## AN ABSTRACT OF THE THESIS OF

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A fully integrated CMOS latched comparator is presented for use as a wake-up circuit that is attached to an RF energy harvester in a battery free wireless sensor network. The system consumes less than 36 nA static current at $20^{\circ} \mathrm{C}$ and dissipates 2 pJ of energy per conversion. The comparator comprises of a series of level-shifting leakage-mode inverters. Its latching behavior is obtained by supplying the power to each stage from the inverted output of the last stage via a resistor-string voltage divider. This 45 nW circuit is the solution with the lowest static power consumption proposed to date for synchronizing nodes in a sensor network.
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# A Nano-Power Wake-Up Circuit for RF Energy Harvesting Wireless Sensor Networks 

 byChristopher J. Lindsley

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A Nano-Power Wake-Up Circuit for RF Energy Harvesting Wireless Sensor Networks

## 1. Introduction

Battery-free wireless sensor networks offer a highly flexible and low-cost method to monitor environmental conditions with minimal human interference [1]. Early generation wireless sensor networks operated with relatively high power, necessitating the use of batteries [2]. Periodic replacement of the batteries adds maintenance that becomes difficult if the sensor network is deployed in hard to access areas. Recent developments in powering wireless sensors have made it possible to harvest power from a remote source [3]. However, the power available in the environment, either ambient power or power delivered from an RF source, is not enough to power the sensor continuously. To reduce the power consumption, the sensor can enter a sleep mode. A wake-up circuit then activates the sensor and returns it to normal operation.

State-of-the-art sensors with wireless communication consume significantly more power than is typically available in the environment. There are two methods to address this problem and allow wireless sensors to operate without a battery: decrease the power consumed by the sensors and increase the available power. Radiating power from a central hub at radio frequencies is one way to power the sensor nodes. However, there is a legal limit to the amount of power that can be transmitted wirelessly, physical limits to the efficiency of transmission, and technological limits to how much can be scavenged. The FCC limit for the maximum peak continuous output power of an intentional radiator is 1 W , (30dBm) [4]. Physical laws limit the amount of power that one antenna can radiate to another for a given distance and frequency. Free-space path loss (FSPL), Eq. (1), is the loss of signal strength in a line-of-sight configuration between two antennas [5],

$$
\begin{equation*}
F S P L=\left(\frac{4 \pi d f}{c}\right)^{2} \tag{1}
\end{equation*}
$$

where $d$ is the distance in meters, $f$ is the frequency in Hertz, and $c$ is the speed of light. A simplified version where the physical constants are embedded is:

$$
\begin{align*}
& 10 \log _{10} F S P L=10 \log _{10}\left(\frac{4 \pi d\left(f \times 10^{6}\right)}{c}\right)^{2} \\
& \begin{aligned}
F S P L(d B) & =20 \log _{10}\left(\frac{4 \pi d\left(f \times 10^{6}\right)}{c}\right) \\
& =20 \log _{10}(d)+20 \log _{10}(f)+20 \log _{10}\left(\frac{4 \pi \times 10^{6}}{2.998 \times 10^{8}}\right) \\
& =20 \log _{10}(d)+20 \log _{10}(f)-27.552 \mathrm{~dB}
\end{aligned} \tag{2}
\end{align*}
$$

where $f$ is the frequency in $\mathrm{MHz}, d$ is the distance in meters, and the FSPL is in decibels. For a fixed distance and frequency, the FSPL limits RF power reception.

The final limitation on scavenging power is the state of the technology of RF energy harvesters. An RF energy harvester with a peak efficiency of $15.43 \%$ can be constructed using off-the-shelf components [6]. A custom, fully integrated, RFharvester using a full-wave floating-gate rectifier is presented in [7] with a peak efficiency of $60.0 \%$, which corresponds to a loss of 2.218 dB .

With a harvester efficiency of $60.0 \%$, Eq. (3) shows that the maximum power that can be harvested from a $1 \mathrm{~W}, 900 \mathrm{MHz}$, isotropic radiator from an identical antenna 10 meters away cannot exceed $4.22 \mu \mathrm{~W}$.

$$
\begin{align*}
P_{\text {harvest }} & =30 \mathrm{dBm}-[20 \log (10)+20 \log (900)-27.552+2.218] \mathrm{dBm}  \tag{3}\\
& =-23.751 \mathrm{dBm}=4.22 \mu \mathrm{~W}
\end{align*}
$$

This is the maximum continuous power available for a battery-free wireless sensor under these conditions, and it is significantly less than the power required to operate the most efficient receivers and transmitters reported to date. Table 1 reports the power requirement of recent wireless sensor network receivers and transmitters.

Table 1 - Performance of wireless sensor network receievers and transmitters.

|  | Otis <br> $2005[8]$ | Cook <br> $2006[9]$ | Panitantum <br> $2008[10]$ | Ayers <br> $2008[11]$ |
| :---: | :---: | :---: | :---: | :---: |
| RX Power $(\mu \mathrm{W})$ | 400 | 300 | - | 244 |
| TX Power $(\mu \mathrm{W})$ | 1600 | 700 | 1940 | - |
| Frequency $(\mathrm{MHz})$ | 1900 | 2400 | 900 | 900 |
| Modulation | OOK | BFSK | BFSK | BFSK |

For an RF-harvester to power a wireless sensor's receiver and transmitter, it must harvest and store energy over a long period for the sensor to sense and communicate over a shorter period. During the storage time, the only operable part of the sensor is the circuit that wakes up the sensor when it is time to sense and communicate. Therefore, it is a requirement of the system that the wake-up method use an insignificant portion of the harvested power.

Because the wake-up circuit must operate at all times while the sensor is asleep, its power consumption directly reduces the power available for storage from the harvester. Consequently, increasing the power consumption of the wake-up circuit increases the time required to store enough energy to power the sensor. Mathematically, this is expressed in Eq. (4).

$$
\begin{align*}
E_{\text {req }} & =P_{\text {store }} \times t_{\text {sleep }} \\
& =\left(P_{\text {harvest }}-P_{\text {wake }-u p}\right) \times t_{\text {sleep }} \tag{4}
\end{align*}
$$

where $E_{\text {req }}$ is the minimum energy required for the sensor to complete one sensing and communicating cycle, $P_{\text {store }}$ is the storage power, $t_{\text {sleep }}$ is the time the sensor is asleep, $P_{\text {harvest }}$ is the harvested power, and $P_{\text {wake-up }}$ is the power consumption of the wake-up circuit. Eq. (4) shows that the power consumption of the wake-up circuit directly affects the overall system performance. Specifically, decreasing $P_{\text {wake -up }}$ decreases $t_{\text {sleep }}$ and increases the number of times the sensor can sense and communicate per day.

Regardless of what type of circuit activates the sensor, it is equally important that the sensor activate at a known time with a fine resolution. If sensors in a network are not synchronized, and activate at random or unpredictable times, the sensor must power its RF receiver for a longer period. Figure 1.1 illustrates a theoretical situation where a sensor is activated using a 10 kHz interrupt timer. The length of time that the receiver must be active is increased by a non-ideal clock. The receiver must turn on early and stay on later to ensure it does not miss the message due to the large coarse resolution of the non-ideal clock.


Figure 1.1 - Total receiver on-time for a theoretical system with single-period clock drift and a maximum possible $100 \mu$ s asynchronization time.

With an ideal clock, the receiver could turn on the instant before the transmitter sends the message. Clock drift error is defined as the error introduced by non-ideal set-up and hold times, requiring the receiver to turn on the clock one cycle prior to the arrival of a message. The magnitude of the error due to clock drift is lessened by a faster clock with a shorter period. However, a faster clock consumes more power. If the clock shown above is an ideal clock that is only consuming power to charge and discharge a capacitor, the minimum dynamic power of the clock is [12]

$$
\begin{equation*}
P_{c l o c k}=\frac{f C V_{D D}^{2}}{2} \tag{5}
\end{equation*}
$$

where $V_{D D}$ is the supply voltage, $f$ is the frequency, and $C$ is the load capacitance. For example, an ideal clock with a 1.25 V supply, a frequency of $10 \mathrm{kHz}(100 \mu \mathrm{~s}$ resolution), and a load capacitance of 10 pF consumes a minimum power of 125 nW . In a recent wireless sensor network [13], the interrupt timer alone consumed $5.68 \mu \mathrm{~W}$. In addition to the interrupt clock, the sensor also needs a programmable sleep period and an event handler, both of which consume additional power.

Asynchronization error is defined as the error introduced by clocks with nonideal frequencies. Over time, the transmitter and receiver clocks can become asynchronous. The magnitude of this error is system dependent and could be greater than the single-period asynchronization shown in Figure 1.1.

In a battery powered system, a globally broadcast RF clock can be used to keep the transmitter and receiver's clocks synchronous [14], but this can use approximately $10 \mu \mathrm{~W}$ of power using a rudimentary low power RF receiver. This approach requires
that a simple RF receiver stays on at all times to receive the timestamp information from a central hub and then synchronize its internal clock to the source.

There is then a design trade-off between wasting power on increased clock precision or wasting power on activating the RF receiver early. Furthermore, in each of the cases described above, the wake-up method consumes dynamic power. The circuit presented in this thesis utilizes a RF energy harvesting topology to achieve wake-up resolution analogous to a 125 kHz clock, but uses tens of nano-watts of static leakage power and near-zero dynamic power. This is several orders of magnitude less than any other reported method.

This thesis is organized as follows. Chapter 2 describes the system design including system restrictions and external interfaces. Chapter 3 covers the proposed topology and circuit design. Chapter 4 describes the test setup and the measured results. Chapter 5 concludes this thesis.

## 2. System Design

### 2.1. System Overview

The wake-up circuit described in this thesis utilizes RF energy harvesting technology to synchronize the sensors in a network by monitoring the rectified RF power source and waking the sensor when the RF power source turns off. While the central hub is radiating power to the sensors, shown in Figure 2.1, the radiated RF power disrupts all sensor-to-sensor and sensor-to-hub communications.


Figure 2.1 - RF power broadcast for a three-ring network.
Because the central RF power source must cease broadcasting to allow the sensors to communicate, it is convenient to wake up the sensors when the RF power source turns off. Figure 2.2 is a timing diagram of the transmitter and receiver schedule for a theoretical three-ring wireless sensor network.

| CENTRAL HUB POWER SOURCE | ACTIVE | IDLE |  |  |  |  |  |  | ACTIVE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| CENTRAL HUB DATA SOURCE | IDLE | $\int^{T X}$ | $\mu^{\text {TX }}$ | IDLE | $c^{\text {TX }}$ |  |  | $7^{\mathrm{RX}}$ | IDLE |
| INNER RING SENSOR | ASLEEP, <br> HARVESTING ENERGY |  | IDLE |  | $\Delta_{\text {RX }}$ | $7^{R X}$ | SENSE | ${ }_{\text {TX }}$ | ASLEEP, HARVESTING ENERGY |
| MIDDLE RING SENSOR | ASLEEP, <br> HARVESTING ENERGY | IDLE | $\bigwedge_{\text {RX }}$ | $\nabla^{R X}$ | SENSE | $\bigcirc_{\text {TX }}$ |  | LE | ASLEEP <br> HARVESTING ENERGY |
| OUTER RING SENSOR | ASLEEP, <br> HARVESTING ENERGY | $y_{R X}$ | SENSE | $\_{\text {тX }}$ | IDLE |  |  |  | ASLEEP, <br> HARVESTING ENERGY |
|  | $\underline{t_{0}}$ time | $\mathrm{t}_{0}$ time |  |  |  |  |  |  |  |

Figure 2.2 - Transmitter and receiver operation schedule for a three-ring network assuming each sensor does a complete receive-sense-transmit cycle.

While the RF power source is active, all the sensors are asleep and harvesting energy. At time $t_{0}$, the RF power source ceases broadcasting and the sensors execute their default command. Sensors in the outer ring will have previously been programmed to initialize their receivers at time $t_{0}$. Sensors in the middle and inner rings enter an idle state while their internal clocks delay the initialization of their
receivers for a pre-programmed amount of time. The actions for the sensors in each ring of the wireless sensor network execute in the same order following the initial delay. First, the sensor receives data from the central hub. Second, the sensor receives data from a sensor further from the central hub if there is one. Third, the sensor senses and processes its data. Fourth, the sensor transmits its data to a sensor closer to the central hub or to the central hub itself. Fifth, the sensor enters a low-power mode. Finally, the sensor goes to sleep and resumes harvesting power when the central RF power source resumes broadcasting.

In addition to the power savings discussed earlier, waking up when the RF power source turns off is a de facto global clock synchronization signal. The loss of RF power is a global event experienced by all the sensors in the network at the same time. This gives all the benefits of the globally distributed clock discussed in the previous section without an active receiver. Additionally, synchronizing the nodes with the RF power source eliminates the problem of clock drift.

### 2.2. System Constraints

Figure 2.3 illustrates the functional blocks that interface to the wake-up circuit. The multistage rectifier converts the RF energy into DC energy stored on a large, lowleakage capacitor. The rectified voltage can be as high as 12 V . The regulator converts the rectified voltage into a 1.25 V supply voltage for powering the circuits. The wakeup circuit drives a switch that controls the power for a finite state machine (FSM). The FSM in turn controls the reset signal for the wake-up circuit. The FSM also interfaces with the on-chip sensor, receiver (RX), and transmitter (TX).

For the whole system to operate at peak efficiency, each sensor must wake up at a programmable time with strict timing requirements. The wake-up circuit presented here synchronizes the actions of wireless nodes with a central hub. If there are inconsistencies in the propagation delay, the window allocated for specific operations must be widened. The propagation delay, $\mathrm{t}_{\mathrm{p}}$, for the circuit shown in Figure 2.3 is defined as the time from the falling edge of $\mathrm{V}_{\text {IN }}$ to the rising edge of $\mathrm{V}_{\text {Out }}$.


Figure 2.3 - Wake-up circuit's interface to other on-chip functional blocks.
The absolute value of propagation delay across this circuit is not as important as the consistency of that delay for each value of $\mathrm{V}_{\text {IN }}$. Once a sensor is placed at a static location a constant distance from an RF power source broadcasting at a constant frequency, then from Eq. (2) the free-space path loss (FSPL) will be constant. Therefore, if the RF power source is broadcasting at a constant power level, the RF energy harvester will receive a constant input power and the DC value of $\mathrm{V}_{\text {IN }}$ at that location will remain constant.

Once the sensor has completed all sensing and communication and is ready to sleep, the FSM sends the wake-up circuit a reset signal. If the RF power source is broadcasting, the sensor goes to sleep and the RF-harvester resumes harvesting power.

### 2.3. Electrical Constraints

The wake-up circuit monitors the RF power signal by tapping onto the output of the first stage, $\mathrm{V}_{1}$, of a multistage rectifier shown in Figure 2.4. Connecting the wake-up circuit to any stage marginally adds an additional load to the rectifier. The capacitive loading of a single gate is insignificant compared to the $\mathrm{C}_{2, \mathrm{n}}$ capacitors in Figure 2.4. More significantly, resistive loading occurs due to gate leakage currents flowing from the gate to the substrate. Gate leakage occurs when a voltage potential is applied across the gate-substrate terminals. The magnitude of the leakage current increases as the gate-substrate voltage increases [15]. Connecting the wake-up circuit to the lowest potential node reduces the gate leakage and reduces the resistive loading of the rectifier.


Figure 2.4 - Architecture of a multistage RF rectifier [7].
The system design is further constrained by the supply voltage provided by the regulator shown in Figure 2.3. The harvester/regulator circuit described in the previous section supplies a regulated voltage of 1.25 V [16].

Due to FSPL, the amplitude of $\mathrm{V}_{\mathrm{RF}}$ and subsequently the DC value of $\mathrm{V}_{\text {RECT }}$ are proportional to the square root of the distance to the RF power source for far-field distances, Eq. (1). For a sensor with a 36 -stage RF energy harvester, the output of the first stage, $\mathrm{V}_{1}$, will be $1 / 36^{\text {th }}$ of the rectified voltage. A sensor placed 15 meters away from the RF power source will have a $V_{\text {RECT }}$ of $\sim 2.1 V$. For a sensor at 1 meter, $V_{\text {RECT }}$ will be $\sim 9 \mathrm{~V}$ [16]. Therefore, the DC values of $\mathrm{V}_{\text {IN }}$ for the wake-up circuit will lie in the range of 58 mV to 250 mV .

The output of the wake-up circuit, $\mathrm{V}_{\text {OUT }}$, must drive a CMOS pass-gate switch that supplies power to the FSM. To reduce the on resistance of the switch, Vout should be the highest obtainable voltage available that will not damage the switch. This design uses the output of the regulator to drive the switch.

### 2.4. Standard Comparator

The standard way to trigger a logical ' 1 ' output from a known analog signal is to use a comparator with a reference voltage [17]. Figure 2.5 shows three low-power CMOS comparators with cross-coupled input devices.


Figure 2.5 - Alternative comparator topologies. a) Low power differential current. b) Resistive divider. c) Charge sharing [18].

Table 2 summarizes the performance of the latching comparators shown in Figure 2.5. Each topology consumes orders of magnitude more power than is available to the wake-up circuit. Additionally, the input offset voltage, $\mathrm{V}_{\mathrm{OS}}$, is within an order of magnitude of the minimum value of $\mathrm{V}_{\text {IN }}$. With an offset voltage of this magnitude, these comparators could never reliably monitor the RF power source.

Table 2 - Performance of latched comparators [18].

| Type | Power <br> $[\mu \mathrm{W}]$ | $\mathrm{V}_{\text {OS }}$ <br> $[\mathrm{mV}]$ |
| :---: | :---: | :---: |
| Low power differential <br> current | 138.15 | 164 |
| Resistive divider | 114.02 | 31.9 |
| Charge Sharing | 88.19 | 32.1 |

In addition to the power consumption outlined in Table 2, more power will be consumed in generating the required reference voltage. A low-power reference voltage is presented in [19] that features MOSFETs operating in the subthreshold region. Simulation results for this reference voltage show the power consumption to be $1.84 \mu \mathrm{~W}$ at room temperature. Another low-power reference voltage is presented in [20] that is fabricated in a $1.2 \mu \mathrm{~m}$ CMOS process. The measured power consumption for this reference is $4.32 \mu \mathrm{~W}$ at room temperature.

A new topology for a wake-up circuit that operates as a latched comparator but consumes orders of magnitude less power and has orders of magnitude lower offset voltage is presented in this thesis. The current consumed by the new latched comparator never exceeds off-state leakage currents, and the offset voltage is determined by the inherent characteristics of MOS devices operating in the deepsubthreshold region.

## 3. Circuit Design

### 3.1. Circuit Overview

The latched comparator, shown in Figure 3.1, is composed of three stages. The first stage, $S_{1}$, is a single-ended-input inverting comparator operating from a low supply voltage in the subthreshold region. This stage compares the input to an internal positive reference set by its switching voltage. If the input to the first stage, $\mathrm{V}_{\text {IN }}$, is higher than the reference, then its output is low. The output of the inverting comparator, $\mathrm{V}_{\mathrm{C}}$, is the input to a level-shifting multi-inverter stage, $\mathrm{S}_{2}$.

The second stage includes an even number of inverters and serves two purposes. First, toggling $\mathrm{V}_{\text {RESET }}$ resets the entire circuit to a known state. Second, $\mathrm{S}_{2}$ level-shifts the logical-high voltage from the low voltage sourced by $S_{1}$ to a greater voltage required for the output, $\mathrm{V}_{\text {OUT }}$, as described in Section 2.3. Of the even number of inverters in $\mathrm{S}_{2}$, all but the last inverter are powered by the intermediate voltages in a voltage divider. The last inverter in the second stage, the reset inverter, is directly powered by $\mathrm{V}_{\text {RESET }}$.


Figure 3.1 - Basic latched comparator topology. $S_{1}$ is the inverting input stage, $S_{2}$ is the non-inverting stage consisting of an even number of inverters, and $S_{3}$ is the inverting latching stage.

The third stage, $S_{3}$, provides the latching behavior of the circuit. As long as the circuit's output voltage is low, $S_{3}$ sources power to the previous stages $V_{D D 1}, V_{D D 2}, \cdots, V_{D D n}$ via a voltage dividing string of resistors. When $\mathrm{V}_{\text {IN }}$ decreases to a voltage less than the internal reference voltage of $S_{1}$, the odd number of intermediate inverters ( $S_{1}$ and the even number of inverters in $S_{2}$ ) causes $V_{\text {OUT }}$ to increase to a logical high voltage. A high voltage at $\mathrm{V}_{\text {OUT }}$ causes $\mathrm{V}_{\text {LATCH }}$ to decrease to a logical
low voltage of zero volts, whereby $V_{D D 1}, V_{D D 2}, \cdots, V_{D D n}$ are zero volts. Thus the supply voltage for all inverters is zero except for the reset inverter. The circuit stays in this state, and does not respond to $\mathrm{V}_{\text {IN }}$, until $\mathrm{V}_{\text {RESET }}$ toggles and $\mathrm{V}_{\text {IN }}$ is high.

With an overview of the circuit provided, the following sections describe the subcircuits in more detail. Sections 3.2 and 3.3 describe the design and operation of the input comparator stage. Sections 3.4 and 3.5 describe the process for choosing the number of inverters to use in the second stage, $\mathrm{S}_{2}$. Section 3.6 covers the design of the third stage and the behavior of the latch.

### 3.2. Topology Design of the First Stage

For a sensor at the maximum operable distance from the central hub (10-15m), a recognizable logical 'high' value of $\mathrm{V}_{\mathrm{IN}}$ can be as low as $58 \mathrm{mV}, \mathrm{V}_{\mathrm{IH}, \mathrm{min}}$, and as high as 250 mV , $\mathrm{V}_{\mathrm{IH}, \max }$. The logical 'low' value, $\mathrm{V}_{\mathrm{IL}}$, will always be within a few microvolts of ground. The comparator stage of the wake-up circuit must discern between these two states without wasting current on a PTAT-generated reference voltage and output a voltage large enough to surpass the switching voltage of the first inverter in $\mathrm{S}_{2}$, shown in Figure 3.1.

A traditional way to amplify a voltage is to use a common-source amplifier, as shown in Figure 3.2(a). The current through such a branch can be greatly reduced by replacing the load resistor, ' R ', with a current limiting active load. The active load shown in Figure 3.2(b) is an off-state NMOS device. In Figure 3.2(c), the NMOS devices have been changed to PMOS devices because the charge carriers in PMOS devices have a lower mobility than in NMOS devices [21], reducing the leakage current and power consumption.


Figure 3.2 - Common source amplifiers with a) resistive load, b) off-state NMOS active load, c) off-state PMOS active load.

The topologies shown in Figure 3.2 use a built-in switching voltage as the reference voltage. The output of the circuits shown in Figure 3.2 switch from rail-torail as the input passes the switching voltage, which is set by the physical parameters of the devices and the supply voltage, $V_{D D}$.

Previously, comparators have been presented that use the inherent properties of MOS devices instead of a reference voltage [22]. These comparators use the difference between the threshold voltage of NMOS devices and the threshold voltage of a PMOS device to generate a stable reference. However, by operating near the threshold voltage of the MOS devices, the topology in [22] sinks milliamperes of current. The topology of Figure 3.2(c) uses the high resistance of $\mathrm{M}_{4}$ to limit the current in the branch to tens of picoamperes.

### 3.3. Device Sizing in the First Stage

The sizes of the devices and the supply voltage of the first stage determine the switching-voltage-generated reference voltage for the first stage. The absolute value of the switching is not as important as the range in which it lies. In this application, the switching voltage must be greater than zero and less than 58 mV . A switching voltage of 30 mV should reduce the possibility of the first stage not switching due to process variations. The first stage can fail if $V_{I N}$ is greater than 58 mV and the output remains near $V_{D D 1}$ or if $V_{I N}$ is less than or equal to zero and the output remains near ground.

Figure 3.3 illustrates the DC operating point when $V_{\text {OUT }}$ and $V_{I N}$ are held at the desired switching voltage, $V_{\text {OUT }}=V_{I N}=V_{S W}$. To determine the device sizes that yield a switching voltage of $\sim 30 \mathrm{mV}, \mathrm{I}_{\mathrm{M} 1}$ is set equal to $\mathrm{I}_{\mathrm{M} 0}$ and one solves for the device sizes for a given $V_{D D}$.


Figure 3.3 - DC operating point when the input and output voltages are at the switching voltage.

The basic equation for modeling the drain current of a device operating in the subthreshold region ( $\left|V_{G S}\right|<V_{T}$ ) is shown in Eq. (6) [23], [24], assuming that $V_{B S}=0, V_{D S} \gtrsim 2 v_{t h}$, and the channel length is sufficiently long,

$$
\begin{gather*}
I_{D}=\mu_{\mathrm{o}} C_{\mathrm{ox}} S_{M} \cdot(n-1) \cdot v_{t h}{ }^{2} \cdot e^{\frac{\left(\left|V_{G S} S-\left|V_{T}\right|\right)\right.}{n \cdot v_{t h}}} \\
n=1+\frac{\sqrt{q N_{b} \varepsilon_{s i}}}{C_{\mathrm{ox}} \sqrt{2 \psi_{s}}} \cong 1+\frac{C_{\mathrm{d}}}{C_{\mathrm{ox}}} \tag{6}
\end{gather*}
$$

where $S_{M}$ is the $W / L$ of the device; $n$ is the subthreshold slope factor; $v_{t h}$ is the thermal voltage, $k T / q ; q$ is the unit charge of an electron; $N_{b}$ is the doping concentration of the substrate; $\varepsilon_{s i}$ is the permittivity of silicon; $C_{o x}$ is the oxide capacitance per unit area; $\psi_{s}$ is the surface potential; and $C_{\mathrm{d}}$ is the depletion capacitance per unit area.

Eq. (6) shows that the drain current has no dependence on $V_{D S}$ as long as $V_{D S}>2 v_{t h}$. Since $V_{G S}=0$ for $\mathrm{M}_{0}, I_{M 0}$ will only depend upon $V_{T}$ and the device sizes. The drain current of the input device, $I_{M 1}$, varies exponentially with its gate-source voltage. Setting the drain currents equal to each other yields Eq. (7).

$$
\begin{align*}
I_{M 0} & =I_{M 1} \\
\mu_{o} C_{o x} S_{M 0}(n-1) v_{t h}{ }^{2} e^{\frac{-\left|V_{T}\right|}{n \cdot v_{t h}}} & =\mu_{o} C_{o x} S_{M 1}(n-1) v_{t h}{ }^{2} e^{\frac{\left(V_{D D}-V_{S W}-\left|V_{T}\right|\right)}{n \cdot v_{t h}}} \tag{7}
\end{align*}
$$

or,

$$
S_{M 0} e^{\frac{-\left|V_{T}\right|}{n \cdot v_{t h}}}=S_{M 1} e^{\frac{\left(V_{D D}-V_{S W}-\left|V_{T}\right|\right)}{n \cdot v_{t h}}}
$$

For a given supply voltage, Eq. (9) relates $S_{M 0}$ to $S_{M 1}$ and a switching voltage. Let $R_{M}=S_{M 0} / S_{M 1}$ then

$$
\begin{equation*}
R_{M}=e^{\frac{\left(V_{D D}-V_{S W}\right)}{n \cdot v_{t h}}} \tag{9}
\end{equation*}
$$

The subthreshold slope is a constant in any process. For first-order calculation it can be assumed that operating in the subthreshold region $C_{\mathrm{d}} / C_{\mathrm{ox}} \cong 1$ and $n \cong 2$ [24]. For an input voltage of $V_{S W}=30 \mathrm{mV}$ and a thermal voltage of $v_{t h} \cong 25 \mathrm{mV}$ at $T=300 K$, Eq. (9) yields Eq. (10).

$$
\begin{equation*}
R_{M}=e^{\frac{\left(V_{D D}-30 \mathrm{mV}\right)}{50 \mathrm{mV}}} \tag{10}
\end{equation*}
$$

Figure 3.4 plots Eq. (10) for values of $0<V_{D D}<400 \mathrm{mV}$. As the supply voltage increases, the $W / L$ ratio of the off-state device, $\mathrm{M}_{0}$, must increase exponentially to keep the switching voltage at 30 mV . Eq. (10) indicates that the circuit in Figure 3.3 could operate from a 1.25 V supply voltage, but this would require that $\mathrm{M}_{0}$ is two million times larger than $\mathrm{M}_{1}$. Limiting $R_{M}<1000$, yields a range of possible values for $V_{D D}<375 \mathrm{mV}$ and their corresponding $R_{M}$ values. Figure 3.5
shows the simulated voltage transfer characteristics of the circuit with, $R_{M}=80$ and $V_{D D}=250 \mathrm{mV}$. The switching voltage is $\sim 40 \mathrm{mV}$. The small inconsistency between the simulated value and the calculated value is due to the inaccuracies of the subthreshold equation when $V_{D S}<2 v_{t h}$.


Figure 3.4 - Ratio of the active and load device sizes vs. $\mathrm{V}_{\mathrm{DD}}$ for a switching voltage of 30 mV .


Figure 3.5 - Simulated voltage transfer characteristic for the single-stage common source amplifier.

### 3.4. Two-Inverter Level-Shifting Buffer

In order to satisfy the electrical constraints, a level-shifting multi-inverter stage, $S_{2}$, buffers the low voltage output, $S_{1}$. The output of this stage, $V_{\text {Out }}$, is then large enough to turn off the top device in $S_{3}$. The second stage must have an even number of inverters to retain the inverting behavior from $\mathrm{V}_{\text {IN }}$ to $\mathrm{V}_{\text {Out }}$. Figure 3.6 shows a two-inverter topology. This section will show that a two-inverter levelshifting buffer can be designed with ideal devices and resistors, but a more robust design is needed to account for process variations.


Figure 3.6 - Two inverter topology for the non-inverting level-shifting stage, $S_{2}$.
The topology used for $S_{1}$ cannot be used for $S_{3}$ because $S_{3}$ operates well outside the subthreshold region. To operate from a 1.25 V supply voltage, $\mathrm{S}_{3}$ and the final inverter of $S_{2}$ are standard CMOS inverters. The initial inverter of $S_{2}$ must have a switching voltage less than 400 mV (if $R_{M}<10^{3}$ ) and a large enough output voltage to turn off $\mathrm{M}_{3}$,

$$
\begin{equation*}
V_{2}>\left(1250 m V-\left|V_{T}\right|_{\min }\right) \tag{11}
\end{equation*}
$$

where $V_{T}$ is approximately 430 mV but can be as low as 300 mV . In the ideal case where $S_{2}$ is capable of driving its output from rail-to-rail, Eq. (11) states that $\mathrm{V}_{\mathrm{DD}}$ must be at least 950 mV . However, in practice $\mathrm{V}_{2}$ is less than $\mathrm{V}_{\mathrm{DD} 2}$ due to losses in the top device in the first inverter in $S_{2}$, leading to a minimum $V_{D D 2}$ of $\sim 1000 \mathrm{mV}$. If the first inverter in $S_{2}$ had a $\sim 1000 \mathrm{mV}$ supply voltage, and a maximum input voltage of

400 mV , then it would need to have a switching voltage that is less than $40 \%$ of its supply voltage. This is possible, using a standard CMOS inverter, but attention must be paid to the resistor string that divides and creates the supply voltages.

The resistor string must have a total resistance of approximately $100 \mathrm{M} \Omega$ to limit the current through the string to approximately one hundred times greater than the leakage through the inverters, $\sim 10$ nA. Poly resistors could be used to create the resistor string, but at $235 \Omega / \square$, the resistors would have to have a size ratio of 425,000:1.

Off-state PMOS transistors can be used as resistors due to their large DC resistance, such as $\mathrm{M}_{2}$ in Figure 3.6, but their actual resistance can vary by $\pm 10 \%$ or more due to mismatch, process, and $\mathrm{V}_{\mathrm{T}}$ variations. The ideal resistance ratios are shown in Eq. (12).

$$
\begin{gather*}
V_{D D 2}=1000 \mathrm{mV}=1250 \mathrm{mV} \cdot\left(\frac{R_{1}+R_{2}}{R_{1}+R_{2}+R_{3}}\right)  \tag{12}\\
R_{1}+R_{2}=4 R, \quad R_{3}=R
\end{gather*}
$$

However, to ensure that Eq. (11) is always satisfied in all cases, the following equation yields the upper and lower bounds for $V_{D D 2}$ given a percentage variation in resistance, $x$. The worst-case scenario is defined as the case in which $R_{1}$ and $R_{2}$ are altered by $\pm 10 \%$ and $R_{3}$ is altered by $\mp 10 \%$.

$$
\begin{gather*}
V_{D D 2}=1250 \mathrm{mV} \cdot\left(\frac{(1 \pm x) \cdot\left(R_{1}+R_{2}\right)}{(1 \pm x) \cdot\left(R_{1}+R_{2}\right)+(1 \mp x) \cdot R_{3}}\right)  \tag{13}\\
R_{1}+R_{2}=4 R \cdot(1 \pm x), \quad R_{3}=R \cdot(1 \mp x)
\end{gather*}
$$

Using the resistances in Eq. (13) for $x=10 \%$, the range of $\mathrm{V}_{\mathrm{DD} 2}$ becomes

$$
\begin{equation*}
957 \mathrm{mV}<V_{D D 2}<1037 \mathrm{mV} \tag{14}
\end{equation*}
$$

However, the lower bound in Eq. (14) violates the condition set in Eq. (11) that $V_{D D 2}$ must be greater than 1000 mV in all cases. Increasing the target $V_{D D 2}$ in Eq. (12) yields values of resistances that comply with the condition set in Eq. (11). After an iterative process, it was found that setting $V_{D D 2}=1037 \mathrm{mV}$ in the nominal case, sets $V_{D D 2, \text { min }}$ to 1000 mV , as shown in Eqs. (15) - (17).

$$
\begin{gather*}
V_{D D 2}=1037 \mathrm{mV}=1250 \mathrm{mV} \cdot\left(\frac{R_{1}+R_{2}}{R_{1}+R_{2}+R_{3}}\right)  \tag{15}\\
R_{1}+R_{2}=22 R, \quad R_{3}=9 R \\
V_{D D 2}=1250 \mathrm{mV} \cdot\left(\frac{(1 \pm x) \cdot\left(R_{1}+R_{2}\right)}{(1 \pm x) \cdot\left(R_{1}+R_{2}\right)+(1 \mp x) \cdot R_{3}}\right)  \tag{16}\\
R_{1}+R_{2}=22 R \cdot(1 \pm x), \quad R_{3}=7 R \cdot(1 \mp x) \\
1000 \mathrm{mV}<V_{D D 2}<1070 \mathrm{mV} \tag{17}
\end{gather*}
$$

Since $\mathrm{S}_{2}$ must operate from a supply voltage that is greater than $2 V_{T}, V_{1}$ must swing to at least within a $V_{T}$ of $V_{D D 2}$ in order to shut off the top device in $\mathrm{S}_{2}$, as shown in Eq. (18).

$$
\begin{equation*}
V_{D D 1}>V_{1}>\left(1070 m V-\left|V_{T}\right|_{\min }\right) \tag{18}
\end{equation*}
$$

However, Eq. (10) and the design limit on the size of the devices in $S_{1}$, set an upper limit on the range of $V_{D D 1}$.

$$
\begin{equation*}
V_{D D 1}<375 \mathrm{mV} \tag{19}
\end{equation*}
$$

The condition in Eq. (18) cannot be met with a supply voltage for $S_{1}$ set at 375 mV . Furthermore, the reset inverter in $S_{2}$ cannot use the same topology as $S_{1}$, because its devices operate outside the subthreshold region.

The concerns described in this section rule out the possibility of using a twoinverter level-shifting buffer for the second stage shown in Figure 3.1. The variability of off-state MOS resistors lead to excessive variations in $V_{D D 1}$ and $V_{D D 2}$. At the extremes of variations in the resistor string, the lower boundary of $V_{D D 2}$ violates Eq. (11), and the upper boundary of $V_{D D 1}$ violates Eq. (19), motivating the decision to use a four-inverter level-shifting buffer.

### 3.5. Four-Inverter Level-Shifting Buffer

The cascaded two-inverter level-shifting buffer described in the previous section could not reliably amplify the input signal. Reliable up-translation of the 58 mV input signal requires additional inverters. Each stage shown in Figure 3.7 increases the digital high voltage of the following stage by 250 mV . Limiting the step between any two stages to less than a $\left|V_{T}\right|_{\text {min }}$ ensures that each inverter is capable of turning off the next inverter.


Figure 3.7 - Four inverter topology for the non-inverting level-shifting stage, $\mathrm{S}_{2}$.
In the first three inverters, the supply voltage is less than $2 \cdot\left|V_{T}\right|_{\text {min }}$, allowing use of the topology described in Section 3.2. The last three inverters in Figure 3.7 are traditional CMOS inverters. As nodes $V_{3}, V_{4}$, and $V_{\text {OUT }}$ increase or decrease past the switching voltage for the next stage, the node voltage will pass a point at which both devices in the inverter have $\left|V_{G S}\right|>\left|V_{T}\right|_{\text {min }}$. The devices in the last three inverters have increased lengths, reducing the drive strength of the device when $V_{3}, V_{4}$, and $V_{\text {OUT }}$ are approximately equal to their respective $V_{S W}$, reducing the energy consumed per switching event of each inverter.

### 3.6. Latch Design

The discussion so far has been only on the comparator and voltage translator. The other part of the circuit is its latching method. A latch is a system with two possible stable states that can be used to store information [25]. In this case, the two stable states are 'Output High' and 'Output Low.' The truth table for the wake-up latch in Figure 3.7 is shown in Table 3.

Table 3 - Latch truth table.

| V RESET | $\mathrm{V}_{\text {IN }}$ | Action |
| :---: | :---: | :---: |
| 0 | - | Vout $=0$ |
| 1 | 0 | Vout $=1$ |
| 1 | 1 | Keep State |

The sensor also has an active-low reset command to place the wake-up latch into the " 0 " state. When $\mathrm{V}_{\text {RESET }}$ is high, the latch output is held until the input goes low, forcing $\mathrm{V}_{\text {OUT }}$ high.

To achieve the behavior shown in Table 3, the output of the voltage translator gates its own power supply via an additional inverter, $\mathrm{I}_{6}$, as described in Section 3.1. This configuration is shown in Figure 3.8. Inverters $\mathrm{I}_{2}-\mathrm{I}_{5}$ are the four inverters in $\mathrm{S}_{2}$.


Figure 3.8 - Representation of the latch as a series of inverters.
The resistor string in Figure 3.8 is realized using off-state PMOS devices. Each device was sized to be 100 times the width of the largest device in the inverters. Additional on-chip MOS-capacitors placed at each of the intermediate nodes supply the inverters with instantaneous current.

Figure 3.9 shows the ideal timing sequence for the latch for 0.1 Hz operation. Following a falling edge of $\mathrm{V}_{\text {IN }}$, at time $\mathrm{t}_{\mathrm{o}}$, $\mathrm{V}_{\text {OUT }}$ will rise to $\mathrm{V}_{\mathrm{DD}}$ as long as $\mathrm{V}_{\text {RESET }}$ remains high. The propagation delay of the wake-up circuit, $\mathrm{t}_{\mathrm{p}}$, shown in Figure 3.9 is the delay from the falling edge of $\mathrm{V}_{\text {IN }}$ to the rising edge of $\mathrm{V}_{\text {OUT }}$. The falling edge of $V_{\text {out }}$ will coincide with the falling edge of $\mathrm{V}_{\text {RESET }}$.


Figure 3.9 - Ideal timing sequence for the DC input circuit shown in Figure 3.8.

### 3.7. Variations in Propagation Delay

In the ideal case, $\mathrm{t}_{\mathrm{p}}$ would be constant. This would result in the wake-up circuit having infinite accuracy, and the sensors waking up at exactly the same time. However, process variations affect the leakage rates of the cut-off devices causing chip-to-chip variations in $t_{p}$. In addition to chip-to-chip variations of $t_{p}$, there are also finite variations in $t_{p}$ from one wake-up event to the next within the same chip.

Temperature and process-variation-induced variations in $\mathrm{t}_{\mathrm{p}}$ are predictable for a single chip and a sophisticated communications protocol can account for them. Unpredictable event-to-event propagation delay variations lead to a loss of synchronization accuracy between RF receivers and transmitters, requiring the receiver to power up sooner and stay powered longer to ensure reception of the transmitted data. Figure 3.10 shows the variations in the simulated propagation delay for a wake-up circuit at a constant temperature with thermal and flicker noise included. The simulated $3 \sigma$ range is $0.42 \%$ of the total propagation time of the wakeup circuit.


Figure 3.10 - Simulated variations in propagation delay due to transistor noise.

### 3.8. Latch Failures and Monte Carlo Simulations

In addition to affecting the propagation delays of separate wake-up circuits, process and temperature variations can also cause the wake-up circuit to fail. Figure 3.11 shows the failure rates of the latch over a range of temperature and $\mathrm{V}_{\text {IN }}$. In the temperature range of -10 to $30^{\circ} \mathrm{C}$, the failure rate is less than $10 \%$. Only in the hottest conditions and smallest $\mathrm{V}_{\text {IN }}$ does the failure rate surpass $10 \%$.


Figure 3.11 - Monte Carlo simulations showing failure rates over a range of temperature and $\mathrm{V}_{\text {IN }}$.

## 4. EXPERIMENTAL RESULTS

### 4.1. Fabrication

The wake-up circuit has been fabricated in a $1 \mathrm{P} 6 \mathrm{M} 0.18 \mu \mathrm{~m}$ standard CMOS process. A die photo is shown in Figure 4.1. Three independent test circuits were fabricated. Only the DC input circuit ( $0.3 \mathrm{~mm} \times 0.2 \mathrm{~mm}$ ) is discussed in Chapter 3. The RF input circuit ( $0.3 \mathrm{~mm} \times 0.3 \mathrm{~mm}$ ) is the DC input circuit with a single-stage of the 36-stage RF energy harvester attached to its input. The third circuit is the DC input circuit attached to the full 36 -stage RF energy harvester and voltage regulator ( 0.7 mm x 0.5 mm ), as shown in Figure 2.3; it was fabricated for later, system-wide testing. The perimeter of the design is a conventional pad ring and each pad is fully ESD protected. The wafer was bonded in a MLF48 package (standard QFN package).


Figure 4.1 - Die photo of the test chip.

### 4.2. Test Board

The QFN package is mounted on a standard FR4 printed circuit board. A $120 \mathrm{~V} / 60 \mathrm{~Hz}$ to $6.1 \mathrm{~V} \mathrm{AC} / \mathrm{DC}$ converter supplies power to the test board. A 5 V regulator and a 1.8 V regulator provide the supply voltages required to verify the functionality of the design. The 5 V regulator supplies the on-board buffers and amplifiers. The 1.8 V regulator supplies a variable voltage divider that in turn powers the chip's ESD. Twopin jumpers can then route power to each of the three test circuits' power pins on the chip independently by adding or removing their headers. All inputs and outputs have SMA connectors for improved signal quality and ease of use with the test equipment.


Figure 4.2 - Photo of the test board.
In each of the three test circuits, all test-point outputs are buffered with the EL5427 2.5MHz rail-to-rail buffers. This buffer offers multi-channel packages and has a 1 pF input capacitance. Each power supply pin is buffered with a current sense resistor in the feedback loop.


Figure 4.3 - An operational amplifier (OPA340) and an instrumentation amplifier (INA321) in a current sense configuration.

Figure 4.3 shows an operational amplifier (OPA340) and an instrumentation amplifier (INA321) in a current sense configuration. General-purpose operational amplifiers and instrumentation amplifiers tend to have BJT input devices that have non-negligible input-bias currents. In order to detect currents as low as $1 n A$ accurately, the OPA340 and INA321 were selected for their low input-bias currents. These parts have CMOS input devices that sink or source currents from their inputs that are no more than 10 pA . The OPA340 keeps the $\mathrm{V}_{\mathrm{DD}}$ from the regulator and the $\mathrm{V}_{\mathrm{DD}}$ to the chip at the same voltage. All the current flowing to the chip is sourced by the OPA340 and flows through Rense. $_{\text {Se }}$ The INA321 amplifies the voltage potential across $\mathrm{R}_{\text {SENSE. }}$ Eq. (20) relates the output voltage, $\mathrm{V}_{\text {SENSE }}$, to the measured current, ISENSE.

$$
\begin{equation*}
\mathrm{I}_{\mathrm{SENSE}}=\frac{\mathrm{V}_{\text {SENSE }}}{A_{2} \cdot R_{\text {SENSE }}} \tag{20}
\end{equation*}
$$

The resistor, $R_{\text {SENSE }}$, is a $133 \mathrm{k} \Omega$ resistor, correlating to the desired range of $\mathrm{V}_{\text {SENSE }}, 1 \mathrm{mV}-1 \mathrm{~V}$, to the expected possible supply current, 750pA-750nA. Each resistor was independently measured and recorded prior to installation on the PCB.

### 4.3. Test Set Up

A Tektronix AWG2005 Arbitrary Waveform Generator (AWG) supplied the input stimulus in each test case, and a Tektronix TDS7401 Digital Storage Oscilloscope (DSO) with $10 \mathrm{M} \Omega$ input impedance recorded the results. A 50 5 terminated oscilloscope would have excessively loaded the high-impedance signals and could not have probed them.

To test the DC input circuit, the AWG was used to drive $\mathrm{V}_{\text {IN }}$ with 200 mV , 0.1 Hz and the Reset line with $1 \mathrm{~V}, 0.1 \mathrm{~Hz}$ square-waves in quadrature with the timing shown in Figure 3.9.

### 4.4. Propagation Delay of the DC Circuit

The measured operation of the DC input circuit is illustrated in Figure 4.4. This plot shows the results of 40 transitions and illustrates the range of propagation times $\left(\mathrm{t}_{\mathrm{p}}\right)$ measured from where the falling edge of the input crosses $\mathrm{V}_{\text {SW }}$ to the mid-point on the rising edge of the output for various amplitudes of $\mathrm{V}_{\text {IN }}$. The average value for $\mathrm{t}_{\mathrm{p}}$ is $418 \mu \mathrm{~s}$ with a $\Delta \mathrm{t}_{\mathrm{p}}$ of $33 \mu \mathrm{~s}$.


Figure 4.4 - Measured $V_{\text {IN }}$ and $V_{\text {OUT }}$ for amplitudes of $V_{\text {IN }}=\{50,100,150,200\} \mathrm{mV}$.

Figure 4.5 illustrates the measured propagation delays of a single wake-up circuit versus a range of $\mathrm{V}_{\text {IN }}$ over 100 iterations. The range of the variation due to $\mathrm{V}_{\text {IN }}$ is $33 \mu \mathrm{~s}$. The variation in propagation delay from one wake-up event to the next at the same $\mathrm{V}_{\text {IN }}$ is indicated by the vertical $6 \sigma$ error bars. The $3 \sigma$ variation is approximately $0.9 \%$ of the total propagation delay. This variation in the propagation delay is approximately twice the simulated results of Section 3.7.


Figure 4.5 - Measured propagation delays for various input amplitudes. The bars indicate $6 \sigma$ variations. The $3 \sigma$ variation is approximately $0.9 \%$ of the total propagation delay.

### 4.5. Power Consumption of DC Circuit

Figure 4.6 is a close up of the rising edge of $\mathrm{V}_{\text {OUT }}$, occurring approximately $400 \mu \mathrm{~s}$ after the falling edge of $\mathrm{V}_{\text {IN }}$. The first rising edge in Figure 4.6 is the switching transient of $\mathrm{V}_{\text {SENSE }}$, shown in Figure 4.3. The second rising edge is $\mathrm{V}_{\text {Out }}$. The value of $\mathrm{V}_{\text {SENSE }}$ on the left side of the figure shows the level of the static current. This value of 120 mV translates to a static current of 36 nA using Eq. (20). The circuit consumes 45 nW of static power from a 1.25 V supply at $20^{\circ} \mathrm{C}$.


Figure 4.6 - Measured static current and switching transient.
The area under the $\mathrm{V}_{\text {SENSE }}$ curve shown in Figure 4.7 is proportional to the total energy consumed during a single switching event. Eq. (21) uses Eq. (20) to relate the area under the $V_{\text {SENSE }}$ curve to the energy consumed per switching transient.

$$
\begin{equation*}
E_{S w}=\int_{t} V_{D D} \cdot I_{S E N S E} d t=V_{D D} \int_{t} \frac{V_{S E N S E}}{A_{2} \cdot R_{S E N S E}} d t=\frac{V_{D D}}{A_{2} \cdot R_{S E N S E}} \int_{t} V_{S E N S E} d t \tag{21}
\end{equation*}
$$

The integral of $\mathrm{V}_{\text {SENSE }}$ over time is the area under the $\mathrm{V}_{\text {SENSE }}$ curve in Figure 4.7. The area can be approximated as the area of a triangle shown in Eq. (22). Eq. (23) uses Eq. (21) and Eq. (22) to calculate an approximate value for the total energy consumed.

$$
\begin{align*}
\int_{t} V_{S E N S E} d t \simeq A_{\Delta} & =\frac{\text { base } \cdot h e i g h t}{2}=\frac{t_{s w} \cdot V_{S E N S E, P K}}{2}=\frac{5 \mu s \cdot 870 \mathrm{mV}}{2}  \tag{22}\\
E_{s w} & =\frac{1.2 \mathrm{~V}}{10 \cdot 133 \mathrm{k} \Omega} \cdot \frac{5 \mu \mathrm{~s} \cdot 870 \mathrm{mV}}{2}=2 \mathrm{pJ} \tag{23}
\end{align*}
$$

Each switching event consumes approximately 2 pJ of energy.


Figure 4.7 - Measured current consumed per switching transient.

### 4.6. Temperature Response

Implicit in this design has been the assumption that the wake-up circuit will work across a range of temperatures and that the propagation delays of the wake-up circuits is a predictable function of temperature. Figure 4.8 shows the propagation delays of a wake-up circuit as its temperature changes from -10C to 40C. Each successive rising edge of the output was observed to have a propagation delay greater than the previous rising edge. This is empirical evidence that the propagation delay is a monotonically increasing function of temperature.


Figure 4.8 - Temperature response of the wake-up circuit with constant $\mathrm{V}_{\text {IN }}$ value showing $t_{p}$ to be a monotonically increasing function of temperature.

### 4.7. RF Circuit Response

The only difference between the DC input circuit and the RF input circuit is the presence of a single stage full-wave floating-gate rectifier at the input. The rectifier converts the 900 MHz RF input into the DC level used to test the DC input circuit. The behavior of this floating-gate rectifier is documented in [7]. Figure 4.9 illustrates how the loss of the RF power signal triggers the output to toggle just as the loss of a DC signal triggers the output to toggle in the DC input circuit. The rest of the circuit behaves identically to the DC input circuit.


Figure 4.9 - Measured output response to an RF input.

### 4.8. Comparison to Prior Work

Table 4 compares the work presented in this thesis to other wireless sensor network synchronization methods. None of these has been fabricated in silicon and all consume more power than is available from the RF energy harvester. Table 4 shows that only the wake-up circuit consumes less than 100 nW and no other wireless sensor network synchronization method consumes less than $1 \mu \mathrm{~W}$. The synchronization limiting factor, listed in the table, refer to the accuracy with which each system can predict when any given sensor will wake up. The worst case asynchronization of the wake-up circuit is less than $8 \mu \mathrm{~s}$, more than an order of magnitude better than the next best system.

Table 4 - Comparison of the wireless sensor network synchronization methods.

| Method | Low Power <br> Mode <br> $[26]$ | Continuous <br> Timestamp <br> $[14]$ | Interrupt <br> Timer <br> $[13]$ | Wake-up Circuit <br> (this work) |
| :---: | :---: | :---: | :---: | :---: |
| Continuous <br> Power | $100 \mu \mathrm{~W}$ | $1-10 \mu \mathrm{~W}^{*}$ | $5.68 \mu \mathrm{~W}^{*}$ | 44 nW |
| Synchronization | Accuracy of <br> external <br> interrupt. | $1 \mathrm{~ms}-$ <br> Data rate of <br> 1kbps data <br> stream. Requires <br> line-of-sight. | $100 \mu \mathrm{~s}-$ <br> Period of <br> 10 kHz <br> clock. | $8 \mu \mathrm{~s}-$ <br> $\pm 3 \sigma$ uncertainty <br> of the <br> propagation <br> delay |

*Simulated

Table 5 compares the latched comparators presented in this thesis to prior latched comparators. The values reported for all these comparators were measured at much higher frequencies than this design requires and no static power values were reported. However, all four require a $3-3.3 \mathrm{~V}$ supply. Additionally, the three that consume the least power have offset voltages that disqualify them from this application where the comparator must register a difference between 0 mV and 58 mV . Each of the comparators would also have to work in conjunction with a reference voltage, increasing their power requirements by several microwatts. The minimum power used by a latched comparator and a reference voltage combination is orders of magnitude greater than the total power used by the design presented in this thesis.

Table 5 - Comparision of the latched comparator to prior work

| Method | Variable <br> Load <br> Comparator <br> $[17]$ | Low Power <br> Differential <br> Current <br> $[18]$ | Resistive <br> Divider <br> $[18]$ | Charge <br> Sharing <br> $[18]$ | Threshold Based <br> Reference <br> Latched <br> Comparator <br> (this thesis) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Continuous <br> Power | $340 \mu \mathrm{~W}^{*}$ | $138 \mu \mathrm{~W}^{*}$ | $114 \mu \mathrm{~W}^{*}$ | $88.2 \mu \mathrm{~W}^{*}$ | 44 nW |
| Supply <br> Voltage | 3 V | 3.3 V | 3.3 V | 3.3 V | 1.2 V |
| Max Offset <br> Voltage | 3 mV | 164 mV | 32 mV | 32 mV | 10 mV |

*Requires additional reference voltage

## 5. CONCLUSION

A new low-power latched comparator has been presented as a part of a batteryfree, RF energy harvesting wireless sensor network. It uses multiple common-source amplifiers to amplify the DC input signal to control the power to the system. Combined with a feedback latching circuit, the latching comparator has a threshold voltage less than 58 mV . The design presented in this thesis draws less than 45 nW of static power at $20^{\circ} \mathrm{C}$. Finally, it provides a synchronization method that consumes two orders of magnitude less power with increased synchronization accuracy.

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