- **1** Supplementary Material
- 2 S1: Thermodynamical argument:
- 3 Gas bubble surrounded by intergranular capillary-held water and a thick water film
- 4

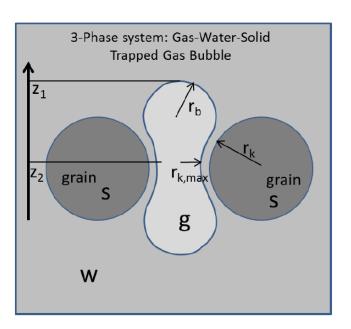




Figure S1 Trapped gas bubble surrounded by intergranular capillary-held water and a thick
water film.

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9 (i) Assumption: The glass beads sediment is completely surrounded by intergranular capillary10 held water and a thick, coherent (= continous) water film (normal water phase with same density
11 and viscosity as the bulk water phase).

(ii) For a stable trapped gas bubble shown in Fig. S1 the gas pressure inside the bubble has to beconstant:

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$$p_g(z_1) = p_g(z_2)$$
. (S1)

(S3)

15 With

$$p_g(z) = p_c(z) + \rho_w g \cdot z, \tag{S2}$$

17 one obtains the *thermodynamic stability condition*:

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20

where the equality sign stands for g = 0, i.e. for a horizontal gas bubble and r_k denotes the grain radius.

23 (iii) Calculation of the capillary pressure by the Young-Laplace equation yields:

 $p_c(z_2) - p_c(z_1) = p_c(z) + \rho_w g(z_1 - z_2) \cong \rho_w g \cdot r_k \ge 0,$

24
$$p_c(z_1) = 2\gamma_{g,w}/r_b \cong 2\gamma_{g,w}/r_{k,max}$$
(S4a)

25
$$p_c(z_2) = \gamma_{g,w} (1/r_{k,max} - 1/r_k)$$
 (S4b)

26 $(r_b - \text{bubble radius}, \gamma_{g,w} - \text{surface tension or excess free energy}).$

(iii) Inserting (S4) into (S3) yields a negative expression for the difference of the capillary
pressures and therfore a contradiction to assumption (i), namely:

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$$p_c(z_2) - p_c(z_1) = -\gamma_{g,w}/r_k(1 + 1/\xi_{max}) < 0$$
(S5)

31 with $r_{k,max} = \xi_{max} \cdot r_k$.

(iv) Conclusion: The result (S5) can be interpreted in two ways: (i) If there exists a *stable* trapped gas bubble with $r_b > r_{k,max}$ a surrounding thick water film is thermodynamically not possible. (ii) If there exists a thick water film, then trapped gas bubbles with $r_b > r_{k,max}$ are thermodynamically *unstable*. Since about 50% of all trapped gas bubbles (see Table S1) have a radius larger than $r_{k,max}$ and the trapped gas bubbles exhibit a negative curvature shown in Fig. 4, a complete wetting of the whole sediment by intergranular capillary-held water and thick water films is thermodynamical not possible.

39 (v) Disjoining pressure and augmented Young-Laplace equation

40 If we add an additional repulsive disjoing pressure to the capillary pressure at z_2 we obtain the 41 augmented Young-Laplace equation:

42 $\tilde{p}_{c}(z_{2}) = p_{c}(z_{2}) + \Pi(h),$

43 where $\Pi(h)$ denotes the short-ranged disjoining pressure, and *h* the film thickness. Inserting (S6) 44 into (S3) yields:

45

$$\Pi(h_{equ}) = \frac{\gamma_{g,w}}{r_k} \left(1 + \frac{1}{\xi_{max}}\right) + \rho_w g r_k \cong 400 \ Pa \ , \tag{S7}$$

(S6)

with $\gamma_{g,w} = 73 \text{ mN/m}$, $r_k = 0.5 \text{ mm}$, and $\xi_{max} = 0.6$ (see Geistlinger et al., 2006). Physically, (S7) means that a new mechanical equilibrium has been established at the gas-water interface for a disjoining pressure of about 400 Pa (see Fig. 3 Disjoining pressure isotherm). In order to obtain a rough estimate of the relevant scale of the equilibrium film thickness h_{equ} we calculate the disjoining pressure by van der Waals forces only (for details see Safran, 1997):

51 $\Pi_{vdW}(h) = \frac{-A_{123}}{6\pi h^3},$ (S8)

with the Hamaker constant $A_{123} = -1.3 \times 10^{-20}$ J (French, 2000). Inserting (S8) into (S7) yields the relevant scale for the equilibrium film thickness of about 12 nm, i.e. the new equilibrium leads to a stable thin adsorbed water film.

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(viii) What about incoherent, *discontinous thick water films*? They are thermodynamically
possible?
According to the *Second Law of Thermodynamics* the system at thermodynamic equilibrium trys
always to find it minimal *Free Energy*. We compare the *Free Energy* of a thick film (thickness =

62 δ that covers a grain and a triangular pendular ring (inner radius = 0, outer radius = r_a). The

63 boundary condition of equal phase volume yields:

64
$$r_a(\delta) = \sqrt[3]{\frac{4}{\sqrt{3}} \cdot \{(r_k + \delta)^3 - r_k^3\}}$$
(S6)

The difference of the *Free Energy* considering only the gas-water *Excess Free Energy* is

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 $\Delta F = \gamma_{g,w} \cdot 4\pi \{ (r_k + \delta)^2 - r_a^2(\delta)/\sqrt{3} \}.$ (S7)

68 Calculating ΔF for $r_k = 0.5$ mm (1mm-GBS), yields for film thicknesses $\delta < r_k$ positive values for

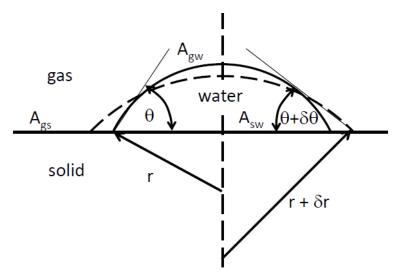
69 ΔF . Hence, the thick film will draw back to a pendular ring, since its *Free engergy* is smaller, i.e.

70 incoherent thick films that cover a grain are thermodynamically not stable!

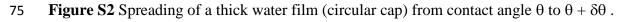
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72 S2: Thermodynamics of Interfaces: Calculation of the Free Energy

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(i) We consider a spherical curved water film with a circular-cap geometry shown in Fig. S2 withthe following boundary lines (or 2D-interfaces):

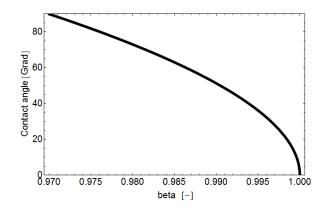
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$$A_{g,w} = 2r\theta, \tag{S9}$$

80
$$A_{s,w} = 2r \cdot \sin(\theta), \qquad (S10)$$

81 and the area or 2D-volume of the water phase:

82
$$V_w = r^2(\theta - \sin(2\theta)/2),$$
 (S11)

83 84 (ii) An increase of the g-w-interface by $dA_{g,w}$, will increase the *Free Energy* of the system by 85 $dF_{g,w} = \gamma_{g,w} \cdot dA_{g,w}$ (S12)86 and $dF_{s.w} = \gamma_{s.w} \cdot dA_{s,w},$ 87 where γ [Nm/m] denotes the Excess Free Energy. Physically, the increase is caused by the loss 88 of binding energy, i.e. water molecules from the phase volume (binding energy $\sim 12 \epsilon$ for face-89 centered coordination) lose ~ 6 ε of their binding energy (= negative energy!), if they reach the 90 surface. 91 92 (iii) The system wins binding energy, if the g-s-interface $dA_{s,g}$ is decreased, since water 93 molecules in general are stronger bounded at the solid surface than gas molecules, i.e.: $dF_{s,g} = -\gamma_{s,g} \cdot |dA_{s,g}|.$ (S13) 94 (iv) The system at thermodynamic equilibrium possesses a minimal Free Energy, therefore 95 96 holds: $dF = \gamma_{g,w} \cdot dA_{g,w} + \gamma_{s,w} \cdot dA_{s,w} - \gamma_{s,g} \cdot |dA_{s,g}| = 0.$ 97 (S14) (v) Boundary condition: The volume of the water phase, V, do not change. 98 dV = 0.99 (S15)With (S11) and (S15) we obtain: 100 $\delta\theta = -2/3 \cdot \theta/r \cdot \delta r.$ 101 (S16) (vi) We consider the geometry of a 2D-circular cap and calculate the changes of the interfaces 102 103 (z-dimension is not considered, i.e. one has to multiply each expression by z_0 to obtain the right 104 dimension): $dA_{a,w} = 2/3 \cdot \theta \cdot \delta r$, 105 $dA_{s,w} = (2 \cdot \sin(\theta) - 4/3 \cdot \theta \cdot \cos(\theta)) \cdot \delta r = B(\theta) \cdot \delta r.$ 106 (S17) 107 (vii) Inserting of (S17) into (S14) yields the following implicite equation for the contact angle in 108 thermodynamic equilbrium: $\theta - \frac{3}{2} \cdot \beta \cdot B(\theta) = 0,$ (S18)109 where $B(\theta)$ is defined in Eq.(S17) and where we have introduced the wetting parameter 110 $\beta = \frac{\omega}{\gamma_{aw}}$, (S19) 111 112 with $\omega = \gamma_{s,g} - \gamma_{sw}$. In Fig. S3 we show the sensitive dependency of the contact angle on the 113 wetting parameter β for partial wetting, i.e. for $0 \le \theta \le 90^\circ$. 114 115



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Figure S3 Contact angle versus wetting parameter β .

118 Complete wetting occurs, if $\beta \ge 1$, i.e. the radius tends to infinity according to

- 119 $r(\theta) = \sqrt{\frac{r_0^2}{(2\theta \sin(2\theta))}},$ (S20)
- 120 with $r_0 = r(\pi/2)$.

(viii) Under the assumption that the interaction of gas molecules with the solid surface is of 121 122 similar order of magnitude as the interaction of NAPL-molecules (like Toluene; see Pan et al., 2007) with the solid surface, we can consider ω as constant or at least as a small increasing 123 124 function compared to $\gamma_{NAPL,w} = \gamma_{g,w} - \gamma_{g,NAPL} \approx (73 - 29)$ mN/m. Therefore, we obtain a larger β -125 value and a according to Fig. S3 a smaller contact angle. Since the area of the fluid-fluid interface is inverse proportial to the contact angle, we anticipate a larger interfacial area for the 126 gas-water system as for the NAPL-water system, i.e. the NAPL-w-interface will extend more 127 128 than the g-w-interface in thermodynamic equilibrium.

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130 S3: Complete histogram with noisy voxels (Voxel-Nr: 1 -10) for experiment 7.

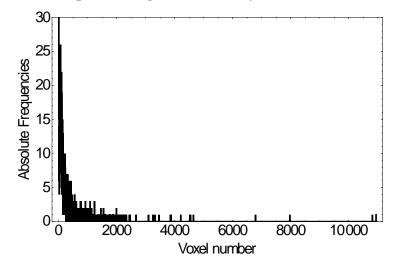


Figure S4 Histogram of unique objects (gas cluster with a certain voxel number) for experiment7.

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135 S4 Cluster statistics, bubble-size distribution, and pore-size distribution for 2nd series of

136 experiments (3 experiments under same WT-rise)

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138 Cluster statistics

- **Table S1** Cluster statistics (sp single-pore trapped gas bubbles with $r_b < r_{k,max}$; mp multipore-
- trapped gas bubbles with $r_{k,max} < r_b < r_k$; and l large trapped gas bubbles; N number of bubbles; V gas volume).

Table S2 LogNormal-Bubble-size distribution: Mean bubble radius and SDV.

Experiment	N _{tot}	N _{sp}	N _{mp}	Nı	V_{sp}	V _{mp}	Vı
		[%]	[%]	[%]	[%]	[%]	[%]
7	3695	53	37	10	16	40	44
8	3687	51	38	11	16	42	42
9	4445	50	38	12	12	35	53

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143 **Bubble-size distribution**

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Experiment	Mean radius [mm]	SDV [mm]
7	0.24	0.07
8	0.24	0.07
9	0.23	0.08





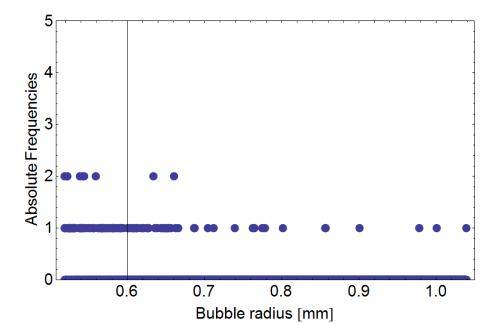


Figure S5 Bubble-size distribution for $r_b > r_k$ (experiment 7).

In Figure S5 the bubble-size distribution is shown for larger bubble radii $r_b > r_k$. Up to $r_b = 0.65$ mm the distribution is nearly uniform; and then rather sparse with only 14 trapped gas bubbles.

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156 **Pore-size distribution**

157 **Table S3** Pore-size distribution. Mean radius and SDV for the Normal (column 2 and 3) and the

158 LogNormal (column 4 and 5) pore-size distribution.

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Experiment	Mean [mm]	SDV [mm]	Mean [mm]	SDV [mm]
7	0.162	0.057	0.175	0.063
8	0.167	0.060	0.181	0.063
9	0.170	0.060	0.181	0.063

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163 **S5 Experimental verification of static bubble distribution**

In order to proof that the trapped gas phase is static and will not dissolved during the experiment, we conduct an experiment for a 0.7mm-GBS ($d_{50} = 0.7$ mm, packing density 1.56 g/mL, porosity = 0.37) for a WT-velocity of 0.5 cm/min that is equal to that of the second experimental series (exp. 7 -9). The CT-images were taken after 3 different times, 20 min, 3h, and 24 h. The evaluated quantities are listed in Table S4.

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Table S4 Porosity, volumetric gas content, total surface and gas-water for 3 different times after
 WT-rise.

Time	Porosity	Error [#]	Gas content	a _g	a _{gw}
	[-]	[%]	[-]	[1/mm]	[1/mm]
20 min	0.386	4	0.0136	0.170	0.161
3 h	0.387	5	0.0138	0.165	0.156
24 h	0.385	4	0.0136	0.171	0.161

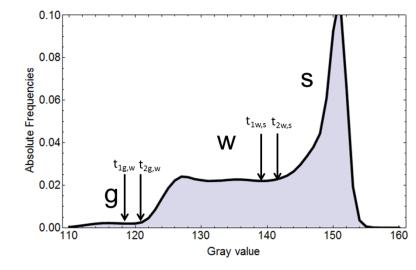
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177 S6 Histogram of the whole origial imgae of experiment 7.

Fig. S5 shows the complete tri-modal histogram of the original image of experiment 7 indicating the different phases and the threshold pairs $(t_{1g,w}, t_{2g,w})$ and $(t_{1w,s}, t_{2w,s})$ for segmentation of the gas phase and water phase and the water phase and the solid phase, respectively.

¹⁶²



183 184 Figure S6 Historgram of the complete CT-image of experiment 7.

