   | 0.000889 | 0.00012 | 0.00123           | 0.0089             | 4.85                     |
| 560        | 68.1  | 0.06   | 10         | 555   | 0.000881 | 0.00012 | 0.00122           | 0.0088             | 4.89                     |
| 570        | 73.3  | 0.04   | 10         | 565   | 0.000545 | 0.00008 | 0.00076           | 0.0055             | 3.08                     |
| 580        | 68.5  | 0.03   | 10         | 575   | 0.000438 | 0.00006 | 0.00061           | 0.0044             | 2.52                     |
| 590        | 69.2  | 0.07   | 10         | 585   | 0.001012 | 0.00014 | 0.00140           | 0.0101             | 5.92                     |
| 600        | 67.9  | 0.05   | 10         | 595   | 0.000736 | 0.00010 | 0.00102           | 0.0074             | 4.38                     |
| 610        | 67.6  | 0.05   | 10         | 605   | 0.000740 | 0.00010 | 0.00102           | 0.0074             | 4.47                     |
| 620        | 66.8  | 0.04   | 10         | 615   | 0.000599 | 0.00008 | 0.00083           | 0.0060             | 3.68                     |
| 630        | 73.9  | 0.06   | 10         | 625   | 0.000812 | 0.00011 | 0.00113           | 0.0081             | 5.08                     |
| 640        | 69.5  | 0.04   | 10         | 635   | 0.000576 | 0.00008 | 0.00080           | 0.0058             | 3.66                     |
| 650        | 66.8  | 0.04   | 10         | 645   | 0.000598 | 0.00008 | 0.00083           | 0.0060             | 3.86                     |
| 660        | 66.6  | 0.02   | 10         | 655   | 0.000300 | 0.00004 | 0.00042           | 0.0030             | 1.97                     |
| 670        | 67.7  | 0.04   | 10         | 665   | 0.000591 | 0.00008 | 0.00082           | 0.0059             | 3.93                     |
| 680        | 75.0  | 0.05   | 10         | 675   | 0.000666 | 0.00009 | 0.00092           | 0.0067             | 4.50                     |
| 690        | 66.3  | 0.02   | 10         | 685   | 0.000302 | 0.00004 | 0.00042           | 0.0030             | 2.07                     |
| 700        | 68.1  | 0.03   | 10         | 695   | 0.000441 | 0.00006 | 0.00061           | 0.0044             | 3.06                     |
| 710        | 68.4  | 0      | 10         | 705   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 720        | 73.2  | 0.03   | 10         | 715   | 0.000410 | 0.00006 | 0.00057           | 0.0041             | 2.93                     |
| 730        | 68.9  | 0.02   | 10         | 725   | 0.000290 | 0.00004 | 0.00040           | 0.0029             | 2.11                     |
| 740        | 68.3  | 0.02   | 10         | 735   | 0.000293 | 0.00004 | 0.00041           | 0.0029             | 2.15                     |
| 750        | 67.2  | 0.04   | 10         | 745   | 0.000595 | 0.00008 | 0.00082           | 0.0060             | 4.44                     |
| 760        | 67.6  | 0.01   | 10         | 755   | 0.000148 | 0.00002 | 0.00020           | 0.0015             | 1.12                     |
| 770        | 75.8  | 0      | 10         | 765   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 780        | 67.8  | 0.02   | 10         | 775   | 0.000295 | 0.00004 | 0.00041           | 0.0030             | 2.29                     |
| 790        | 67.1  | 0.04   | 10         | 785   | 0.000596 | 0.00008 | 0.00083           | 0.0060             | 4.68                     |
| 800        | 68.0  | 0.04   | 10         | 795   | 0.000588 | 0.00008 | 0.00081           | 0.0059             | 4.68                     |
| 810        | 67.9  | 0.01   | 10         | 805   | 0.000147 | 0.00002 | 0.00020           | 0.0015             | 1.19                     |
| 820        | 74.7  | 0.01   | 10         | 815   | 0.000134 | 0.00002 | 0.00019           | 0.0013             | 1.09                     |
| 830        | 68.6  | 0.01   | 10         | 825   | 0.000146 | 0.00002 | 0.00020           | 0.0015             | 1.20                     |
| 840        | 67.9  | 0      | 10         | 835   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 850        | 68.5  | 0.02   | 10         | 845   | 0.000292 | 0.00004 | 0.00040           | 0.0029             | 2.47                     |
| 860        | 72.4  | 0.01   | 10         | 855   | 0.000138 | 0.00002 | 0.00019           | 0.0014             | 1.18                     |
| 870        | 72.0  | 0.01   | 10         | 865   | 0.000139 | 0.00002 | 0.00019           | 0.0014             | 1.20                     |
| 880        | 66.7  | 0      | 10         | 875   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 890        | 67.0  | 0.01   | 10         | 885   | 0.000149 | 0.00002 | 0.00021           | 0.0015             | 1.32                     |
| 900        | 67.2  | 0.02   | 10         | 895   | 0.000298 | 0.00004 | 0.00041           | 0.0030             | 2.66                     |
| 910        | 73.9  | 0      | 10         | 905   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 920        | 69.0  | 0.01   | 10         | 915   | 0.000145 | 0.00002 | 0.00020           | 0.0014             | 1.33                     |
| 930        | 66.6  | 0.01   | 10         | 925   | 0.000150 | 0.00002 | 0.00021           | 0.0015             | 1.39                     |
| 940        | 67.4  | 0.01   | 10         | 935   | 0.000148 | 0.00002 | 0.00021           | 0.0015             | 1.39                     |
| 950        | 70.0  | 0      | 10         | 945   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 960        | 73.1  | 0.01   | 10         | 955   | 0.000137 | 0.00002 | 0.00019           | 0.0014             | 1.31                     |
| 970        | 68.2  | 0      | 10         | 965   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 980        | 66.8  | 0      | 10         | 975   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 990        | 68.5  | 0      | 10         | 985   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 1000       | 73.6  | 0      | 10         | 995   | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 1010       | 68.9  | 0      | 10         | 1005  | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 1020       | 68.5  | 0      | 10         | 1015  | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 1030       | 67.5  | 0      | 10         | 1025  | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 1040       | 69.0  | 0      | 10         | 1035  | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |

$$\Sigma E(t) \Delta t_i = 0.9988$$

|                       |
|-----------------------|
| $S_o = 6.927$ g/s     |
| Bed weight = 1198.0 g |
| $\tau = 172.95$ sec   |

|                      |                                      |
|----------------------|--------------------------------------|
| $\tau_{obs} = 172.9$ | $\Sigma C_i t_i \Delta t_i = 1246.6$ |
|                      | $\Sigma C_i \Delta t_i = 7.21$       |

Table D.2 Data Run #1031

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t \cdot E(t)$ | $C_i \cdot \Delta t$ | $C_i \cdot t_i \cdot \Delta t$ |
|------------|-------|--------|------------|-------|---------|---------|-----------------------|----------------------|--------------------------------|
| 0          | 58.8  | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000               | 0.0000               | 0.00                           |
| 20         | 58.8  | 0.00   | 10         | 10    | 0.00000 | 0.00000 | 0.00000               | 0.0000               | 0.00                           |
| 30         | 58.8  | 0.00   | 10         | 25    | 0.00000 | 0.00000 | 0.00000               | 0.0000               | 0.00                           |
| 40         | 57.1  | 0.00   | 10         | 35    | 0.00000 | 0.00000 | 0.00000               | 0.0000               | 0.00                           |
| 50         | 65.9  | 4.61   | 10         | 45    | 0.06997 | 0.00823 | 0.08226               | 0.6997               | 31.48                          |
| 60         | 57.5  | 9.13   | 10         | 55    | 0.15889 | 0.01868 | 0.18682               | 1.5889               | 87.39                          |
| 70         | 58.1  | 4.30   | 10         | 65    | 0.07404 | 0.00870 | 0.08705               | 0.7404               | 48.12                          |
| 80         | 58.0  | 2.69   | 10         | 75    | 0.04642 | 0.00546 | 0.05458               | 0.4642               | 34.81                          |
| 90         | 64.6  | 2.19   | 10         | 85    | 0.03391 | 0.00399 | 0.03987               | 0.3391               | 28.82                          |
| 100        | 57.2  | 1.56   | 10         | 95    | 0.02726 | 0.00321 | 0.03206               | 0.2726               | 25.90                          |
| 110        | 56.7  | 1.15   | 10         | 105   | 0.02029 | 0.00239 | 0.02385               | 0.2029               | 21.30                          |
| 120        | 58.6  | 1.28   | 10         | 115   | 0.02183 | 0.00257 | 0.02566               | 0.2183               | 25.10                          |
| 130        | 60.3  | 1.15   | 10         | 125   | 0.01906 | 0.00224 | 0.02241               | 0.1906               | 23.82                          |
| 140        | 62.4  | 1.16   | 10         | 135   | 0.01859 | 0.00219 | 0.02185               | 0.1859               | 25.09                          |
| 150        | 58.3  | 0.98   | 10         | 145   | 0.01680 | 0.00198 | 0.01976               | 0.1680               | 24.36                          |
| 160        | 64.2  | 0.88   | 10         | 155   | 0.01370 | 0.00161 | 0.01611               | 0.1370               | 21.24                          |
| 170        | 51.8  | 0.81   | 10         | 165   | 0.01564 | 0.00184 | 0.01839               | 0.1564               | 25.81                          |
| 180        | 57.4  | 0.87   | 10         | 175   | 0.01515 | 0.00178 | 0.01782               | 0.1515               | 26.52                          |
| 190        | 63.2  | 0.74   | 10         | 185   | 0.01171 | 0.00138 | 0.01377               | 0.1171               | 21.67                          |
| 200        | 57.9  | 0.56   | 10         | 195   | 0.00967 | 0.00114 | 0.01137               | 0.0967               | 18.86                          |
| 210        | 57.5  | 0.62   | 10         | 205   | 0.01078 | 0.00127 | 0.01268               | 0.1078               | 22.10                          |
| 220        | 57.1  | 0.59   | 10         | 215   | 0.01034 | 0.00122 | 0.01215               | 0.1034               | 22.22                          |
| 230        | 62.5  | 0.66   | 10         | 225   | 0.01057 | 0.00124 | 0.01242               | 0.1057               | 23.78                          |
| 240        | 53.5  | 0.58   | 10         | 235   | 0.01085 | 0.00128 | 0.01276               | 0.1085               | 25.49                          |
| 250        | 58.1  | 0.71   | 10         | 245   | 0.01221 | 0.00144 | 0.01436               | 0.1221               | 29.92                          |
| 260        | 58.8  | 0.62   | 10         | 255   | 0.01054 | 0.00124 | 0.01239               | 0.1054               | 26.87                          |
| 270        | 63.3  | 0.63   | 10         | 265   | 0.00995 | 0.00117 | 0.01170               | 0.0995               | 26.38                          |
| 280        | 58.7  | 0.52   | 10         | 275   | 0.00886 | 0.00104 | 0.01042               | 0.0886               | 24.36                          |
| 290        | 58.8  | 0.48   | 10         | 285   | 0.00817 | 0.00096 | 0.00960               | 0.0817               | 23.27                          |
| 300        | 57.7  | 0.44   | 10         | 295   | 0.00762 | 0.00090 | 0.00896               | 0.0762               | 22.49                          |
| 310        | 60.3  | 0.45   | 10         | 305   | 0.00746 | 0.00088 | 0.00877               | 0.0746               | 22.75                          |
| 320        | 61.2  | 0.4    | 10         | 315   | 0.00654 | 0.00077 | 0.00769               | 0.0654               | 20.61                          |
| 330        | 57.1  | 0.29   | 10         | 325   | 0.00508 | 0.00060 | 0.00597               | 0.0508               | 16.50                          |
| 340        | 57.5  | 0.37   | 10         | 335   | 0.00644 | 0.00076 | 0.00757               | 0.0644               | 21.57                          |
| 350        | 57.5  | 0.32   | 10         | 345   | 0.00557 | 0.00065 | 0.00655               | 0.0557               | 19.21                          |
| 360        | 58.4  | 0.47   | 10         | 355   | 0.00805 | 0.00095 | 0.00946               | 0.0805               | 28.56                          |
| 370        | 60.8  | 0.46   | 10         | 365   | 0.00756 | 0.00089 | 0.00889               | 0.0756               | 27.60                          |
| 380        | 58.2  | 0.31   | 10         | 375   | 0.00533 | 0.00063 | 0.00626               | 0.0533               | 19.97                          |
| 390        | 62.9  | 0.33   | 10         | 385   | 0.00525 | 0.00062 | 0.00617               | 0.0525               | 20.20                          |
| 400        | 53.4  | 0.34   | 10         | 395   | 0.00637 | 0.00075 | 0.00749               | 0.0637               | 25.17                          |
| 410        | 59.0  | 0.33   | 10         | 405   | 0.00560 | 0.00066 | 0.00658               | 0.0560               | 22.67                          |
| 420        | 58.2  | 0.22   | 10         | 415   | 0.00378 | 0.00044 | 0.00445               | 0.0378               | 15.70                          |
| 430        | 57.9  | 0.24   | 10         | 425   | 0.00415 | 0.00049 | 0.00487               | 0.0415               | 17.62                          |
| 440        | 56.8  | 0.25   | 10         | 435   | 0.00440 | 0.00052 | 0.00518               | 0.0440               | 19.15                          |
| 450        | 57.9  | 0.23   | 10         | 445   | 0.00398 | 0.00047 | 0.00467               | 0.0398               | 17.69                          |
| 460        | 65.6  | 0.25   | 10         | 455   | 0.00381 | 0.00045 | 0.00448               | 0.0381               | 17.34                          |
| 470        | 55.7  | 0.195  | 10         | 465   | 0.00350 | 0.00041 | 0.00412               | 0.0350               | 16.29                          |
| 480        | 57.1  | 0.22   | 10         | 475   | 0.00385 | 0.00045 | 0.00453               | 0.0385               | 18.29                          |
| 490        | 61.0  | 0.18   | 10         | 485   | 0.00295 | 0.00035 | 0.00347               | 0.0295               | 14.31                          |
| 500        | 58.6  | 0.205  | 10         | 495   | 0.00350 | 0.00041 | 0.00411               | 0.0350               | 17.32                          |
| 510        | 58.4  | 0.16   | 10         | 505   | 0.00274 | 0.00032 | 0.00322               | 0.0274               | 13.83                          |
| 520        | 55.0  | 0.14   | 10         | 515   | 0.00254 | 0.00030 | 0.00299               | 0.0254               | 13.104                         |
| 530        | 57.3  | 0.16   | 10         | 525   | 0.00279 | 0.00033 | 0.00328               | 0.0279               | 14.66                          |



## Run #1031 (Cont..)

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t^* E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|-------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 540        | 59.3  | 0.18   | 10         | 535   | 0.00304 | 0.00036 | 0.00357           | 0.0304           | 16.25                  |
| 550        | 63.4  | 0.16   | 10         | 545   | 0.00244 | 0.00029 | 0.00287           | 0.0244           | 13.32                  |
| 560        | 58.4  | 0.14   | 10         | 555   | 0.00231 | 0.00027 | 0.00272           | 0.0231           | 12.82                  |
| 570        | 53.1  | 0.15   | 10         | 565   | 0.00282 | 0.00033 | 0.00332           | 0.0282           | 15.95                  |
| 580        | 63.4  | 0.12   | 10         | 575   | 0.00189 | 0.00022 | 0.00223           | 0.0189           | 10.89                  |
| 590        | 58.9  | 0.16   | 10         | 585   | 0.00272 | 0.00032 | 0.00319           | 0.0272           | 15.89                  |
| 600        | 57.8  | 0.09   | 10         | 595   | 0.00156 | 0.00018 | 0.00183           | 0.0156           | 9.27                   |
| 610        | 57.8  | 0.10   | 10         | 605   | 0.00164 | 0.00019 | 0.00193           | 0.0164           | 9.95                   |
| 620        | 57.7  | 0.08   | 10         | 615   | 0.00139 | 0.00016 | 0.00163           | 0.0139           | 8.52                   |
| 630        | 64.1  | 0.12   | 10         | 625   | 0.00187 | 0.00022 | 0.00220           | 0.0187           | 11.71                  |
| 640        | 58.6  | 0.07   | 10         | 635   | 0.00120 | 0.00014 | 0.00141           | 0.0120           | 7.59                   |
| 650        | 57.8  | 0.10   | 10         | 645   | 0.00173 | 0.00020 | 0.00203           | 0.0173           | 11.16                  |
| 660        | 55.8  | 0.11   | 10         | 655   | 0.00197 | 0.00023 | 0.00232           | 0.0197           | 12.92                  |
| 670        | 59.3  | 0.09   | 10         | 665   | 0.00152 | 0.00018 | 0.00178           | 0.0152           | 10.09                  |
| 680        | 60.8  | 0.07   | 10         | 675   | 0.00115 | 0.00014 | 0.00135           | 0.0115           | 7.77                   |
| 690        | 58.2  | 0.07   | 10         | 685   | 0.00112 | 0.00013 | 0.00131           | 0.0112           | 7.65                   |
| 700        | 56.7  | 0.09   | 10         | 695   | 0.00159 | 0.00019 | 0.00186           | 0.0159           | 11.02                  |
| 710        | 58.7  | 0.08   | 10         | 705   | 0.00136 | 0.00016 | 0.00160           | 0.0136           | 9.61                   |
| 720        | 64.7  | 0.10   | 10         | 715   | 0.00154 | 0.00018 | 0.00182           | 0.0154           | 11.05                  |
| 730        | 58.3  | 0.06   | 10         | 725   | 0.00103 | 0.00012 | 0.00121           | 0.0103           | 7.47                   |
| 740        | 56.3  | 0.03   | 10         | 735   | 0.00053 | 0.00006 | 0.00063           | 0.0053           | 3.92                   |
| 750        | 58.6  | 0.14   | 10         | 745   | 0.00230 | 0.00027 | 0.00271           | 0.0230           | 17.15                  |
| 760        | 58.1  | 0.04   | 10         | 755   | 0.00069 | 0.00008 | 0.00081           | 0.0069           | 5.20                   |
| 770        | 63.4  | 0.07   | 10         | 765   | 0.00110 | 0.00013 | 0.00130           | 0.0110           | 8.45                   |
| 780        | 57.2  | 0.04   | 10         | 775   | 0.00070 | 0.00008 | 0.00082           | 0.0070           | 5.42                   |
| 790        | 56.9  | 0.05   | 10         | 785   | 0.00088 | 0.00010 | 0.00103           | 0.0088           | 6.90                   |
| 800        | 60.8  | 0.07   | 10         | 795   | 0.00115 | 0.00014 | 0.00135           | 0.0115           | 9.16                   |
| 810        | 59.5  | 0.03   | 10         | 805   | 0.00050 | 0.00006 | 0.00059           | 0.0050           | 4.06                   |
| 820        | 58.1  | 0.05   | 10         | 815   | 0.00077 | 0.00009 | 0.00091           | 0.0077           | 6.31                   |
| 830        | 58.4  | 0.05   | 10         | 825   | 0.00086 | 0.00010 | 0.00101           | 0.0086           | 7.07                   |
| 840        | 58.4  | 0.05   | 10         | 835   | 0.00086 | 0.00010 | 0.00101           | 0.0086           | 7.14                   |
| 850        | 60.2  | 0.08   | 10         | 845   | 0.00133 | 0.00016 | 0.00156           | 0.0133           | 11.23                  |
| 860        | 59.5  | 0.04   | 10         | 855   | 0.00067 | 0.00008 | 0.00079           | 0.0067           | 5.75                   |
| 870        | 57.8  | 0.02   | 10         | 865   | 0.00035 | 0.00004 | 0.00041           | 0.0035           | 3.00                   |
| 880        | 57.9  | 0.02   | 10         | 875   | 0.00035 | 0.00004 | 0.00041           | 0.0035           | 3.03                   |
| 890        | 51.6  | 0.03   | 10         | 885   | 0.00058 | 0.00007 | 0.00068           | 0.0058           | 5.15                   |
| 900        | 62.1  | 0.05   | 10         | 895   | 0.00073 | 0.00009 | 0.00085           | 0.0073           | 6.49                   |
| 910        | 58.1  | 0.02   | 10         | 905   | 0.00034 | 0.00004 | 0.00040           | 0.0034           | 3.12                   |
| 920        | 57.2  | 0.04   | 10         | 915   | 0.00061 | 0.00007 | 0.00072           | 0.0061           | 5.60                   |
| 930        | 58.2  | 0.01   | 10         | 925   | 0.00017 | 0.00002 | 0.00020           | 0.0017           | 1.59                   |
| 940        | 63.7  | 0.04   | 10         | 935   | 0.00063 | 0.00007 | 0.00074           | 0.0063           | 5.87                   |
| 950        | 59.5  | 0.03   | 10         | 945   | 0.00050 | 0.00006 | 0.00059           | 0.0050           | 4.76                   |
| 960        | 57.7  | 0.03   | 10         | 955   | 0.00052 | 0.00006 | 0.00061           | 0.0052           | 4.97                   |
| 970        | 53.7  | 0.01   | 10         | 965   | 0.00019 | 0.00002 | 0.00022           | 0.0019           | 1.80                   |
| 980        | 63.9  | 0.02   | 10         | 975   | 0.00031 | 0.00004 | 0.00037           | 0.0031           | 3.05                   |
| 990        | 58.2  | 0.02   | 10         | 985   | 0.00034 | 0.00004 | 0.00040           | 0.0034           | 3.38                   |
| 1000       | 56.3  | 0.04   | 10         | 995   | 0.00071 | 0.00008 | 0.00084           | 0.0071           | 7.07                   |
| 1010       | 56.7  | 0.01   | 10         | 1005  | 0.00018 | 0.00002 | 0.00021           | 0.0018           | 1.77                   |

$$\Sigma E(t) \Delta t_i = 0.99$$

|              |        |     |
|--------------|--------|-----|
| $S_o =$      | 5.88   | g/s |
| Bed weight = | 1200   | g   |
| $\tau =$     | 204.08 | sec |

|                |       |                               |        |
|----------------|-------|-------------------------------|--------|
| $\tau_{obs} =$ | 185.6 | $\Sigma C_i t_i \Delta t_i =$ | 1556.6 |
|                |       | $\Sigma C_i \Delta t_i =$     | 8.4    |

Table D.3 Data Run # 1032

| Time(sec) | Total | Red   | $\Delta t$ | $t_i$ | C(t)    | E(t)    | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|-----------|-------|-------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0         | 119.1 | 0.00  | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 10        | 119.1 | 0.00  | 10         | 5     | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 20        | 122.0 | 0.28  | 10         | 15    | 0.00230 | 0.00055 | 0.00547           | 0.3444           | 0.02                   |
| 30        | 118.4 | 1.16  | 10         | 25    | 0.00979 | 0.00233 | 0.02333           | 2.4484           | 0.10                   |
| 40        | 120.2 | 5.33  | 10         | 35    | 0.04433 | 0.01056 | 0.10561           | 15.5154          | 0.44                   |
| 50        | 121.3 | 5.61  | 10         | 45    | 0.04625 | 0.01102 | 0.11019           | 20.8138          | 0.46                   |
| 60        | 121.1 | 5.1   | 10         | 55    | 0.04213 | 0.01004 | 0.10037           | 23.1703          | 0.42                   |
| 70        | 118.5 | 4.22  | 10         | 65    | 0.03562 | 0.00849 | 0.08486           | 23.1516          | 0.36                   |
| 80        | 118.1 | 3.83  | 10         | 75    | 0.03242 | 0.00772 | 0.07725           | 24.3175          | 0.32                   |
| 90        | 120.5 | 3.06  | 10         | 85    | 0.02539 | 0.00605 | 0.06049           | 21.5833          | 0.25                   |
| 100       | 120.0 | 2.7   | 10         | 95    | 0.02250 | 0.00536 | 0.05360           | 21.3714          | 0.22                   |
| 110       | 118.7 | 2.4   | 10         | 105   | 0.02022 | 0.00482 | 0.04817           | 21.2282          | 0.20                   |
| 120       | 118.1 | 2.12  | 10         | 115   | 0.01796 | 0.00428 | 0.04278           | 20.6488          | 0.18                   |
| 130       | 117.8 | 1.64  | 10         | 125   | 0.01392 | 0.00332 | 0.03317           | 17.4024          | 0.14                   |
| 140       | 121.0 | 1.56  | 10         | 135   | 0.01289 | 0.00307 | 0.03071           | 17.3992          | 0.13                   |
| 150       | 118.4 | 1.39  | 10         | 145   | 0.01174 | 0.00280 | 0.02796           | 17.0185          | 0.12                   |
| 160       | 118.1 | 1.25  | 10         | 155   | 0.01059 | 0.00252 | 0.02522           | 16.4111          | 0.11                   |
| 170       | 122.5 | 1.07  | 10         | 165   | 0.00873 | 0.00208 | 0.02081           | 14.4111          | 0.09                   |
| 180       | 121.5 | 0.97  | 10         | 175   | 0.00798 | 0.00190 | 0.01902           | 13.9677          | 0.08                   |
| 190       | 113.4 | 0.72  | 10         | 185   | 0.00635 | 0.00151 | 0.01512           | 11.7429          | 0.06                   |
| 200       | 119.3 | 0.67  | 10         | 195   | 0.00562 | 0.00134 | 0.01338           | 10.9523          | 0.06                   |
| 210       | 119.5 | 0.67  | 10         | 205   | 0.00561 | 0.00134 | 0.01336           | 11.4976          | 0.06                   |
| 220       | 120.5 | 0.56  | 10         | 215   | 0.00465 | 0.00111 | 0.01108           | 9.9950           | 0.05                   |
| 230       | 121.4 | 0.5   | 10         | 225   | 0.00412 | 0.00098 | 0.00981           | 9.2684           | 0.04                   |
| 240       | 119.6 | 0.33  | 10         | 235   | 0.00276 | 0.00066 | 0.00658           | 6.4857           | 0.03                   |
| 250       | 118.8 | 0.35  | 10         | 245   | 0.00295 | 0.00070 | 0.00702           | 7.2204           | 0.03                   |
| 260       | 120.5 | 0.28  | 10         | 255   | 0.00232 | 0.00055 | 0.00554           | 5.9268           | 0.02                   |
| 270       | 119.7 | 0.25  | 10         | 265   | 0.00209 | 0.00050 | 0.00497           | 5.5328           | 0.02                   |
| 280       | 119.2 | 0.24  | 10         | 275   | 0.00201 | 0.00048 | 0.00480           | 5.5385           | 0.02                   |
| 290       | 118.9 | 0.18  | 10         | 285   | 0.00151 | 0.00036 | 0.00361           | 4.3149           | 0.02                   |
| 300       | 118.9 | 0.27  | 10         | 295   | 0.00227 | 0.00054 | 0.00541           | 6.7012           | 0.02                   |
| 310       | 120.9 | 0.16  | 10         | 305   | 0.00132 | 0.00032 | 0.00315           | 4.0354           | 0.01                   |
| 320       | 116.5 | 0.06  | 10         | 315   | 0.00051 | 0.00012 | 0.00123           | 1.6218           | 0.01                   |
| 330       | 122.2 | 0.09  | 10         | 325   | 0.00074 | 0.00018 | 0.00175           | 2.3936           | 0.01                   |
| 340       | 115.3 | 0.14  | 10         | 335   | 0.00121 | 0.00029 | 0.00289           | 4.0666           | 0.01                   |
| 350       | 123.2 | 0.04  | 10         | 345   | 0.00032 | 0.00008 | 0.00077           | 1.1199           | 0.00                   |
| 360       | 120.3 | 0.09  | 10         | 355   | 0.00075 | 0.00018 | 0.00178           | 2.6567           | 0.01                   |
| 370       | 119.4 | 0.11  | 10         | 365   | 0.00092 | 0.00022 | 0.00219           | 3.3626           | 0.01                   |
| 380       | 120.2 | 0.07  | 10         | 375   | 0.00058 | 0.00014 | 0.00139           | 2.1839           | 0.01                   |
| 390       | 118.0 | 0.07  | 10         | 385   | 0.00059 | 0.00014 | 0.00141           | 2.2837           | 0.01                   |
| 400       | 120.7 | 0.06  | 10         | 395   | 0.00050 | 0.00012 | 0.00118           | 1.9644           | 0.00                   |
| 410       | 118.8 | 0.03  | 10         | 405   | 0.00025 | 0.00006 | 0.00060           | 1.0230           | 0.00                   |
| 420       | 119.6 | 0.06  | 10         | 415   | 0.00050 | 0.00012 | 0.00120           | 2.0828           | 0.01                   |
| 430       | 118.0 | 0.05  | 10         | 425   | 0.00042 | 0.00010 | 0.00101           | 1.8008           | 0.00                   |
| 440       | 117.3 | 0.02  | 10         | 435   | 0.00017 | 0.00004 | 0.00041           | 0.7414           | 0.00                   |
| 450       | 123.8 | 0.04  | 10         | 445   | 0.00032 | 0.00008 | 0.00077           | 1.4380           | 0.00                   |
| 460       | 118.1 | 0.03  | 10         | 455   | 0.00025 | 0.00006 | 0.00061           | 1.1557           | 0.00                   |
| 470       | 117.9 | 0     | 10         | 465   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 480       | 116.3 | 0.03  | 10         | 475   | 0.00026 | 0.00006 | 0.00061           | 1.2250           | 0.00                   |
| 490       | 119.0 | 0.02  | 10         | 485   | 0.00017 | 0.00004 | 0.00040           | 0.8154           | 0.00                   |
| 500       | 122.0 | 0     | 10         | 495   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 510       | 118.3 | 0     | 10         | 505   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 520       | 120.0 | 0.02  | 10         | 515   | 0.00017 | 0.00004 | 0.00040           | 0.8585           | 0.00                   |
| 530       | 118.2 | 0.015 | 10         | 525   | 0.00013 | 0.00003 | 0.00030           | 0.6660           | 0.00                   |

## Run # 1032 (Cont..)

| Time (sec) | Total | Red  | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|-------|------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 540        | 120.1 | 0.00 | 10         | 535   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 550        | 119.5 | 0.00 | 10         | 545   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 560        | 119.4 | 0.00 | 10         | 555   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 570        | 115.2 | 0.00 | 10         | 565   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 580        | 120.6 | 0.00 | 10         | 575   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 590        | 117.1 | 0    | 10         | 585   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 600        | 118.7 | 0    | 10         | 595   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 610        | 117.2 | 0    | 10         | 605   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 620        | 120.1 | 0    | 10         | 615   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 630        | 114.4 | 0.01 | 10         | 625   | 0.00009 | 0.00002 | 0.00021           | 0.5464           | 0.00                   |
| 640        | 119.7 | 0.05 | 10         | 635   | 0.00042 | 0.00010 | 0.00100           | 2.6522           | 0.00                   |
| 650        | 114.4 | 0    | 10         | 645   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 660        | 117.0 | 0    | 10         | 655   | 0.00000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |

$$\Sigma E(t) \Delta t_i = 0.9949$$

|                     |
|---------------------|
| $S_o = 11.91$ g/s   |
| Bed weight = 1218 g |
| $\tau = 102.30$ sec |

|                      |                                     |
|----------------------|-------------------------------------|
| $\tau_{obs} = 102.3$ | $\Sigma C_i t_i \Delta t_i = 427.1$ |
|                      | $\Sigma C_i \Delta t_i = 4.18$      |

Table D.4 Data Run#1033

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | C(t)    | E(t)    | $\Delta t * E(t)$ | Ci * $\Delta t$ | Ci * $t_i$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|-----------------|------------|
| 0          | 48.38  | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000           | 0.00       |
| 10         | 48.38  | 0.00   | 10         | 5     | 0.00000 | 0.00000 | 0.00000           | 0.000           | 0.00       |
| 20         | 48.38  | 0.00   | 10         | 15    | 0.00000 | 0.00000 | 0.00000           | 0.000           | 0.00       |
| 30         | 48.37  | 0.00   | 10         | 25    | 0.00000 | 0.00000 | 0.00000           | 0.000           | 0.00       |
| 40         | 44.73  | 0.00   | 10         | 35    | 0.00000 | 0.00000 | 0.00000           | 0.000           | 0.00       |
| 50         | 47.68  | 0.00   | 10         | 40    | 0.00000 | 0.00000 | 0.00000           | 0.000           | 0.00       |
| 60         | 142.20 | 5.45   | 30         | 45    | 0.03833 | 0.00371 | 0.11131           | 1.150           | 51.74      |
| 70         | 45.78  | 2.00   | 10         | 55    | 0.04369 | 0.00423 | 0.04229           | 0.437           | 24.03      |
| 80         | 51.25  | 2.30   | 10         | 65    | 0.04488 | 0.00434 | 0.04345           | 0.449           | 29.17      |
| 90         | 47.72  | 2.03   | 10         | 75    | 0.04254 | 0.00412 | 0.04118           | 0.425           | 31.90      |
| 100        | 50.30  | 2.04   | 10         | 85    | 0.04056 | 0.00393 | 0.03926           | 0.406           | 34.47      |
| 110        | 50.90  | 2.01   | 10         | 95    | 0.03949 | 0.00382 | 0.03823           | 0.395           | 37.51      |
| 120        | 50.33  | 1.55   | 10         | 105   | 0.03080 | 0.00298 | 0.02981           | 0.308           | 32.34      |
| 130        | 45.57  | 1.52   | 10         | 115   | 0.03336 | 0.00323 | 0.03229           | 0.334           | 38.36      |
| 140        | 50.07  | 1.90   | 10         | 125   | 0.03795 | 0.00367 | 0.03674           | 0.379           | 47.43      |
| 150        | 50.68  | 1.50   | 10         | 135   | 0.02960 | 0.00287 | 0.02865           | 0.296           | 39.96      |
| 160        | 46.31  | 1.31   | 10         | 145   | 0.02829 | 0.00274 | 0.02739           | 0.283           | 41.02      |
| 170        | 51.72  | 1.40   | 10         | 155   | 0.02707 | 0.00262 | 0.02621           | 0.271           | 41.96      |
| 180        | 51.14  | 1.53   | 10         | 165   | 0.02992 | 0.00290 | 0.02896           | 0.299           | 49.36      |
| 190        | 46.62  | 1.09   | 10         | 175   | 0.02338 | 0.00226 | 0.02263           | 0.234           | 40.92      |
| 200        | 51.17  | 1.24   | 10         | 185   | 0.02423 | 0.00235 | 0.02346           | 0.242           | 44.83      |
| 210        | 51.05  | 1.14   | 10         | 195   | 0.02233 | 0.00216 | 0.02162           | 0.223           | 43.55      |
| 220        | 44.33  | 0.96   | 10         | 205   | 0.02166 | 0.00210 | 0.02096           | 0.217           | 44.39      |
| 230        | 50.72  | 1.03   | 10         | 215   | 0.02031 | 0.00197 | 0.01966           | 0.203           | 43.66      |
| 240        | 50.06  | 0.96   | 10         | 225   | 0.01918 | 0.00186 | 0.01857           | 0.192           | 43.15      |
| 250        | 43.44  | 0.76   | 10         | 235   | 0.01750 | 0.00169 | 0.01694           | 0.175           | 41.11      |
| 260        | 49.75  | 0.91   | 10         | 245   | 0.01829 | 0.00177 | 0.01771           | 0.183           | 44.81      |
| 270        | 46.70  | 0.80   | 10         | 255   | 0.01713 | 0.00166 | 0.01658           | 0.171           | 43.68      |
| 280        | 44.37  | 0.57   | 10         | 265   | 0.01285 | 0.00124 | 0.01244           | 0.128           | 34.04      |
| 290        | 49.53  | 0.62   | 10         | 275   | 0.01252 | 0.00121 | 0.01212           | 0.125           | 34.42      |
| 300        | 49.84  | 0.67   | 10         | 285   | 0.01344 | 0.00130 | 0.01301           | 0.134           | 38.31      |
| 310        | 47.55  | 0.65   | 10         | 295   | 0.01367 | 0.00132 | 0.01323           | 0.137           | 40.33      |
| 320        | 45.96  | 0.50   | 10         | 305   | 0.01088 | 0.00105 | 0.01053           | 0.109           | 33.18      |
| 330        | 50.08  | 0.56   | 10         | 315   | 0.01118 | 0.00108 | 0.01083           | 0.112           | 35.22      |
| 340        | 50.15  | 0.48   | 10         | 325   | 0.00957 | 0.00093 | 0.00927           | 0.096           | 31.11      |
| 350        | 43.56  | 0.42   | 10         | 335   | 0.00964 | 0.00093 | 0.00933           | 0.096           | 32.30      |
| 360        | 47.91  | 0.59   | 10         | 345   | 0.01231 | 0.00119 | 0.01192           | 0.123           | 42.49      |
| 370        | 49.40  | 0.38   | 10         | 355   | 0.00769 | 0.00074 | 0.00745           | 0.077           | 27.31      |
| 380        | 46.16  | 0.42   | 10         | 365   | 0.00910 | 0.00088 | 0.00881           | 0.091           | 33.21      |
| 390        | 46.59  | 0.38   | 10         | 375   | 0.00816 | 0.00079 | 0.00790           | 0.082           | 30.59      |
| 400        | 50.57  | 0.45   | 10         | 385   | 0.00890 | 0.00086 | 0.00861           | 0.089           | 34.26      |
| 410        | 49.78  | 0.44   | 10         | 395   | 0.00884 | 0.00086 | 0.00856           | 0.088           | 34.91      |
| 420        | 46.23  | 0.37   | 10         | 405   | 0.00800 | 0.00077 | 0.00775           | 0.080           | 32.41      |
| 430        | 53.14  | 0.32   | 10         | 415   | 0.00602 | 0.00058 | 0.00583           | 0.060           | 24.99      |
| 440        | 51.27  | 0.33   | 10         | 425   | 0.00644 | 0.00062 | 0.00623           | 0.064           | 27.36      |
| 450        | 49.05  | 0.31   | 10         | 435   | 0.00632 | 0.00061 | 0.00612           | 0.063           | 27.49      |
| 460        | 45.25  | 0.27   | 10         | 445   | 0.00597 | 0.00058 | 0.00578           | 0.060           | 26.55      |
| 470        | 51.80  | 0.37   | 10         | 455   | 0.00714 | 0.00069 | 0.00691           | 0.071           | 32.50      |
| 480        | 45.38  | 0.19   | 10         | 465   | 0.00419 | 0.00041 | 0.00405           | 0.042           | 19.47      |
| 490        | 51.50  | 0.28   | 10         | 475   | 0.00544 | 0.00053 | 0.00526           | 0.054           | 25.83      |
| 500        | 48.40  | 0.20   | 10         | 485   | 0.00413 | 0.00040 | 0.00400           | 0.041           | 20.04      |
| 510        | 47.35  | 0.19   | 10         | 495   | 0.00401 | 0.00039 | 0.00388           | 0.040           | 19.86      |
| 520        | 48.63  | 0.31   | 10         | 505   | 0.00637 | 0.00062 | 0.00617           | 0.064           | 32.19      |
| 530        | 51.08  | 0.23   | 10         | 515   | 0.00450 | 0.00044 | 0.00436           | 0.045           | 23.19      |
| 540        | 51.94  | 0.21   | 10         | 525   | 0.00404 | 0.00039 | 0.00391           | 0.040           | 21.23      |
| 550        | 45.64  | 0.18   | 10         | 535   | 0.00394 | 0.00038 | 0.00382           | 0.039           | 21.10      |
| 560        | 52.77  | 0.27   | 10         | 545   | 0.00512 | 0.00050 | 0.00495           | 0.051           | 27.89      |
| 570        | 50.91  | 0.18   | 10         | 555   | 0.00354 | 0.00034 | 0.00342           | 0.035           | 19.62      |
| 580        | 45.66  | 0.16   | 10         | 565   | 0.00350 | 0.00034 | 0.00339           | 0.035           | 19.80      |
| 590        | 49.04  | 0.20   | 10         | 575   | 0.00408 | 0.00039 | 0.00395           | 0.041           | 23.45      |
| 600        | 51.25  | 0.24   | 10         | 585   | 0.00468 | 0.00045 | 0.00453           | 0.047           | 27.40      |
| 610        | 45.53  | 0.15   | 10         | 595   | 0.00318 | 0.00031 | 0.00308           | 0.032           | 18.95      |
| 620        | 50.08  | 0.11   | 10         | 605   | 0.00220 | 0.00021 | 0.00213           | 0.022           | 13.29      |
| 630        | 51.97  | 0.12   | 10         | 615   | 0.00231 | 0.00022 | 0.00224           | 0.023           | 14.20      |
| 640        | 47.66  | 0.15   | 10         | 625   | 0.00315 | 0.00030 | 0.00305           | 0.031           | 19.67      |

## Run#1033 ( Cont..)

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|-------|--------|------------|-------|---------|---------|-------------------|--------------------|--------------------------|
| 650        | 47.78 | 0.17   | 10         | 635   | 0.00356 | 0.00034 | 0.00344           | 0.036              | 22.60                    |
| 660        | 49.86 | 0.08   | 10         | 645   | 0.00160 | 0.00016 | 0.00155           | 0.016              | 10.35                    |
| 670        | 49.42 | 0.10   | 10         | 655   | 0.00202 | 0.00020 | 0.00196           | 0.020              | 13.25                    |
| 680        | 48.15 | 0.12   | 10         | 665   | 0.00249 | 0.00024 | 0.00241           | 0.025              | 16.57                    |
| 690        | 51.39 | 0.07   | 10         | 675   | 0.00136 | 0.00013 | 0.00132           | 0.014              | 9.19                     |
| 700        | 45.90 | 0.13   | 10         | 685   | 0.00283 | 0.00027 | 0.00274           | 0.028              | 19.40                    |
| 710        | 52.60 | 0.08   | 10         | 695   | 0.00152 | 0.00015 | 0.00147           | 0.015              | 10.57                    |
| 720        | 52.64 | 0.12   | 10         | 705   | 0.00228 | 0.00022 | 0.00221           | 0.023              | 16.07                    |
| 730        | 46.00 | 0.14   | 10         | 715   | 0.00304 | 0.00029 | 0.00295           | 0.030              | 21.76                    |
| 740        | 49.80 | 0.06   | 10         | 725   | 0.00120 | 0.00012 | 0.00117           | 0.012              | 8.73                     |
| 750        | 48.11 | 0.04   | 10         | 735   | 0.00083 | 0.00008 | 0.00080           | 0.008              | 6.11                     |
| 760        | 47.02 | 0.04   | 10         | 745   | 0.00085 | 0.00008 | 0.00082           | 0.009              | 6.34                     |
| 770        | 49.43 | 0.07   | 10         | 755   | 0.00142 | 0.00014 | 0.00137           | 0.014              | 10.69                    |
| 780        | 45.20 | 0.03   | 10         | 765   | 0.00066 | 0.00006 | 0.00064           | 0.007              | 5.08                     |
| 790        | 46.40 | 0.03   | 10         | 775   | 0.00065 | 0.00006 | 0.00063           | 0.006              | 5.01                     |
| 800        | 49.24 | 0.08   | 10         | 785   | 0.00162 | 0.00016 | 0.00157           | 0.016              | 12.75                    |
| 810        | 48.35 | 0.02   | 10         | 795   | 0.00041 | 0.00004 | 0.00040           | 0.004              | 3.29                     |
| 820        | 51.78 | 0.06   | 10         | 805   | 0.00116 | 0.00011 | 0.00112           | 0.012              | 9.33                     |
| 830        | 45.71 | 0.01   | 10         | 815   | 0.00022 | 0.00002 | 0.00021           | 0.002              | 1.78                     |
| 840        | 50.50 | 0.02   | 10         | 825   | 0.00040 | 0.00004 | 0.00038           | 0.004              | 3.27                     |
| 850        | 46.02 | 0.03   | 10         | 835   | 0.00065 | 0.00006 | 0.00063           | 0.007              | 5.44                     |
| 860        | 44.72 | 0.02   | 10         | 845   | 0.00045 | 0.00004 | 0.00043           | 0.004              | 3.78                     |
| 870        | 52.20 | 0.03   | 10         | 855   | 0.00057 | 0.00006 | 0.00056           | 0.006              | 4.91                     |
| 880        | 50.67 | 0.08   | 10         | 865   | 0.00158 | 0.00015 | 0.00153           | 0.016              | 13.66                    |
| 890        | 46.70 | 0.02   | 10         | 875   | 0.00043 | 0.00004 | 0.00041           | 0.004              | 3.75                     |
| 900        | 47.97 | 0.04   | 10         | 885   | 0.00083 | 0.00008 | 0.00081           | 0.008              | 7.38                     |
| 910        | 48.22 | 0.01   | 10         | 895   | 0.00010 | 0.00001 | 0.00010           | 0.001              | 0.93                     |
| 920        | 45.39 | 0.02   | 10         | 905   | 0.00044 | 0.00004 | 0.00043           | 0.004              | 3.99                     |
| 930        | 44.00 | 0.03   | 10         | 915   | 0.00068 | 0.00007 | 0.00066           | 0.007              | 6.24                     |
| 940        | 46.86 | 0.03   | 10         | 925   | 0.00064 | 0.00006 | 0.00062           | 0.006              | 5.92                     |
| 950        | 47.54 | 0.01   | 10         | 935   | 0.00021 | 0.00002 | 0.00020           | 0.002              | 1.97                     |
| 960        | 48.72 | 0.04   | 10         | 945   | 0.00082 | 0.00008 | 0.00079           | 0.008              | 7.76                     |
| 970        | 49.50 | 0.02   | 10         | 955   | 0.00030 | 0.00003 | 0.00029           | 0.003              | 2.89                     |
| 980        | 44.81 | 0.02   | 10         | 965   | 0.00045 | 0.00004 | 0.00043           | 0.004              | 4.31                     |
| 990        | 49.54 | 0.02   | 10         | 975   | 0.00040 | 0.00004 | 0.00039           | 0.004              | 3.94                     |
| 1000       | 51.25 | 0.01   | 10         | 985   | 0.00020 | 0.00002 | 0.00019           | 0.002              | 1.92                     |
| 1010       | 47.57 | 0.02   | 10         | 995   | 0.00042 | 0.00004 | 0.00041           | 0.004              | 4.18                     |
| 1020       | 43.45 | 0.02   | 10         | 1005  | 0.00046 | 0.00004 | 0.00045           | 0.005              | 4.63                     |
| 1030       | 50.59 | 0.04   | 10         | 1015  | 0.00069 | 0.00007 | 0.00067           | 0.007              | 7.02                     |
| 1040       | 47.98 | 0.01   | 10         | 1025  | 0.00010 | 0.00001 | 0.00010           | 0.001              | 1.07                     |
| 1050       | 46.90 | 0.01   | 10         | 1035  | 0.00011 | 0.00001 | 0.00010           | 0.001              | 1.10                     |
| 1060       | 51.24 | 0.01   | 10         | 1045  | 0.00010 | 0.00001 | 0.00009           | 0.001              | 1.02                     |
| 1070       | 51.56 | 0.00   | 10         | 1055  | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 1080       | 46.81 | 0.01   | 10         | 1065  | 0.00011 | 0.00001 | 0.00010           | 0.001              | 1.14                     |
| 1090       | 44.39 | 0.02   | 10         | 1075  | 0.00045 | 0.00004 | 0.00044           | 0.005              | 4.84                     |
| 1100       | 46.68 | 0.01   | 10         | 1085  | 0.00021 | 0.00002 | 0.00021           | 0.002              | 2.32                     |
| 1110       | 44.97 | 0.02   | 10         | 1095  | 0.00044 | 0.00004 | 0.00043           | 0.004              | 4.87                     |
| 1120       | 50.49 | 0.01   | 10         | 1105  | 0.00020 | 0.00002 | 0.00019           | 0.002              | 2.19                     |
| 1130       | 51.33 | 0.01   | 10         | 1115  | 0.00019 | 0.00002 | 0.00019           | 0.002              | 2.17                     |
| 1140       | 44.45 | 0.01   | 10         | 1125  | 0.00022 | 0.00002 | 0.00022           | 0.002              | 2.53                     |
| 1150       | 41.34 | 0.02   | 10         | 1135  | 0.00048 | 0.00005 | 0.00047           | 0.005              | 5.49                     |
| 1160       | 50.67 | 0.02   | 10         | 1145  | 0.00039 | 0.00004 | 0.00038           | 0.004              | 4.52                     |
| 1170       | 44.97 | 0.01   | 10         | 1155  | 0.00022 | 0.00002 | 0.00022           | 0.002              | 2.57                     |
| 1180       | 51.97 | 0.00   | 10         | 1165  | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 1190       | 48.67 | 0.02   | 10         | 1175  | 0.00041 | 0.00004 | 0.00040           | 0.004              | 4.83                     |
| 1200       | 46.43 | 0.01   | 10         | 1185  | 0.00022 | 0.00002 | 0.00021           | 0.002              | 2.55                     |
| 1210       | 48.04 | 0.00   | 10         | 1195  | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 1220       | 49.93 | 0.01   | 10         | 1205  | 0.00020 | 0.00002 | 0.00019           | 0.002              | 2.41                     |
| 1230       | 49.44 | 0.00   | 10         | 1215  | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 1240       | 41.00 | 0.00   | 10         | 1225  | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 1250       | 51.32 | 0.03   | 10         | 1235  | 0.00058 | 0.00006 | 0.00057           | 0.006              | 7.22                     |

$$\Sigma E(t) \Delta t_i = 0.9964$$

|                     |
|---------------------|
| $S_o = 4.84$ g/s    |
| Bed weight = 1136 g |
| $\tau = 234.77$ sec |

|                      |                                      |
|----------------------|--------------------------------------|
| $\tau_{obs} = 220.5$ | $\Sigma C_i t_i \Delta t_i = 2269.1$ |
|                      | $\Sigma C_i \Delta t_i = 10.29$      |

**Table D.5 Data Run#1034**

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|-------|--------|------------|-------|---------|---------|-------------------|--------------------|--------------------------|
| 0          | 82.31 | 0.00   | 0          | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 10         | 82.31 | 0.08   | 10         | 5     | 0.00097 | 0.00016 | 0.00160           | 0.049              | 0.01                     |
| 20         | 87.88 | 14.62  | 10         | 15    | 0.16636 | 0.02739 | 0.27386           | 24.954             | 1.66                     |
| 30         | 87.93 | 10.92  | 10         | 25    | 0.12419 | 0.02044 | 0.20443           | 31.047             | 1.24                     |
| 40         | 78.23 | 6.13   | 10         | 35    | 0.07835 | 0.01290 | 0.12898           | 27.424             | 0.78                     |
| 50         | 81.91 | 4.48   | 10         | 45    | 0.05464 | 0.00899 | 0.08994           | 24.587             | 0.55                     |
| 60         | 85.73 | 3.36   | 10         | 55    | 0.03914 | 0.00644 | 0.06443           | 21.525             | 0.39                     |
| 70         | 86.42 | 3.00   | 10         | 65    | 0.03475 | 0.00572 | 0.05720           | 22.584             | 0.35                     |
| 80         | 75.87 | 2.01   | 10         | 75    | 0.02655 | 0.00437 | 0.04370           | 19.911             | 0.27                     |
| 90         | 81.93 | 1.39   | 10         | 85    | 0.01701 | 0.00280 | 0.02799           | 14.455             | 0.17                     |
| 100        | 85.45 | 0.88   | 10         | 95    | 0.01033 | 0.00170 | 0.01700           | 9.812              | 0.10                     |
| 110        | 86.02 | 0.63   | 10         | 105   | 0.00729 | 0.00120 | 0.01200           | 7.655              | 0.07                     |
| 120        | 71.37 | 0.43   | 10         | 115   | 0.00602 | 0.00099 | 0.00992           | 6.929              | 0.06                     |
| 130        | 85.57 | 0.35   | 10         | 125   | 0.00409 | 0.00067 | 0.00673           | 5.113              | 0.04                     |
| 140        | 86.02 | 0.31   | 10         | 135   | 0.00360 | 0.00059 | 0.00593           | 4.865              | 0.04                     |
| 150        | 84.56 | 0.25   | 10         | 145   | 0.00296 | 0.00049 | 0.00487           | 4.287              | 0.03                     |
| 160        | 72.54 | 0.20   | 10         | 155   | 0.00276 | 0.00045 | 0.00454           | 4.274              | 0.03                     |
| 170        | 84.21 | 0.22   | 10         | 165   | 0.00261 | 0.00043 | 0.00430           | 4.311              | 0.03                     |
| 180        | 85.57 | 0.17   | 10         | 175   | 0.00199 | 0.00033 | 0.00327           | 3.477              | 0.02                     |
| 190        | 85.64 | 0.12   | 10         | 185   | 0.00140 | 0.00023 | 0.00231           | 2.592              | 0.01                     |
| 200        | 71.63 | 0.07   | 10         | 195   | 0.00098 | 0.00016 | 0.00161           | 1.906              | 0.01                     |
| 210        | 85.28 | 0.09   | 10         | 205   | 0.00106 | 0.00017 | 0.00174           | 2.163              | 0.01                     |
| 220        | 84.88 | 0.12   | 10         | 215   | 0.00141 | 0.00023 | 0.00233           | 3.040              | 0.01                     |
| 230        | 83.30 | 0.09   | 10         | 225   | 0.00108 | 0.00018 | 0.00178           | 2.431              | 0.01                     |
| 240        | 73.20 | 0.07   | 10         | 235   | 0.00096 | 0.00016 | 0.00157           | 2.247              | 0.01                     |
| 250        | 85.31 | 0.01   | 10         | 245   | 0.00007 | 0.00001 | 0.00012           | 0.172              | 0.00                     |
| 260        | 85.38 | 0.00   | 10         | 255   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 270        | 79.26 | 0.00   | 10         | 265   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 280        | 76.91 | 0.00   | 10         | 275   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 290        | 85.20 | 0.00   | 10         | 285   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 300        | 85.38 | 0.00   | 10         | 295   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 310        | 82.06 | 0.00   | 10         | 305   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 320        | 74.12 | 0.00   | 10         | 315   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 330        | 85.96 | 0.00   | 10         | 325   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 340        | 83.76 | 0.00   | 10         | 335   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 350        | 83.96 | 0.00   | 10         | 345   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |

$$\Sigma E(t) \Delta t_i = 0.97$$

|                                       |
|---------------------------------------|
| <b>So = 8.23 g/s</b>                  |
| <b>Bed weight = 977 g</b>             |
| <b><math>\tau = 118.76</math> sec</b> |

|                                       |                                                       |
|---------------------------------------|-------------------------------------------------------|
| <b><math>\tau_{obs} = 42.6</math></b> | <b><math>\Sigma C_i t_i \Delta t_i = 251.8</math></b> |
|                                       | <b><math>\Sigma C_i \Delta t_i = 5.91</math></b>      |

Table D.6 Data Run#1035

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|-------|--------|------------|-------|---------|---------|-------------------|--------------------|--------------------------|
| 0          | 59.63 | 0.00   | 20         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.00               | 0.00                     |
| 10         | 59.63 | 0.00   | 20         | 5     | 0.00000 | 0.00000 | 0.00000           | 0.00               | 0.00                     |
| 30         | 59.63 | 0.00   | 20         | 20    | 0.00000 | 0.00000 | 0.00000           | 0.00               | 0.00                     |
| 50         | 59.63 | 0.00   | 20         | 40    | 0.00000 | 0.00000 | 0.00000           | 0.00               | 0.00                     |
| 70         | 59.03 | 0.06   | 20         | 60    | 0.00102 | 0.00006 | 0.0012            | 0.02               | 1.22                     |
| 90         | 63.78 | 5.89   | 20         | 80    | 0.09235 | 0.00551 | 0.1101            | 1.85               | 147.76                   |
| 11         | 63.22 | 7.08   | 20         | 100   | 0.1119  | 0.00668 | 0.13355           | 2.24               | 223.98                   |
| 130        | 60.13 | 3.63   | 20         | 120   | 0.06037 | 0.00360 | 0.07199           | 1.2                | 144.89                   |
| 150        | 61.45 | 2.85   | 20         | 140   | 0.04638 | 0.00277 | 0.05531           | 0.93               | 129.86                   |
| 170        | 61.98 | 1.76   | 20         | 160   | 0.02832 | 0.00169 | 0.03377           | 0.57               | 90.61                    |
| 190        | 61.96 | 1.69   | 20         | 180   | 0.02728 | 0.00163 | 0.03253           | 0.55               | 98.19                    |
| 210        | 61.42 | 1.64   | 20         | 200   | 0.02670 | 0.00159 | 0.03184           | 0.53               | 106.8                    |
| 230        | 61.75 | 1.52   | 20         | 220   | 0.02462 | 0.00147 | 0.02935           | 0.49               | 108.3                    |
| 250        | 61.60 | 1.36   | 20         | 240   | 0.02208 | 0.00132 | 0.02633           | 0.44               | 105.97                   |
| 270        | 61.53 | 1.48   | 20         | 260   | 0.02405 | 0.00143 | 0.02868           | 0.48               | 125.08                   |
| 290        | 60.50 | 1.32   | 20         | 280   | 0.02182 | 0.00130 | 0.02602           | 0.44               | 122.1                    |
| 310        | 61.2  | 1.22   | 20         | 300   | 0.01993 | 0.0011  | 0.02377           | 0.40               | 119.5                    |
| 330        | 58.38 | 0.99   | 20         | 320   | 0.01696 | 0.0010  | 0.02022           | 0.34               | 108.53                   |
| 350        | 60.48 | 0.88   | 20         | 340   | 0.01455 | 0.00087 | 0.01735           | 0.29               | 98.94                    |
| 370        | 62.08 | 0.97   | 20         | 360   | 0.01563 | 0.00093 | 0.01863           | 0.31               | 112.5                    |
| 390        | 60.06 | 0.92   | 20         | 380   | 0.01523 | 0.00091 | 0.0181            | 0.30               | 115.7                    |
| 410        | 54.1  | 0.81   | 20         | 400   | 0.01497 | 0.00089 | 0.01785           | 0.30               | 119.7                    |
| 430        | 63.66 | 0.82   | 20         | 420   | 0.01288 | 0.00077 | 0.01536           | 0.26               | 108.20                   |
| 450        | 56.59 | 0.69   | 20         | 440   | 0.0121  | 0.00073 | 0.01454           | 0.24               | 107.30                   |
| 470        | 55.90 | 0.64   | 20         | 460   | 0.0114  | 0.00068 | 0.01365           | 0.23               | 105.33                   |
| 490        | 47.53 | 0.60   | 20         | 480   | 0.01262 | 0.00075 | 0.01505           | 0.25               | 121.1                    |
| 510        | 60.31 | 0.68   | 20         | 500   | 0.0112  | 0.00067 | 0.01345           | 0.23               | 112.7                    |
| 530        | 59.57 | 0.60   | 20         | 520   | 0.01007 | 0.00060 | 0.0120            | 0.20               | 104.75                   |
| 550        | 57.99 | 0.47   | 20         | 540   | 0.00810 | 0.00048 | 0.00967           | 0.16               | 87.53                    |
| 570        | 60.29 | 0.45   | 20         | 560   | 0.00746 | 0.00045 | 0.00890           | 0.15               | 83.60                    |
| 590        | 60.45 | 0.40   | 20         | 580   | 0.00662 | 0.00039 | 0.00789           | 0.13               | 76.76                    |
| 610        | 57.95 | 0.48   | 20         | 600   | 0.00820 | 0.00049 | 0.00977           | 0.16               | 98.36                    |
| 630        | 60.83 | 0.43   | 20         | 620   | 0.00707 | 0.00042 | 0.00843           | 0.14               | 87.65                    |
| 650        | 59.95 | 0.51   | 20         | 640   | 0.00851 | 0.00051 | 0.0101            | 0.17               | 108.89                   |
| 670        | 61.09 | 0.45   | 20         | 660   | 0.00737 | 0.00044 | 0.00878           | 0.15               | 97.23                    |
| 690        | 60.67 | 0.38   | 20         | 680   | 0.00626 | 0.00037 | 0.00747           | 0.13               | 85.18                    |
| 710        | 57.35 | 0.36   | 20         | 700   | 0.00628 | 0.00037 | 0.00749           | 0.13               | 87.88                    |
| 730        | 60.41 | 0.33   | 20         | 720   | 0.00546 | 0.00033 | 0.00651           | 0.1                | 78.66                    |
| 750        | 59.35 | 0.32   | 20         | 740   | 0.00539 | 0.00032 | 0.00643           | 0.1                | 79.80                    |
| 770        | 60.07 | 0.35   | 20         | 760   | 0.00574 | 0.00034 | 0.00685           | 0.1                | 87.30                    |
| 790        | 59.20 | 0.28   | 20         | 780   | 0.00473 | 0.00028 | 0.00564           | 0.09               | 73.78                    |
| 810        | 58.51 | 0.17   | 20         | 800   | 0.00291 | 0.00017 | 0.00346           | 0.06               | 46.49                    |
| 830        | 59.31 | 0.27   | 20         | 820   | 0.00455 | 0.00027 | 0.00543           | 0.09               | 74.66                    |
| 850        | 59.35 | 0.23   | 20         | 840   | 0.00379 | 0.00023 | 0.00452           | 0.08               | 63.69                    |
| 870        | 59.84 | 0.19   | 20         | 860   | 0.00318 | 0.00019 | 0.00379           | 0.06               | 54.61                    |
| 890        | 59.62 | 0.15   | 20         | 880   | 0.00252 | 0.00015 | 0.00300           | 0.05               | 44.28                    |
| 910        | 60.30 | 0.21   | 20         | 900   | 0.00348 | 0.00021 | 0.00415           | 0.07               | 62.69                    |
| 930        | 59.74 | 0.20   | 20         | 920   | 0.00335 | 0.00020 | 0.00399           | 0.07               | 61.60                    |
| 950        | 60.22 | 0.13   | 20         | 940   | 0.00216 | 0.00013 | 0.00257           | 0.04               | 40.58                    |
| 970        | 58.1  | 0.15   | 20         | 960   | 0.00258 | 0.00015 | 0.00308           | 0.05               | 49.56                    |
| 990        | 60.07 | 0.13   | 20         | 980   | 0.00216 | 0.00013 | 0.00258           | 0.04               | 42.42                    |
| 101        | 59.74 | 0.1    | 20         | 1000  | 0.00184 | 0.0001  | 0.00220           | 0.04               | 36.83                    |
| 1030       | 60.50 | 0.08   | 20         | 1020  | 0.00126 | 0.00007 | 0.00150           | 0.03               | 25.63                    |
| 1050       | 59.45 | 0.12   | 20         | 1040  | 0.00202 | 0.00012 | 0.00241           | 0.04               | 41.98                    |
| 1070       | 59.61 | 0.16   | 20         | 1060  | 0.00268 | 0.00016 | 0.00320           | 0.05               | 56.90                    |
| 1090       | 59.33 | 0.13   | 20         | 1080  | 0.00219 | 0.00013 | 0.00261           | 0.04               | 47.33                    |
| 111        | 59.48 | 0.12   | 20         | 110   | 0.00202 | 0.00012 | 0.00241           | 0.04               | 44.38                    |
| 113        | 60.02 | 0.13   | 20         | 112   | 0.00217 | 0.00013 | 0.00258           | 0.04               | 48.52                    |
| 115        | 59.32 | 0.16   | 20         | 114   | 0.00270 | 0.00016 | 0.00322           | 0.05               | 61.50                    |
| 117        | 60.10 | 0.08   | 20         | 116   | 0.00125 | 0.00007 | 0.00149           | 0.02               | 28.95                    |
| 119        | 59.91 | 0.1    | 20         | 118   | 0.00184 | 0.0001  | 0.00219           | 0.04               | 43.33                    |
| 121        | 59.25 | 0.12   | 20         | 1200  | 0.00194 | 0.00012 | 0.00231           | 0.04               | 46.58                    |
| 1230       | 60.09 | 0.05   | 20         | 1220  | 0.00083 | 0.00005 | 0.00099           | 0.02               | 20.30                    |
| 1250       | 59.02 | 0.07   | 20         | 1240  | 0.0011  | 0.00007 | 0.0014            | 0.02               | 29.41                    |

$$\Sigma E(t) \Delta t_i = 0.950$$

|                     |
|---------------------|
| $S_o = 2.98$ g/s    |
| Bed weight = 993 g  |
| $\tau = 333.22$ sec |

|                      |                                      |
|----------------------|--------------------------------------|
| $\tau_{obs} = 310.4$ | $\Sigma C_i t_i \Delta t_i = 4944.3$ |
|                      | $\Sigma C_i \Delta t_i = 15.93$      |

Table D.7 Data Run#1036

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|-------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 204.3 | 0.0    | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 11         | 204.3 | 0.0    | 10         | 5.5   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 24         | 262.8 | 25.3   | 13         | 17.5  | 0.09620 | 0.03928 | 0.51070           | 1.251            | 21.89                  |
| 44         | 412.7 | 9.6    | 20         | 34    | 0.02328 | 0.00951 | 0.19016           | 0.466            | 15.83                  |
| 54         | 203.7 | 2.8    | 10         | 49    | 0.01380 | 0.00563 | 0.05634           | 0.138            | 6.76                   |
| 64         | 217.4 | 2.2    | 10         | 59    | 0.01003 | 0.00409 | 0.04094           | 0.100            | 5.92                   |
| 74         | 209.6 | 1.9    | 10         | 69    | 0.00883 | 0.00360 | 0.03604           | 0.088            | 6.09                   |
| 84         | 205.1 | 1.2    | 10         | 79    | 0.00600 | 0.00245 | 0.02449           | 0.060            | 4.74                   |
| 94         | 204.3 | 1.2    | 10         | 89    | 0.00597 | 0.00244 | 0.02439           | 0.060            | 5.32                   |
| 104        | 206.0 | 1.1    | 10         | 99    | 0.00539 | 0.00220 | 0.02201           | 0.054            | 5.34                   |
| 114        | 204.6 | 0.8    | 10         | 109   | 0.00376 | 0.00154 | 0.01537           | 0.038            | 4.10                   |
| 124        | 214.7 | 0.6    | 10         | 119   | 0.00293 | 0.00120 | 0.01198           | 0.029            | 3.49                   |
| 134        | 205.4 | 0.5    | 10         | 129   | 0.00258 | 0.00105 | 0.01054           | 0.026            | 3.33                   |
| 144        | 202.5 | 0.4    | 10         | 139   | 0.00217 | 0.00089 | 0.00887           | 0.022            | 3.02                   |
| 154        | 211.2 | 0.3    | 10         | 149   | 0.00152 | 0.00062 | 0.00619           | 0.015            | 2.26                   |
| 164        | 204.4 | 0.4    | 10         | 159   | 0.00181 | 0.00074 | 0.00739           | 0.018            | 2.88                   |
| 174        | 204.4 | 0.2    | 10         | 169   | 0.00098 | 0.00040 | 0.00400           | 0.010            | 1.65                   |
| 184        | 207.5 | 0.2    | 10         | 179   | 0.00101 | 0.00041 | 0.00413           | 0.010            | 1.81                   |
| 194        | 209.1 | 0.2    | 10         | 189   | 0.00096 | 0.00039 | 0.00391           | 0.010            | 1.81                   |
| 204        | 205.1 | 0.1    | 10         | 199   | 0.00068 | 0.00028 | 0.00279           | 0.007            | 1.36                   |
| 214        | 201.7 | 0.2    | 10         | 209   | 0.00079 | 0.00032 | 0.00324           | 0.008            | 1.66                   |
| 224        | 202.0 | 0.1    | 10         | 219   | 0.00069 | 0.00028 | 0.00283           | 0.007            | 1.52                   |
| 234        | 201.0 | 0.1    | 10         | 229   | 0.00055 | 0.00022 | 0.00224           | 0.005            | 1.25                   |
| 244        | 198.4 | 0.1    | 10         | 239   | 0.00030 | 0.00012 | 0.00124           | 0.003            | 0.72                   |
| 254        | 206.1 | 0.1    | 10         | 249   | 0.00029 | 0.00012 | 0.00119           | 0.003            | 0.72                   |
| 264        | 205.3 | 0.1    | 10         | 259   | 0.00029 | 0.00012 | 0.00119           | 0.003            | 0.76                   |
| 274        | 203.0 | 0.0    | 10         | 269   | 0.00015 | 0.00006 | 0.00060           | 0.001            | 0.40                   |
| 284        | 202.3 | 0.0    | 10         | 279   | 0.00015 | 0.00006 | 0.00061           | 0.001            | 0.41                   |
| 294        | 198.6 | 0.1    | 10         | 289   | 0.00025 | 0.00010 | 0.00103           | 0.003            | 0.73                   |
| 304        | 199.3 | 0.0    | 10         | 299   | 0.00015 | 0.00006 | 0.00061           | 0.002            | 0.45                   |
| 314        | 198.2 | 0.0    | 10         | 309   | 0.00015 | 0.00006 | 0.00062           | 0.002            | 0.47                   |
| 324        | 204.8 | 0.0    | 10         | 319   | 0.00020 | 0.00008 | 0.00080           | 0.002            | 0.62                   |
| 334        | 203.8 | 0.0    | 10         | 329   | 0.00005 | 0.00002 | 0.00020           | 0.000            | 0.16                   |
| 344        | 196.3 | 0.0    | 10         | 339   | 0.00015 | 0.00006 | 0.00062           | 0.002            | 0.52                   |
| 354        | 201.5 | 0.0    | 10         | 349   | 0.00005 | 0.00002 | 0.00020           | 0.000            | 0.17                   |
| 364        | 196.0 | 0.0    | 10         | 359   | 0.00005 | 0.00002 | 0.00021           | 0.001            | 0.18                   |

$$\Sigma E(t) \Delta t_i = 0.998$$

|                     |
|---------------------|
| $S_o = 20.42$ g/s   |
| Bed weight = 1069 g |
| $\tau = 52.35$ sec  |

|                     |                                     |
|---------------------|-------------------------------------|
| $\tau_{obs} = 44.3$ | $\Sigma C_i t_i \Delta t_i = 108.3$ |
|                     | $\Sigma C_i \Delta t_i = 2.44$      |



Table D.8 Data Run# 1037

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$   | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|-------|--------|------------|-------|----------|---------|-------------------|------------------|------------------------|
| 0          | 2.71  | 0.00   | 5          | 0     | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 10         | 2.71  | 0.00   | 10         | 5     | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 20         | 2.71  | 0.00   | 10         | 15    | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 30         | 2.71  | 0.00   | 10         | 25    | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 40         | 2.71  | 0.00   | 10         | 35    | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 50         | 2.71  | 0.00   | 10         | 45    | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 70         | 2.71  | 0.00   | 20         | 55    | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 92         | 2.71  | 0.00   | 22         | 75    | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 110        | 2.71  | 0.18   | 18         | 97    | 0.067796 | 0.00367 | 0.06548           | 0.0655           | 117.41                 |
| 130        | 2.71  | 0.17   | 20         | 115   | 0.064207 | 0.00348 | 0.06960           | 0.0696           | 147.68                 |
| 150        | 2.71  | 0.15   | 20         | 135   | 0.054428 | 0.00295 | 0.05900           | 0.0590           | 146.96                 |
| 170        | 2.71  | 0.15   | 20         | 155   | 0.057011 | 0.00309 | 0.06180           | 0.0618           | 176.73                 |
| 190        | 2.71  | 0.14   | 20         | 175   | 0.052399 | 0.00284 | 0.05680           | 0.0568           | 183.39                 |
| 210        | 2.71  | 0.13   | 20         | 195   | 0.046125 | 0.00250 | 0.05000           | 0.0500           | 179.89                 |
| 230        | 2.71  | 0.12   | 20         | 215   | 0.042989 | 0.00233 | 0.04660           | 0.0466           | 184.85                 |
| 250        | 2.71  | 0.10   | 20         | 235   | 0.037269 | 0.00202 | 0.04040           | 0.0404           | 175.17                 |
| 270        | 2.71  | 0.10   | 20         | 255   | 0.037269 | 0.00202 | 0.04040           | 0.0404           | 190.07                 |
| 290        | 2.71  | 0.09   | 20         | 275   | 0.033210 | 0.00180 | 0.03600           | 0.0360           | 182.66                 |
| 310        | 2.71  | 0.09   | 20         | 295   | 0.034133 | 0.00185 | 0.03700           | 0.0370           | 201.38                 |
| 330        | 2.71  | 0.07   | 20         | 315   | 0.027491 | 0.00149 | 0.02980           | 0.0298           | 173.19                 |
| 350        | 2.71  | 0.08   | 20         | 335   | 0.030074 | 0.00163 | 0.03260           | 0.0326           | 201.49                 |
| 370        | 2.71  | 0.06   | 20         | 355   | 0.023247 | 0.00126 | 0.02520           | 0.0252           | 165.06                 |
| 390        | 2.71  | 0.08   | 20         | 375   | 0.028044 | 0.00152 | 0.03040           | 0.0304           | 210.33                 |
| 410        | 2.71  | 0.06   | 20         | 395   | 0.022878 | 0.00124 | 0.02480           | 0.0248           | 180.74                 |
| 430        | 2.71  | 0.04   | 20         | 415   | 0.016052 | 0.00087 | 0.01740           | 0.0174           | 133.23                 |
| 450        | 2.71  | 0.06   | 20         | 435   | 0.021218 | 0.00115 | 0.02300           | 0.0230           | 184.59                 |
| 470        | 2.71  | 0.05   | 20         | 455   | 0.019188 | 0.00104 | 0.02080           | 0.0208           | 174.61                 |
| 490        | 2.71  | 0.05   | 20         | 475   | 0.018450 | 0.00100 | 0.02000           | 0.0200           | 175.28                 |
| 510        | 2.71  | 0.03   | 20         | 495   | 0.011993 | 0.00065 | 0.01300           | 0.0130           | 118.73                 |
| 530        | 2.71  | 0.04   | 20         | 515   | 0.014945 | 0.00081 | 0.01620           | 0.0162           | 153.93                 |
| 550        | 2.71  | 0.04   | 20         | 535   | 0.014022 | 0.00076 | 0.01520           | 0.0152           | 150.04                 |
| 570        | 2.71  | 0.04   | 20         | 555   | 0.014022 | 0.00076 | 0.01520           | 0.0152           | 155.65                 |
| 590        | 2.71  | 0.03   | 20         | 575   | 0.011993 | 0.00065 | 0.01300           | 0.0130           | 137.92                 |
| 610        | 2.71  | 0.04   | 20         | 595   | 0.014945 | 0.00081 | 0.01620           | 0.0162           | 177.84                 |
| 630        | 2.71  | 0.03   | 20         | 615   | 0.011439 | 0.00062 | 0.01240           | 0.0124           | 140.70                 |
| 650        | 2.71  | 0.03   | 20         | 635   | 0.012362 | 0.00067 | 0.01340           | 0.0134           | 156.99                 |
| 670        | 2.71  | 0.02   | 20         | 655   | 0.006827 | 0.00037 | 0.00740           | 0.0074           | 89.43                  |
| 690        | 2.71  | 0.03   | 20         | 675   | 0.009779 | 0.00053 | 0.01060           | 0.0106           | 132.01                 |
| 710        | 2.71  | 0.02   | 20         | 695   | 0.006273 | 0.00034 | 0.00680           | 0.0068           | 87.20                  |
| 730        | 2.71  | 0.02   | 20         | 715   | 0.006827 | 0.00037 | 0.00740           | 0.0074           | 97.62                  |
| 750        | 2.71  | 0.02   | 20         | 735   | 0.006827 | 0.00037 | 0.00740           | 0.0074           | 100.35                 |
| 770        | 2.71  | 0.02   | 20         | 755   | 0.007196 | 0.00039 | 0.00780           | 0.0078           | 108.65                 |
| 790        | 2.71  | 0.02   | 20         | 775   | 0.006273 | 0.00034 | 0.00680           | 0.0068           | 97.23                  |
| 810        | 2.71  | 0.01   | 20         | 795   | 0.004059 | 0.00022 | 0.00440           | 0.0044           | 64.54                  |
| 830        | 2.71  | 0.02   | 20         | 815   | 0.007196 | 0.00039 | 0.00780           | 0.0078           | 117.29                 |
| 850        | 2.71  | 0.01   | 20         | 835   | 0.005166 | 0.00028 | 0.00560           | 0.0056           | 86.27                  |
| 870        | 2.71  | 0.01   | 20         | 855   | 0.004059 | 0.00022 | 0.00440           | 0.0044           | 69.41                  |
| 890        | 2.71  | 0.02   | 20         | 875   | 0.006273 | 0.00034 | 0.00680           | 0.0068           | 109.78                 |
| 910        | 2.71  | 0.01   | 20         | 895   | 0.003690 | 0.00020 | 0.00400           | 0.0040           | 66.05                  |
| 930        | 2.71  | 0.01   | 20         | 915   | 0.003137 | 0.00017 | 0.00340           | 0.0034           | 57.40                  |
| 950        | 2.71  | 0.01   | 20         | 935   | 0.002030 | 0.00011 | 0.00220           | 0.0022           | 37.95                  |
| 970        | 2.71  | 0.01   | 20         | 955   | 0.002583 | 0.00014 | 0.00280           | 0.0028           | 49.34                  |
| 990        | 2.71  | 0.00   | 20         | 975   | 0.001476 | 0.00008 | 0.00160           | 0.0016           | 28.78                  |

## Run# 1037 (Cont..)

| Time (sec) | Total | Tracer    | $\Delta t$ | $t_i$ | $C(t)$   | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|-------|-----------|------------|-------|----------|---------|-------------------|------------------|------------------------|
| 1010       | 2.7   | 0.01      | 20         | 995   | 0.004059 | 0.00022 | 0.00440           | 0.0812           | 80.77                  |
| 1030       | 2.7   | 0.00      | 20         | 1015  | 0.000000 | 0.00000 | 0.00000           | 0.0000           | 0.00                   |
| 1050       | 2.7   | 0.01      | 20         | 1035  | 0.003690 | 0.00020 | 0.00400           | 0.0738           | 76.38                  |
| 1070       | 2.7   | 0.01      | 20         | 1055  | 0.003137 | 0.00017 | 0.00340           | 0.0627           | 66.18                  |
| 1090       | 2.7   | 0.01      | 20         | 1075  | 0.002030 | 0.00011 | 0.00220           | 0.0406           | 43.63                  |
| 1110       | 2.7   | 0.007     | 20         | 1095  | 0.002583 | 0.00014 | 0.00280           | 0.0517           | 56.57                  |
| 1130       | 2.7   | 0.0055    | 20         | 1115  | 0.002030 | 0.00011 | 0.00220           | 0.0406           | 45.26                  |
| 1150       | 2.7   | 0.0085874 | 20         | 1135  | 0.003169 | 0.00017 | 0.00343           | 0.0634           | 71.93                  |
| 1170       | 2.7   | 0.01      | 20         | 1155  | 0.003690 | 0.00020 | 0.00400           | 0.0738           | 85.24                  |
| 1190       | 2.7   | 0.0055    | 20         | 1175  | 0.002030 | 0.00011 | 0.00220           | 0.0406           | 47.69                  |
| 1210       | 2.7   | 0.007     | 20         | 1195  | 0.002583 | 0.00014 | 0.00280           | 0.0517           | 61.73                  |
| 1230       | 2.7   | 0.0031291 | 20         | 1215  | 0.001155 | 0.00006 | 0.00125           | 0.0231           | 28.06                  |
| 1250       | 2.7   | 0.0024309 | 20         | 1235  | 0.000897 | 0.00005 | 0.00097           | 0.0179           | 22.16                  |
| 1270       | 2.7   | 0.0018883 | 20         | 1255  | 0.000697 | 0.00004 | 0.00076           | 0.0139           | 17.49                  |
| 1290       | 2.7   | 0.0014668 | 20         | 1275  | 0.000541 | 0.00003 | 0.00059           | 0.0108           | 13.80                  |
| 1310       | 2.7   | 0.0011392 | 20         | 1295  | 0.000420 | 0.00002 | 0.00046           | 0.0084           | 10.89                  |
| 1330       | 2.7   | 0.0008846 | 20         | 1315  | 0.000326 | 0.00002 | 0.00035           | 0.0065           | 8.59                   |
| 1350       | 2.7   | 0.0006868 | 20         | 1335  | 0.000253 | 0.00001 | 0.00027           | 0.0051           | 6.77                   |
| 1370       | 2.7   | 0.0005331 | 20         | 1355  | 0.000197 | 0.00001 | 0.00021           | 0.0039           | 5.33                   |
| 1390       | 2.7   | 0.0004137 | 20         | 1375  | 0.000153 | 0.00001 | 0.00017           | 0.0031           | 4.20                   |
| 1410       | 2.7   | 0.0003209 | 20         | 1395  | 0.000118 | 0.00001 | 0.00013           | 0.0024           | 3.30                   |
| 1430       | 2.7   | 0.0002488 | 20         | 1415  | 0.000092 | 0.00000 | 0.00010           | 0.0018           | 2.60                   |
| 1450       | 2.7   | 0.0001928 | 20         | 1435  | 0.000071 | 0.00000 | 0.00008           | 0.0014           | 2.04                   |
| 1470       | 2.7   | 0.0001492 | 20         | 1455  | 0.000055 | 0.00000 | 0.00006           | 0.0011           | 1.60                   |
| 1490       | 2.7   | 0.0001154 | 20         | 1475  | 0.000043 | 0.00000 | 0.00005           | 0.0009           | 1.26                   |

$$\Sigma E(t) \Delta t_i = 1.0$$

|              |        |     |
|--------------|--------|-----|
| $S_o =$      | 2.710  | g/s |
| Bed weight = | 969.89 | g   |
| $\tau =$     | 357.89 | sec |

|                |       |                               |        |
|----------------|-------|-------------------------------|--------|
| $\tau_{obs} =$ | 357.9 | $\Sigma C_i t_i \Delta t_i =$ | 6839.3 |
|                |       | $\Sigma C_i \Delta t_i =$     | 19.11  |

Table D.9 Data Run# 1038

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$   | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|--------|--------|------------|-------|----------|---------|-------------------|--------------------|--------------------------|
| 0          | 169.90 | 0.00   | 10         | 0     | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 10         | 169.90 | 0.00   | 10         | 5     | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 30         | 169.90 | 0.00   | 20         | 20    | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 40         | 169.90 | 0.00   | 10         | 35    | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 50         | 169.90 | 0.00   | 10         | 45    | 0.000000 | 0.00000 | 0.00000           | 0.0000             | 0.00                     |
| 60         | 169.85 | 7.43   | 10         | 55    | 0.043745 | 0.01486 | 0.14864           | 0.4374             | 14.44                    |
| 70         | 167.63 | 5.88   | 10         | 65    | 0.034600 | 0.01176 | 0.11757           | 0.3460             | 14.88                    |
| 80         | 169.58 | 5.17   | 10         | 75    | 0.030429 | 0.01034 | 0.10340           | 0.3043             | 16.13                    |
| 90         | 166.67 | 4.49   | 10         | 85    | 0.026400 | 0.00897 | 0.08971           | 0.2640             | 16.63                    |
| 100        | 168.32 | 3.43   | 10         | 95    | 0.020200 | 0.00686 | 0.06864           | 0.2020             | 14.75                    |
| 110        | 169.37 | 3.00   | 10         | 105   | 0.017653 | 0.00600 | 0.05999           | 0.1765             | 14.65                    |
| 120        | 169.80 | 2.50   | 10         | 115   | 0.014723 | 0.00500 | 0.05003           | 0.1472             | 13.69                    |
| 130        | 169.39 | 2.09   | 10         | 125   | 0.012280 | 0.00417 | 0.04173           | 0.1228             | 12.65                    |
| 140        | 169.89 | 1.58   | 10         | 135   | 0.009300 | 0.00316 | 0.03160           | 0.0930             | 10.51                    |
| 150        | 169.75 | 1.45   | 10         | 145   | 0.008542 | 0.00290 | 0.02903           | 0.0854             | 10.51                    |
| 160        | 169.33 | 1.27   | 10         | 155   | 0.007500 | 0.00255 | 0.02549           | 0.0750             | 9.98                     |
| 170        | 169.70 | 1.12   | 10         | 165   | 0.006600 | 0.00224 | 0.02243           | 0.0660             | 9.44                     |
| 180        | 169.51 | 0.84   | 10         | 175   | 0.004956 | 0.00168 | 0.01684           | 0.0496             | 7.58                     |
| 190        | 170.00 | 0.85   | 10         | 185   | 0.005000 | 0.00170 | 0.01699           | 0.0500             | 8.15                     |
| 200        | 171.16 | 0.59   | 10         | 195   | 0.003447 | 0.00117 | 0.01171           | 0.0345             | 5.96                     |
| 210        | 170.59 | 0.58   | 10         | 205   | 0.003400 | 0.00116 | 0.01155           | 0.0340             | 6.22                     |
| 220        | 168.75 | 0.27   | 10         | 215   | 0.001600 | 0.00054 | 0.00544           | 0.0160             | 3.09                     |
| 230        | 169.98 | 0.34   | 10         | 225   | 0.002000 | 0.00068 | 0.00680           | 0.0200             | 4.06                     |
| 240        | 167.87 | 0.28   | 10         | 235   | 0.001668 | 0.00057 | 0.00567           | 0.0167             | 3.55                     |
| 250        | 166.67 | 0.31   | 10         | 245   | 0.001800 | 0.00061 | 0.00612           | 0.0180             | 4.01                     |
| 260        | 172.44 | 0.20   | 10         | 255   | 0.001160 | 0.00039 | 0.00394           | 0.0116             | 2.70                     |
| 270        | 167.09 | 0.16   | 10         | 265   | 0.000958 | 0.00033 | 0.00325           | 0.0096             | 2.33                     |
| 280        | 172.49 | 0.14   | 10         | 275   | 0.000812 | 0.00028 | 0.00276           | 0.0081             | 2.05                     |
| 290        | 163.40 | 0.11   | 10         | 285   | 0.000673 | 0.00023 | 0.00229           | 0.0067             | 1.77                     |
| 300        | 162.76 | 0.09   | 10         | 295   | 0.000553 | 0.00019 | 0.00188           | 0.0055             | 1.51                     |
| 310        | 171.02 | 0.08   | 10         | 305   | 0.000468 | 0.00016 | 0.00159           | 0.0047             | 1.32                     |

$$\Sigma E(t) \Delta t_i = 0.991$$

|                        |
|------------------------|
| $S_o = 16.99$ g/s      |
| Bed weight = 1310.00 g |
| $\tau = 77.10$ sec     |

|                     |                                     |
|---------------------|-------------------------------------|
| $\tau_{obs} = 77.1$ | $\Sigma C_i t_i \Delta t_i = 200.8$ |
|                     | $\Sigma C_i \Delta t_i = 2.60$      |

Table D.10 Data Run#1039

| Time (sec) | Total | Tracer | $\Delta t$ | ti   | C(t)    | E(t)    | $\Delta t * E(t)$ | Ci * $\Delta t$ | Ci * ti * $\Delta t$ |
|------------|-------|--------|------------|------|---------|---------|-------------------|-----------------|----------------------|
| 0          | 33.43 | 0.00   | 20         | 0    | 0.00000 | 0.00000 | 0.00000           | 0.000           | 0.00                 |
| 38         | 35.16 | 0.00   | 20         | 19   | 0.00000 | 0.00000 | 0.00000           | 0.000           | 0.00                 |
| 58         | 35.05 | 0.01   | 20         | 48   | 0.00017 | 0.00001 | 0.0001            | 0.003           | 0.16                 |
| 78         | 32.95 | 0.38   | 20         | 68   | 0.0115  | 0.00039 | 0.00771           | 0.231           | 15.68                |
| 98         | 33.04 | 1.23   | 20         | 88   | 0.03723 | 0.00124 | 0.02489           | 0.745           | 65.52                |
| 11         | 33.16 | 1.64   | 20         | 108  | 0.04946 | 0.00165 | 0.03307           | 0.989           | 106.83               |
| 138        | 33.46 | 1.50   | 20         | 128  | 0.04468 | 0.00149 | 0.02987           | 0.894           | 114.3                |
| 158        | 36.22 | 1.69   | 20         | 148  | 0.04666 | 0.00156 | 0.03120           | 0.933           | 138.1                |
| 178        | 34.03 | 1.4    | 20         | 168  | 0.04143 | 0.00139 | 0.02770           | 0.829           | 139.22               |
| 198        | 33.66 | 1.2    | 20         | 188  | 0.03595 | 0.00120 | 0.02403           | 0.719           | 135.1                |
| 218        | 33.49 | 1.1    | 20         | 208  | 0.03464 | 0.0011  | 0.02316           | 0.693           | 144.09               |
| 238        | 33.53 | 1.20   | 20         | 228  | 0.03564 | 0.0011  | 0.02383           | 0.713           | 162.52               |
| 258        | 33.38 | 1.1    | 20         | 248  | 0.03385 | 0.0011  | 0.02263           | 0.677           | 167.9                |
| 278        | 36.56 | 1.32   | 20         | 268  | 0.0361  | 0.0012  | 0.02414           | 0.722           | 193.52               |
| 298        | 33.99 | 1.1    | 20         | 288  | 0.03236 | 0.00108 | 0.02164           | 0.647           | 186.4                |
| 318        | 33.16 | 0.89   | 20         | 308  | 0.02684 | 0.00090 | 0.01794           | 0.537           | 165.33               |
| 338        | 32.97 | 1.26   | 20         | 328  | 0.03822 | 0.00128 | 0.02555           | 0.764           | 250.70               |
| 358        | 33.04 | 1.05   | 20         | 348  | 0.03178 | 0.00106 | 0.02125           | 0.636           | 221.1                |
| 378        | 33.00 | 0.97   | 20         | 368  | 0.02939 | 0.00098 | 0.01965           | 0.588           | 216.34               |
| 398        | 35.62 | 1.03   | 20         | 388  | 0.02892 | 0.00097 | 0.01933           | 0.578           | 224.39               |
| 418        | 32.38 | 1.02   | 20         | 408  | 0.03150 | 0.00105 | 0.02106           | 0.630           | 257.05               |
| 438        | 33.28 | 0.80   | 20         | 428  | 0.02389 | 0.00080 | 0.01597           | 0.478           | 204.48               |
| 458        | 33.36 | 0.94   | 20         | 448  | 0.02818 | 0.00094 | 0.01884           | 0.564           | 252.47               |
| 478        | 32.07 | 0.85   | 20         | 468  | 0.02650 | 0.00089 | 0.01772           | 0.530           | 248.08               |
| 498        | 32.63 | 0.78   | 20         | 488  | 0.02390 | 0.00080 | 0.01598           | 0.478           | 233.31               |
| 518        | 36.73 | 0.79   | 20         | 508  | 0.0215  | 0.00072 | 0.01438           | 0.430           | 218.52               |
| 538        | 33.01 | 0.82   | 20         | 528  | 0.02484 | 0.00083 | 0.0166            | 0.497           | 262.32               |
| 558        | 33.03 | 0.77   | 20         | 548  | 0.02331 | 0.00078 | 0.01559           | 0.466           | 255.50               |
| 578        | 32.51 | 0.61   | 20         | 568  | 0.0186  | 0.00062 | 0.01244           | 0.372           | 211.4                |
| 598        | 32.83 | 0.64   | 20         | 588  | 0.01949 | 0.00065 | 0.01303           | 0.390           | 229.25               |
| 618        | 32.73 | 0.71   | 20         | 608  | 0.02169 | 0.00073 | 0.01450           | 0.434           | 263.78               |
| 638        | 36.77 | 0.64   | 20         | 628  | 0.0174  | 0.00058 | 0.0116            | 0.348           | 218.6                |
| 658        | 33.04 | 0.57   | 20         | 648  | 0.01725 | 0.00058 | 0.0115            | 0.345           | 223.58               |
| 678        | 32.45 | 0.53   | 20         | 668  | 0.01633 | 0.00055 | 0.01092           | 0.327           | 218.2                |
| 698        | 32.68 | 0.51   | 20         | 688  | 0.0156  | 0.00052 | 0.01043           | 0.312           | 214.74               |
| 718        | 32.75 | 0.52   | 20         | 708  | 0.01588 | 0.00053 | 0.01062           | 0.318           | 224.83               |
| 738        | 32.88 | 0.55   | 20         | 728  | 0.01673 | 0.00056 | 0.0111            | 0.335           | 243.55               |
| 758        | 36.21 | 0.66   | 20         | 748  | 0.01823 | 0.00061 | 0.0121            | 0.365           | 272.68               |
| 778        | 32.50 | 0.54   | 20         | 768  | 0.01662 | 0.00056 | 0.0111            | 0.332           | 255.21               |
| 798        | 32.26 | 0.45   | 20         | 788  | 0.01395 | 0.00047 | 0.00933           | 0.279           | 219.84               |
| 818        | 33.03 | 0.53   | 20         | 808  | 0.01605 | 0.00054 | 0.01073           | 0.321           | 259.30               |
| 838        | 32.32 | 0.45   | 20         | 828  | 0.01392 | 0.00047 | 0.00931           | 0.278           | 230.57               |
| 858        | 33.04 | 0.44   | 20         | 848  | 0.0131  | 0.00044 | 0.00880           | 0.263           | 223.29               |
| 878        | 36.30 | 0.41   | 20         | 868  | 0.0112  | 0.00038 | 0.00755           | 0.226           | 196.08               |
| 898        | 32.00 | 0.49   | 20         | 888  | 0.0153  | 0.00051 | 0.01024           | 0.306           | 271.95               |
| 918        | 32.36 | 0.35   | 20         | 908  | 0.01082 | 0.00036 | 0.00723           | 0.216           | 196.42               |
| 938        | 32.43 | 0.36   | 20         | 928  | 0.0111  | 0.00037 | 0.00742           | 0.222           | 206.03               |
| 958        | 32.45 | 0.47   | 20         | 948  | 0.01448 | 0.00048 | 0.00968           | 0.290           | 274.61               |
| 978        | 32.31 | 0.36   | 20         | 968  | 0.0111  | 0.00037 | 0.00745           | 0.223           | 215.7                |
| 998        | 31.77 | 0.42   | 20         | 988  | 0.01322 | 0.00044 | 0.00884           | 0.264           | 261.23               |
| 101        | 36.77 | 0.37   | 20         | 1008 | 0.01006 | 0.00034 | 0.00673           | 0.201           | 202.86               |
| 1038       | 33.85 | 0.29   | 20         | 1028 | 0.00857 | 0.00029 | 0.00573           | 0.17            | 176.1                |
| 1058       | 32.63 | 0.28   | 20         | 1048 | 0.00858 | 0.00029 | 0.00574           | 0.172           | 179.86               |
| 1078       | 32.87 | 0.31   | 20         | 1068 | 0.00928 | 0.00031 | 0.00620           | 0.186           | 198.20               |
| 1098       | 32.91 | 0.28   | 20         | 1088 | 0.00851 | 0.00028 | 0.00569           | 0.170           | 185.1                |
| 111        | 34.08 | 0.30   | 20         | 110  | 0.00880 | 0.00029 | 0.00589           | 0.176           | 195.07               |
| 113        | 35.04 | 0.25   | 20         | 112  | 0.00713 | 0.00024 | 0.00477           | 0.143           | 160.96               |
| 115        | 31.8  | 0.22   | 20         | 114  | 0.00692 | 0.00023 | 0.00462           | 0.138           | 158.79               |
| 117        | 33.28 | 0.32   | 20         | 116  | 0.00962 | 0.00032 | 0.00643           | 0.192           | 224.62               |
| 119        | 33.17 | 0.28   | 20         | 118  | 0.00844 | 0.00028 | 0.00564           | 0.169           | 200.57               |
| 121        | 31.7  | 0.26   | 20         | 1208 | 0.00820 | 0.00027 | 0.00548           | 0.164           | 198.1                |
| 1238       | 36.14 | 0.26   | 20         | 1228 | 0.00719 | 0.00024 | 0.00481           | 0.144           | 176.69               |
| 1258       | 32.64 | 0.20   | 20         | 1248 | 0.00613 | 0.00020 | 0.00410           | 0.123           | 152.94               |
| 1278       | 32.86 | 0.26   | 20         | 1268 | 0.00791 | 0.00026 | 0.00529           | 0.158           | 200.66               |
| 1298       | 32.45 | 0.18   | 20         | 1288 | 0.00555 | 0.00019 | 0.00371           | 0.11            | 142.89               |
| 131        | 32.58 | 0.21   | 20         | 1308 | 0.00645 | 0.00022 | 0.00431           | 0.129           | 168.62               |
| 1338       | 32.84 | 0.15   | 20         | 1328 | 0.00457 | 0.00015 | 0.00305           | 0.091           | 121.3                |
| 1358       | 36.67 | 0.29   | 20         | 1348 | 0.00777 | 0.00026 | 0.00520           | 0.155           | 209.53               |

## Run#1039 ( Cont..)

| Time (sec) | Total | Tracer | $\Delta t$ | ti   | C(t)    | E(t)    | $\Delta t * E(t)$ | Ci * $\Delta t$ | Ci * ti * $\Delta t$ |
|------------|-------|--------|------------|------|---------|---------|-------------------|-----------------|----------------------|
| 1378       | 31.94 | 0.09   | 20         | 1368 | 0.00282 | 0.00009 | 0.00188           | 0.056           | 77.09                |
| 1398       | 31.98 | 0.21   | 20         | 1388 | 0.00657 | 0.00022 | 0.00439           | 0.131           | 182.29               |
| 1418       | 33.12 | 0.21   | 20         | 1408 | 0.00634 | 0.00021 | 0.00424           | 0.127           | 178.55               |
| 1438       | 32.39 | 0.18   | 20         | 1428 | 0.00556 | 0.00019 | 0.00372           | 0.111           | 158.72               |
| 1458       | 34.68 | 0.15   | 20         | 1448 | 0.00433 | 0.00014 | 0.00289           | 0.087           | 125.26               |
| 1478       | 33.13 | 0.19   | 20         | 1468 | 0.00573 | 0.00019 | 0.00383           | 0.115           | 168.38               |
| 1498       | 33.35 | 0.19   | 20         | 1488 | 0.00570 | 0.00019 | 0.00381           | 0.114           | 169.55               |
| 1518       | 32.79 | 0.18   | 20         | 1508 | 0.00549 | 0.00018 | 0.00367           | 0.110           | 165.56               |
| 1538       | 32.88 | 0.16   | 20         | 1528 | 0.00487 | 0.00016 | 0.00325           | 0.097           | 148.71               |
| 1558       | 32.67 | 0.24   | 20         | 1548 | 0.00735 | 0.00025 | 0.00491           | 0.147           | 227.44               |
| 1578       | 36.43 | 0.11   | 20         | 1568 | 0.00302 | 0.00010 | 0.00202           | 0.060           | 94.69                |
| 1598       | 33.18 | 0.11   | 20         | 1588 | 0.00332 | 0.00011 | 0.00222           | 0.066           | 105.29               |
| 1618       | 32.48 | 0.20   | 20         | 1608 | 0.00616 | 0.00021 | 0.00412           | 0.123           | 198.03               |
| 1638       | 32.93 | 0.13   | 20         | 1628 | 0.00395 | 0.00013 | 0.00264           | 0.079           | 128.54               |
| 1658       | 31.99 | 0.20   | 20         | 1648 | 0.00625 | 0.00021 | 0.00418           | 0.125           | 206.06               |
| 1678       | 32.72 | 0.16   | 20         | 1668 | 0.00489 | 0.00016 | 0.00327           | 0.098           | 163.13               |
| 1698       | 36.58 | 0.13   | 20         | 1688 | 0.00355 | 0.00012 | 0.00238           | 0.071           | 119.98               |
| 1718       | 33.01 | 0.09   | 20         | 1708 | 0.00273 | 0.00009 | 0.00182           | 0.055           | 93.14                |
| 1738       | 33.15 | 0.11   | 20         | 1728 | 0.00332 | 0.00011 | 0.00222           | 0.066           | 114.68               |
| 1758       | 32.59 | 0.17   | 20         | 1748 | 0.00522 | 0.00017 | 0.00349           | 0.104           | 182.36               |
| 1778       | 32.49 | 0.15   | 20         | 1768 | 0.00462 | 0.00015 | 0.00309           | 0.092           | 163.25               |
| 1798       | 36.34 | 0.10   | 20         | 1788 | 0.00275 | 0.00009 | 0.00184           | 0.055           | 98.40                |
| 1818       | 33.34 | 0.15   | 20         | 1808 | 0.00450 | 0.00015 | 0.00301           | 0.090           | 162.69               |
| 1838       | 33.14 | 0.11   | 20         | 1828 | 0.00332 | 0.00011 | 0.00222           | 0.066           | 121.35               |
| 1858       | 32.54 | 0.09   | 20         | 1848 | 0.00277 | 0.00009 | 0.00185           | 0.055           | 102.22               |
| 1878       | 33.47 | 0.11   | 20         | 1868 | 0.00314 | 0.00010 | 0.00210           | 0.063           | 117.20               |
| 1908       | 36.71 | 0.10   | 20         | 1893 | 0.00272 | 0.00009 | 0.00273           | 0.082           | 154.70               |
| 1928       | 33.29 | 0.09   | 20         | 1918 | 0.00270 | 0.00009 | 0.00181           | 0.054           | 103.71               |
| 1948       | 37.02 | 0.08   | 20         | 1938 | 0.00216 | 0.00007 | 0.00144           | 0.043           | 83.76                |
| 1968       | 33.21 | 0.10   | 20         | 1958 | 0.00301 | 0.00010 | 0.00201           | 0.060           | 117.92               |
| 1988       | 32.83 | 0.07   | 20         | 1978 | 0.00213 | 0.00007 | 0.00143           | 0.043           | 84.35                |
| 2008       | 33.14 | 0.05   | 20         | 1998 | 0.00151 | 0.00005 | 0.00101           | 0.030           | 60.29                |
| 2028       | 32.88 | 0.08   | 20         | 2018 | 0.00243 | 0.00008 | 0.00163           | 0.049           | 98.20                |
| 2048       | 34.37 | 0.07   | 20         | 2038 | 0.00189 | 0.00006 | 0.00126           | 0.038           | 77.08                |
| 2068       | 35.05 | 0.06   | 20         | 2058 | 0.00171 | 0.00006 | 0.00114           | 0.034           | 70.46                |
| 2088       | 33.30 | 0.07   | 20         | 2078 | 0.00210 | 0.00007 | 0.00141           | 0.042           | 87.36                |
| 2108       | 33.15 | 0.11   | 20         | 2098 | 0.00332 | 0.00011 | 0.00222           | 0.066           | 139.23               |
| 2128       | 32.86 | 0.07   | 20         | 2118 | 0.00213 | 0.00007 | 0.00142           | 0.043           | 90.24                |
| 2148       | 32.99 | 0.09   | 20         | 2138 | 0.00273 | 0.00009 | 0.00182           | 0.055           | 116.65               |
| 2168       | 34.42 | 0.06   | 20         | 2158 | 0.00174 | 0.00006 | 0.00117           | 0.035           | 75.24                |
| 2188       | 34.87 | 0.08   | 20         | 2178 | 0.00229 | 0.00008 | 0.00153           | 0.046           | 99.94                |
| 2208       | 33.09 | 0.03   | 20         | 2198 | 0.00076 | 0.00003 | 0.00051           | 0.015           | 33.21                |
| 2228       | 32.80 | 0.09   | 20         | 2218 | 0.00274 | 0.00009 | 0.00183           | 0.055           | 121.72               |
| 2248       | 33.39 | 0.07   | 20         | 2238 | 0.00210 | 0.00007 | 0.00140           | 0.042           | 93.84                |
| 2268       | 33.10 | 0.05   | 20         | 2258 | 0.00151 | 0.00005 | 0.00101           | 0.030           | 68.22                |
| 2288       | 32.93 | 0.09   | 20         | 2278 | 0.00258 | 0.00009 | 0.00173           | 0.052           | 117.60               |
| 2308       | 36.27 | 0.05   | 20         | 2298 | 0.00138 | 0.00005 | 0.00092           | 0.028           | 63.37                |
| 2328       | 32.89 | 0.02   | 20         | 2318 | 0.00046 | 0.00002 | 0.00030           | 0.009           | 21.14                |
| 2348       | 32.90 | 0.04   | 20         | 2338 | 0.00122 | 0.00004 | 0.00081           | 0.024           | 56.85                |
| 2368       | 32.67 | 0.05   | 20         | 2358 | 0.00153 | 0.00005 | 0.00102           | 0.031           | 72.18                |
| 2388       | 33.16 | 0.04   | 20         | 2378 | 0.00121 | 0.00004 | 0.00081           | 0.024           | 57.37                |
| 2408       | 32.88 | 0.01   | 20         | 2398 | 0.00030 | 0.00001 | 0.00020           | 0.006           | 14.59                |
| 2428       | 35.54 | 0.08   | 20         | 2418 | 0.00225 | 0.00008 | 0.00150           | 0.045           | 108.86               |
| 2448       | 32.26 | 0.04   | 20         | 2438 | 0.00124 | 0.00004 | 0.00083           | 0.025           | 60.46                |
| 2468       | 32.88 | 0.02   | 20         | 2458 | 0.00061 | 0.00002 | 0.00041           | 0.012           | 29.90                |
| 2488       | 32.30 | 0.04   | 20         | 2478 | 0.00124 | 0.00004 | 0.00083           | 0.025           | 61.37                |
| 2508       | 33.03 | 0.02   | 20         | 2498 | 0.00061 | 0.00002 | 0.00040           | 0.012           | 30.25                |
| 2528       | 35.70 | 0.03   | 20         | 2518 | 0.00084 | 0.00003 | 0.00056           | 0.017           | 42.32                |
| 2548       | 33.21 | 0.03   | 20         | 2538 | 0.00090 | 0.00003 | 0.00060           | 0.018           | 45.85                |
| 2578       | 51.13 | 0.05   | 30         | 2563 | 0.00098 | 0.00003 | 0.00098           | 0.029           | 50.13                |
| 2608       | 46.87 | 0.07   | 30         | 2593 | 0.00149 | 0.00005 | 0.00150           | 0.045           | 77.45                |
| 2638       | 51.03 | 0.04   | 30         | 2623 | 0.00078 | 0.00003 | 0.00079           | 0.024           | 41.12                |
| 2668       | 50.32 | 0.06   | 30         | 2653 | 0.00119 | 0.00004 | 0.00120           | 0.036           | 63.27                |
| 2698       | 47.48 | 0.05   | 30         | 2683 | 0.00105 | 0.00004 | 0.00106           | 0.032           | 56.51                |

## Run#1039 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 2728       | 50.30  | 0.07   | 30         | 2713  | 0.00139 | 0.00005 | 0.00140           | 0.042            | 75.51                  |
| 2758       | 50.18  | 0.07   | 30         | 2743  | 0.00130 | 0.00004 | 0.00130           | 0.039            | 71.06                  |
| 2788       | 50.16  | 0.03   | 30         | 2773  | 0.00060 | 0.00002 | 0.00060           | 0.018            | 33.17                  |
| 2818       | 47.31  | 0.04   | 30         | 2803  | 0.00085 | 0.00003 | 0.00085           | 0.025            | 47.40                  |
| 2848       | 50.35  | 0.03   | 30         | 2833  | 0.00050 | 0.00002 | 0.00050           | 0.015            | 28.13                  |
| 2878       | 51.50  | 0.03   | 30         | 2863  | 0.00058 | 0.00002 | 0.00058           | 0.017            | 33.36                  |
| 2908       | 50.59  | 0.04   | 30         | 2893  | 0.00069 | 0.00002 | 0.00069           | 0.021            | 40.03                  |
| 2938       | 50.10  | 0.06   | 30         | 2923  | 0.00120 | 0.00004 | 0.00120           | 0.036            | 70.01                  |
| 2998       | 98.65  | 0.06   | 60         | 2968  | 0.00061 | 0.00002 | 0.00122           | 0.036            | 36.10                  |
| 3058       | 101.35 | 0.05   | 60         | 3028  | 0.00049 | 0.00002 | 0.00099           | 0.030            | 29.88                  |
| 3118       | 97.82  | 0.06   | 60         | 3088  | 0.00061 | 0.00002 | 0.00123           | 0.037            | 37.88                  |
| 3178       | 101.44 | 0.05   | 60         | 3148  | 0.00049 | 0.00002 | 0.00099           | 0.030            | 31.03                  |
| 3238       | 97.93  | 0.05   | 60         | 3208  | 0.00051 | 0.00002 | 0.00102           | 0.031            | 32.76                  |
| 3298       | 101.75 | 0.05   | 60         | 3268  | 0.00049 | 0.00002 | 0.00099           | 0.029            | 32.12                  |
| 3358       | 97.40  | 0.02   | 60         | 3328  | 0.00021 | 0.00001 | 0.00041           | 0.012            | 13.67                  |
| 3418       | 101.99 | 0.03   | 60         | 3388  | 0.00025 | 0.00001 | 0.00049           | 0.015            | 16.61                  |
| 3478       | 97.97  | 0.08   | 60         | 3448  | 0.00082 | 0.00003 | 0.00164           | 0.049            | 56.31                  |
| 3538       | 101.13 | 0.04   | 60         | 3508  | 0.00040 | 0.00001 | 0.00079           | 0.024            | 27.75                  |
| 3598       | 99.11  | 0.03   | 60         | 3568  | 0.00030 | 0.00001 | 0.00061           | 0.018            | 21.60                  |
| 3658       | 101.82 | 0.02   | 60         | 3628  | 0.00015 | 0.00000 | 0.00030           | 0.009            | 10.69                  |
| 3778       | 200.65 | 0.06   | 120        | 3718  | 0.00030 | 0.00001 | 0.00120           | 0.036            | 22.24                  |
| 3898       | 199.58 | 0.04   | 120        | 3838  | 0.00020 | 0.00001 | 0.00080           | 0.024            | 15.38                  |
| 4018       | 201.47 | 0.04   | 120        | 3958  | 0.00020 | 0.00001 | 0.00080           | 0.024            | 15.72                  |
| 4138       | 201.40 | 0.02   | 120        | 4078  | 0.00010 | 0.00000 | 0.00040           | 0.012            | 8.10                   |
| 4258       | 202.72 | 0.02   | 120        | 4198  | 0.00010 | 0.00000 | 0.00040           | 0.012            | 8.28                   |
| 4378       | 202.33 | 0.03   | 120        | 4318  | 0.00015 | 0.00000 | 0.00059           | 0.018            | 12.80                  |
| 4498       | 204.18 | 0.03   | 120        | 4438  | 0.00015 | 0.00000 | 0.00059           | 0.018            | 13.04                  |
| 4618       | 202.19 | 0.02   | 120        | 4558  | 0.00010 | 0.00000 | 0.00040           | 0.012            | 9.02                   |
| 4738       | 202.76 | 0.01   | 120        | 4678  | 0.00005 | 0.00000 | 0.00020           | 0.006            | 4.61                   |

$$\Sigma E(t) \Delta t_i = 1.00$$

|                     |
|---------------------|
| $S_o = 1.67$ g/s    |
| Bed weight = 1142 g |
| $\tau = 683.83$ sec |

|                      |                                                                     |
|----------------------|---------------------------------------------------------------------|
| $\tau_{obs} = 682.6$ | $\frac{\Sigma C_i t_i \Delta t_i}{\Sigma C_i \Delta t_i} = 20436.6$ |
|                      | $\Sigma C_i \Delta t_i = 29.94$                                     |

Table D.11 Data Run#1040

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 46.20  | 0.00   | 20         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 20         | 46.20  | 0.00   | 20         | 10    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 40         | 46.20  | 0.00   | 20         | 30    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 60         | 46.33  | 0.03   | 20         | 50    | 0.00065 | 0.00003 | 0.00060           | 0.013            | 0.65                   |
| 80         | 46.43  | 0.64   | 20         | 70    | 0.01378 | 0.00064 | 0.01279           | 0.276            | 19.30                  |
| 100        | 46.15  | 1.91   | 20         | 90    | 0.04139 | 0.00192 | 0.03839           | 0.828            | 74.50                  |
| 120        | 46.11  | 1.98   | 20         | 110   | 0.04294 | 0.00199 | 0.03983           | 0.859            | 94.47                  |
| 140        | 46.16  | 1.97   | 20         | 130   | 0.04268 | 0.00198 | 0.03959           | 0.854            | 110.96                 |
| 160        | 45.75  | 1.91   | 20         | 150   | 0.04164 | 0.00193 | 0.03862           | 0.833            | 124.92                 |
| 180        | 46.39  | 1.62   | 20         | 170   | 0.03493 | 0.00162 | 0.03239           | 0.699            | 118.75                 |
| 200        | 45.97  | 1.75   | 20         | 190   | 0.03807 | 0.00177 | 0.03531           | 0.761            | 144.66                 |
| 220        | 53.81  | 1.84   | 20         | 210   | 0.03419 | 0.00159 | 0.03172           | 0.684            | 143.62                 |
| 240        | 39.17  | 1.29   | 20         | 230   | 0.03293 | 0.00153 | 0.03055           | 0.659            | 151.49                 |
| 260        | 58.51  | 1.96   | 20         | 250   | 0.03350 | 0.00155 | 0.03107           | 0.670            | 167.49                 |
| 280        | 48.09  | 1.39   | 20         | 270   | 0.02890 | 0.00134 | 0.02681           | 0.578            | 156.08                 |
| 300        | 46.59  | 1.32   | 20         | 290   | 0.02833 | 0.00131 | 0.02628           | 0.567            | 164.33                 |
| 320        | 46.01  | 1.33   | 20         | 310   | 0.02891 | 0.00134 | 0.02681           | 0.578            | 179.22                 |
| 340        | 45.95  | 1.19   | 20         | 330   | 0.02590 | 0.00120 | 0.02402           | 0.518            | 170.92                 |
| 360        | 46.78  | 1.13   | 20         | 350   | 0.02405 | 0.00112 | 0.02231           | 0.481            | 168.34                 |
| 380        | 46.38  | 1.08   | 20         | 370   | 0.02329 | 0.00108 | 0.02160           | 0.466            | 172.32                 |
| 400        | 46.21  | 0.99   | 20         | 390   | 0.02142 | 0.00099 | 0.01987           | 0.428            | 167.11                 |
| 420        | 46.53  | 1.03   | 20         | 410   | 0.02214 | 0.00103 | 0.02053           | 0.443            | 181.52                 |
| 440        | 46.37  | 0.89   | 20         | 430   | 0.01919 | 0.00089 | 0.01780           | 0.384            | 165.06                 |
| 460        | 46.40  | 0.97   | 20         | 450   | 0.02091 | 0.00097 | 0.01939           | 0.418            | 188.15                 |
| 480        | 45.87  | 0.75   | 20         | 470   | 0.01635 | 0.00076 | 0.01517           | 0.327            | 153.70                 |
| 500        | 46.22  | 0.81   | 20         | 490   | 0.01752 | 0.00081 | 0.01626           | 0.350            | 171.74                 |
| 520        | 45.89  | 0.69   | 20         | 510   | 0.01504 | 0.00070 | 0.01395           | 0.301            | 153.37                 |
| 540        | 46.13  | 0.78   | 20         | 530   | 0.01691 | 0.00078 | 0.01568           | 0.338            | 179.23                 |
| 560        | 46.22  | 0.68   | 20         | 550   | 0.01471 | 0.00068 | 0.01365           | 0.294            | 161.83                 |
| 580        | 45.53  | 0.74   | 20         | 570   | 0.01625 | 0.00075 | 0.01508           | 0.325            | 185.28                 |
| 600        | 45.82  | 0.67   | 20         | 590   | 0.01462 | 0.00068 | 0.01356           | 0.292            | 172.54                 |
| 620        | 46.30  | 0.75   | 20         | 610   | 0.01620 | 0.00075 | 0.01503           | 0.324            | 197.62                 |
| 640        | 45.44  | 0.74   | 20         | 630   | 0.01629 | 0.00076 | 0.01511           | 0.326            | 205.19                 |
| 660        | 46.05  | 0.59   | 20         | 650   | 0.01281 | 0.00059 | 0.01188           | 0.256            | 166.56                 |
| 680        | 46.06  | 0.67   | 20         | 670   | 0.01455 | 0.00067 | 0.01349           | 0.291            | 194.92                 |
| 700        | 46.40  | 0.58   | 20         | 690   | 0.01250 | 0.00058 | 0.01159           | 0.250            | 172.50                 |
| 720        | 45.77  | 0.50   | 20         | 710   | 0.01081 | 0.00050 | 0.01003           | 0.216            | 153.57                 |
| 740        | 46.24  | 0.48   | 20         | 730   | 0.01027 | 0.00048 | 0.00953           | 0.205            | 149.98                 |
| 760        | 46.55  | 0.46   | 20         | 750   | 0.00988 | 0.00046 | 0.00917           | 0.198            | 148.23                 |
| 780        | 45.40  | 0.54   | 20         | 770   | 0.01189 | 0.00055 | 0.01103           | 0.238            | 183.17                 |
| 800        | 45.97  | 0.44   | 20         | 790   | 0.00957 | 0.00044 | 0.00888           | 0.191            | 151.23                 |
| 820        | 45.95  | 0.39   | 20         | 810   | 0.00849 | 0.00039 | 0.00787           | 0.170            | 137.51                 |
| 840        | 45.75  | 0.50   | 20         | 830   | 0.01093 | 0.00051 | 0.01014           | 0.219            | 181.42                 |
| 860        | 45.36  | 0.37   | 20         | 850   | 0.00816 | 0.00038 | 0.00757           | 0.163            | 138.67                 |
| 880        | 45.78  | 0.43   | 20         | 870   | 0.00939 | 0.00044 | 0.00871           | 0.188            | 163.43                 |
| 900        | 45.64  | 0.39   | 20         | 890   | 0.00855 | 0.00040 | 0.00793           | 0.171            | 152.10                 |
| 920        | 45.83  | 0.37   | 20         | 910   | 0.00807 | 0.00037 | 0.00749           | 0.161            | 146.93                 |
| 940        | 45.93  | 0.34   | 20         | 930   | 0.00740 | 0.00034 | 0.00687           | 0.148            | 137.69                 |
| 960        | 46.23  | 0.37   | 20         | 950   | 0.00800 | 0.00037 | 0.00742           | 0.160            | 152.07                 |
| 1000       | 91.77  | 0.63   | 40         | 980   | 0.00686 | 0.00032 | 0.01274           | 0.275            | 269.11                 |
| 1040       | 104.91 | 0.69   | 40         | 1020  | 0.00658 | 0.00031 | 0.01220           | 0.263            | 268.34                 |
| 1080       | 94.50  | 0.54   | 40         | 1060  | 0.00571 | 0.00027 | 0.01060           | 0.229            | 242.29                 |
| 1120       | 91.94  | 0.44   | 40         | 1100  | 0.00479 | 0.00022 | 0.00888           | 0.191            | 210.57                 |
| 1160       | 91.77  | 0.43   | 40         | 1140  | 0.00469 | 0.00022 | 0.00869           | 0.187            | 213.66                 |

# Run#1040 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 650        | 92.09  | 0.32   | 40         | 1180  | 0.00347 | 0.00016 | 0.00645           | 0.139            | 164.01                 |
| 660        | 92.31  | 0.41   | 40         | 1220  | 0.00444 | 0.00021 | 0.00824           | 0.178            | 216.75                 |
| 670        | 91.51  | 0.32   | 40         | 1260  | 0.00350 | 0.00016 | 0.00649           | 0.140            | 176.24                 |
| 680        | 92.06  | 0.35   | 40         | 1300  | 0.00380 | 0.00018 | 0.00705           | 0.152            | 197.70                 |
| 690        | 91.67  | 0.31   | 40         | 1340  | 0.00338 | 0.00016 | 0.00627           | 0.135            | 181.26                 |
| 700        | 91.61  | 0.32   | 40         | 1380  | 0.00349 | 0.00016 | 0.00648           | 0.140            | 192.82                 |
| 710        | 91.60  | 0.23   | 40         | 1420  | 0.00251 | 0.00012 | 0.00466           | 0.100            | 142.62                 |
| 720        | 137.92 | 0.39   | 60         | 1470  | 0.00283 | 0.00013 | 0.00787           | 0.170            | 249.41                 |
| 730        | 138.10 | 0.29   | 60         | 1530  | 0.00210 | 0.00010 | 0.00584           | 0.126            | 192.77                 |
| 740        | 138.36 | 0.22   | 60         | 1590  | 0.00159 | 0.00007 | 0.00442           | 0.095            | 151.69                 |
| 750        | 138.74 | 0.19   | 60         | 1650  | 0.00137 | 0.00006 | 0.00381           | 0.082            | 135.58                 |
| 760        | 290.89 | 0.43   | 120        | 1740  | 0.00148 | 0.00007 | 0.00823           | 0.177            | 308.65                 |
| 770        | 275.21 | 0.30   | 120        | 1860  | 0.00109 | 0.00005 | 0.00607           | 0.131            | 243.31                 |
| 780        | 274.73 | 0.19   | 120        | 1980  | 0.00069 | 0.00003 | 0.00385           | 0.083            | 164.32                 |
| 790        | 273.82 | 0.22   | 120        | 2100  | 0.00080 | 0.00004 | 0.00447           | 0.096            | 202.47                 |
| 800        | 106.93 | 0.05   | 45         | 2183  | 0.00047 | 0.00002 | 0.00098           | 0.021            | 45.92                  |

$$\Sigma E(t) \Delta t_i = 0.9836$$

|                     |
|---------------------|
| $S_o = 2.32$ g/s    |
| Bed weight = 1215 g |
| $\tau = 523.59$ sec |

|                      |                                       |
|----------------------|---------------------------------------|
| $\tau_{obs} = 523.6$ | $\Sigma C_i t_i \Delta t_i = 11097.9$ |
|                      | $\Sigma C_i \Delta t_i = 21.19$       |



Table D.12 Data Run#1041

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 28.40  | 0.00   | 20         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 20         | 28.40  | 0.00   | 20         | 10    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 40         | 28.40  | 0.00   | 20         | 30    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 60         | 57.98  | 0.29   | 20         | 50    | 0.00500 | 0.00028 | 0.00568           | 0.100            | 5.00                   |
| 80         | 58.44  | 1.73   | 20         | 70    | 0.02960 | 0.00168 | 0.03362           | 0.592            | 41.44                  |
| 100        | 58.52  | 2.46   | 20         | 90    | 0.04204 | 0.00239 | 0.04774           | 0.841            | 75.67                  |
| 120        | 58.21  | 2.36   | 20         | 110   | 0.04054 | 0.00230 | 0.04604           | 0.811            | 89.19                  |
| 140        | 58.69  | 2.36   | 20         | 130   | 0.04013 | 0.00228 | 0.04557           | 0.803            | 104.33                 |
| 160        | 58.80  | 2.16   | 20         | 150   | 0.03673 | 0.00209 | 0.04172           | 0.735            | 110.20                 |
| 180        | 58.67  | 2.14   | 20         | 170   | 0.03648 | 0.00207 | 0.04142           | 0.730            | 124.02                 |
| 200        | 48.46  | 1.72   | 20         | 190   | 0.03549 | 0.00202 | 0.04031           | 0.710            | 134.87                 |
| 220        | 48.45  | 1.64   | 20         | 210   | 0.03385 | 0.00192 | 0.03844           | 0.677            | 142.17                 |
| 240        | 59.17  | 1.61   | 20         | 230   | 0.02721 | 0.00155 | 0.03090           | 0.544            | 125.16                 |
| 260        | 58.60  | 1.61   | 20         | 250   | 0.02747 | 0.00156 | 0.03120           | 0.549            | 137.37                 |
| 280        | 59.27  | 1.66   | 20         | 270   | 0.02801 | 0.00159 | 0.03181           | 0.560            | 151.24                 |
| 300        | 59.96  | 1.53   | 20         | 290   | 0.02552 | 0.00145 | 0.02898           | 0.510            | 148.00                 |
| 320        | 59.25  | 1.51   | 20         | 310   | 0.02549 | 0.00145 | 0.02894           | 0.510            | 158.01                 |
| 340        | 59.02  | 1.26   | 20         | 330   | 0.02135 | 0.00121 | 0.02425           | 0.427            | 140.90                 |
| 360        | 58.91  | 1.40   | 20         | 350   | 0.02377 | 0.00135 | 0.02699           | 0.475            | 166.36                 |
| 380        | 59.21  | 1.20   | 20         | 370   | 0.02027 | 0.00115 | 0.02302           | 0.405            | 149.97                 |
| 400        | 58.93  | 1.20   | 20         | 390   | 0.02036 | 0.00116 | 0.02313           | 0.407            | 158.83                 |
| 420        | 59.28  | 0.95   | 20         | 410   | 0.01603 | 0.00091 | 0.01820           | 0.321            | 131.41                 |
| 440        | 59.90  | 1.24   | 20         | 430   | 0.02070 | 0.00118 | 0.02351           | 0.414            | 178.03                 |
| 460        | 59.73  | 0.94   | 20         | 450   | 0.01574 | 0.00089 | 0.01787           | 0.315            | 141.64                 |
| 480        | 48.94  | 0.73   | 20         | 470   | 0.01492 | 0.00085 | 0.01694           | 0.298            | 140.21                 |
| 500        | 49.09  | 0.73   | 20         | 490   | 0.01487 | 0.00084 | 0.01689           | 0.297            | 145.73                 |
| 520        | 58.61  | 0.79   | 20         | 510   | 0.01348 | 0.00077 | 0.01531           | 0.270            | 137.49                 |
| 540        | 59.04  | 0.65   | 20         | 530   | 0.01101 | 0.00063 | 0.01250           | 0.220            | 116.70                 |
| 548        | 22.26  | 0.25   | 8          | 543.9 | 0.01123 | 0.00064 | 0.00500           | 0.088            | 47.88                  |
| 568        | 52.04  | 0.60   | 20         | 557.8 | 0.01153 | 0.00065 | 0.01309           | 0.231            | 128.63                 |
| 588        | 46.22  | 0.49   | 20         | 577.8 | 0.01060 | 0.00060 | 0.01204           | 0.212            | 122.52                 |
| 608        | 59.26  | 0.61   | 20         | 597.8 | 0.01029 | 0.00058 | 0.01169           | 0.206            | 123.08                 |
| 628        | 59.26  | 0.63   | 20         | 617.8 | 0.01063 | 0.00060 | 0.01207           | 0.213            | 131.37                 |
| 648        | 59.55  | 0.67   | 20         | 637.8 | 0.01125 | 0.00064 | 0.01278           | 0.225            | 143.53                 |
| 688        | 118.12 | 1.30   | 40         | 667.8 | 0.01101 | 0.00062 | 0.02500           | 0.440            | 294.00                 |
| 728        | 117.93 | 1.08   | 40         | 707.8 | 0.00916 | 0.00052 | 0.02080           | 0.366            | 259.29                 |
| 768        | 117.21 | 0.84   | 40         | 747.8 | 0.00717 | 0.00041 | 0.01628           | 0.287            | 214.38                 |
| 808        | 117.57 | 0.87   | 40         | 787.8 | 0.00740 | 0.00042 | 0.01681           | 0.296            | 233.20                 |
| 848        | 97.61  | 0.61   | 40         | 827.8 | 0.00625 | 0.00035 | 0.01419           | 0.250            | 206.94                 |
| 888        | 117.74 | 0.73   | 40         | 867.8 | 0.00620 | 0.00035 | 0.01408           | 0.248            | 215.23                 |
| 928        | 118.15 | 0.58   | 40         | 907.8 | 0.00491 | 0.00028 | 0.01115           | 0.196            | 178.26                 |
| 968        | 117.40 | 0.41   | 40         | 947.8 | 0.00349 | 0.00020 | 0.00793           | 0.140            | 132.41                 |
| 1008       | 116.84 | 0.33   | 40         | 987.8 | 0.00282 | 0.00016 | 0.00642           | 0.113            | 111.60                 |
| 1068       | 176.01 | 0.61   | 60         | 1038  | 0.00347 | 0.00020 | 0.01181           | 0.208            | 215.81                 |
| 1128       | 155.17 | 0.37   | 60         | 1098  | 0.00238 | 0.00014 | 0.00812           | 0.143            | 157.07                 |
| 1188       | 174.88 | 0.52   | 60         | 1158  | 0.00297 | 0.00017 | 0.01013           | 0.178            | 206.57                 |
| 1248       | 175.27 | 0.39   | 60         | 1218  | 0.00223 | 0.00013 | 0.00758           | 0.134            | 162.59                 |
| 1308       | 177.27 | 0.38   | 60         | 1278  | 0.00214 | 0.00012 | 0.00730           | 0.129            | 164.35                 |
| 1368       | 174.85 | 0.29   | 60         | 1338  | 0.00166 | 0.00009 | 0.00565           | 0.100            | 133.13                 |
| 1428       | 156.72 | 0.23   | 60         | 1398  | 0.00147 | 0.00008 | 0.00500           | 0.088            | 123.09                 |
| 1488       | 174.82 | 0.19   | 60         | 1458  | 0.00109 | 0.00006 | 0.00370           | 0.065            | 95.07                  |
| 1548       | 173.34 | 0.16   | 60         | 1518  | 0.00092 | 0.00005 | 0.00314           | 0.055            | 84.06                  |
| 1608       | 173.45 | 0.19   | 60         | 1578  | 0.00110 | 0.00006 | 0.00373           | 0.066            | 103.70                 |
| 1668       | 174.27 | 0.15   | 60         | 1638  | 0.00086 | 0.00005 | 0.00293           | 0.052            | 84.58                  |
| 1728       | 155.84 | 0.06   | 60         | 1698  | 0.00039 | 0.00002 | 0.00131           | 0.023            | 39.22                  |
| 1788       | 175.04 | 0.05   | 60         | 1758  | 0.00029 | 0.00002 | 0.00097           | 0.017            | 30.13                  |
| 1884       | 272.56 | 0.15   | 96         | 1836  | 0.00055 | 0.00003 | 0.00300           | 0.053            | 96.96                  |

$$\Sigma E(t) \Delta t_i = 0.98$$

|                     |
|---------------------|
| $S_o = 2.84$ g/s    |
| Bed weight = 1211 g |
| $\tau = 426.41$ sec |

|                      |                                      |
|----------------------|--------------------------------------|
| $\tau_{obs} = 426.3$ | $\Sigma C_i t_i \Delta t_i = 7392.6$ |
|                      | $\Sigma C_i \Delta t_i = 17.34$      |

**Table D.13 Data Run#1042**

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 18.62  | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 5          | 18.62  | 0.00   | 10         | 2.5   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 15         | 18.62  | 0.00   | 10         | 10    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 25         | 18.62  | 0.00   | 10         | 20    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 35         | 187.25 | 6.84   | 10         | 30    | 0.03651 | 0.01360 | 0.13596           | 0.365            | 10.95                  |
| 45         | 186.61 | 7.92   | 10         | 40    | 0.04243 | 0.01580 | 0.15800           | 0.424            | 16.97                  |
| 55         | 188.57 | 7.61   | 10         | 45    | 0.04033 | 0.01502 | 0.15019           | 0.403            | 18.15                  |
| 65         | 184.35 | 6.02   | 10         | 60    | 0.03263 | 0.01215 | 0.12151           | 0.326            | 19.58                  |
| 75         | 185.93 | 4.52   | 10         | 70    | 0.02431 | 0.00905 | 0.09053           | 0.243            | 17.02                  |
| 85         | 186.21 | 3.64   | 10         | 80    | 0.01955 | 0.00728 | 0.07280           | 0.195            | 15.64                  |
| 95         | 184.60 | 2.88   | 10         | 90    | 0.01560 | 0.00581 | 0.05810           | 0.156            | 14.04                  |
| 105        | 184.51 | 2.29   | 10         | 100   | 0.01238 | 0.00461 | 0.04612           | 0.124            | 12.38                  |
| 115        | 183.13 | 1.84   | 10         | 110   | 0.01002 | 0.00373 | 0.03732           | 0.100            | 11.02                  |
| 125        | 185.67 | 1.44   | 10         | 120   | 0.00776 | 0.00289 | 0.02888           | 0.078            | 9.31                   |
| 135        | 181.83 | 1.24   | 10         | 130   | 0.00682 | 0.00254 | 0.02540           | 0.068            | 8.87                   |
| 145        | 187.72 | 1.00   | 10         | 140   | 0.00533 | 0.00198 | 0.01984           | 0.053            | 7.46                   |
| 155        | 182.77 | 0.70   | 10         | 150   | 0.00383 | 0.00143 | 0.01426           | 0.038            | 5.74                   |
| 165        | 186.24 | 0.53   | 10         | 160   | 0.00285 | 0.00106 | 0.01060           | 0.028            | 4.55                   |
| 175        | 185.56 | 0.47   | 10         | 170   | 0.00253 | 0.00094 | 0.00943           | 0.025            | 4.31                   |
| 185        | 182.00 | 0.47   | 10         | 180   | 0.00255 | 0.00095 | 0.00951           | 0.026            | 4.60                   |
| 195        | 187.04 | 0.32   | 10         | 190   | 0.00171 | 0.00064 | 0.00637           | 0.017            | 3.25                   |
| 205        | 185.55 | 0.21   | 10         | 200   | 0.00113 | 0.00042 | 0.00421           | 0.011            | 2.26                   |
| 215        | 190.07 | 0.16   | 10         | 210   | 0.00084 | 0.00031 | 0.00313           | 0.008            | 1.77                   |
| 225        | 183.53 | 0.12   | 10         | 220   | 0.00065 | 0.00024 | 0.00243           | 0.007            | 1.44                   |
| 235        | 183.02 | 0.15   | 10         | 230   | 0.00082 | 0.00031 | 0.00305           | 0.008            | 1.89                   |
| 245        | 185.42 | 0.11   | 10         | 240   | 0.00059 | 0.00022 | 0.00221           | 0.006            | 1.42                   |
| 255        | 186.02 | 0.07   | 10         | 250   | 0.00038 | 0.00014 | 0.00140           | 0.004            | 0.94                   |
| 265        | 184.70 | 0.08   | 10         | 260   | 0.00043 | 0.00016 | 0.00161           | 0.004            | 1.13                   |
| 275        | 186.81 | 0.04   | 10         | 270   | 0.00021 | 0.00008 | 0.00080           | 0.002            | 0.58                   |
| 285        | 186.21 | 0.05   | 10         | 280   | 0.00027 | 0.00010 | 0.00100           | 0.003            | 0.75                   |
| 295        | 185.68 | 0.03   | 10         | 290   | 0.00016 | 0.00006 | 0.00060           | 0.002            | 0.47                   |
| 305        | 187.94 | 0.04   | 10         | 300   | 0.00021 | 0.00008 | 0.00079           | 0.002            | 0.64                   |
| 315        | 184.75 | 0.01   | 10         | 310   | 0.00005 | 0.00002 | 0.00020           | 0.001            | 0.17                   |
| 325        | 189.18 | 0.00   | 10         | 320   | 0.00016 | 0.00006 | 0.00059           | 0.002            | 0.51                   |

$$\Sigma E(t) \Delta t_i = 1.0$$

|                                   |
|-----------------------------------|
| <b>So = 18.62 g/s</b>             |
| <b>Bed weight = 1357 g</b>        |
| <b><math>\tau = 73</math> sec</b> |

|                                       |                                                       |
|---------------------------------------|-------------------------------------------------------|
| <b><math>\tau_{obs} = 72.9</math></b> | <b><math>\Sigma C_i t_i \Delta t_i = 199.0</math></b> |
|                                       | <b><math>\Sigma C_i \Delta t_i = 2.73</math></b>      |

Table D.14 Data Run#1043

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | C(t)    | E(t)    | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 53.45  | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 10         | 53.45  | 0.00   | 10         | 5     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 20         | 53.45  | 0.00   | 10         | 15    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 30         | 52.45  | 0.00   | 10         | 25    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 40         | 53.61  | 0.00   | 10         | 35    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 50         | 54.30  | 0.61   | 10         | 45    | 0.01123 | 0.00120 | 0.01201           | 0.112            | 5.06                   |
| 60         | 53.44  | 2.52   | 10         | 55    | 0.04716 | 0.00504 | 0.05040           | 0.472            | 25.94                  |
| 70         | 53.68  | 2.37   | 10         | 65    | 0.04415 | 0.00472 | 0.04719           | 0.442            | 28.70                  |
| 80         | 53.02  | 2.28   | 10         | 75    | 0.04300 | 0.00460 | 0.04596           | 0.430            | 32.25                  |
| 90         | 55.94  | 2.44   | 10         | 85    | 0.04362 | 0.00466 | 0.04662           | 0.436            | 37.08                  |
| 100        | 52.39  | 2.14   | 10         | 95    | 0.04085 | 0.00437 | 0.04366           | 0.408            | 38.81                  |
| 110        | 52.66  | 1.96   | 10         | 105   | 0.03722 | 0.00398 | 0.03978           | 0.372            | 39.08                  |
| 120        | 53.95  | 2.05   | 10         | 115   | 0.03800 | 0.00406 | 0.04062           | 0.380            | 43.70                  |
| 130        | 54.14  | 1.92   | 10         | 125   | 0.03546 | 0.00379 | 0.03791           | 0.355            | 44.33                  |
| 140        | 52.36  | 1.71   | 10         | 135   | 0.03266 | 0.00349 | 0.03491           | 0.327            | 44.09                  |
| 150        | 55.06  | 1.88   | 10         | 145   | 0.03414 | 0.00365 | 0.03650           | 0.341            | 49.51                  |
| 160        | 52.86  | 1.39   | 10         | 155   | 0.02630 | 0.00281 | 0.02811           | 0.263            | 40.76                  |
| 170        | 53.35  | 1.40   | 10         | 165   | 0.02624 | 0.00280 | 0.02805           | 0.262            | 43.30                  |
| 180        | 53.30  | 1.52   | 10         | 175   | 0.02852 | 0.00305 | 0.03048           | 0.285            | 49.91                  |
| 190        | 53.83  | 1.34   | 10         | 185   | 0.02489 | 0.00266 | 0.02661           | 0.249            | 46.05                  |
| 200        | 52.39  | 1.11   | 10         | 195   | 0.02119 | 0.00226 | 0.02265           | 0.212            | 41.32                  |
| 210        | 55.33  | 1.32   | 10         | 205   | 0.02386 | 0.00255 | 0.02550           | 0.239            | 48.91                  |
| 220        | 53.24  | 0.92   | 10         | 215   | 0.01728 | 0.00185 | 0.01847           | 0.173            | 37.15                  |
| 230        | 52.40  | 0.95   | 10         | 225   | 0.01813 | 0.00194 | 0.01938           | 0.181            | 40.79                  |
| 240        | 53.03  | 0.96   | 10         | 235   | 0.01810 | 0.00193 | 0.01935           | 0.181            | 42.54                  |
| 250        | 51.52  | 0.92   | 10         | 245   | 0.01786 | 0.00191 | 0.01909           | 0.179            | 43.75                  |
| 260        | 54.14  | 0.92   | 10         | 255   | 0.01699 | 0.00182 | 0.01816           | 0.170            | 43.33                  |
| 270        | 53.76  | 0.80   | 10         | 265   | 0.01488 | 0.00159 | 0.01591           | 0.149            | 39.43                  |
| 280        | 54.28  | 0.73   | 10         | 275   | 0.01345 | 0.00144 | 0.01438           | 0.134            | 36.98                  |
| 290        | 54.80  | 0.75   | 10         | 285   | 0.01369 | 0.00146 | 0.01463           | 0.137            | 39.01                  |
| 300        | 52.44  | 0.72   | 10         | 295   | 0.01373 | 0.00147 | 0.01468           | 0.137            | 40.50                  |
| 310        | 54.28  | 0.65   | 10         | 305   | 0.01197 | 0.00128 | 0.01280           | 0.120            | 36.52                  |
| 320        | 52.98  | 0.56   | 10         | 315   | 0.01057 | 0.00113 | 0.01130           | 0.106            | 33.30                  |
| 330        | 53.58  | 0.60   | 10         | 325   | 0.01120 | 0.00120 | 0.01197           | 0.112            | 36.39                  |
| 340        | 52.42  | 0.45   | 10         | 335   | 0.00858 | 0.00092 | 0.00918           | 0.086            | 28.76                  |
| 350        | 53.78  | 0.53   | 10         | 345   | 0.00985 | 0.00105 | 0.01053           | 0.099            | 34.00                  |
| 360        | 53.49  | 0.51   | 10         | 355   | 0.00953 | 0.00102 | 0.01019           | 0.095            | 33.85                  |
| 370        | 53.19  | 0.54   | 10         | 365   | 0.01015 | 0.00109 | 0.01085           | 0.102            | 37.06                  |
| 380        | 53.00  | 0.41   | 10         | 375   | 0.00774 | 0.00083 | 0.00827           | 0.077            | 29.01                  |
| 390        | 53.18  | 0.46   | 10         | 385   | 0.00865 | 0.00092 | 0.00925           | 0.086            | 33.30                  |
| 400        | 53.50  | 0.46   | 10         | 395   | 0.00860 | 0.00092 | 0.00919           | 0.086            | 33.96                  |
| 410        | 53.27  | 0.32   | 10         | 405   | 0.00601 | 0.00064 | 0.00642           | 0.060            | 24.33                  |
| 420        | 52.73  | 0.33   | 10         | 415   | 0.00626 | 0.00067 | 0.00669           | 0.063            | 25.97                  |
| 440        | 107.10 | 0.69   | 20         | 430   | 0.00644 | 0.00069 | 0.01377           | 0.129            | 55.41                  |
| 460        | 107.15 | 0.56   | 20         | 450   | 0.00523 | 0.00056 | 0.01117           | 0.105            | 47.04                  |
| 480        | 106.20 | 0.48   | 20         | 470   | 0.00452 | 0.00048 | 0.00966           | 0.090            | 42.49                  |
| 500        | 106.03 | 0.40   | 20         | 490   | 0.00377 | 0.00040 | 0.00806           | 0.075            | 36.97                  |
| 520        | 104.65 | 0.42   | 20         | 510   | 0.00401 | 0.00043 | 0.00858           | 0.080            | 40.94                  |
| 540        | 106.64 | 0.49   | 20         | 530   | 0.00459 | 0.00049 | 0.00982           | 0.092            | 48.71                  |
| 560        | 108.95 | 0.35   | 20         | 550   | 0.00321 | 0.00034 | 0.00687           | 0.064            | 35.34                  |
| 580        | 105.71 | 0.21   | 20         | 570   | 0.00199 | 0.00021 | 0.00425           | 0.040            | 22.65                  |
| 600        | 107.86 | 0.35   | 20         | 590   | 0.00324 | 0.00035 | 0.00694           | 0.065            | 38.29                  |
| 620        | 107.59 | 0.27   | 20         | 610   | 0.00251 | 0.00027 | 0.00536           | 0.050            | 30.62                  |
| 640        | 107.49 | 0.22   | 20         | 630   | 0.00205 | 0.00022 | 0.00438           | 0.041            | 25.79                  |

## Run#1043 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|--------------------|--------------------------|
| 660        | 108.69 | 0.18   | 20         | 650   | 0.00166 | 0.00018 | 0.00354           | 0.033              | 21.53                    |
| 680        | 105.86 | 0.17   | 20         | 670   | 0.00161 | 0.00017 | 0.00343           | 0.032              | 21.52                    |
| 700        | 106.89 | 0.20   | 20         | 690   | 0.00187 | 0.00020 | 0.00400           | 0.037              | 25.82                    |
| 720        | 107.73 | 0.18   | 20         | 710   | 0.00167 | 0.00018 | 0.00357           | 0.033              | 23.73                    |
| 760        | 214.00 | 0.28   | 40         | 740   | 0.00131 | 0.00014 | 0.00559           | 0.052              | 38.73                    |
| 800        | 215.06 | 0.23   | 40         | 780   | 0.00107 | 0.00011 | 0.00457           | 0.043              | 33.37                    |
| 840        | 215.25 | 0.17   | 40         | 820   | 0.00079 | 0.00008 | 0.00338           | 0.032              | 25.90                    |
| 880        | 214.71 | 0.14   | 40         | 860   | 0.00065 | 0.00007 | 0.00279           | 0.026              | 22.43                    |
| 920        | 212.58 | 0.12   | 40         | 900   | 0.00056 | 0.00006 | 0.00241           | 0.023              | 20.32                    |
| 960        | 211.80 | 0.10   | 40         | 940   | 0.00047 | 0.00005 | 0.00202           | 0.019              | 17.75                    |
| 1000       | 214.80 | 0.08   | 40         | 980   | 0.00037 | 0.00004 | 0.00159           | 0.015              | 14.60                    |
| 1040       | 213.14 | 0.05   | 40         | 1020  | 0.00023 | 0.00003 | 0.00100           | 0.009              | 9.57                     |
| 1080       | 211.41 | 0.07   | 40         | 1060  | 0.00033 | 0.00004 | 0.00142           | 0.013              | 14.04                    |
| 1120       | 214.06 | 0.06   | 40         | 1100  | 0.00028 | 0.00003 | 0.00120           | 0.011              | 12.33                    |
| 1154.2     | 181.04 | 0.04   | 34         | 1137  | 0.00022 | 0.00002 | 0.00081           | 0.008              | 8.59                     |

$$\Sigma E(t) \Delta t_i = 0.9700$$

|                     |
|---------------------|
| $S_o = 5.344$ g/s   |
| Bed weight = 1227 g |
| $\tau = 229.57$ sec |

|                      |                                      |
|----------------------|--------------------------------------|
| $\tau_{obs} = 229.6$ | $\Sigma C_i t_i \Delta t_i = 2143.2$ |
|                      | $\Sigma C_i \Delta t_i = 9.34$       |

Table D.15 Data Run#2000

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|-------|--------|------------|-------|---------|---------|-------------------|--------------------|--------------------------|
| 0          | 21.1  | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 10         | 21.1  | 0.00   | 10         | 5     | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 20         | 21.1  | 0.00   | 10         | 15    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 30         | 21.1  | 0.00   | 10         | 25    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 40         | 21.1  | 0.00   | 10         | 35    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 50         | 21.1  | 0.00   | 10         | 45    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 60         | 21.1  | 0.00   | 10         | 55    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 70         | 21.1  | 0.00   | 10         | 65    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 80         | 21.1  | 0.00   | 10         | 75    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 90         | 21.1  | 0.00   | 10         | 85    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 100        | 21.1  | 0.00   | 10         | 95    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 110        | 21.1  | 0.00   | 10         | 105   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 120        | 21.1  | 0.00   | 10         | 115   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 130        | 21.1  | 0.00   | 10         | 125   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 140        | 21.1  | 0.00   | 10         | 135   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 150        | 21.1  | 0.00   | 10         | 145   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 160        | 21.1  | 0.00   | 10         | 155   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 170        | 21.1  | 0.00   | 10         | 165   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 180        | 21.1  | 0.00   | 10         | 175   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 190        | 21.08 | 0.00   | 10         | 185   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 200        | 23.28 | 0.00   | 10         | 195   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 210        | 23.88 | 0.00   | 10         | 205   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 220        | 23.92 | 0.00   | 10         | 215   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 230        | 21.1  | 0.00   | 10         | 225   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 240        | 21.75 | 0.01   | 10         | 235   | 0.00046 | 0.00002 | 0.00020           | 0.005              | 1.08                     |
| 250        | 21.69 | 0.00   | 10         | 245   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 260        | 20.84 | 0.00   | 10         | 255   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 270        | 21.04 | 0.00   | 10         | 265   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 280        | 21.1  | 0.01   | 10         | 275   | 0.00047 | 0.00002 | 0.00020           | 0.005              | 1.30                     |
| 300        | 42.34 | 0.01   | 20         | 290   | 0.00024 | 0.00001 | 0.00020           | 0.005              | 1.37                     |
| 320        | 47.97 | 0.03   | 20         | 310   | 0.00063 | 0.00003 | 0.00054           | 0.013              | 3.88                     |
| 340        | 40.97 | 0.03   | 20         | 330   | 0.00073 | 0.00003 | 0.00063           | 0.015              | 4.83                     |
| 360        | 44.26 | 0.05   | 20         | 350   | 0.0011  | 0.00005 | 0.00097           | 0.023              | 7.91                     |
| 380        | 41.32 | 0.06   | 20         | 370   | 0.00145 | 0.00006 | 0.00125           | 0.029              | 10.75                    |
| 400        | 42.02 | 0.07   | 20         | 390   | 0.00167 | 0.00007 | 0.00144           | 0.033              | 12.99                    |
| 420        | 42.05 | 0.12   | 20         | 410   | 0.00285 | 0.00012 | 0.00246           | 0.057              | 23.40                    |
| 440        | 41.59 | 0.16   | 20         | 430   | 0.00385 | 0.00017 | 0.00331           | 0.077              | 33.08                    |
| 460        | 48.57 | 0.12   | 20         | 450   | 0.00247 | 0.0001  | 0.00213           | 0.049              | 22.24                    |
| 480        | 41.9  | 0.12   | 20         | 470   | 0.00286 | 0.00012 | 0.00247           | 0.057              | 26.91                    |
| 500        | 40.86 | 0.18   | 20         | 490   | 0.00441 | 0.00019 | 0.00379           | 0.088              | 43.17                    |
| 520        | 40.89 | 0.17   | 20         | 510   | 0.00416 | 0.00018 | 0.00358           | 0.083              | 42.41                    |
| 540        | 41.80 | 0.19   | 20         | 530   | 0.00455 | 0.00020 | 0.00392           | 0.091              | 48.18                    |
| 560        | 43.05 | 0.25   | 20         | 550   | 0.00581 | 0.00025 | 0.00500           | 0.11               | 63.88                    |
| 580        | 46.66 | 0.33   | 20         | 570   | 0.00707 | 0.00030 | 0.00609           | 0.14               | 80.63                    |
| 600        | 40.54 | 0.26   | 20         | 590   | 0.00641 | 0.00028 | 0.00552           | 0.128              | 75.68                    |
| 620        | 41.84 | 0.29   | 20         | 610   | 0.00693 | 0.00030 | 0.00597           | 0.139              | 84.56                    |
| 640        | 41.64 | 0.26   | 20         | 630   | 0.00624 | 0.00027 | 0.00538           | 0.125              | 78.67                    |
| 660        | 41.36 | 0.23   | 20         | 650   | 0.00556 | 0.00024 | 0.00479           | 0.11               | 72.29                    |
| 680        | 48.69 | 0.31   | 20         | 670   | 0.00637 | 0.00027 | 0.00548           | 0.127              | 85.32                    |
| 700        | 41.58 | 0.31   | 20         | 690   | 0.00746 | 0.00032 | 0.00642           | 0.149              | 102.89                   |
| 720        | 42.36 | 0.35   | 20         | 710   | 0.00826 | 0.00036 | 0.00712           | 0.165              | 117.3                    |
| 740        | 37.74 | 0.29   | 20         | 730   | 0.00768 | 0.00033 | 0.00662           | 0.154              | 112.1                    |
| 760        | 39.72 | 0.26   | 20         | 750   | 0.00655 | 0.00028 | 0.00564           | 0.13               | 98.19                    |
| 780        | 42.06 | 0.28   | 20         | 770   | 0.00666 | 0.00029 | 0.00573           | 0.133              | 102.52                   |
| 800        | 48.58 | 0.50   | 20         | 790   | 0.01029 | 0.00044 | 0.00887           | 0.206              | 162.62                   |
| 820        | 41.99 | 0.35   | 20         | 810   | 0.00834 | 0.00036 | 0.00718           | 0.167              | 135.03                   |
| 840        | 41.99 | 0.35   | 20         | 830   | 0.00834 | 0.00036 | 0.00718           | 0.167              | 138.37                   |
| 860        | 41.55 | 0.42   | 20         | 850   | 0.0101  | 0.00044 | 0.00871           | 0.202              | 171.8                    |
| 880        | 41.38 | 0.41   | 20         | 870   | 0.00991 | 0.00043 | 0.00854           | 0.198              | 172.40                   |
| 900        | 37.16 | 0.32   | 20         | 890   | 0.00861 | 0.00037 | 0.00742           | 0.172              | 153.28                   |
| 920        | 48.68 | 0.54   | 20         | 910   | 0.0110  | 0.00048 | 0.00956           | 0.222              | 201.89                   |
| 940        | 42.29 | 0.41   | 20         | 930   | 0.00958 | 0.00041 | 0.00825           | 0.192              | 178.1                    |
| 960        | 41.42 | 0.43   | 20         | 950   | 0.01038 | 0.00045 | 0.00894           | 0.208              | 197.25                   |
| 980        | 41.48 | 0.36   | 20         | 970   | 0.00868 | 0.00037 | 0.00748           | 0.174              | 168.37                   |
| 1000       | 42.47 | 0.29   | 20         | 990   | 0.00683 | 0.00029 | 0.00588           | 0.137              | 135.20                   |
| 1020       | 37.96 | 0.37   | 20         | 1010  | 0.00975 | 0.00042 | 0.00840           | 0.195              | 196.89                   |
| 1040       | 45.17 | 0.43   | 20         | 1030  | 0.00952 | 0.00041 | 0.00820           | 0.190              | 196.1                    |
| 1060       | 44.77 | 0.36   | 20         | 1050  | 0.00804 | 0.00035 | 0.00693           | 0.16               | 168.86                   |

## Run#2000 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | C(t)    | E(t)    | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 1080       | 39.80  | 0.45   | 20         | 1070  | 0.01131 | 0.00049 | 0.00974           | 0.226            | 241.99                 |
| 1100       | 41.33  | 0.34   | 20         | 1090  | 0.00811 | 0.00035 | 0.00698           | 0.162            | 176.70                 |
| 1120       | 39.38  | 0.47   | 20         | 1110  | 0.01194 | 0.00051 | 0.01028           | 0.239            | 264.99                 |
| 1140       | 38.51  | 0.36   | 20         | 1130  | 0.00935 | 0.00040 | 0.00805           | 0.187            | 211.27                 |
| 1160       | 47.97  | 0.51   | 20         | 1150  | 0.01063 | 0.00046 | 0.00916           | 0.213            | 244.53                 |
| 1180       | 42.02  | 0.48   | 20         | 1170  | 0.01142 | 0.00049 | 0.00984           | 0.228            | 267.30                 |
| 1200       | 41.35  | 0.51   | 20         | 1190  | 0.01233 | 0.00053 | 0.01062           | 0.247            | 293.54                 |
| 1220       | 41.01  | 0.43   | 20         | 1210  | 0.01049 | 0.00045 | 0.00903           | 0.210            | 253.74                 |
| 1240       | 40.41  | 0.46   | 20         | 1230  | 0.01138 | 0.00049 | 0.00981           | 0.228            | 280.03                 |
| 1260       | 41.24  | 0.51   | 20         | 1250  | 0.01237 | 0.00053 | 0.01065           | 0.247            | 309.17                 |
| 1280       | 43.48  | 0.48   | 20         | 1270  | 0.01104 | 0.00048 | 0.00951           | 0.221            | 280.40                 |
| 1300       | 45.02  | 0.45   | 20         | 1290  | 0.01000 | 0.00043 | 0.00861           | 0.200            | 257.89                 |
| 1320       | 40.65  | 0.55   | 20         | 1310  | 0.01353 | 0.00058 | 0.01166           | 0.271            | 354.49                 |
| 1340       | 40.88  | 0.48   | 20         | 1330  | 0.01174 | 0.00051 | 0.01011           | 0.235            | 312.33                 |
| 1360       | 42.42  | 0.50   | 20         | 1350  | 0.01179 | 0.00051 | 0.01015           | 0.236            | 318.25                 |
| 1380       | 41.05  | 0.45   | 20         | 1370  | 0.01096 | 0.00047 | 0.00944           | 0.219            | 300.37                 |
| 1400       | 42.30  | 0.48   | 20         | 1390  | 0.01135 | 0.00049 | 0.00977           | 0.227            | 315.46                 |
| 1420       | 47.05  | 0.45   | 20         | 1410  | 0.00956 | 0.00041 | 0.00824           | 0.191            | 269.71                 |
| 1440       | 41.06  | 0.44   | 20         | 1430  | 0.01072 | 0.00046 | 0.00923           | 0.214            | 306.48                 |
| 1460       | 41.58  | 0.46   | 20         | 1450  | 0.01106 | 0.00048 | 0.00953           | 0.221            | 320.83                 |
| 1480       | 42.10  | 0.43   | 20         | 1470  | 0.01021 | 0.00044 | 0.00880           | 0.204            | 300.29                 |
| 1500       | 40.68  | 0.47   | 20         | 1490  | 0.01155 | 0.00050 | 0.00995           | 0.231            | 344.30                 |
| 1520       | 45.09  | 0.40   | 20         | 1510  | 0.00876 | 0.00038 | 0.00755           | 0.175            | 264.56                 |
| 1540       | 41.84  | 0.38   | 20         | 1530  | 0.00908 | 0.00039 | 0.00782           | 0.182            | 277.92                 |
| 1560       | 39.46  | 0.46   | 20         | 1550  | 0.01166 | 0.00050 | 0.01004           | 0.233            | 361.38                 |
| 1590       | 60.65  | 0.55   | 30         | 1575  | 0.00907 | 0.00039 | 0.01172           | 0.272            | 428.48                 |
| 1620       | 62.09  | 0.60   | 30         | 1605  | 0.00966 | 0.00042 | 0.01249           | 0.290            | 465.29                 |
| 1650       | 66.42  | 0.64   | 30         | 1635  | 0.00964 | 0.00042 | 0.01245           | 0.289            | 472.63                 |
| 1680       | 58.83  | 0.58   | 30         | 1665  | 0.00986 | 0.00042 | 0.01274           | 0.296            | 492.45                 |
| 1710       | 60.36  | 0.45   | 30         | 1695  | 0.00746 | 0.00032 | 0.00963           | 0.224            | 379.10                 |
| 1740       | 59.87  | 0.57   | 30         | 1725  | 0.00952 | 0.00041 | 0.01230           | 0.286            | 492.69                 |
| 1770       | 65.98  | 0.64   | 30         | 1755  | 0.00970 | 0.00042 | 0.01253           | 0.291            | 510.70                 |
| 1800       | 59.28  | 0.50   | 30         | 1785  | 0.00843 | 0.00036 | 0.01090           | 0.253            | 451.67                 |
| 1830       | 58.96  | 0.40   | 30         | 1815  | 0.00678 | 0.00029 | 0.00877           | 0.204            | 369.40                 |
| 1860       | 63.25  | 0.65   | 30         | 1845  | 0.01028 | 0.00044 | 0.01328           | 0.308            | 568.81                 |
| 1890       | 60.03  | 0.52   | 30         | 1875  | 0.00858 | 0.00037 | 0.01109           | 0.257            | 482.57                 |
| 1920       | 57.01  | 0.51   | 30         | 1905  | 0.00895 | 0.00039 | 0.01156           | 0.268            | 511.25                 |
| 1950       | 58.83  | 0.52   | 30         | 1935  | 0.00884 | 0.00038 | 0.01142           | 0.265            | 513.11                 |
| 1980       | 59.33  | 0.44   | 30         | 1965  | 0.00742 | 0.00032 | 0.00958           | 0.222            | 437.18                 |
| 2040       | 120.66 | 0.97   | 60         | 2010  | 0.00804 | 0.00035 | 0.02078           | 0.482            | 969.52                 |
| 2100       | 120.58 | 0.98   | 60         | 2070  | 0.00813 | 0.00035 | 0.02100           | 0.488            | 1009.42                |
| 2160       | 121.00 | 0.80   | 60         | 2130  | 0.00661 | 0.00028 | 0.01709           | 0.397            | 844.96                 |
| 2220       | 118.77 | 0.84   | 60         | 2190  | 0.00707 | 0.00030 | 0.01828           | 0.424            | 929.33                 |
| 2280       | 126.39 | 0.89   | 60         | 2250  | 0.00704 | 0.00030 | 0.01820           | 0.423            | 950.63                 |
| 2340       | 121.80 | 0.72   | 60         | 2310  | 0.00591 | 0.00025 | 0.01528           | 0.355            | 819.31                 |
| 2460       | 252.18 | 1.32   | 120        | 2400  | 0.00523 | 0.00023 | 0.02705           | 0.628            | 1507.49                |
| 2520       | 128.65 | 0.68   | 60         | 2490  | 0.00529 | 0.00023 | 0.01366           | 0.317            | 789.68                 |
| 2580       | 125.96 | 0.67   | 60         | 2550  | 0.00532 | 0.00023 | 0.01375           | 0.319            | 813.83                 |
| 2640       | 127.45 | 0.70   | 60         | 2610  | 0.00549 | 0.00024 | 0.01419           | 0.330            | 860.10                 |
| 2700       | 124.69 | 0.70   | 60         | 2670  | 0.00561 | 0.00024 | 0.01451           | 0.337            | 899.35                 |
| 2747       | 99.59  | 0.42   | 47         | 2724  | 0.00422 | 0.00018 | 0.00854           | 0.198            | 539.83                 |
| 2807       | 125.24 | 0.53   | 60         | 2777  | 0.00423 | 0.00018 | 0.01094           | 0.254            | 705.11                 |
| 2867       | 130.36 | 0.68   | 60         | 2837  | 0.00522 | 0.00022 | 0.01348           | 0.313            | 887.92                 |
| 2927       | 137.15 | 0.54   | 60         | 2897  | 0.00394 | 0.00017 | 0.01017           | 0.236            | 684.38                 |
| 2987       | 136.70 | 0.61   | 60         | 2957  | 0.00446 | 0.00019 | 0.01153           | 0.268            | 791.71                 |
| 3047       | 121.82 | 0.38   | 60         | 3017  | 0.00312 | 0.00013 | 0.00806           | 0.187            | 564.67                 |
| 3107       | 135.20 | 0.40   | 60         | 3077  | 0.00292 | 0.00013 | 0.00755           | 0.175            | 539.39                 |
| 3167       | 129.83 | 0.49   | 60         | 3137  | 0.00377 | 0.00016 | 0.00975           | 0.226            | 710.37                 |
| 3227       | 135.62 | 0.32   | 60         | 3197  | 0.00236 | 0.00010 | 0.00610           | 0.142            | 452.61                 |
| 3287       | 130.90 | 0.36   | 60         | 3257  | 0.00275 | 0.00012 | 0.00711           | 0.165            | 537.44                 |
| 3347       | 137.78 | 0.41   | 60         | 3317  | 0.00298 | 0.00013 | 0.00769           | 0.179            | 592.24                 |
| 3407       | 130.55 | 0.36   | 60         | 3377  | 0.00276 | 0.00012 | 0.00713           | 0.165            | 558.74                 |
| 3467       | 135.66 | 0.38   | 60         | 3437  | 0.00280 | 0.00012 | 0.00724           | 0.168            | 577.65                 |
| 3527       | 128.70 | 0.22   | 60         | 3497  | 0.00171 | 0.00007 | 0.00442           | 0.103            | 358.67                 |

**Run#2000 ( Cont..)**

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|--------------------|--------------------------|
| 3587       | 136.52 | 0.28   | 60         | 3557  | 0.00205 | 0.00009 | 0.00530           | 0.123              | 437.72                   |
| 3647       | 128.17 | 0.20   | 60         | 3617  | 0.00156 | 0.00007 | 0.00403           | 0.094              | 338.64                   |
| 3707       | 130.73 | 0.26   | 60         | 3677  | 0.00199 | 0.00009 | 0.00514           | 0.119              | 438.78                   |
| 3767       | 126.54 | 0.20   | 60         | 3737  | 0.00158 | 0.00007 | 0.00408           | 0.095              | 354.39                   |
| 3827       | 136.97 | 0.18   | 60         | 3797  | 0.00131 | 0.00006 | 0.00340           | 0.079              | 299.39                   |
| 3887       | 127.25 | 0.20   | 60         | 3857  | 0.00157 | 0.00007 | 0.00406           | 0.094              | 363.72                   |
| 3947       | 135.81 | 0.18   | 60         | 3917  | 0.00133 | 0.00006 | 0.00343           | 0.080              | 311.49                   |
| 4007       | 125.09 | 0.14   | 60         | 3977  | 0.00112 | 0.00005 | 0.00289           | 0.067              | 267.06                   |
| 4067       | 131.30 | 0.09   | 60         | 4037  | 0.00069 | 0.00003 | 0.00177           | 0.041              | 166.03                   |
| 4127       | 121.37 | 0.10   | 60         | 4097  | 0.00082 | 0.00004 | 0.00213           | 0.049              | 202.54                   |
| 4187       | 125.28 | 0.16   | 60         | 4157  | 0.00128 | 0.00006 | 0.00330           | 0.077              | 318.54                   |

$$\Sigma E(t)\Delta t_i = 0.9600$$

|                                     |
|-------------------------------------|
| <b>So = 2.11 g/s</b>                |
| <b>Bed weight = 3785 g</b>          |
| <b><math>\tau = 1794</math> sec</b> |

|                                         |                                                         |
|-----------------------------------------|---------------------------------------------------------|
| <b><math>\tau_{obs} = 1793.6</math></b> | <b><math>\Sigma C_i t_i \Delta t_i = 39829.8</math></b> |
|                                         | <b><math>\Sigma C_i \Delta t_i = 22.21</math></b>       |

Table D.16 Data Run#2001

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t_i)$ | $E(t_i)$ | $\Delta t * E(t_i)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|-------|--------|------------|-------|----------|----------|---------------------|--------------------|--------------------------|
| 0          | 20.70 | 0.00   | 10         | 0     | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 10         | 20.70 | 0.00   | 10         | 5     | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 20         | 20.70 | 0.00   | 10         | 15    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 30         | 20.70 | 0.00   | 10         | 25    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 40         | 20.70 | 0.00   | 10         | 35    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 50         | 20.70 | 0.00   | 10         | 45    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 60         | 20.70 | 0.00   | 10         | 55    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 70         | 20.70 | 0.00   | 10         | 65    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 80         | 20.70 | 0.00   | 10         | 75    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 90         | 20.70 | 0.00   | 10         | 85    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 100        | 20.70 | 0.00   | 10         | 95    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 110        | 20.70 | 0.00   | 10         | 105   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 120        | 20.70 | 0.00   | 10         | 115   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 130        | 20.70 | 0.00   | 10         | 125   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 140        | 20.70 | 0.00   | 10         | 135   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 150        | 20.70 | 0.00   | 10         | 145   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 160        | 20.70 | 0.00   | 10         | 155   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 170        | 20.70 | 0.00   | 10         | 165   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 180        | 20.70 | 0.00   | 10         | 175   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 190        | 22.74 | 0.00   | 10         | 185   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 200        | 17.06 | 0.00   | 10         | 195   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 210        | 23.73 | 0.00   | 10         | 205   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 220        | 17.72 | 0.02   | 10         | 215   | 0.0011   | 0.00005  | 0.00047             | 0.01               | 2.43                     |
| 230        | 24.14 | 0.09   | 10         | 225   | 0.00373  | 0.00015  | 0.00154             | 0.037              | 8.39                     |
| 240        | 17.46 | 0.07   | 10         | 235   | 0.00401  | 0.00017  | 0.00166             | 0.040              | 9.42                     |
| 260        | 40.38 | 0.15   | 20         | 250   | 0.00371  | 0.00015  | 0.00307             | 0.074              | 18.57                    |
| 280        | 46.08 | 0.19   | 20         | 270   | 0.00412  | 0.00017  | 0.00341             | 0.082              | 22.27                    |
| 300        | 41.02 | 0.34   | 20         | 290   | 0.00829  | 0.00034  | 0.00686             | 0.166              | 48.07                    |
| 320        | 40.38 | 0.22   | 20         | 310   | 0.00545  | 0.00023  | 0.00451             | 0.109              | 33.78                    |
| 340        | 40.61 | 0.37   | 20         | 330   | 0.0091   | 0.00038  | 0.00754             | 0.182              | 60.13                    |
| 360        | 42.08 | 0.46   | 20         | 350   | 0.01093  | 0.00045  | 0.00904             | 0.219              | 76.52                    |
| 380        | 40.54 | 0.45   | 20         | 370   | 0.0111   | 0.00046  | 0.00918             | 0.222              | 82.14                    |
| 400        | 40.45 | 0.51   | 20         | 390   | 0.01248  | 0.00052  | 0.01033             | 0.250              | 97.38                    |
| 420        | 41.54 | 0.49   | 20         | 410   | 0.0118   | 0.00049  | 0.00976             | 0.236              | 96.74                    |
| 440        | 46.47 | 0.46   | 20         | 430   | 0.00990  | 0.00041  | 0.00819             | 0.198              | 85.13                    |
| 460        | 40.60 | 0.46   | 20         | 450   | 0.0113   | 0.00047  | 0.00937             | 0.227              | 101.9                    |
| 480        | 40.82 | 0.49   | 20         | 470   | 0.01200  | 0.00050  | 0.00993             | 0.240              | 112.8                    |
| 500        | 41.96 | 0.43   | 20         | 490   | 0.01025  | 0.00042  | 0.00848             | 0.205              | 100.44                   |
| 520        | 41.08 | 0.42   | 20         | 510   | 0.01022  | 0.00042  | 0.00846             | 0.204              | 104.28                   |
| 540        | 40.69 | 0.63   | 20         | 530   | 0.01536  | 0.00064  | 0.0127              | 0.307              | 162.82                   |
| 560        | 39.78 | 0.55   | 20         | 550   | 0.01383  | 0.00057  | 0.0114              | 0.277              | 152.09                   |
| 580        | 41.0  | 0.47   | 20         | 570   | 0.0114   | 0.00047  | 0.00948             | 0.229              | 130.65                   |
| 600        | 41.54 | 0.50   | 20         | 590   | 0.01204  | 0.00050  | 0.00996             | 0.241              | 142.03                   |
| 620        | 46.20 | 0.54   | 20         | 610   | 0.0116   | 0.00048  | 0.00967             | 0.234              | 142.6                    |
| 640        | 40.59 | 0.58   | 20         | 630   | 0.01429  | 0.00059  | 0.0118              | 0.286              | 180.04                   |
| 660        | 42.47 | 0.56   | 20         | 650   | 0.0131   | 0.00055  | 0.0109              | 0.264              | 171.4                    |
| 680        | 41.70 | 0.50   | 20         | 670   | 0.0119   | 0.00050  | 0.00992             | 0.240              | 160.67                   |
| 700        | 40.51 | 0.58   | 20         | 690   | 0.0141   | 0.00059  | 0.0117              | 0.284              | 195.88                   |
| 720        | 41.0  | 0.64   | 20         | 710   | 0.0156   | 0.00065  | 0.0129              | 0.312              | 221.60                   |
| 740        | 39.95 | 0.57   | 20         | 730   | 0.01427  | 0.00059  | 0.0118              | 0.285              | 208.31                   |
| 760        | 41.68 | 0.56   | 20         | 750   | 0.01344  | 0.00056  | 0.0111              | 0.269              | 201.54                   |
| 780        | 43.05 | 0.68   | 20         | 770   | 0.01580  | 0.00065  | 0.01307             | 0.316              | 243.25                   |
| 800        | 46.60 | 0.66   | 20         | 790   | 0.0141   | 0.00059  | 0.0117              | 0.283              | 223.78                   |
| 820        | 41.39 | 0.59   | 20         | 810   | 0.01425  | 0.00059  | 0.0117              | 0.285              | 230.93                   |
| 840        | 40.10 | 0.51   | 20         | 830   | 0.01272  | 0.00053  | 0.01052             | 0.254              | 211.1                    |
| 860        | 41.25 | 0.63   | 20         | 850   | 0.01527  | 0.00063  | 0.01264             | 0.305              | 259.67                   |
| 880        | 37.77 | 0.54   | 20         | 870   | 0.01430  | 0.00059  | 0.0118              | 0.286              | 248.77                   |
| 900        | 40.62 | 0.61   | 20         | 890   | 0.01502  | 0.00062  | 0.01242             | 0.300              | 267.31                   |
| 920        | 40.01 | 0.54   | 20         | 910   | 0.01350  | 0.00056  | 0.0111              | 0.270              | 245.64                   |
| 940        | 46.41 | 0.60   | 20         | 930   | 0.01293  | 0.00053  | 0.01070             | 0.259              | 240.47                   |
| 960        | 40.78 | 0.61   | 20         | 950   | 0.01496  | 0.00062  | 0.01238             | 0.299              | 284.21                   |
| 980        | 40.60 | 0.48   | 20         | 970   | 0.0118   | 0.00049  | 0.00978             | 0.236              | 229.36                   |
| 1000       | 40.58 | 0.46   | 20         | 990   | 0.0113   | 0.00047  | 0.00938             | 0.227              | 224.45                   |
| 1020       | 41.29 | 0.57   | 20         | 1010  | 0.01380  | 0.00057  | 0.0114              | 0.276              | 278.86                   |
| 1040       | 41.25 | 0.56   | 20         | 1030  | 0.01358  | 0.00056  | 0.0112              | 0.272              | 279.66                   |
| 1060       | 42.02 | 0.53   | 20         | 1050  | 0.0126   | 0.00052  | 0.01044             | 0.252              | 264.87                   |
| 1080       | 40.69 | 0.52   | 20         | 1070  | 0.01278  | 0.00053  | 0.01057             | 0.256              | 273.48                   |
| 110        | 43.75 | 0.63   | 20         | 1090  | 0.01440  | 0.00060  | 0.0119              | 0.288              | 313.92                   |



## Run#2001 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | C(t)    | E(t)    | $\Delta t * E(t)$ | Ci * $\Delta t$ | Ci * $t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|-----------------|-----------------------|
| 1120       | 46.61  | 0.56   | 20         | 1110  | 0.01201 | 0.00050 | 0.00994           | 0.240           | 266.72                |
| 1140       | 41.06  | 0.45   | 20         | 1130  | 0.01096 | 0.00045 | 0.00907           | 0.219           | 247.69                |
| 1160       | 40.86  | 0.57   | 20         | 1150  | 0.01395 | 0.00058 | 0.01154           | 0.279           | 320.85                |
| 1180       | 40.31  | 0.49   | 20         | 1170  | 0.01203 | 0.00050 | 0.00995           | 0.241           | 281.54                |
| 1200       | 41.48  | 0.54   | 20         | 1190  | 0.01302 | 0.00054 | 0.01077           | 0.260           | 309.84                |
| 1220       | 41.84  | 0.51   | 20         | 1210  | 0.01219 | 0.00050 | 0.01008           | 0.244           | 294.98                |
| 1240       | 41.34  | 0.47   | 20         | 1230  | 0.01137 | 0.00047 | 0.00941           | 0.227           | 279.68                |
| 1260       | 41.85  | 0.66   | 20         | 1250  | 0.01577 | 0.00065 | 0.01305           | 0.315           | 394.27                |
| 1280       | 46.62  | 0.53   | 20         | 1270  | 0.01137 | 0.00047 | 0.00941           | 0.227           | 288.76                |
| 1300       | 41.35  | 0.49   | 20         | 1290  | 0.01185 | 0.00049 | 0.00980           | 0.237           | 305.73                |
| 1320       | 41.89  | 0.41   | 20         | 1310  | 0.00979 | 0.00040 | 0.00810           | 0.196           | 256.43                |
| 1340       | 41.03  | 0.43   | 20         | 1330  | 0.01048 | 0.00043 | 0.00867           | 0.210           | 278.77                |
| 1360       | 40.95  | 0.49   | 20         | 1350  | 0.01197 | 0.00049 | 0.00990           | 0.239           | 323.08                |
| 1380       | 40.97  | 0.42   | 20         | 1370  | 0.01025 | 0.00042 | 0.00848           | 0.205           | 280.89                |
| 1400       | 41.27  | 0.51   | 20         | 1390  | 0.01236 | 0.00051 | 0.01022           | 0.247           | 343.54                |
| 1420       | 43.87  | 0.45   | 20         | 1410  | 0.01026 | 0.00042 | 0.00849           | 0.205           | 289.26                |
| 1440       | 45.07  | 0.37   | 20         | 1430  | 0.00821 | 0.00034 | 0.00679           | 0.164           | 234.79                |
| 1460       | 40.68  | 0.35   | 20         | 1450  | 0.00860 | 0.00036 | 0.00712           | 0.172           | 249.51                |
| 1480       | 40.81  | 0.39   | 20         | 1470  | 0.00956 | 0.00040 | 0.00791           | 0.191           | 280.96                |
| 1500       | 42.49  | 0.47   | 20         | 1490  | 0.01106 | 0.00046 | 0.00915           | 0.221           | 329.67                |
| 1530       | 63.06  | 0.60   | 30         | 1515  | 0.00951 | 0.00039 | 0.01181           | 0.285           | 432.45                |
| 1560       | 58.17  | 0.54   | 30         | 1545  | 0.00928 | 0.00038 | 0.01152           | 0.278           | 430.27                |
| 1590       | 63.85  | 0.48   | 30         | 1575  | 0.00752 | 0.00031 | 0.00933           | 0.226           | 355.21                |
| 1620       | 63.71  | 0.62   | 30         | 1605  | 0.00973 | 0.00040 | 0.01208           | 0.292           | 468.58                |
| 1650       | 62.04  | 0.53   | 30         | 1635  | 0.00854 | 0.00035 | 0.01060           | 0.256           | 419.03                |
| 1680       | 58.59  | 0.42   | 30         | 1665  | 0.00717 | 0.00030 | 0.00890           | 0.215           | 358.06                |
| 1710       | 64.63  | 0.57   | 30         | 1695  | 0.00882 | 0.00036 | 0.01094           | 0.265           | 448.47                |
| 1740       | 64.32  | 0.41   | 30         | 1725  | 0.00630 | 0.00026 | 0.00781           | 0.189           | 325.85                |
| 1770       | 58.83  | 0.52   | 30         | 1755  | 0.00884 | 0.00037 | 0.01097           | 0.265           | 465.37                |
| 1800       | 61.26  | 0.42   | 30         | 1785  | 0.00686 | 0.00028 | 0.00851           | 0.206           | 367.14                |
| 1830       | 64.80  | 0.47   | 30         | 1815  | 0.00725 | 0.00030 | 0.00900           | 0.218           | 394.93                |
| 1860       | 57.47  | 0.35   | 30         | 1845  | 0.00609 | 0.00025 | 0.00756           | 0.183           | 337.09                |
| 1890       | 64.20  | 0.49   | 30         | 1875  | 0.00763 | 0.00032 | 0.00947           | 0.229           | 429.32                |
| 1920       | 64.65  | 0.45   | 30         | 1905  | 0.00696 | 0.00029 | 0.00864           | 0.209           | 397.80                |
| 1950       | 59.60  | 0.37   | 30         | 1935  | 0.00621 | 0.00026 | 0.00770           | 0.186           | 360.38                |
| 1980       | 65.38  | 0.41   | 30         | 1965  | 0.00627 | 0.00026 | 0.00778           | 0.188           | 369.68                |
| 2040       | 123.67 | 0.70   | 60         | 2010  | 0.00562 | 0.00023 | 0.01395           | 0.337           | 677.75                |
| 2100       | 131.22 | 0.68   | 60         | 2070  | 0.00518 | 0.00021 | 0.01286           | 0.311           | 643.62                |
| 2160       | 125.53 | 0.60   | 60         | 2130  | 0.00478 | 0.00020 | 0.01186           | 0.287           | 610.85                |
| 2220       | 130.35 | 0.57   | 60         | 2190  | 0.00437 | 0.00018 | 0.01085           | 0.262           | 574.59                |
| 2280       | 123.78 | 0.52   | 60         | 2250  | 0.00420 | 0.00017 | 0.01043           | 0.252           | 567.14                |
| 2340       | 123.29 | 0.49   | 60         | 2310  | 0.00397 | 0.00016 | 0.00986           | 0.238           | 550.85                |
| 2400       | 128.54 | 0.44   | 60         | 2370  | 0.00342 | 0.00014 | 0.00850           | 0.205           | 486.76                |
| 2460       | 124.43 | 0.41   | 60         | 2430  | 0.00330 | 0.00014 | 0.00818           | 0.198           | 480.41                |
| 2520       | 122.57 | 0.43   | 60         | 2490  | 0.00351 | 0.00015 | 0.00871           | 0.210           | 524.12                |
| 2580       | 130.08 | 0.29   | 60         | 2550  | 0.00223 | 0.00009 | 0.00553           | 0.134           | 341.10                |
| 2640       | 124.92 | 0.29   | 60         | 2610  | 0.00232 | 0.00010 | 0.00576           | 0.139           | 363.54                |
| 2700       | 126.94 | 0.35   | 60         | 2670  | 0.00276 | 0.00011 | 0.00684           | 0.165           | 441.70                |
| 2760       | 125.87 | 0.30   | 60         | 2730  | 0.00238 | 0.00010 | 0.00592           | 0.143           | 390.40                |
| 2820       | 125.27 | 0.29   | 60         | 2790  | 0.00231 | 0.00010 | 0.00575           | 0.139           | 387.53                |
| 2880       | 133.34 | 0.29   | 60         | 2850  | 0.00217 | 0.00009 | 0.00540           | 0.130           | 371.91                |
| 2940       | 125.50 | 0.21   | 60         | 2910  | 0.00167 | 0.00007 | 0.00415           | 0.100           | 292.16                |
| 3000       | 125.59 | 0.17   | 60         | 2970  | 0.00131 | 0.00005 | 0.00326           | 0.079           | 234.12                |
| 3060       | 131.33 | 0.18   | 60         | 3030  | 0.00137 | 0.00006 | 0.00340           | 0.082           | 249.17                |
| 3120       | 122.09 | 0.15   | 60         | 3090  | 0.00123 | 0.00005 | 0.00305           | 0.074           | 227.78                |
| 3180       | 132.98 | 0.16   | 60         | 3150  | 0.00120 | 0.00005 | 0.00299           | 0.072           | 227.40                |
| 3240       | 125.81 | 0.10   | 60         | 3210  | 0.00079 | 0.00003 | 0.00197           | 0.048           | 153.09                |
| 3300       | 123.33 | 0.14   | 60         | 3270  | 0.00109 | 0.00005 | 0.00272           | 0.066           | 214.77                |
| 3360       | 129.85 | 0.13   | 60         | 3330  | 0.00100 | 0.00004 | 0.00248           | 0.060           | 200.03                |
| 3420       | 122.37 | 0.16   | 60         | 3390  | 0.00131 | 0.00005 | 0.00325           | 0.078           | 265.95                |
| 3480       | 125.54 | 0.12   | 60         | 3450  | 0.00096 | 0.00004 | 0.00237           | 0.057           | 197.87                |
| 3540       | 131.32 | 0.12   | 60         | 3510  | 0.00091 | 0.00004 | 0.00227           | 0.055           | 192.45                |
| 3600       | 125.09 | 0.08   | 60         | 3570  | 0.00060 | 0.00002 | 0.00149           | 0.036           | 128.43                |
| 3660       | 129.23 | 0.08   | 60         | 3630  | 0.00062 | 0.00003 | 0.00154           | 0.037           | 134.83                |

## Run#2001 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 3720       | 124.75 | 0.05   | 60         | 3690  | 0.00040 | 0.00002 | 0.00099           | 0.024            | 88.74                  |
| 3780       | 123.28 | 0.07   | 60         | 3750  | 0.00057 | 0.00002 | 0.00141           | 0.034            | 127.76                 |
| 3840       | 128.06 | 0.09   | 60         | 3810  | 0.00070 | 0.00003 | 0.00174           | 0.042            | 160.66                 |
| 3900       | 125.29 | 0.07   | 60         | 3870  | 0.00056 | 0.00002 | 0.00139           | 0.034            | 129.73                 |
| 3954       | 129.26 | 0.05   | 54         | 3927  | 0.00039 | 0.00002 | 0.00086           | 0.021            | 82.03                  |

$$\Sigma E(t) \Delta t_i = 0.9600$$

|                     |
|---------------------|
| $S_o = 2.068$ g/s   |
| Bed weight = 3068 g |
| $\tau = 1483.3$ sec |

|                     |                                       |
|---------------------|---------------------------------------|
| $\tau_{obs} = 1323$ | $\Sigma C_i t_i \Delta t_i = 30402.5$ |
|                     | $\Sigma C_i \Delta t_i = 22.98$       |

Table D.17 Data Run#2002

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t_i)$ | $E(t_i)$ | $\Delta t * E(t_i)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|-------|--------|------------|-------|----------|----------|---------------------|--------------------|--------------------------|
| 0          | 18.90 | 0.00   | 10         | 0     | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 10         | 18.90 | 0.00   | 10         | 5     | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 20         | 18.90 | 0.00   | 10         | 15    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 30         | 18.90 | 0.00   | 10         | 25    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 40         | 18.90 | 0.00   | 10         | 35    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 50         | 18.90 | 0.00   | 10         | 45    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 60         | 18.90 | 0.00   | 10         | 55    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 70         | 18.90 | 0.00   | 10         | 65    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 80         | 18.90 | 0.00   | 10         | 75    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 90         | 18.90 | 0.00   | 10         | 85    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 100        | 18.90 | 0.00   | 10         | 95    | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 110        | 18.90 | 0.00   | 10         | 105   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 120        | 18.90 | 0.00   | 10         | 115   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 130        | 18.90 | 0.00   | 10         | 125   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 140        | 18.90 | 0.00   | 10         | 135   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 150        | 18.90 | 0.00   | 10         | 145   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 160        | 18.90 | 0.00   | 10         | 155   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 170        | 18.90 | 0.00   | 10         | 165   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 180        | 18.90 | 0.00   | 10         | 175   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 190        | 18.90 | 0.00   | 10         | 185   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 200        | 18.90 | 0.00   | 10         | 195   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 210        | 17.1  | 0.00   | 10         | 205   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 220        | 23.12 | 0.00   | 10         | 215   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 230        | 16.90 | 0.00   | 10         | 225   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 240        | 17.74 | 0.00   | 10         | 235   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 250        | 22.53 | 0.00   | 10         | 245   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 260        | 16.94 | 0.00   | 10         | 255   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 270        | 17.53 | 0.00   | 10         | 265   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 280        | 22.56 | 0.00   | 10         | 275   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 290        | 17.29 | 0.00   | 10         | 285   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 300        | 16.94 | 0.00   | 10         | 295   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 310        | 23.82 | 0.00   | 10         | 305   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 320        | 16.82 | 0.00   | 10         | 315   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 330        | 21.32 | 0.01   | 10         | 325   | 0.00047  | 0.00002  | 0.00021             | 0.005              | 1.52                     |
| 340        | 19.47 | 0.00   | 10         | 335   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 350        | 17.1  | 0.00   | 10         | 345   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 360        | 23.12 | 0.01   | 10         | 355   | 0.00043  | 0.00002  | 0.00020             | 0.004              | 1.54                     |
| 370        | 17.27 | 0.00   | 10         | 365   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 380        | 17.55 | 0.01   | 10         | 375   | 0.00057  | 0.00002  | 0.00026             | 0.006              | 2.14                     |
| 390        | 23.75 | 0.01   | 10         | 385   | 0.00042  | 0.00002  | 0.00019             | 0.004              | 1.62                     |
| 400        | 16.42 | 0.01   | 10         | 395   | 0.00061  | 0.00002  | 0.00027             | 0.006              | 2.41                     |
| 410        | 13.95 | 0.00   | 10         | 405   | 0.00000  | 0.00000  | 0.00000             | 0.000              | 0.00                     |
| 420        | 21.46 | 0.02   | 10         | 415   | 0.00093  | 0.00004  | 0.00042             | 0.009              | 3.87                     |
| 430        | 17.23 | 0.02   | 10         | 425   | 0.0011   | 0.00004  | 0.00052             | 0.012              | 4.93                     |
| 440        | 17.78 | 0.03   | 10         | 435   | 0.00169  | 0.00006  | 0.00076             | 0.017              | 7.34                     |
| 450        | 22.64 | 0.03   | 10         | 445   | 0.00133  | 0.00005  | 0.00060             | 0.013              | 5.90                     |
| 460        | 17.49 | 0.03   | 10         | 455   | 0.00172  | 0.00006  | 0.00077             | 0.017              | 7.80                     |
| 470        | 17.1  | 0.03   | 10         | 465   | 0.00175  | 0.00007  | 0.00079             | 0.017              | 8.14                     |
| 480        | 22.93 | 0.01   | 10         | 475   | 0.00044  | 0.00002  | 0.00020             | 0.004              | 2.07                     |
| 490        | 16.24 | 0.03   | 10         | 485   | 0.00185  | 0.00007  | 0.00083             | 0.018              | 8.96                     |
| 500        | 23.44 | 0.02   | 10         | 495   | 0.00085  | 0.00003  | 0.00039             | 0.009              | 4.22                     |
| 510        | 17.30 | 0.04   | 10         | 505   | 0.00231  | 0.00009  | 0.00104             | 0.023              | 11.6                     |
| 520        | 17.03 | 0.02   | 10         | 515   | 0.0011   | 0.00004  | 0.00053             | 0.012              | 6.05                     |
| 530        | 22.36 | 0.06   | 10         | 525   | 0.00268  | 0.00010  | 0.0012              | 0.027              | 14.09                    |
| 540        | 17.9  | 0.04   | 10         | 535   | 0.00223  | 0.00008  | 0.0010              | 0.022              | 11.9                     |
| 550        | 17.06 | 0.04   | 10         | 545   | 0.00234  | 0.00009  | 0.00106             | 0.023              | 12.78                    |
| 560        | 22.83 | 0.04   | 10         | 555   | 0.00175  | 0.00007  | 0.00079             | 0.018              | 9.72                     |
| 570        | 17.1  | 0.04   | 10         | 565   | 0.00234  | 0.00009  | 0.00105             | 0.023              | 13.1                     |
| 580        | 16.77 | 0.03   | 10         | 575   | 0.00179  | 0.00007  | 0.00081             | 0.018              | 10.29                    |
| 590        | 22.57 | 0.13   | 10         | 585   | 0.00576  | 0.00022  | 0.00260             | 0.058              | 33.70                    |
| 600        | 17.06 | 0.05   | 10         | 595   | 0.00293  | 0.0001   | 0.00132             | 0.029              | 17.44                    |
| 610        | 16.95 | 0.07   | 10         | 605   | 0.00413  | 0.00016  | 0.00186             | 0.041              | 24.99                    |
| 620        | 22.48 | 0.05   | 10         | 615   | 0.00222  | 0.00008  | 0.00100             | 0.022              | 13.68                    |
| 630        | 17.59 | 0.04   | 10         | 625   | 0.00227  | 0.00009  | 0.00103             | 0.023              | 14.2                     |
| 640        | 22.60 | 0.08   | 10         | 635   | 0.00354  | 0.00013  | 0.00160             | 0.035              | 22.48                    |
| 650        | 16.8  | 0.07   | 10         | 645   | 0.00416  | 0.00016  | 0.00188             | 0.042              | 26.86                    |
| 660        | 16.9  | 0.05   | 10         | 655   | 0.00296  | 0.0001   | 0.00133             | 0.030              | 19.37                    |
| 670        | 22.30 | 0.08   | 10         | 665   | 0.00359  | 0.00014  | 0.00162             | 0.036              | 23.86                    |

## Run#2002 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | C(t)    | E(t)    | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 680        | 17.59  | 0.05   | 10         | 675   | 0.00284 | 0.00011 | 0.00128           | 0.028            | 19.19                  |
| 690        | 17.26  | 0.09   | 10         | 685   | 0.00521 | 0.00020 | 0.00235           | 0.052            | 35.72                  |
| 700        | 22.56  | 0.07   | 10         | 695   | 0.00310 | 0.00012 | 0.00140           | 0.031            | 21.56                  |
| 710        | 16.10  | 0.09   | 10         | 705   | 0.00559 | 0.00021 | 0.00252           | 0.056            | 39.41                  |
| 720        | 17.39  | 0.08   | 10         | 715   | 0.00460 | 0.00017 | 0.00208           | 0.046            | 32.89                  |
| 730        | 22.35  | 0.08   | 10         | 725   | 0.00358 | 0.00014 | 0.00162           | 0.036            | 25.95                  |
| 740        | 16.51  | 0.05   | 10         | 735   | 0.00303 | 0.00011 | 0.00137           | 0.030            | 22.27                  |
| 750        | 16.98  | 0.05   | 10         | 745   | 0.00294 | 0.00011 | 0.00133           | 0.029            | 21.94                  |
| 760        | 22.09  | 0.09   | 10         | 755   | 0.00407 | 0.00015 | 0.00184           | 0.041            | 30.76                  |
| 770        | 16.75  | 0.07   | 10         | 765   | 0.00418 | 0.00016 | 0.00189           | 0.042            | 31.97                  |
| 780        | 17.34  | 0.06   | 10         | 775   | 0.00346 | 0.00013 | 0.00156           | 0.035            | 26.82                  |
| 800        | 39.02  | 0.23   | 20         | 790   | 0.00589 | 0.00022 | 0.00532           | 0.118            | 93.13                  |
| 820        | 38.47  | 0.13   | 20         | 810   | 0.00325 | 0.00012 | 0.00293           | 0.065            | 52.64                  |
| 840        | 38.34  | 0.15   | 20         | 830   | 0.00391 | 0.00015 | 0.00353           | 0.078            | 64.95                  |
| 860        | 33.59  | 0.15   | 20         | 850   | 0.00447 | 0.00017 | 0.00403           | 0.089            | 75.92                  |
| 880        | 39.55  | 0.18   | 20         | 870   | 0.00455 | 0.00017 | 0.00411           | 0.091            | 79.19                  |
| 900        | 39.97  | 0.21   | 20         | 890   | 0.00525 | 0.00020 | 0.00474           | 0.105            | 93.53                  |
| 920        | 33.60  | 0.14   | 20         | 910   | 0.00417 | 0.00016 | 0.00376           | 0.083            | 75.83                  |
| 940        | 39.39  | 0.20   | 20         | 930   | 0.00508 | 0.00019 | 0.00458           | 0.102            | 94.45                  |
| 960        | 39.63  | 0.21   | 20         | 950   | 0.00530 | 0.00020 | 0.00478           | 0.106            | 100.69                 |
| 980        | 39.01  | 0.25   | 20         | 970   | 0.00641 | 0.00024 | 0.00578           | 0.128            | 124.33                 |
| 1000       | 33.88  | 0.23   | 20         | 990   | 0.00664 | 0.00025 | 0.00599           | 0.133            | 131.49                 |
| 1020       | 40.48  | 0.20   | 20         | 1010  | 0.00494 | 0.00019 | 0.00446           | 0.099            | 99.80                  |
| 1040       | 39.82  | 0.30   | 20         | 1030  | 0.00753 | 0.00028 | 0.00680           | 0.151            | 155.22                 |
| 1060       | 33.86  | 0.29   | 20         | 1050  | 0.00842 | 0.00032 | 0.00760           | 0.168            | 176.76                 |
| 1080       | 39.52  | 0.24   | 20         | 1070  | 0.00607 | 0.00023 | 0.00548           | 0.121            | 129.96                 |
| 1100       | 40.08  | 0.25   | 20         | 1090  | 0.00624 | 0.00024 | 0.00563           | 0.125            | 135.98                 |
| 1120       | 39.55  | 0.28   | 20         | 1110  | 0.00708 | 0.00027 | 0.00639           | 0.142            | 157.17                 |
| 1140       | 33.71  | 0.26   | 20         | 1130  | 0.00771 | 0.00029 | 0.00696           | 0.154            | 174.31                 |
| 1160       | 39.66  | 0.28   | 20         | 1150  | 0.00706 | 0.00027 | 0.00637           | 0.141            | 162.38                 |
| 1180       | 39.91  | 0.31   | 20         | 1170  | 0.00777 | 0.00029 | 0.00701           | 0.155            | 181.76                 |
| 1200       | 33.65  | 0.29   | 20         | 1190  | 0.00862 | 0.00033 | 0.00778           | 0.172            | 205.11                 |
| 1220       | 33.93  | 0.30   | 20         | 1210  | 0.00869 | 0.00033 | 0.00785           | 0.174            | 210.40                 |
| 1240       | 40.74  | 0.31   | 20         | 1230  | 0.00761 | 0.00029 | 0.00687           | 0.152            | 187.19                 |
| 1260       | 37.52  | 0.33   | 20         | 1250  | 0.00880 | 0.00033 | 0.00794           | 0.176            | 219.88                 |
| 1280       | 36.22  | 0.27   | 20         | 1270  | 0.00745 | 0.00028 | 0.00673           | 0.149            | 189.34                 |
| 1300       | 39.92  | 0.38   | 20         | 1290  | 0.00952 | 0.00036 | 0.00859           | 0.190            | 245.59                 |
| 1320       | 40.63  | 0.30   | 20         | 1310  | 0.00738 | 0.00028 | 0.00666           | 0.148            | 193.48                 |
| 1350       | 56.33  | 0.43   | 30         | 1335  | 0.00763 | 0.00029 | 0.01033           | 0.229            | 305.73                 |
| 1380       | 56.92  | 0.44   | 30         | 1365  | 0.00773 | 0.00029 | 0.01046           | 0.232            | 316.55                 |
| 1410       | 56.12  | 0.40   | 30         | 1395  | 0.00713 | 0.00027 | 0.00965           | 0.214            | 298.29                 |
| 1440       | 56.73  | 0.54   | 30         | 1425  | 0.00952 | 0.00036 | 0.01289           | 0.286            | 406.93                 |
| 1470       | 58.09  | 0.47   | 30         | 1455  | 0.00809 | 0.00031 | 0.01095           | 0.243            | 353.17                 |
| 1500       | 57.15  | 0.42   | 30         | 1485  | 0.00735 | 0.00028 | 0.00995           | 0.220            | 327.40                 |
| 1530       | 56.38  | 0.48   | 30         | 1515  | 0.00851 | 0.00032 | 0.01153           | 0.255            | 386.95                 |
| 1560       | 55.84  | 0.49   | 30         | 1545  | 0.00878 | 0.00033 | 0.01188           | 0.263            | 406.72                 |
| 1590       | 55.46  | 0.42   | 30         | 1575  | 0.00757 | 0.00029 | 0.01025           | 0.227            | 357.83                 |
| 1620       | 55.90  | 0.50   | 30         | 1605  | 0.00894 | 0.00034 | 0.01211           | 0.268            | 430.68                 |
| 1650       | 57.56  | 0.43   | 30         | 1635  | 0.00747 | 0.00028 | 0.01011           | 0.224            | 366.43                 |
| 1680       | 56.77  | 0.38   | 30         | 1665  | 0.00669 | 0.00025 | 0.00906           | 0.201            | 334.35                 |
| 1710       | 61.33  | 0.48   | 30         | 1695  | 0.00783 | 0.00030 | 0.01059           | 0.235            | 397.98                 |
| 1740       | 55.76  | 0.48   | 30         | 1725  | 0.00861 | 0.00033 | 0.01165           | 0.258            | 445.48                 |
| 1770       | 57.02  | 0.58   | 30         | 1755  | 0.01017 | 0.00038 | 0.01377           | 0.305            | 535.55                 |
| 1800       | 56.15  | 0.60   | 30         | 1785  | 0.01060 | 0.00040 | 0.01434           | 0.318            | 567.45                 |
| 1830       | 57.26  | 0.50   | 30         | 1815  | 0.00873 | 0.00033 | 0.01182           | 0.262            | 475.46                 |
| 1860       | 55.98  | 0.48   | 30         | 1845  | 0.00857 | 0.00032 | 0.01161           | 0.257            | 474.60                 |
| 1890       | 56.44  | 0.47   | 30         | 1875  | 0.00833 | 0.00031 | 0.01127           | 0.250            | 468.42                 |
| 1920       | 56.82  | 0.48   | 30         | 1905  | 0.00845 | 0.00032 | 0.01144           | 0.253            | 482.83                 |
| 1950       | 55.59  | 0.52   | 30         | 1935  | 0.00935 | 0.00035 | 0.01266           | 0.281            | 543.01                 |
| 1980       | 55.84  | 0.41   | 30         | 1965  | 0.00734 | 0.00028 | 0.00994           | 0.220            | 432.83                 |
| 2010       | 57.29  | 0.51   | 30         | 1995  | 0.00890 | 0.00034 | 0.01205           | 0.267            | 532.79                 |
| 2040       | 54.57  | 0.50   | 30         | 2025  | 0.00907 | 0.00034 | 0.01228           | 0.272            | 551.06                 |
| 2100       | 114.38 | 0.84   | 60         | 2070  | 0.00734 | 0.00028 | 0.01988           | 0.441            | 912.12                 |
| 2160       | 110.25 | 0.89   | 60         | 2130  | 0.00807 | 0.00030 | 0.02186           | 0.484            | 1031.67                |

## Run#2002 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 2220       | 119.03 | 1.10   | 60         | 2190  | 0.00924 | 0.00035 | 0.02502           | 0.554            | 1214.32                |
| 2280       | 114.38 | 0.92   | 60         | 2250  | 0.00804 | 0.00030 | 0.02178           | 0.483            | 1085.85                |
| 2340       | 115.75 | 0.91   | 60         | 2310  | 0.00786 | 0.00030 | 0.02129           | 0.472            | 1089.64                |
| 2460       | 224.88 | 1.71   | 120        | 2400  | 0.00760 | 0.00029 | 0.04117           | 0.912            | 2189.97                |
| 2580       | 224.22 | 1.72   | 120        | 2520  | 0.00767 | 0.00029 | 0.04154           | 0.921            | 2319.77                |
| 2700       | 231.19 | 1.49   | 120        | 2640  | 0.00642 | 0.00024 | 0.03478           | 0.771            | 2034.90                |
| 2820       | 226.20 | 1.57   | 120        | 2760  | 0.00694 | 0.00026 | 0.03758           | 0.833            | 2298.78                |
| 2940       | 225.95 | 1.26   | 120        | 2880  | 0.00558 | 0.00021 | 0.03020           | 0.669            | 1927.22                |
| 3060       | 228.62 | 1.26   | 120        | 3000  | 0.00551 | 0.00021 | 0.02984           | 0.661            | 1984.12                |
| 3180       | 229.26 | 1.20   | 120        | 3120  | 0.00523 | 0.00020 | 0.02834           | 0.628            | 1959.70                |
| 3300       | 227.25 | 1.10   | 120        | 3240  | 0.00484 | 0.00018 | 0.02621           | 0.581            | 1881.98                |
| 3420       | 228.55 | 1.15   | 120        | 3360  | 0.00503 | 0.00019 | 0.02725           | 0.604            | 2028.79                |
| 3540       | 235.37 | 1.07   | 120        | 3480  | 0.00455 | 0.00017 | 0.02462           | 0.546            | 1898.42                |
| 3660       | 229.47 | 0.86   | 120        | 3600  | 0.00375 | 0.00014 | 0.02029           | 0.450            | 1619.04                |
| 3780       | 224.04 | 0.84   | 120        | 3720  | 0.00375 | 0.00014 | 0.02030           | 0.450            | 1673.70                |
| 3900       | 226.95 | 0.76   | 120        | 3840  | 0.00335 | 0.00013 | 0.01813           | 0.402            | 1543.11                |
| 4020       | 234.13 | 0.76   | 120        | 3960  | 0.00325 | 0.00012 | 0.01758           | 0.390            | 1542.53                |
| 4140       | 125.93 | 0.42   | 120        | 4080  | 0.00330 | 0.00012 | 0.01784           | 0.395            | 1613.47                |

$$\Sigma E(t) \Delta t_i = 1.0000$$

|                                       |
|---------------------------------------|
| <b>So = 1.888 g/s</b>                 |
| <b>Bed weight = 4117.0 g</b>          |
| <b><math>\tau = 2180.1</math> sec</b> |

|                                       |                                                         |
|---------------------------------------|---------------------------------------------------------|
| <b><math>\tau_{obs} = 2180</math></b> | <b><math>\Sigma C_i t_i \Delta t_i = 48515.3</math></b> |
|                                       | <b><math>\Sigma C_i \Delta t_i = 22.25</math></b>       |

Table D.18 Data Run#2003

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 174.30 | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 10         | 174.30 | 0.00   | 10         | 5     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 20         | 174.30 | 0.00   | 10         | 15    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 30         | 174.30 | 0.00   | 10         | 25    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 40         | 174.30 | 0.00   | 10         | 35    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 50         | 171.8  | 0.06   | 10         | 45    | 0.00035 | 0.00012 | 0.00123           | 0.003            | 0.16                   |
| 60         | 179.45 | 0.29   | 10         | 60    | 0.00162 | 0.00057 | 0.00568           | 0.016            | 0.97                   |
| 70         | 174.98 | 0.76   | 10         | 75    | 0.00434 | 0.00153 | 0.01527           | 0.043            | 3.26                   |
| 80         | 173.05 | 1.54   | 10         | 85    | 0.00887 | 0.00312 | 0.0311            | 0.089            | 7.54                   |
| 90         | 175.57 | 1.90   | 10         | 95    | 0.01082 | 0.00380 | 0.03804           | 0.108            | 10.28                  |
| 100        | 178.26 | 2.10   | 10         | 105   | 0.0117  | 0.00413 | 0.0413            | 0.11             | 12.34                  |
| 110        | 175.00 | 2.36   | 10         | 115   | 0.01349 | 0.00474 | 0.04740           | 0.135            | 15.5                   |
| 120        | 171.0  | 2.47   | 10         | 125   | 0.01444 | 0.00508 | 0.05075           | 0.144            | 18.05                  |
| 130        | 176.35 | 2.70   | 10         | 135   | 0.0153  | 0.00538 | 0.05382           | 0.153            | 20.67                  |
| 140        | 177.39 | 2.85   | 10         | 145   | 0.01604 | 0.00564 | 0.05637           | 0.160            | 23.26                  |
| 150        | 170.48 | 2.87   | 10         | 155   | 0.0168  | 0.00591 | 0.05907           | 0.168            | 26.05                  |
| 160        | 173.1  | 2.49   | 10         | 165   | 0.01435 | 0.00504 | 0.05044           | 0.143            | 23.68                  |
| 170        | 173.79 | 2.61   | 10         | 175   | 0.01502 | 0.00528 | 0.05279           | 0.150            | 26.28                  |
| 180        | 169.64 | 2.31   | 10         | 185   | 0.01362 | 0.00479 | 0.04786           | 0.136            | 25.19                  |
| 190        | 170.94 | 2.39   | 10         | 195   | 0.01398 | 0.00491 | 0.04915           | 0.140            | 27.26                  |
| 200        | 177.20 | 1.98   | 10         | 205   | 0.0111  | 0.00393 | 0.03928           | 0.11             | 22.91                  |
| 210        | 176.24 | 2.14   | 10         | 215   | 0.0121  | 0.00427 | 0.04268           | 0.12             | 26.1                   |
| 220        | 173.65 | 1.84   | 10         | 225   | 0.01060 | 0.00372 | 0.03725           | 0.106            | 23.84                  |
| 230        | 169.62 | 1.56   | 10         | 235   | 0.00920 | 0.00323 | 0.03233           | 0.092            | 21.6                   |
| 240        | 176.35 | 1.46   | 10         | 245   | 0.00828 | 0.00291 | 0.02910           | 0.083            | 20.28                  |
| 250        | 167.8  | 1.30   | 10         | 255   | 0.00775 | 0.00272 | 0.02723           | 0.077            | 19.75                  |
| 260        | 179.39 | 1.23   | 10         | 265   | 0.00686 | 0.00241 | 0.02410           | 0.069            | 18.1                   |
| 270        | 176.98 | 0.92   | 10         | 275   | 0.00520 | 0.00183 | 0.01827           | 0.052            | 14.30                  |
| 280        | 174.06 | 0.92   | 10         | 285   | 0.00526 | 0.00185 | 0.01848           | 0.053            | 14.98                  |
| 290        | 180.4  | 0.93   | 10         | 295   | 0.00515 | 0.0018  | 0.0181            | 0.052            | 15.2                   |
| 300        | 163.64 | 0.67   | 10         | 305   | 0.00409 | 0.00144 | 0.01439           | 0.041            | 12.49                  |
| 310        | 174.97 | 0.70   | 10         | 315   | 0.00400 | 0.0014  | 0.01406           | 0.040            | 12.60                  |
| 320        | 172.69 | 0.59   | 10         | 325   | 0.00342 | 0.00120 | 0.0120            | 0.034            | 11.1                   |
| 330        | 176.47 | 0.49   | 10         | 335   | 0.00278 | 0.00098 | 0.00976           | 0.028            | 9.30                   |
| 340        | 174.33 | 0.40   | 10         | 345   | 0.00229 | 0.00081 | 0.00807           | 0.023            | 7.92                   |
| 350        | 175.89 | 0.33   | 10         | 355   | 0.00188 | 0.00066 | 0.00659           | 0.019            | 6.66                   |
| 360        | 166.37 | 0.31   | 10         | 365   | 0.00186 | 0.00065 | 0.00655           | 0.019            | 6.80                   |
| 370        | 176.53 | 0.30   | 10         | 375   | 0.00170 | 0.00060 | 0.00597           | 0.017            | 6.37                   |
| 380        | 175.94 | 0.24   | 10         | 385   | 0.00136 | 0.00048 | 0.00479           | 0.014            | 5.25                   |
| 390        | 172.05 | 0.17   | 10         | 395   | 0.00099 | 0.00035 | 0.00347           | 0.010            | 3.90                   |
| 400        | 173.78 | 0.14   | 10         | 405   | 0.00081 | 0.00028 | 0.00283           | 0.008            | 3.26                   |
| 410        | 177.87 | 0.16   | 10         | 415   | 0.00090 | 0.00032 | 0.00316           | 0.009            | 3.73                   |
| 420        | 172.99 | 0.18   | 10         | 425   | 0.00104 | 0.00037 | 0.00366           | 0.010            | 4.42                   |
| 430        | 173.32 | 0.08   | 10         | 435   | 0.00046 | 0.00016 | 0.00162           | 0.005            | 2.01                   |
| 440        | 173.63 | 0.12   | 10         | 445   | 0.00069 | 0.00024 | 0.00243           | 0.007            | 3.08                   |
| 450        | 175.09 | 0.08   | 10         | 455   | 0.00046 | 0.00016 | 0.0016            | 0.005            | 2.08                   |
| 460        | 174.99 | 0.1    | 10         | 465   | 0.00063 | 0.00022 | 0.00221           | 0.006            | 2.92                   |
| 470        | 171.3  | 0.04   | 10         | 475   | 0.00023 | 0.00008 | 0.00082           | 0.002            | 1.1                    |
| 480        | 176.0  | 0.07   | 10         | 485   | 0.00040 | 0.00014 | 0.00140           | 0.004            | 1.93                   |
| 490        | 177.42 | 0.03   | 10         | 495   | 0.00017 | 0.00006 | 0.00059           | 0.002            | 0.84                   |
| 500        | 173.1  | 0.04   | 10         | 505   | 0.00023 | 0.00008 | 0.00081           | 0.002            | 1.1                    |
| 510        | 173.5  | 0.03   | 10         | 515   | 0.00017 | 0.00006 | 0.00061           | 0.002            | 0.89                   |
| 520        | 172.53 | 0.03   | 10         | 525   | 0.00014 | 0.00005 | 0.00051           | 0.001            | 0.76                   |
| 530        | 176.56 | 0.04   | 10         | 535   | 0.00023 | 0.00008 | 0.00080           | 0.002            | 1.2                    |
| 540        | 171.8  | 0.03   | 10         | 545   | 0.00017 | 0.00006 | 0.00061           | 0.002            | 0.95                   |
| 550        | 177.38 | 0.02   | 10         | 555   | 0.0001  | 0.00004 | 0.00040           | 0.001            | 0.63                   |
| 560        | 174.40 | 0.03   | 10         | 565   | 0.00017 | 0.00006 | 0.00060           | 0.002            | 0.97                   |
| 570        | 180.64 | 0.01   | 10         | 575   | 0.00006 | 0.00002 | 0.00019           | 0.001            | 0.32                   |
| 580        | 171.9  | 0.03   | 10         | 585   | 0.00017 | 0.00006 | 0.00061           | 0.002            | 1.02                   |
| 590        | 172.1  | 0.02   | 10         | 595   | 0.00012 | 0.00004 | 0.00041           | 0.001            | 0.69                   |
| 600        | 178.79 | 0.01   | 10         | 605   | 0.00006 | 0.00002 | 0.00020           | 0.001            | 0.34                   |
| 610        | 176.44 | 0.01   | 10         | 615   | 0.00006 | 0.00002 | 0.00020           | 0.001            | 0.35                   |
| 620        | 174.54 | 0.01   | 10         | 625   | 0.00006 | 0.00002 | 0.00020           | 0.001            | 0.36                   |

$$\Sigma E(t) \Delta t_i = 0.99934$$

$$S_o = 17.430 \text{ g/s}$$

$$\text{Bed weight} = 3403.0 \text{ g}$$

$$\tau = 195.2 \text{ sec}$$

$$\tau_{\text{obs}} = 195$$

$$\Sigma C_i t_i \Delta t_i = 555.1$$

$$\Sigma C_i \Delta t_i = 2.84$$

Table D.19 Data Run#2004

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | C(t)    | E(t)    | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 148.20 | 0.00   | 20         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 20         | 148.20 | 0.00   | 20         | 10    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 40         | 148.20 | 0.00   | 20         | 30    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 60         | 148.20 | 0.00   | 20         | 50    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 80         | 148.20 | 0.00   | 20         | 70    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 100        | 147.91 | 0.00   | 20         | 90    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 120        | 145.13 | 0.01   | 20         | 110   | 0.00007 | 0.00001 | 0.00021           | 0.001            | 0.15                   |
| 140        | 144.76 | 0.12   | 20         | 130   | 0.00083 | 0.00012 | 0.00248           | 0.017            | 2.16                   |
| 160        | 153.60 | 0.41   | 20         | 150   | 0.00267 | 0.00040 | 0.00798           | 0.053            | 8.01                   |
| 180        | 152.42 | 0.68   | 20         | 170   | 0.00446 | 0.00067 | 0.01334           | 0.089            | 15.17                  |
| 200        | 151.90 | 0.90   | 20         | 190   | 0.00589 | 0.00088 | 0.01761           | 0.118            | 22.39                  |
| 220        | 152.72 | 1.41   | 20         | 210   | 0.00923 | 0.00138 | 0.02760           | 0.185            | 38.78                  |
| 240        | 148.36 | 1.43   | 20         | 230   | 0.00964 | 0.00144 | 0.02881           | 0.193            | 44.34                  |
| 260        | 152.25 | 1.81   | 20         | 250   | 0.01189 | 0.00178 | 0.03554           | 0.238            | 59.44                  |
| 280        | 148.72 | 1.78   | 20         | 270   | 0.01197 | 0.00179 | 0.03578           | 0.239            | 64.63                  |
| 300        | 152.84 | 2.21   | 20         | 290   | 0.01446 | 0.00216 | 0.04323           | 0.289            | 83.87                  |
| 320        | 149.05 | 2.42   | 20         | 310   | 0.01624 | 0.00243 | 0.04854           | 0.325            | 100.66                 |
| 340        | 156.70 | 2.41   | 20         | 330   | 0.01538 | 0.00230 | 0.04598           | 0.308            | 101.51                 |
| 360        | 141.80 | 2.23   | 20         | 350   | 0.01573 | 0.00235 | 0.04701           | 0.315            | 110.08                 |
| 380        | 150.24 | 2.28   | 20         | 370   | 0.01518 | 0.00227 | 0.04537           | 0.304            | 112.30                 |
| 400        | 150.07 | 2.20   | 20         | 390   | 0.01466 | 0.00219 | 0.04383           | 0.293            | 114.35                 |
| 420        | 148.72 | 2.12   | 20         | 410   | 0.01425 | 0.00213 | 0.04261           | 0.285            | 116.89                 |
| 440        | 150.71 | 2.02   | 20         | 430   | 0.01340 | 0.00200 | 0.04007           | 0.268            | 115.27                 |
| 460        | 151.13 | 2.12   | 20         | 450   | 0.01403 | 0.00210 | 0.04194           | 0.281            | 126.25                 |
| 480        | 150.66 | 1.85   | 20         | 470   | 0.01228 | 0.00184 | 0.03671           | 0.246            | 115.43                 |
| 500        | 151.58 | 1.69   | 20         | 490   | 0.01115 | 0.00167 | 0.03333           | 0.223            | 109.26                 |
| 520        | 152.03 | 1.73   | 20         | 510   | 0.01138 | 0.00170 | 0.03402           | 0.228            | 116.07                 |
| 540        | 150.11 | 1.34   | 20         | 530   | 0.00893 | 0.00133 | 0.02669           | 0.179            | 94.62                  |
| 560        | 150.56 | 1.37   | 20         | 550   | 0.00910 | 0.00136 | 0.02720           | 0.182            | 100.09                 |
| 580        | 142.68 | 1.17   | 20         | 570   | 0.00820 | 0.00123 | 0.02451           | 0.164            | 93.48                  |
| 600        | 149.59 | 1.07   | 20         | 590   | 0.00715 | 0.00107 | 0.02138           | 0.143            | 84.40                  |
| 620        | 148.23 | 1.19   | 20         | 610   | 0.00803 | 0.00120 | 0.02400           | 0.161            | 97.94                  |
| 640        | 148.53 | 0.95   | 20         | 630   | 0.00640 | 0.00096 | 0.01912           | 0.128            | 80.59                  |
| 660        | 144.20 | 0.73   | 20         | 650   | 0.00506 | 0.00076 | 0.01513           | 0.101            | 65.81                  |
| 680        | 150.50 | 0.79   | 20         | 670   | 0.00525 | 0.00078 | 0.01569           | 0.105            | 70.34                  |
| 700        | 146.06 | 0.73   | 20         | 690   | 0.00500 | 0.00075 | 0.01494           | 0.100            | 68.97                  |
| 720        | 146.39 | 0.73   | 20         | 710   | 0.00499 | 0.00075 | 0.01491           | 0.100            | 70.81                  |
| 740        | 144.75 | 0.70   | 20         | 730   | 0.00484 | 0.00072 | 0.01446           | 0.097            | 70.60                  |
| 760        | 147.11 | 0.51   | 20         | 750   | 0.00347 | 0.00052 | 0.01036           | 0.069            | 52.00                  |
| 780        | 143.88 | 0.55   | 20         | 770   | 0.00382 | 0.00057 | 0.01143           | 0.076            | 58.87                  |
| 800        | 146.24 | 0.44   | 20         | 790   | 0.00301 | 0.00045 | 0.00899           | 0.060            | 47.54                  |
| 820        | 155.52 | 0.38   | 20         | 810   | 0.00244 | 0.00037 | 0.00730           | 0.049            | 39.58                  |
| 840        | 142.55 | 0.32   | 20         | 830   | 0.00224 | 0.00034 | 0.00671           | 0.045            | 37.26                  |
| 860        | 145.46 | 0.36   | 20         | 850   | 0.00247 | 0.00037 | 0.00740           | 0.049            | 42.07                  |
| 880        | 148.32 | 0.35   | 20         | 870   | 0.00236 | 0.00035 | 0.00705           | 0.047            | 41.06                  |
| 900        | 140.36 | 0.29   | 20         | 890   | 0.00207 | 0.00031 | 0.00618           | 0.041            | 36.78                  |
| 920        | 147.32 | 0.26   | 20         | 910   | 0.00176 | 0.00026 | 0.00528           | 0.035            | 32.12                  |
| 940        | 141.45 | 0.21   | 20         | 930   | 0.00148 | 0.00022 | 0.00444           | 0.030            | 27.61                  |
| 960        | 146.61 | 0.20   | 20         | 950   | 0.00136 | 0.00020 | 0.00408           | 0.027            | 25.92                  |
| 980        | 152.39 | 0.15   | 20         | 970   | 0.00098 | 0.00015 | 0.00294           | 0.020            | 19.10                  |
| 1000       | 143.42 | 0.15   | 20         | 990   | 0.00105 | 0.00016 | 0.00313           | 0.021            | 20.71                  |
| 1020       | 136.46 | 0.08   | 20         | 1010  | 0.00059 | 0.00009 | 0.00175           | 0.012            | 11.84                  |
| 1040       | 149.28 | 0.11   | 20         | 1030  | 0.00074 | 0.00011 | 0.00220           | 0.015            | 15.18                  |
| 1060       | 142.46 | 0.12   | 20         | 1050  | 0.00084 | 0.00013 | 0.00252           | 0.017            | 17.69                  |
| 1080       | 152.88 | 0.09   | 20         | 1070  | 0.00059 | 0.00009 | 0.00176           | 0.012            | 12.60                  |
| 1100       | 147.41 | 0.12   | 20         | 1090  | 0.00081 | 0.00012 | 0.00243           | 0.016            | 17.75                  |
| 1120       | 147.79 | 0.18   | 20         | 1110  | 0.00122 | 0.00018 | 0.00364           | 0.024            | 27.04                  |
| 1140       | 144.35 | 0.08   | 20         | 1130  | 0.00055 | 0.00008 | 0.00166           | 0.011            | 12.53                  |
| 1160       | 224.49 | 0.04   | 30         | 1150  | 0.00018 | 0.00003 | 0.00080           | 0.005            | 6.15                   |
| 1180       | 221.11 | 0.06   | 30         | 1170  | 0.00025 | 0.00004 | 0.00112           | 0.007            | 8.73                   |
| 1200       | 224.98 | 0.07   | 30         | 1190  | 0.00031 | 0.00005 | 0.00140           | 0.009            | 11.11                  |

**Run#2004 (Cont..)**

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 1220       | 223.65 | 0.06   | 30         | 1210  | 0.00027 | 0.00004 | 0.00120           | 0.008            | 9.74                   |
| 1240       | 223.55 | 0.01   | 30         | 1230  | 0.00004 | 0.00001 | 0.00020           | 0.001            | 1.65                   |
| 1260       | 218.75 | 0.02   | 30         | 1250  | 0.00009 | 0.00001 | 0.00041           | 0.003            | 3.43                   |
| 1280       | 230.20 | 0.06   | 30         | 1270  | 0.00024 | 0.00004 | 0.00107           | 0.007            | 9.10                   |
| 1300       | 225.66 | 0.04   | 30         | 1290  | 0.00018 | 0.00003 | 0.00079           | 0.005            | 6.86                   |
| 1320       | 220.86 | 0.01   | 30         | 1310  | 0.00002 | 0.00000 | 0.00010           | 0.001            | 0.89                   |
| 1340       | 229.92 | 0.00   | 30         | 1330  | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 1360       | 221.55 | 0.01   | 30         | 1350  | 0.00005 | 0.00001 | 0.00020           | 0.001            | 1.83                   |
| 1380       | 222.17 | 0.02   | 30         | 1370  | 0.00009 | 0.00001 | 0.00040           | 0.003            | 3.70                   |
| 1240       | 187.77 | 0.02   | 25         | 1294  | 0.00011 | 0.00002 | 0.00040           | 0.003            | 3.48                   |

$$\Sigma E(t) \Delta t_i = 0.99937$$

|                                      |
|--------------------------------------|
| <b>So = 7.414 g/s</b>                |
| <b>Bed weight = 3478.0 g</b>         |
| <b><math>\tau = 469.1</math> sec</b> |

|                                      |                                                        |
|--------------------------------------|--------------------------------------------------------|
| <b><math>\tau_{obs} = 469</math></b> | <b><math>\Sigma C_i t_i \Delta t_i = 3136.6</math></b> |
|                                      | <b><math>\Sigma C_i \Delta t_i = 6.69</math></b>       |



Table D.20 Data Run#2005

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | C(t)    | E(t)    | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 162.40 | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 10         | 162.40 | 0.00   | 10         | 5     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 20         | 162.40 | 0.00   | 10         | 15    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 30         | 162.40 | 0.00   | 10         | 25    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 40         | 162.40 | 0.00   | 10         | 35    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 50         | 162.40 | 0.00   | 10         | 45    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 60         | 158.06 | 0.00   | 10         | 55    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 70         | 163.10 | 0.01   | 10         | 65    | 0.00006 | 0.00002 | 0.00020           | 0.001            | 0.04                   |
| 80         | 162.83 | 0.06   | 10         | 75    | 0.00037 | 0.00012 | 0.00121           | 0.004            | 0.28                   |
| 90         | 163.79 | 0.25   | 10         | 85    | 0.00153 | 0.00050 | 0.00500           | 0.015            | 1.30                   |
| 100        | 163.12 | 0.61   | 10         | 95    | 0.00374 | 0.00122 | 0.01224           | 0.037            | 3.55                   |
| 110        | 159.13 | 1.12   | 10         | 105   | 0.00704 | 0.00230 | 0.02304           | 0.070            | 7.39                   |
| 120        | 161.75 | 1.99   | 10         | 115   | 0.01230 | 0.00403 | 0.04028           | 0.123            | 14.15                  |
| 130        | 163.69 | 2.22   | 10         | 125   | 0.01356 | 0.00444 | 0.04441           | 0.136            | 16.95                  |
| 140        | 163.32 | 2.75   | 10         | 135   | 0.01684 | 0.00551 | 0.05513           | 0.168            | 22.73                  |
| 150        | 163.59 | 3.10   | 10         | 145   | 0.01895 | 0.00620 | 0.06205           | 0.189            | 27.48                  |
| 160        | 154.73 | 3.32   | 10         | 155   | 0.02146 | 0.00703 | 0.07025           | 0.215            | 33.26                  |
| 170        | 165.11 | 3.16   | 10         | 165   | 0.01914 | 0.00627 | 0.06266           | 0.191            | 31.58                  |
| 180        | 170.53 | 3.11   | 10         | 175   | 0.01824 | 0.00597 | 0.05971           | 0.182            | 31.92                  |
| 190        | 158.25 | 3.05   | 10         | 185   | 0.01927 | 0.00631 | 0.06311           | 0.193            | 35.66                  |
| 200        | 164.22 | 2.94   | 10         | 195   | 0.01787 | 0.00585 | 0.05852           | 0.179            | 34.85                  |
| 210        | 164.16 | 2.30   | 10         | 205   | 0.01401 | 0.00459 | 0.04587           | 0.140            | 28.72                  |
| 220        | 163.32 | 2.27   | 10         | 215   | 0.01390 | 0.00455 | 0.04551           | 0.139            | 29.88                  |
| 230        | 163.30 | 1.87   | 10         | 225   | 0.01145 | 0.00375 | 0.03749           | 0.115            | 25.77                  |
| 240        | 160.47 | 2.08   | 10         | 235   | 0.01296 | 0.00424 | 0.04244           | 0.130            | 30.46                  |
| 250        | 160.99 | 1.80   | 10         | 245   | 0.01118 | 0.00366 | 0.03661           | 0.112            | 27.39                  |
| 260        | 162.15 | 1.56   | 10         | 255   | 0.00962 | 0.00315 | 0.03150           | 0.096            | 24.53                  |
| 270        | 164.78 | 1.41   | 10         | 265   | 0.00856 | 0.00280 | 0.02802           | 0.086            | 22.68                  |
| 280        | 160.47 | 1.11   | 10         | 275   | 0.00692 | 0.00226 | 0.02265           | 0.069            | 19.02                  |
| 290        | 163.78 | 1.08   | 10         | 285   | 0.00659 | 0.00216 | 0.02159           | 0.066            | 18.79                  |
| 300        | 161.31 | 0.99   | 10         | 295   | 0.00614 | 0.00201 | 0.02009           | 0.061            | 18.10                  |
| 310        | 160.32 | 1.09   | 10         | 305   | 0.00677 | 0.00222 | 0.02216           | 0.068            | 20.64                  |
| 320        | 163.00 | 0.81   | 10         | 315   | 0.00497 | 0.00163 | 0.01627           | 0.050            | 15.65                  |
| 330        | 164.42 | 0.54   | 10         | 325   | 0.00328 | 0.00108 | 0.01075           | 0.033            | 10.67                  |
| 340        | 162.88 | 0.53   | 10         | 335   | 0.00325 | 0.00107 | 0.01065           | 0.033            | 10.90                  |
| 350        | 161.63 | 0.45   | 10         | 345   | 0.00278 | 0.00091 | 0.00912           | 0.028            | 9.61                   |
| 360        | 161.97 | 0.39   | 10         | 355   | 0.00241 | 0.00079 | 0.00788           | 0.024            | 8.55                   |
| 370        | 162.07 | 0.44   | 10         | 365   | 0.00271 | 0.00089 | 0.00889           | 0.027            | 9.91                   |
| 380        | 165.17 | 0.25   | 10         | 375   | 0.00151 | 0.00050 | 0.00496           | 0.015            | 5.68                   |
| 390        | 164.51 | 0.26   | 10         | 385   | 0.00158 | 0.00052 | 0.00517           | 0.016            | 6.08                   |
| 400        | 162.24 | 0.19   | 10         | 395   | 0.00117 | 0.00038 | 0.00383           | 0.012            | 4.63                   |
| 410        | 165.54 | 0.19   | 10         | 405   | 0.00112 | 0.00037 | 0.00366           | 0.011            | 4.53                   |
| 420        | 161.89 | 0.15   | 10         | 415   | 0.00093 | 0.00030 | 0.00303           | 0.009            | 3.85                   |
| 430        | 162.53 | 0.09   | 10         | 425   | 0.00052 | 0.00017 | 0.00171           | 0.005            | 2.22                   |
| 440        | 162.94 | 0.11   | 10         | 435   | 0.00068 | 0.00022 | 0.00221           | 0.007            | 2.94                   |
| 450        | 164.83 | 0.07   | 10         | 445   | 0.00042 | 0.00014 | 0.00139           | 0.004            | 1.89                   |
| 460        | 160.84 | 0.06   | 10         | 455   | 0.00037 | 0.00012 | 0.00122           | 0.004            | 1.70                   |
| 470        | 161.89 | 0.05   | 10         | 465   | 0.00031 | 0.00010 | 0.00101           | 0.003            | 1.44                   |
| 480        | 160.12 | 0.05   | 10         | 475   | 0.00031 | 0.00010 | 0.00102           | 0.003            | 1.48                   |
| 490        | 160.88 | 0.03   | 10         | 485   | 0.00019 | 0.00006 | 0.00061           | 0.002            | 0.90                   |
| 500        | 161.98 | 0.03   | 10         | 495   | 0.00019 | 0.00006 | 0.00061           | 0.002            | 0.92                   |
| 510        | 163.02 | 0.02   | 10         | 505   | 0.00012 | 0.00004 | 0.00040           | 0.001            | 0.62                   |
| 520        | 162.31 | 0.02   | 10         | 515   | 0.00009 | 0.00003 | 0.00030           | 0.001            | 0.48                   |
| 530        | 163.01 | 0.03   | 10         | 525   | 0.00015 | 0.00005 | 0.00050           | 0.002            | 0.81                   |
| 540        | 162.36 | 0.02   | 10         | 535   | 0.00012 | 0.00004 | 0.00040           | 0.001            | 0.66                   |
| 550        | 166.20 | 0.01   | 10         | 545   | 0.00006 | 0.00002 | 0.00020           | 0.001            | 0.33                   |
| 560        | 160.69 | 0.01   | 10         | 555   | 0.00006 | 0.00002 | 0.00020           | 0.001            | 0.35                   |
| 570        | 164.90 | 0.01   | 10         | 565   | 0.00006 | 0.00002 | 0.00020           | 0.001            | 0.34                   |
| 580        | 159.14 | 0.00   | 10         | 575   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 590        | 166.14 | 0.00   | 10         | 585   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 600        | 155.30 | 0.01   | 10         | 595   | 0.00006 | 0.00002 | 0.00021           | 0.001            | 0.38                   |

### Run#2005 (Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|--------------------|--------------------------|
| 610        | 163.46 | 0.00   | 10         | 605   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 620        | 163.84 | 0.00   | 10         | 615   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 630        | 161.17 | 0.00   | 10         | 625   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 640        | 164.04 | 0.00   | 10         | 635   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 650        | 161.75 | 0.00   | 10         | 645   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 660        | 155.46 | 0.00   | 10         | 655   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 670        | 163.20 | 0.00   | 10         | 665   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 680        | 162.62 | 0.00   | 10         | 675   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 690        | 163.48 | 0.01   | 10         | 685   | 0.00006 | 0.00002 | 0.00020           | 0.001              | 0.42                     |

$$\Sigma E(t) \Delta t_i = 1.00838$$

|                                      |
|--------------------------------------|
| <b>So = 16.240 g/s</b>               |
| <b>Bed weight = 3370.0 g</b>         |
| <b><math>\tau = 207.5</math> sec</b> |

|                                        |                                                       |
|----------------------------------------|-------------------------------------------------------|
| <b><math>\tau_{obs} = 206.2</math></b> | <b><math>\Sigma C_i t_i \Delta t_i = 635.0</math></b> |
|                                        | <b><math>\Sigma C_i \Delta t_i = 3.08</math></b>      |

Table D.21 Data Run#2006

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t_i$ | $C_i * t_i * \Delta t_i$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|--------------------|--------------------------|
| 0          | 147.00 | 0.00   | 20         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 20         | 147.00 | 0.00   | 20         | 10    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 40         | 147.00 | 0.00   | 20         | 30    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 60         | 147.00 | 0.00   | 20         | 50    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 80         | 147.00 | 0.00   | 20         | 70    | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 100        | 147.00 | 0.01   | 20         | 90    | 0.00007 | 0.00001 | 0.00020           | 0.001              | 0.12                     |
| 120        | 147.00 | 0.00   | 20         | 110   | 0.00000 | 0.00000 | 0.00000           | 0.000              | 0.00                     |
| 140        | 147.00 | 0.07   | 20         | 130   | 0.00048 | 0.00007 | 0.00143           | 0.010              | 1.24                     |
| 160        | 145.88 | 0.28   | 20         | 150   | 0.00192 | 0.00029 | 0.00577           | 0.038              | 5.76                     |
| 180        | 147.28 | 0.49   | 20         | 170   | 0.00333 | 0.00050 | 0.01000           | 0.067              | 11.31                    |
| 200        | 142.49 | 0.81   | 20         | 190   | 0.00568 | 0.00085 | 0.01709           | 0.114              | 21.60                    |
| 220        | 142.83 | 1.13   | 20         | 210   | 0.00791 | 0.00119 | 0.02379           | 0.158              | 33.23                    |
| 240        | 139.89 | 1.44   | 20         | 230   | 0.01029 | 0.00155 | 0.03095           | 0.206              | 47.35                    |
| 260        | 137.65 | 1.50   | 20         | 250   | 0.01090 | 0.00164 | 0.03277           | 0.218              | 54.49                    |
| 280        | 140.01 | 1.76   | 20         | 270   | 0.01257 | 0.00189 | 0.03780           | 0.251              | 67.88                    |
| 300        | 142.36 | 1.94   | 20         | 290   | 0.01363 | 0.00205 | 0.04098           | 0.273              | 79.04                    |
| 320        | 144.58 | 2.19   | 20         | 310   | 0.01515 | 0.00228 | 0.04555           | 0.303              | 93.91                    |
| 340        | 141.96 | 2.04   | 20         | 330   | 0.01437 | 0.00216 | 0.04321           | 0.287              | 94.84                    |
| 360        | 153.66 | 2.11   | 20         | 350   | 0.01373 | 0.00206 | 0.04129           | 0.275              | 96.12                    |
| 380        | 157.83 | 2.32   | 20         | 370   | 0.01470 | 0.00221 | 0.04420           | 0.294              | 108.78                   |
| 400        | 147.13 | 2.23   | 20         | 390   | 0.01516 | 0.00228 | 0.04558           | 0.303              | 118.22                   |
| 420        | 151.04 | 2.23   | 20         | 410   | 0.01476 | 0.00222 | 0.04440           | 0.295              | 121.07                   |
| 440        | 144.04 | 2.18   | 20         | 430   | 0.01513 | 0.00228 | 0.04551           | 0.303              | 130.16                   |
| 460        | 148.52 | 2.05   | 20         | 450   | 0.01380 | 0.00208 | 0.04151           | 0.276              | 124.23                   |
| 480        | 146.32 | 1.67   | 20         | 470   | 0.01141 | 0.00172 | 0.03432           | 0.228              | 107.29                   |
| 500        | 151.54 | 1.76   | 20         | 490   | 0.01161 | 0.00175 | 0.03492           | 0.232              | 113.82                   |
| 520        | 151.11 | 1.63   | 20         | 510   | 0.01079 | 0.00162 | 0.03244           | 0.216              | 110.03                   |
| 540        | 146.88 | 1.75   | 20         | 530   | 0.01191 | 0.00179 | 0.03583           | 0.238              | 126.29                   |
| 560        | 149.40 | 1.45   | 20         | 550   | 0.00971 | 0.00146 | 0.02918           | 0.194              | 106.76                   |
| 580        | 151.16 | 1.36   | 20         | 570   | 0.00900 | 0.00135 | 0.02705           | 0.180              | 102.57                   |
| 600        | 151.15 | 1.26   | 20         | 590   | 0.00834 | 0.00125 | 0.02507           | 0.167              | 98.37                    |
| 620        | 151.70 | 1.13   | 20         | 610   | 0.00745 | 0.00112 | 0.02240           | 0.149              | 90.88                    |
| 640        | 147.67 | 1.04   | 20         | 630   | 0.00704 | 0.00106 | 0.02118           | 0.141              | 88.74                    |
| 660        | 152.28 | 0.82   | 20         | 650   | 0.00538 | 0.00081 | 0.01619           | 0.108              | 70.00                    |
| 680        | 146.48 | 0.75   | 20         | 670   | 0.00512 | 0.00077 | 0.01540           | 0.102              | 68.61                    |
| 700        | 146.39 | 0.65   | 20         | 690   | 0.00444 | 0.00067 | 0.01335           | 0.089              | 61.27                    |
| 720        | 150.84 | 0.68   | 20         | 710   | 0.00451 | 0.00068 | 0.01356           | 0.090              | 64.01                    |
| 740        | 150.54 | 0.69   | 20         | 730   | 0.00458 | 0.00069 | 0.01378           | 0.092              | 66.92                    |
| 760        | 146.42 | 0.55   | 20         | 750   | 0.00376 | 0.00056 | 0.01130           | 0.075              | 56.34                    |
| 780        | 153.02 | 0.50   | 20         | 770   | 0.00327 | 0.00049 | 0.00983           | 0.065              | 50.32                    |
| 800        | 150.66 | 0.55   | 20         | 790   | 0.00365 | 0.00055 | 0.01098           | 0.073              | 57.68                    |
| 820        | 142.99 | 0.47   | 20         | 810   | 0.00329 | 0.00049 | 0.00988           | 0.066              | 53.25                    |
| 840        | 149.94 | 0.23   | 20         | 830   | 0.00153 | 0.00023 | 0.00461           | 0.031              | 25.46                    |
| 860        | 148.34 | 0.34   | 20         | 850   | 0.00229 | 0.00034 | 0.00689           | 0.046              | 38.96                    |
| 880        | 158.11 | 0.25   | 20         | 870   | 0.00158 | 0.00024 | 0.00475           | 0.032              | 27.51                    |
| 900        | 138.24 | 0.20   | 20         | 890   | 0.00145 | 0.00022 | 0.00435           | 0.029              | 25.75                    |
| 920        | 150.00 | 0.30   | 20         | 910   | 0.00200 | 0.00030 | 0.00601           | 0.040              | 36.40                    |
| 940        | 147.52 | 0.26   | 20         | 930   | 0.00176 | 0.00026 | 0.00530           | 0.035              | 32.78                    |
| 960        | 150.96 | 0.21   | 20         | 950   | 0.00139 | 0.00021 | 0.00418           | 0.028              | 26.43                    |
| 980        | 153.75 | 0.13   | 20         | 970   | 0.00085 | 0.00013 | 0.00254           | 0.017              | 16.40                    |
| 1000       | 147.10 | 0.15   | 20         | 990   | 0.00102 | 0.00015 | 0.00307           | 0.020              | 20.19                    |
| 1020       | 149.60 | 0.12   | 20         | 1010  | 0.00080 | 0.00012 | 0.00241           | 0.016              | 16.20                    |
| 1050       | 222.74 | 0.19   | 30         | 1035  | 0.00085 | 0.00013 | 0.00385           | 0.026              | 26.49                    |

1

**Run#2006 (Cont..)**

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 1080       | 223.43 | 0.16   | 30         | 1065  | 0.00072 | 0.00011 | 0.00323           | 0.021            | 22.88                  |
| 1110       | 209.39 | 0.09   | 30         | 1095  | 0.00043 | 0.00006 | 0.00194           | 0.013            | 14.12                  |
| 1140       | 221.26 | 0.08   | 30         | 1125  | 0.00036 | 0.00005 | 0.00163           | 0.011            | 12.20                  |
| 1170       | 219.77 | 0.07   | 30         | 1155  | 0.00032 | 0.00005 | 0.00144           | 0.010            | 11.04                  |
| 1200       | 220.18 | 0.05   | 30         | 1185  | 0.00023 | 0.00003 | 0.00102           | 0.007            | 8.07                   |
| 1230       | 222.47 | 0.07   | 30         | 1215  | 0.00031 | 0.00005 | 0.00142           | 0.009            | 11.47                  |
| 1260       | 222.29 | 0.06   | 30         | 1245  | 0.00027 | 0.00004 | 0.00122           | 0.008            | 10.08                  |
| 1290       | 218.43 | 0.04   | 30         | 1275  | 0.00018 | 0.00003 | 0.00083           | 0.005            | 7.00                   |
| 1320       | 219.43 | 0.01   | 30         | 1305  | 0.00005 | 0.00001 | 0.00021           | 0.001            | 1.78                   |
| 1350       | 212.70 | 0.02   | 30         | 1335  | 0.00009 | 0.00001 | 0.00042           | 0.003            | 3.77                   |
| 1380       | 206.53 | 0.02   | 30         | 1365  | 0.00010 | 0.00001 | 0.00044           | 0.003            | 3.97                   |
| 1404.68    | 181.93 | 0.03   | 25         | 1392  | 0.00016 | 0.00002 | 0.00061           | 0.004            | 5.67                   |

$$\Sigma E(t) \Delta t = 0.99107$$

|                                       |
|---------------------------------------|
| <b><math>S_o = 7.369</math> g/s</b>   |
| <b>Bed weight = 3474.0 g</b>          |
| <b><math>\tau = 471.45</math> sec</b> |

|                                        |                                                      |
|----------------------------------------|------------------------------------------------------|
| <b><math>\tau_{obs} = 471.4</math></b> | <b><math>\Sigma C_i t_i \Delta t = 3107.1</math></b> |
|                                        | <b><math>\Sigma C_i \Delta t = 6.59</math></b>       |

Table D.22 Data Run#2007

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 170.90 | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 10         | 170.90 | 0.00   | 10         | 5     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 20         | 170.90 | 0.00   | 10         | 15    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 30         | 170.90 | 0.00   | 10         | 25    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 40         | 170.90 | 0.00   | 10         | 35    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 50         | 170.90 | 0.00   | 10         | 45    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 60         | 166.70 | 0.00   | 10         | 55    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 80         | 343.89 | 8.06   | 20         | 70    | 0.02344 | 0.00804 | 0.16074           | 0.469            | 32.81                  |
| 100        | 345.63 | 6.95   | 20         | 90    | 0.02011 | 0.00690 | 0.13790           | 0.402            | 36.19                  |
| 110        | 174.22 | 2.74   | 10         | 105   | 0.01573 | 0.00539 | 0.05393           | 0.157            | 16.51                  |
| 120        | 172.67 | 2.26   | 10         | 115   | 0.01309 | 0.00449 | 0.04488           | 0.131            | 15.05                  |
| 130        | 168.95 | 2.09   | 10         | 125   | 0.01237 | 0.00424 | 0.04242           | 0.124            | 15.46                  |
| 140        | 171.15 | 1.97   | 10         | 135   | 0.01151 | 0.00395 | 0.03947           | 0.115            | 15.54                  |
| 150        | 168.40 | 1.97   | 10         | 145   | 0.01010 | 0.00346 | 0.03462           | 0.101            | 14.64                  |
| 160        | 172.76 | 1.70   | 10         | 155   | 0.00891 | 0.00306 | 0.03057           | 0.089            | 13.82                  |
| 170        | 172.42 | 1.54   | 10         | 165   | 0.00882 | 0.00302 | 0.03023           | 0.088            | 14.55                  |
| 180        | 171.09 | 1.52   | 10         | 175   | 0.00810 | 0.00278 | 0.02776           | 0.081            | 14.17                  |
| 190        | 172.87 | 1.39   | 10         | 185   | 0.00758 | 0.00260 | 0.02599           | 0.076            | 14.02                  |
| 200        | 168.60 | 1.31   | 10         | 195   | 0.00712 | 0.00244 | 0.02441           | 0.071            | 13.88                  |
| 210        | 168.24 | 1.20   | 10         | 205   | 0.00684 | 0.00234 | 0.02344           | 0.068            | 14.01                  |
| 220        | 171.58 | 1.15   | 10         | 215   | 0.00688 | 0.00236 | 0.02358           | 0.069            | 14.79                  |
| 230        | 174.68 | 1.18   | 10         | 225   | 0.00492 | 0.00169 | 0.01688           | 0.049            | 11.08                  |
| 240        | 170.99 | 0.86   | 10         | 235   | 0.00526 | 0.00180 | 0.01805           | 0.053            | 12.37                  |
| 250        | 170.43 | 0.90   | 10         | 245   | 0.00434 | 0.00149 | 0.01489           | 0.043            | 10.64                  |
| 260        | 169.46 | 0.74   | 10         | 255   | 0.00378 | 0.00130 | 0.01295           | 0.038            | 9.63                   |
| 270        | 169.45 | 0.64   | 10         | 265   | 0.00354 | 0.00121 | 0.01214           | 0.035            | 9.38                   |
| 280        | 170.98 | 0.60   | 10         | 275   | 0.00386 | 0.00132 | 0.01324           | 0.039            | 10.62                  |
| 290        | 168.84 | 0.66   | 10         | 285   | 0.00361 | 0.00124 | 0.01239           | 0.036            | 10.30                  |
| 300        | 172.44 | 0.61   | 10         | 295   | 0.00336 | 0.00115 | 0.01153           | 0.034            | 9.92                   |
| 310        | 169.62 | 0.58   | 10         | 305   | 0.00318 | 0.00109 | 0.01092           | 0.032            | 9.71                   |
| 320        | 171.18 | 0.54   | 10         | 315   | 0.00292 | 0.00100 | 0.01002           | 0.029            | 9.20                   |
| 330        | 172.03 | 0.50   | 10         | 325   | 0.00221 | 0.00076 | 0.00757           | 0.022            | 7.18                   |
| 340        | 171.23 | 0.38   | 10         | 335   | 0.00228 | 0.00078 | 0.00781           | 0.023            | 7.63                   |
| 350        | 172.60 | 0.39   | 10         | 345   | 0.00197 | 0.00068 | 0.00675           | 0.020            | 6.80                   |
| 360        | 174.00 | 0.34   | 10         | 355   | 0.00132 | 0.00045 | 0.00453           | 0.013            | 4.69                   |
| 370        | 169.03 | 0.23   | 10         | 365   | 0.00175 | 0.00060 | 0.00598           | 0.017            | 6.37                   |
| 380        | 172.42 | 0.30   | 10         | 375   | 0.00180 | 0.00062 | 0.00617           | 0.018            | 6.74                   |
| 390        | 165.89 | 0.31   | 10         | 385   | 0.00181 | 0.00062 | 0.00620           | 0.018            | 6.96                   |
| 400        | 173.65 | 0.30   | 10         | 395   | 0.00104 | 0.00036 | 0.00355           | 0.010            | 4.09                   |
| 410        | 171.12 | 0.18   | 10         | 405   | 0.00169 | 0.00058 | 0.00581           | 0.017            | 6.86                   |
| 420        | 171.34 | 0.29   | 10         | 415   | 0.00152 | 0.00052 | 0.00520           | 0.015            | 6.30                   |
| 430        | 169.41 | 0.26   | 10         | 425   | 0.00118 | 0.00040 | 0.00405           | 0.012            | 5.02                   |
| 440        | 174.58 | 0.20   | 10         | 435   | 0.00115 | 0.00039 | 0.00393           | 0.011            | 4.98                   |
| 450        | 170.27 | 0.20   | 10         | 445   | 0.00150 | 0.00051 | 0.00514           | 0.015            | 6.66                   |
| 460        | 168.82 | 0.26   | 10         | 455   | 0.00124 | 0.00043 | 0.00427           | 0.012            | 5.66                   |
| 470        | 171.17 | 0.21   | 10         | 465   | 0.00099 | 0.00034 | 0.00341           | 0.010            | 4.62                   |
| 480        | 168.65 | 0.17   | 10         | 475   | 0.00053 | 0.00018 | 0.00183           | 0.005            | 2.53                   |
| 490        | 170.22 | 0.09   | 10         | 485   | 0.00094 | 0.00032 | 0.00322           | 0.009            | 4.56                   |
| 500        | 169.71 | 0.16   | 10         | 495   | 0.00106 | 0.00036 | 0.00364           | 0.011            | 5.25                   |
| 510        | 169.90 | 0.18   | 10         | 505   | 0.00059 | 0.00020 | 0.00202           | 0.006            | 2.97                   |
| 520        | 165.85 | 0.10   | 10         | 515   | 0.00054 | 0.00019 | 0.00186           | 0.005            | 2.79                   |
| 530        | 175.32 | 0.09   | 10         | 525   | 0.00063 | 0.00022 | 0.00215           | 0.006            | 3.29                   |
| 540        | 172.00 | 0.11   | 10         | 535   | 0.00047 | 0.00016 | 0.00159           | 0.005            | 2.49                   |

## Run#2007 (Cont..)

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|-------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 550        | 0.08  | 17.05  | 10         | 545   | 0.00070 | 0.00024 | 0.00241           | 0.007            | 3.84                   |
| 560        | 0.12  | 17.07  | 10         | 555   | 0.00070 | 0.00024 | 0.00241           | 0.007            | 3.90                   |
| 570        | 0.12  | 17.24  | 10         | 565   | 0.00052 | 0.00018 | 0.00179           | 0.005            | 2.95                   |
| 580        | 0.09  | 17.23  | 10         | 575   | 0.00029 | 0.00010 | 0.00099           | 0.003            | 1.67                   |
| 590        | 0.05  | 16.93  | 10         | 585   | 0.00024 | 0.00008 | 0.00081           | 0.002            | 1.38                   |
| 600        | 0.04  | 17.24  | 10         | 595   | 0.00070 | 0.00024 | 0.00239           | 0.007            | 4.14                   |
| 610        | 0.12  | 17.07  | 10         | 605   | 0.00018 | 0.00006 | 0.00060           | 0.002            | 1.06                   |
| 620        | 0.03  | 16.83  | 10         | 615   | 0.00018 | 0.00006 | 0.00061           | 0.002            | 1.10                   |
| 630        | 0.03  | 17.07  | 10         | 625   | 0.00023 | 0.00008 | 0.00080           | 0.002            | 1.46                   |
| 640        | 0.04  | 17.16  | 10         | 635   | 0.00035 | 0.00012 | 0.00120           | 0.003            | 2.22                   |
| 650        | 0.06  | 16.92  | 10         | 645   | 0.00050 | 0.00017 | 0.00172           | 0.005            | 3.24                   |
| 660        | 0.09  | 17.14  | 10         | 655   | 0.00023 | 0.00008 | 0.00080           | 0.002            | 1.53                   |
| 664        | 0.04  | 17.09  | 4          | 662.1 | 0.00056 | 0.00019 | 0.00080           | 0.002            | 1.55                   |

$$\Sigma E(t) \Delta t = 0.94697$$

|                       |
|-----------------------|
| $S_o = 17.1$ g/s      |
| Bed weight = 3074.0 g |
| $\tau = 180$ sec      |

|                      |                                   |
|----------------------|-----------------------------------|
| $\tau_{obs} = 179.9$ | $\Sigma C_i t_i \Delta t = 496.5$ |
|                      | $\Sigma C_i \Delta t = 2.76$      |

Table D.23 Data Run#2008

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 0          | 70.90  | 0.00   | 20         | 0     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 6          | 70.90  | 0.00   | 20         | 6     | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 26         | 70.90  | 0.00   | 20         | 16    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 46         | 70.90  | 0.00   | 20         | 36    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 66         | 70.90  | 0.00   | 20         | 56    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 86         | 70.90  | 0.00   | 20         | 76    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 106        | 70.90  | 0.00   | 20         | 96    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 126        | 70.90  | 0.00   | 20         | 11    | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 146        | 70.90  | 0.00   | 20         | 136   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 166        | 70.90  | 0.00   | 20         | 156   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 186        | 70.90  | 0.00   | 20         | 176   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 206        | 70.90  | 0.00   | 20         | 196   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 226        | 70.90  | 0.00   | 20         | 216   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 246        | 70.90  | 0.00   | 20         | 236   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 266        | 70.90  | 0.00   | 20         | 256   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 286        | 70.90  | 0.00   | 20         | 276   | 0.00000 | 0.00000 | 0.00000           | 0.000            | 0.00                   |
| 306        | 36.48  | 0.01   | 5          | 286   | 0.00027 | 0.00004 | 0.00019           | 0.001            | 0.39                   |
| 316        | 73.19  | 1.1    | 10         | 31    | 0.01599 | 0.00227 | 0.02267           | 0.160            | 49.72                  |
| 326        | 70.86  | 5.24   | 10         | 321   | 0.07395 | 0.01049 | 0.10487           | 0.739            | 237.38                 |
| 336        | 69.86  | 7.48   | 10         | 331   | 0.10707 | 0.0151  | 0.1518            | 1.07             | 354.41                 |
| 346        | 72.44  | 7.23   | 10         | 341   | 0.09981 | 0.0141  | 0.1415            | 0.998            | 340.34                 |
| 356        | 70.89  | 5.02   | 10         | 351   | 0.07081 | 0.01004 | 0.10043           | 0.708            | 248.56                 |
| 366        | 72.55  | 4.08   | 10         | 361   | 0.05624 | 0.00798 | 0.07976           | 0.562            | 203.02                 |
| 376        | 72.13  | 2.73   | 10         | 371   | 0.03778 | 0.00536 | 0.05358           | 0.378            | 140.1                  |
| 386        | 70.08  | 2.47   | 10         | 381   | 0.03525 | 0.00500 | 0.04999           | 0.352            | 134.29                 |
| 396        | 72.08  | 1.93   | 10         | 391   | 0.02678 | 0.00380 | 0.03797           | 0.268            | 104.69                 |
| 406        | 70.07  | 1.57   | 10         | 401   | 0.02241 | 0.00318 | 0.03178           | 0.224            | 89.85                  |
| 416        | 70.51  | 1.1    | 10         | 41    | 0.0161  | 0.00229 | 0.02293           | 0.162            | 66.45                  |
| 426        | 69.62  | 1.1    | 10         | 421   | 0.01580 | 0.00224 | 0.02241           | 0.158            | 66.52                  |
| 436        | 71.25  | 0.98   | 10         | 431   | 0.01375 | 0.00195 | 0.0195            | 0.138            | 59.28                  |
| 446        | 71.25  | 0.80   | 10         | 441   | 0.0112  | 0.00159 | 0.01592           | 0.11             | 49.52                  |
| 456        | 71.1   | 0.72   | 10         | 451   | 0.0101  | 0.00143 | 0.01435           | 0.10             | 45.62                  |
| 466        | 69.82  | 0.60   | 10         | 461   | 0.00859 | 0.00122 | 0.0121            | 0.086            | 39.62                  |
| 476        | 70.35  | 0.48   | 10         | 471   | 0.00682 | 0.00097 | 0.00968           | 0.068            | 32.14                  |
| 486        | 70.35  | 0.57   | 10         | 481   | 0.00810 | 0.0011  | 0.0114            | 0.081            | 38.97                  |
| 496        | 70.17  | 0.44   | 10         | 491   | 0.00627 | 0.00089 | 0.00889           | 0.063            | 30.79                  |
| 506        | 70.48  | 0.33   | 10         | 501   | 0.00468 | 0.00066 | 0.00664           | 0.047            | 23.46                  |
| 516        | 71.1   | 0.36   | 10         | 51    | 0.00506 | 0.00072 | 0.00718           | 0.051            | 25.87                  |
| 526        | 70.66  | 0.32   | 10         | 521   | 0.00453 | 0.00064 | 0.00642           | 0.045            | 23.59                  |
| 536        | 71.50  | 0.28   | 10         | 531   | 0.00392 | 0.00056 | 0.00555           | 0.039            | 20.79                  |
| 546        | 72.04  | 0.17   | 10         | 541   | 0.00236 | 0.00033 | 0.00335           | 0.024            | 12.77                  |
| 556        | 72.27  | 0.21   | 10         | 551   | 0.00291 | 0.00041 | 0.00412           | 0.029            | 16.0                   |
| 566        | 69.60  | 0.17   | 10         | 561   | 0.00244 | 0.00035 | 0.00346           | 0.024            | 13.70                  |
| 576        | 70.95  | 0.15   | 10         | 571   | 0.0021  | 0.00030 | 0.00300           | 0.021            | 12.07                  |
| 586        | 69.69  | 0.16   | 10         | 581   | 0.00230 | 0.00033 | 0.00326           | 0.023            | 13.34                  |
| 596        | 73.83  | 0.13   | 10         | 591   | 0.00176 | 0.00025 | 0.00250           | 0.018            | 10.4                   |
| 606        | 68.14  | 0.10   | 10         | 601   | 0.00147 | 0.00021 | 0.00208           | 0.015            | 8.82                   |
| 626        | 140.1  | 0.29   | 20         | 616   | 0.00207 | 0.00029 | 0.00587           | 0.041            | 25.49                  |
| 646        | 143.40 | 0.19   | 20         | 636   | 0.00132 | 0.00019 | 0.00376           | 0.026            | 16.85                  |
| 666        | 142.34 | 0.19   | 20         | 656   | 0.00133 | 0.00019 | 0.00379           | 0.027            | 17.5                   |
| 686        | 141.2  | 0.13   | 20         | 676   | 0.00092 | 0.00013 | 0.00261           | 0.018            | 12.45                  |
| 706        | 140.92 | 0.15   | 20         | 696   | 0.00106 | 0.00015 | 0.00302           | 0.021            | 14.82                  |
| 726        | 141.7  | 0.15   | 20         | 716   | 0.00106 | 0.00015 | 0.00300           | 0.021            | 15.1                   |
| 756        | 213.3  | 0.1    | 30         | 741   | 0.00052 | 0.00007 | 0.00219           | 0.015            | 11.4                   |
| 786        | 211.1  | 0.08   | 30         | 771   | 0.00038 | 0.00005 | 0.0016            | 0.01             | 8.76                   |
| 816        | 213.59 | 0.05   | 30         | 801   | 0.00023 | 0.00003 | 0.00100           | 0.007            | 5.63                   |
| 846        | 211.2  | 0.06   | 30         | 831   | 0.00028 | 0.00004 | 0.0012            | 0.009            | 7.08                   |
| 876        | 211.5  | 0.03   | 30         | 861   | 0.00014 | 0.00002 | 0.00060           | 0.004            | 3.66                   |
| 906        | 209.75 | 0.06   | 30         | 891   | 0.00029 | 0.00004 | 0.00122           | 0.009            | 7.65                   |
| 936        | 211.7  | 0.05   | 30         | 921   | 0.00024 | 0.00003 | 0.00100           | 0.007            | 6.53                   |
| 956        | 139.92 | 0.02   | 20         | 945.9 | 0.00014 | 0.00002 | 0.00040           | 0.003            | 2.67                   |

$$\Sigma E(t) \Delta t = 0.99083$$

|                       |
|-----------------------|
| $S_o = 7.09$ g/s      |
| Bed weight = 2763.0 g |
| $\tau = 389.80$ sec   |

|                      |                                    |
|----------------------|------------------------------------|
| $\tau_{obs} = 381.9$ | $\Sigma C_i t_i \Delta t = 2668.2$ |
|                      | $\Sigma C_i \Delta t = 6.99$       |

Table D.24 Data Run#2009

| Time (sec) | Total | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t \cdot E(t)$ | $C_i \cdot \Delta t$ | $C_i \cdot t_i \cdot \Delta t$ |
|------------|-------|--------|------------|-------|---------|---------|-----------------------|----------------------|--------------------------------|
| 0          | 70.30 | 0.00   | 10         | 0     | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 4          | 70.30 | 0.00   | 10         | 2     | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 14         | 70.30 | 0.00   | 10         | 9     | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 24         | 70.30 | 0.00   | 10         | 19    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 34         | 70.30 | 0.00   | 10         | 29    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 44         | 70.30 | 0.00   | 10         | 39    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 54         | 70.30 | 0.00   | 10         | 49    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 64         | 70.30 | 0.00   | 10         | 59    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 74         | 70.30 | 0.00   | 10         | 69    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 84         | 70.30 | 0.00   | 10         | 79    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 94         | 70.30 | 0.00   | 10         | 89    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 104        | 70.30 | 0.00   | 10         | 99    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 11         | 70.30 | 0.00   | 10         | 109   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 124        | 70.30 | 0.00   | 10         | 11    | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 134        | 70.30 | 0.00   | 10         | 129   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 144        | 70.30 | 0.00   | 10         | 139   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 154        | 70.30 | 0.00   | 10         | 149   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 164        | 70.30 | 0.00   | 10         | 159   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 174        | 70.30 | 0.00   | 10         | 169   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 184        | 70.30 | 0.00   | 10         | 179   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 194        | 70.30 | 0.00   | 10         | 189   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 204        | 70.30 | 0.00   | 10         | 199   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 214        | 70.30 | 0.00   | 10         | 209   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 224        | 70.30 | 0.00   | 10         | 219   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 234        | 70.30 | 0.00   | 10         | 229   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 244        | 70.30 | 0.00   | 10         | 239   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 254        | 74.40 | 0.00   | 10         | 249   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 264        | 76.12 | 0.00   | 10         | 259   | 0.00000 | 0.00000 | 0.00000               | 0.000                | 0.00                           |
| 274        | 73.18 | 0.03   | 10         | 269   | 0.00041 | 0.00012 | 0.00124               | 0.001                | 1.1                            |
| 284        | 75.46 | 0.71   | 10         | 279   | 0.00941 | 0.00285 | 0.02852               | 0.029                | 26.25                          |
| 294        | 72.44 | 0.67   | 10         | 289   | 0.00925 | 0.00280 | 0.02803               | 0.028                | 26.73                          |
| 304        | 68.62 | 0.46   | 10         | 299   | 0.00670 | 0.00203 | 0.02032               | 0.020                | 20.04                          |
| 314        | 71.39 | 0.60   | 10         | 309   | 0.00840 | 0.00255 | 0.02547               | 0.025                | 25.97                          |
| 324        | 70.1  | 0.59   | 10         | 319   | 0.00842 | 0.00255 | 0.02551               | 0.026                | 26.85                          |
| 334        | 72.37 | 0.44   | 10         | 329   | 0.00608 | 0.00184 | 0.01843               | 0.018                | 20.00                          |
| 344        | 70.43 | 0.58   | 10         | 339   | 0.00824 | 0.00250 | 0.02496               | 0.025                | 27.92                          |
| 354        | 73.79 | 0.50   | 10         | 349   | 0.00678 | 0.00205 | 0.02054               | 0.021                | 23.65                          |
| 364        | 72.48 | 0.53   | 10         | 359   | 0.00731 | 0.00222 | 0.02216               | 0.022                | 26.25                          |
| 374        | 71.59 | 0.43   | 10         | 369   | 0.00601 | 0.00182 | 0.0182                | 0.018                | 22.16                          |
| 384        | 70.91 | 0.49   | 10         | 379   | 0.00691 | 0.00209 | 0.02094               | 0.021                | 26.19                          |
| 394        | 68.42 | 0.59   | 10         | 389   | 0.00862 | 0.00261 | 0.02614               | 0.026                | 33.54                          |
| 404        | 68.00 | 0.42   | 10         | 399   | 0.00618 | 0.00187 | 0.01872               | 0.019                | 24.64                          |
| 414        | 73.90 | 0.44   | 10         | 409   | 0.00595 | 0.00180 | 0.01805               | 0.018                | 24.35                          |
| 424        | 68.45 | 0.47   | 10         | 419   | 0.00687 | 0.00208 | 0.02081               | 0.021                | 28.77                          |
| 434        | 75.42 | 0.39   | 10         | 429   | 0.00517 | 0.00157 | 0.01567               | 0.016                | 22.18                          |
| 444        | 70.18 | 0.49   | 10         | 439   | 0.00698 | 0.00212 | 0.0211                | 0.021                | 30.65                          |
| 454        | 69.63 | 0.38   | 10         | 449   | 0.00546 | 0.00165 | 0.01654               | 0.017                | 24.50                          |
| 464        | 71.23 | 0.46   | 10         | 459   | 0.00646 | 0.00196 | 0.01957               | 0.020                | 29.64                          |
| 474        | 71.1  | 0.43   | 10         | 469   | 0.00604 | 0.00183 | 0.01832               | 0.018                | 28.34                          |
| 484        | 71.95 | 0.46   | 10         | 479   | 0.00639 | 0.00194 | 0.01938               | 0.019                | 30.62                          |
| 494        | 72.78 | 0.37   | 10         | 489   | 0.00508 | 0.00154 | 0.0154                | 0.015                | 24.86                          |
| 504        | 65.44 | 0.43   | 10         | 499   | 0.00657 | 0.00199 | 0.01992               | 0.020                | 32.79                          |
| 514        | 71.3  | 0.50   | 10         | 509   | 0.00701 | 0.00213 | 0.02125               | 0.021                | 35.69                          |
| 524        | 72.32 | 0.44   | 10         | 519   | 0.00608 | 0.00184 | 0.01844               | 0.018                | 31.58                          |
| 534        | 69.56 | 0.39   | 10         | 529   | 0.00561 | 0.00170 | 0.01699               | 0.017                | 29.66                          |
| 544        | 73.45 | 0.34   | 10         | 539   | 0.00463 | 0.00140 | 0.01403               | 0.014                | 24.95                          |
| 554        | 69.39 | 0.28   | 10         | 549   | 0.00404 | 0.00122 | 0.01223               | 0.012                | 22.15                          |
| 564        | 72.90 | 0.35   | 10         | 559   | 0.00480 | 0.00146 | 0.01455               | 0.015                | 26.84                          |
| 574        | 72.29 | 0.46   | 10         | 569   | 0.00636 | 0.00193 | 0.01929               | 0.019                | 36.21                          |
| 584        | 70.56 | 0.34   | 10         | 579   | 0.00482 | 0.00146 | 0.0146                | 0.015                | 27.90                          |
| 594        | 71.32 | 0.33   | 10         | 589   | 0.00463 | 0.00140 | 0.01402               | 0.014                | 27.25                          |
| 604        | 73.45 | 0.28   | 10         | 599   | 0.00381 | 0.0011  | 0.0115                | 0.012                | 22.83                          |
| 614        | 70.67 | 0.24   | 10         | 609   | 0.00340 | 0.00103 | 0.01029               | 0.010                | 20.68                          |
| 624        | 68.90 | 0.30   | 10         | 619   | 0.00435 | 0.00132 | 0.01320               | 0.013                | 26.95                          |
| 634        | 67.80 | 0.23   | 10         | 629   | 0.00339 | 0.00103 | 0.01028               | 0.010                | 21.34                          |
| 644        | 69.97 | 0.26   | 10         | 639   | 0.00372 | 0.0011  | 0.0112                | 0.01                 | 23.74                          |
| 654        | 65.45 | 0.23   | 10         | 649   | 0.00351 | 0.00107 | 0.01065               | 0.01                 | 22.81                          |
| 664        | 74.18 | 0.29   | 10         | 659   | 0.00391 | 0.0011  | 0.0118                | 0.012                | 25.76                          |



## Run#2009 ( Cont..)

| Time (sec) | Total  | Tracer | $\Delta t$ | $t_i$ | $C(t)$  | $E(t)$  | $\Delta t * E(t)$ | $C_i * \Delta t$ | $C_i * t_i * \Delta t$ |
|------------|--------|--------|------------|-------|---------|---------|-------------------|------------------|------------------------|
| 674        | 69.95  | 0.23   | 10         | 669   | 0.00329 | 0.00100 | 0.00997           | 0.033            | 22.00                  |
| 684        | 70.06  | 0.22   | 10         | 679   | 0.00314 | 0.00095 | 0.00952           | 0.031            | 21.32                  |
| 694        | 71.32  | 0.25   | 10         | 689   | 0.00351 | 0.00106 | 0.01062           | 0.035            | 24.15                  |
| 704        | 70.47  | 0.17   | 10         | 699   | 0.00241 | 0.00073 | 0.00731           | 0.024            | 16.86                  |
| 714        | 68.36  | 0.19   | 10         | 709   | 0.00278 | 0.00084 | 0.00842           | 0.028            | 19.71                  |
| 724        | 72.38  | 0.20   | 10         | 719   | 0.00276 | 0.00084 | 0.00838           | 0.028            | 19.87                  |
| 734        | 74.85  | 0.16   | 10         | 729   | 0.00214 | 0.00065 | 0.00648           | 0.021            | 15.58                  |
| 744        | 70.17  | 0.16   | 10         | 739   | 0.00228 | 0.00069 | 0.00691           | 0.023            | 16.85                  |
| 754        | 70.70  | 0.14   | 10         | 749   | 0.00198 | 0.00060 | 0.00600           | 0.020            | 14.83                  |
| 764        | 71.64  | 0.20   | 10         | 759   | 0.00279 | 0.00085 | 0.00846           | 0.028            | 21.19                  |
| 784        | 71.47  | 0.22   | 20         | 774   | 0.00308 | 0.00093 | 0.01866           | 0.062            | 47.65                  |
| 804        | 138.91 | 0.28   | 20         | 794   | 0.00202 | 0.00061 | 0.01222           | 0.040            | 32.01                  |
| 824        | 140.85 | 0.30   | 20         | 814   | 0.00213 | 0.00065 | 0.01291           | 0.043            | 34.68                  |
| 844        | 140.53 | 0.32   | 20         | 834   | 0.00228 | 0.00069 | 0.01380           | 0.046            | 37.98                  |
| 864        | 145.76 | 0.22   | 20         | 854   | 0.00151 | 0.00046 | 0.00915           | 0.030            | 25.78                  |
| 884        | 141.37 | 0.29   | 20         | 874   | 0.00205 | 0.00062 | 0.01244           | 0.041            | 35.86                  |
| 904        | 141.17 | 0.15   | 20         | 894   | 0.00106 | 0.00032 | 0.00644           | 0.021            | 19.00                  |
| 924        | 141.98 | 0.29   | 20         | 914   | 0.00204 | 0.00062 | 0.01238           | 0.041            | 37.34                  |
| 944        | 140.30 | 0.22   | 20         | 934   | 0.00157 | 0.00048 | 0.00951           | 0.031            | 29.29                  |
| 964        | 140.02 | 0.20   | 20         | 954   | 0.00143 | 0.00043 | 0.00866           | 0.029            | 27.25                  |
| 984        | 143.00 | 0.19   | 20         | 974   | 0.00133 | 0.00040 | 0.00805           | 0.027            | 25.88                  |
| 1004       | 145.08 | 0.21   | 20         | 994   | 0.00145 | 0.00044 | 0.00877           | 0.029            | 28.78                  |
| 1024       | 141.26 | 0.18   | 20         | 1014  | 0.00127 | 0.00039 | 0.00772           | 0.025            | 25.84                  |
| 1044       | 139.06 | 0.13   | 20         | 1034  | 0.00093 | 0.00028 | 0.00567           | 0.019            | 19.33                  |
| 1064       | 146.55 | 0.11   | 20         | 1054  | 0.00075 | 0.00023 | 0.00455           | 0.015            | 15.82                  |
| 1084       | 135.28 | 0.11   | 20         | 1074  | 0.00081 | 0.00025 | 0.00493           | 0.016            | 17.47                  |
| 1104       | 137.31 | 0.11   | 20         | 1094  | 0.00080 | 0.00024 | 0.00486           | 0.016            | 17.53                  |
| 1124       | 140.64 | 0.10   | 20         | 1114  | 0.00071 | 0.00022 | 0.00431           | 0.014            | 15.84                  |
| 1144       | 137.60 | 0.15   | 20         | 1134  | 0.00109 | 0.00033 | 0.00661           | 0.022            | 24.72                  |
| 1164       | 140.88 | 0.07   | 20         | 1154  | 0.00050 | 0.00015 | 0.00301           | 0.010            | 11.47                  |
| 1184       | 142.99 | 0.11   | 20         | 1174  | 0.00077 | 0.00023 | 0.00466           | 0.015            | 18.06                  |
| 1204       | 142.30 | 0.05   | 20         | 1194  | 0.00035 | 0.00011 | 0.00213           | 0.007            | 8.39                   |
| 1224       | 139.34 | 0.07   | 20         | 1214  | 0.00050 | 0.00015 | 0.00305           | 0.010            | 12.20                  |
| 1244       | 140.76 | 0.05   | 20         | 1234  | 0.00036 | 0.00011 | 0.00215           | 0.007            | 8.77                   |
| 1264       | 137.65 | 0.03   | 20         | 1254  | 0.00022 | 0.00007 | 0.00132           | 0.004            | 5.47                   |
| 1284       | 142.31 | 0.08   | 20         | 1274  | 0.00056 | 0.00017 | 0.00341           | 0.011            | 14.32                  |
| 1304       | 138.15 | 0.06   | 20         | 1294  | 0.00043 | 0.00013 | 0.00263           | 0.009            | 11.24                  |
| 1334       | 142.07 | 0.05   | 30         | 1319  | 0.00035 | 0.00011 | 0.00320           | 0.011            | 13.93                  |
| 1364       | 214.81 | 0.07   | 30         | 1349  | 0.00033 | 0.00010 | 0.00296           | 0.010            | 13.19                  |
| 1394       | 212.73 | 0.07   | 30         | 1379  | 0.00033 | 0.00010 | 0.00299           | 0.010            | 13.61                  |
| 1424       | 217.46 | 0.06   | 30         | 1409  | 0.00028 | 0.00008 | 0.00251           | 0.008            | 11.66                  |
| 1454       | 211.65 | 0.09   | 30         | 1439  | 0.00043 | 0.00013 | 0.00387           | 0.013            | 18.36                  |
| 1484       | 213.39 | 0.03   | 30         | 1469  | 0.00014 | 0.00004 | 0.00128           | 0.004            | 6.20                   |
| 1514       | 209.91 | 0.04   | 30         | 1499  | 0.00019 | 0.00006 | 0.00173           | 0.006            | 8.57                   |
| 1544       | 205.56 | 0.02   | 30         | 1529  | 0.00010 | 0.00003 | 0.00088           | 0.003            | 4.46                   |
| 1574       | 210.24 | 0.01   | 30         | 1559  | 0.00005 | 0.00001 | 0.00043           | 0.001            | 2.22                   |
| 1604       | 213.50 | 0.03   | 30         | 1589  | 0.00014 | 0.00004 | 0.00128           | 0.004            | 6.70                   |
| 1634       | 214.65 | 0.04   | 30         | 1619  | 0.00019 | 0.00006 | 0.00169           | 0.006            | 9.05                   |
| 1664       | 214.31 | 0.03   | 30         | 1649  | 0.00014 | 0.00004 | 0.00127           | 0.004            | 6.93                   |
| 1660.78    | 188.29 | 0.02   | 27         | 1653  | 0.00011 | 0.00003 | 0.00086           | 0.003            | 4.70                   |

$$\Sigma E(t) \Delta t_i = 1.0000$$

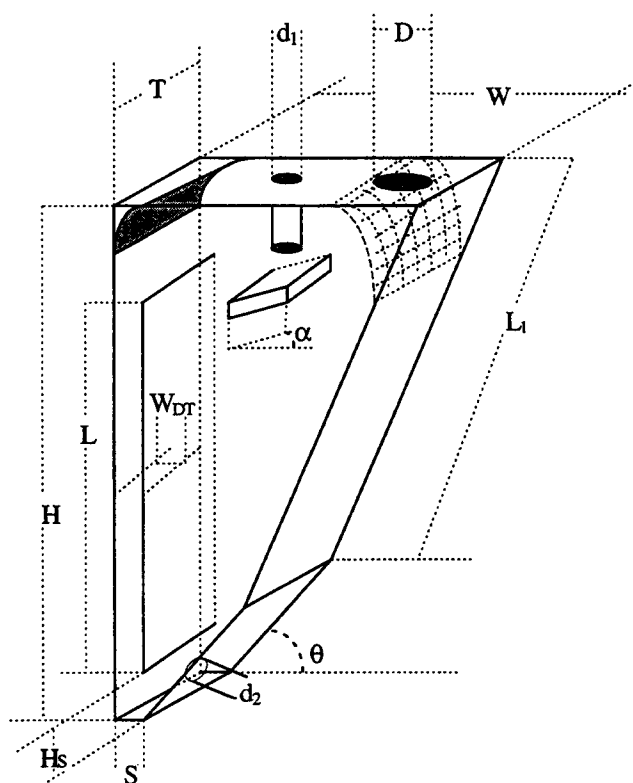
|                     |
|---------------------|
| $S_o = 7.029$ g/s   |
| Bed weight = 2962 g |
| $\tau = 421.4$ sec  |

|                      |                                       |
|----------------------|---------------------------------------|
| $\tau_{obs} = 414.2$ | $\Sigma C_i t_i \Delta t_i = 1379.77$ |
|                      | $\Sigma C_i \Delta t_i = 3.331$       |

## APPENDIX E

### IDENTICAL STAGES TEST

The three-stage column was built using three stages as close to identical as possible. The following diagram (Figure E.1) shows the particular geometry of the designed vessels. Table E.1 shows the experimental measurements for each vessel, and Table E.2 the experimental data used/obtained in a particular set of operating-test conditions.



**Figure E.1** Diagram of the designed vessels.

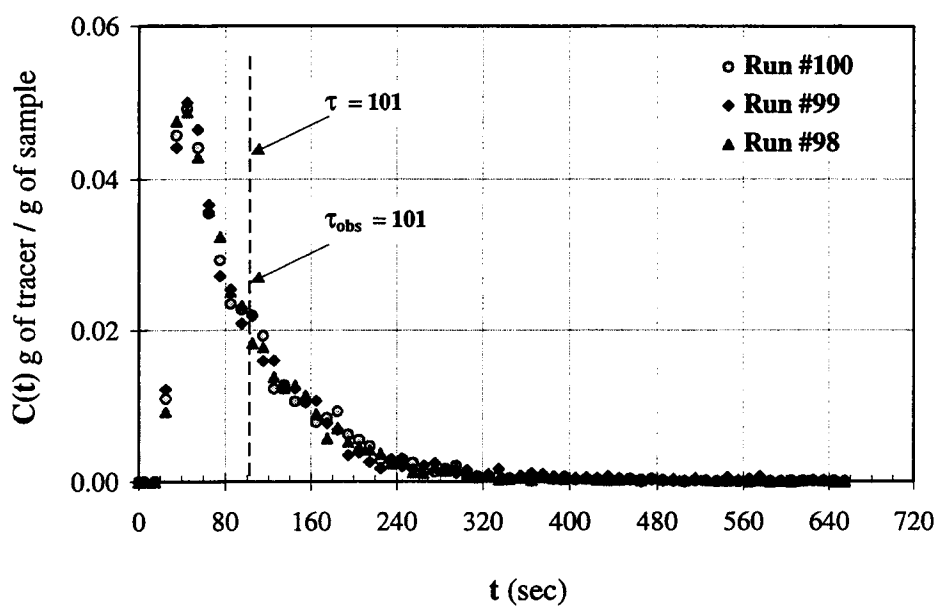
|                                | VESSEL 1 | VESSEL 2 | VESSEL 3 |
|--------------------------------|----------|----------|----------|
| <b>H</b>                       | 33.0     | 33.0     | 33.0     |
| <b>W</b>                       | 18.0     | 18.0     | 18.0     |
| <b>T</b>                       | 4.0      | 4.0      | 4.0      |
| <b>L</b>                       | 22.7     | 22.7     | 22.4     |
| <b>L<sub>1</sub></b>           | 30.0     | 30.1     | 30.0     |
| <b>H<sub>S</sub></b>           | 1.6      | 1.7      | 1.6      |
| <b>S</b>                       | 0.32     | 0.32     | 0.32     |
| <b>D</b>                       | 3.0      | 3.0      | 3.0      |
| <b>d<sub>1</sub></b>           | 1.6      | 1.6      | 1.6      |
| <b>d<sub>2</sub></b>           | 1.6      | 1.6      | 1.6      |
| <b>W<sub>DT</sub></b>          | 1.9      | 1.9      | 1.9      |
| <b><math>\alpha</math> (°)</b> | 25       | 24       | 23       |
| <b><math>\theta</math> (°)</b> | 44       | 44       | 42       |

**Table E.1** Construction data. Experimental measurements in cm.

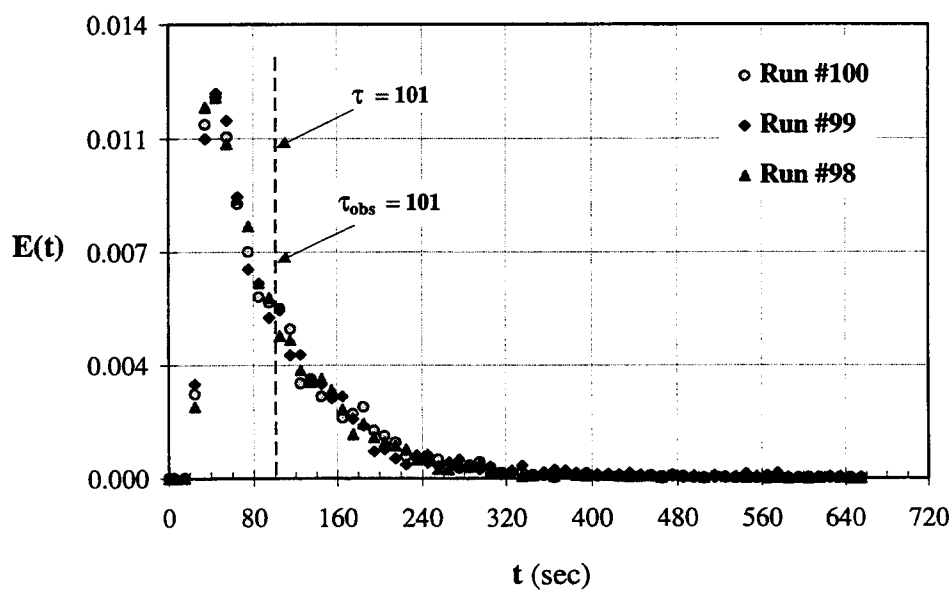
|                                    | RUN #98 | RUN #99 | RUN #100 |
|------------------------------------|---------|---------|----------|
| <b>Bed weight (g)</b>              | 1215.5  | 1225    | 1210     |
| <b>S<sub>o</sub> (g/s)</b>         | 12.03   | 11.88   | 11.95    |
| <b><math>\tau</math> (s)</b>       | 101.0   | 103.1   | 101.25   |
| <b><math>\tau_{obs}</math> (s)</b> | 100.2   | 102.7   | 100.6    |
| <b><math>\tau_p</math> (s)</b>     | 28.4    | 28.38   | 27.64    |
| <b><math>\tau_M</math> (s)</b>     | 71.8    | 74.3    | 73.0     |
| <b>GFR (lit/sec)</b>               | 3.7     | 3.7     | 3.7      |
| <b>Tracer weight (g)</b>           | 50.0    | 50.0    | 50.0     |

**Table E.2** Operating data used/obtained in testing the vessels.

Figure E.2 shows the concentration curves from these experiments, while Figure E.3 shows the corresponding  $E(t)$  curves. There is no reason to suspect that the stages would behave differently when used separately.



**Figure E.2**  $C(t)$  curves of experiments to test identical stage behavior.



**Figure E.3**  $E(t)$  curves of experiments to test identical stage behavior.