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Graph production by computer requires a blending of human effort in scale selection with computer precision in datum point placement. Existing techniques are designed primarily for computer scientists; the average scientific investigator, educator, or businessman tends to avoid them for one or more of the following reasons: expense, complexity, or excessive turnaround. This dissertation describes development and application of a graph preparation system designed for unsophisticated users which is moderate in cost, easy to use, and provides immediate interactive response.

It is written in BASIC on a Univac 1108 and utilizes low cost Tektronix graphics terminals. Through menu selection, the user defines scale factors, datum point indicators, axis type (linear or logarithmic), and adds
optional functions which may be displayed superimposed on the data. Immediate display of the results to encourage user creativity in modification of parameters is an important feature of the system.

Step-wise implementation, which maximized user input to system design, is described. Extensive modification of commercially obtained plot driving routines allowed expansion of program features in accord with user requests.

Four detailed examples illustrate the use of the system by biologists and ecologists in communication of results and in analysis of data. A complete program listing and user's manual are appended.

# AN INTERACTIVE COMPUTER GRAPHICS SYSTEM APPLIED TO THE LIFE SCIENCES 

by

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## A THESIS

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## TABLE OF CONTENTS

I. Introduction ..... 1
II. Background ..... 5
Manual Graph Preparation ..... 7
Computer Aided Graph Presentation ..... 10
Mechanical Plotters ..... 12
On-Line Printers. ..... 13
Cathode Ray Tube (Refreshed). ..... 16
Cathode Ray Tube (Storage Tube) ..... 18
Comparison of Computer Graphing Systems ..... 19
III. Strategy ..... 21
Computer Environment ..... 21
BASIC ..... 25
BASIC at CSC ..... 27
Techniques for Interactive Programming. ..... 29
Goals for EZPLOT. ..... 31
IV. Implementation ..... 34
TEKPLOT Subroutines ..... 36
EZPLOT Subroutines. ..... 40
EZPLOT Logic ..... 44
Example of Use. ..... 47
Conversion Considerations ..... 55
V. Applications ..... 59
Ant Activity Analysis ..... 59
Einsteinium-253 Excretion ..... 70
Probit Analysis ..... 76
Zinc-65 in Algae ..... 80
VI. Summary and Conclusions. ..... 87
Bibliography ..... 91
Appendix A - Text of EZPLOT ..... 95
Appendix B - EZPLOT Users Manual ..... 120

## LIST OF ILLUSTRATIONS

| Figure |  | Page |
| :---: | :---: | :---: |
| 1 | Example of the type of graph produced by EZPLOT (reduced from original size). | 2 |
| 2 | Graph of hypothetical data drawn by a offline mechanical (CalComp) plotter. | 14 |
| 3 | Graph of hypothetical data printed by a teletype. | 15 |
| 4 | Relationship between hardware components used by EZPLOT. | 22 |
| 5 | Flow chart of main logic of EZPLOT. | 35 |
| 6 | Logic of horizontal axis drawing portion of EZPLOT. | 42 |
| 7 | Display of data file for EZPLOT example. | 50 |
| 8 | Graph of hypothetical data using automatic scaling option. | 51 |
| 9 | Graph of hypothetical data obtained by using manual scaling routine. | 51 |
| 10 | Interactions between EZPLOT and user which preceeded display of figure 9 . | 53 |
| 11 | Graph of hypothetical data with superimposed functions. | 54 |
| 12 | Graph of hypothetical data with superimposed functions on semi-log axes. | 54 |
| 13 | Number of active ants at a given soil surface temperature, composite of 3 days of observation. | 61 |
| 14 | Printout of a portion of the interactive polynomial regression analysis of ant activity data. | 63 |


| Figure |  | Page |
| :---: | :---: | :---: |
| 15 | Detailed printout of portion of third degree polynomial fit to ant activity data. | 64 |
| 16 | Number of active ants at given temperature with 3rd and 4th degree polynomial fits superimposed. | 66 |
| 17 | Number of active ants observed after noon at a given temperature, with polynomial regression fit superimposed. | 68 |
| 18 | Number of active ants observed before noon at a given temperature, with polynomial regression fit superimposed. | 68 |
| 19 | Number of active ants observed after noon at a given temperature, with linear model superimposed. | 69 |
| 20 | Number of active ants observed before noon at a given temperature, with linear model superimposed. | 69 |
| 21 | Percent of injected einsteinium-253 excreted in urine of miniature swine. | 74 |
| 22 | Mean and 95\% confidence interval of percent of injected einsteinium-253 excreted in urine | 74 |
| 23 | Mean percent einsteinium-253 excreted with two non-linear regression lines shown. Horizontal scale extended to 200 days. | 75 |
| 24 | Mean percent einsteinium-253 excreted with outliers removed, illustrating rounded regression function. | 75 |
| 25 | Output of probit analysis computer program. | 78 |

Figure Page
26 Graph of output of probit analysis program ..... 79 with partially erased grid lines used to highlight the $\mathrm{LD}_{50}$ point.
27 Radioactivity observed in algae colony ..... 83after fresh water replaced Zinc-65 labeledwater. Results of two non-linear modelsare superimposed on the data.
28 Residuals from the modeling of Zinc-65 ..... 85 activity in algae after freshwater added fit to a sine function. This illustrates the circadian rhythm discovered in the algae.

# AN INTERACTIVE COMPUTER GRAPHICS SYSTEM APPLIED TO THE LIFE SCIENCES 

## I. INTRODUCTION

Graphs are an important mode of communication in science, education and business. They may be prepared manually or with the aid of mechanical and electronic devices. This report describes development and application of an interactive computer graphics system based on low cost, storage type, cathode ray tube (CRT), computer terminals. It is designed primarily for use by persons unfamiliar with computer techniques. It allows them to prepare linear or logarithmic graphs by answering a series of questions about their data and the desired scale factors. While still seated at the terminal, they may view the resulting graph, modify the data and/or the scale factors, view the new graph, make further modifications, and so on, until satisfied with the results. A hard copy generating device produces output as shown in Figure 1.

The system, called EZPLOT, does not replace existing computer techniques for displaying data, rather it compliments them. These techniques are compared through discussion of their advantages and disadvantages in the second chapter of this dissertation. Some give excellent results
hifothetical data to illustrate ezplot

but are either costly or slow, others are quick and inexpensive but give relatively crude results. EZPLOT falls in the middle of this spectrum of graph drawing computer techniques. Its main advantage is immediacy, its primary disadvantages are the fixed physical size of the output and the premium cost generally charged for interactive computer usage. Throughout the design phase of system development, the paramount concern was to make EZPLOT responsive to the needs of persons who understand graph drawing but are uninterested in computer technology. Four elements of system design, discussed in Chapter Three, were carefully considered prior to implementation. These four, hardware environment, software environment, techniques of interaction with the user, and reasonable goals for the system, determined the character of EZPLOT.

The fourth chapter of the dissertation deals with implementation, which progressed step-wise as new groups of goals were added to operational ones. This type of implementation insured that the system fit the needs of the users. New features were added in response to user requests rather than as a result of the computer scientist's idea of what the user might want.

The system is used by researchers in the Biology and Ecosystem Departments of Battelle Northwest. The fifth chapter deals with examples of statistical analysis of their data in which EZPLOT made a significant contribution to understanding of experimental results.

The essential configuration for operation of this system is: 1) a computer, 2) a CRT graphics terminal, 3) a hard copy generator (optional), 4) availability of BASIC computer language, and 5) the program EZPLOT. The implementation described at Battelle Northwest uses the following specific items:

- Computer - Univac 1108 (operated by Computer Sciences Corp.)
- Operating System - CSCX
- Language - BASIC (enhanced version by CSC)
- Terminal - Tektronix 4002 or 4010
- Hard Copy Unit - Tektronix 4610 .

EZPLOT could be installed on another computer with similar terminals; however, variations in BASIC compilers could require program modifications which would limit the flexibility of the system.
II. BACKGROUND

Scientific investigators are accustomed to presenting their findings in the form of a graph. People in other disciplines also make liberal use of graphic techniques for presenting data. Experts on the art of technical report writing assume that their readers are familiar with and frequently use graphs.

Graphs are so useful -- and so common -- that definition is almost pedantry: everyone is familiar with them and knows quite well what they are. They are particularly the instrument for representing pictorially all kinds of numerical data. . . . graphs are useful in a multiple variety of technical, industrial and governmental communications -- so useful, indeed, for so many purposes that every kind of report writer employs them and every kind of reader is accustomed to them (9, p. 192).

It is true that graphs are useful and ubiquitous;
however, at the risk of being pedantic, a dictionary definition is inserted here for clarity.

GRAPH (graf), n. I. A drawing that exhibits a relationship, often functional, between two sets of numbers as a set of points having coordinates determined by the relationship. 2. Any pictorial device, as a pie chart or bar graph, used to display numerical relationships. Also called "chart". 3. A representation of a quantity, as of a complex number, by a geometric object such as a point in a plane. (l, p. 574)

The first and more common meaning is, of course, the type of graph that EZPLOT produces.

Although these definitions stress the ability of a graph to make clear some relationship that has been deter-
mined, there are two reasons for preparing a graph of one's data: 1) to communicate, and 2) to analyze.

The primary purpose of the graph is to present numerical data in visual form. With the growth of its use in numerous fields of endeavor, the functions of the graph have multiplied. It serves as a means of presenting visually tables of statistics in a simple, readable, and interesting form. The graph also makes clear undiscernible facts, such as correlations, which might be overlooked in tabulated data. It facilitates the presentation of facts for comparative purposes, and in many instances the graph indicates significant facts not obviously apparent in numerical form.

The most useful purpose of the graph is to save time and effort in analyzing statistics and tables. . . . In addition, it permits the drawing of logical conclusions on the basis of the data depicted (4, p. 3).

This dual purpose for drawing graphs is usually overlooked in discussions of graphing techniques. The usefulness of a graph as an indicator of "significant facts not obviously apparent" (4, p. 3) is limited by the time and effort required to prepare each graph. For example, if one has ten sets of similar data, there is a strong temptation to graph one set carefully and assume that the relationship is similar for the other nine. Or, if a set of data is graphed on linear paper and there is no apparent reason for re-drawing the same graph on logarithmic or semi-logarithmic paper, it will probably not be re-drawn.

For these reasons, instructions on graph preparation tacitly assume that the person preparing the graph intends to use the graph as an aid in communication rather than as an aid in analysis. This assumption implies that graphs intended for communication should follow guidelines for effective communication and that graphs for analysis need not be as carefully prepared. With the help of computers to do the drudgery, it is possible to prepare precise and easily understood graphs for both purposes.

The limitations and advantages of computerized approaches to graphing must be viewed in light of the manual procedure.

MANUAL GRAPH PREPARATION
The manual technique for preparing a graph is a twostep process. The first phase is creative; it involves human judgement and imagination in selecting the appropriate axes and scale factors to produce a pleasing graph. The second phase is mechanical or routine: data symbols are placed at the proper coordinates, axes are labeled, titles are supplied, etc. Instructions for graph preparation usually contain a list similar to the following:

1. Select the type of coordinate paper.
2. Determine the variables for ordinate and abscissa.
3. Determine the scale units.
4. Locate the axes and mark the scale values in pencil.
5. Plot the points representing the data.
6. Draw the curve. If the curve is to strike an average among the plotted points, a trial curve should be drawn in pencil. If the curve consists of a broken line, as is the case with discontinuous data, the curve need not be drawn until the graph is traced in ink.
7. Label the axes directly in ink.
8. Letter the titles, notes, and so on. The title should be lettered on a trial sheet that can be used as a guide for lettering directly in ink on the graph.
9. Check the work and complete the diagram by tracing the curve in ink (18, p. 529).

The two phases are clear: steps 1, 2, and 3 are the only ones that require judgement, the others are more mechanical.

For small sets of data, the manual procedure is convenient and simple. The person preparing the graph probably has a supply of various types of graph paper at his desk and has an intuitive feel about selecting the paper and preparing the graph. Problems appear when he finds that his choice of scale factors emphasize the wrong aspect of his data. Should he re-draw the graph, or are there more pressing things to do with his time? Another problem arises when a colleague asks the casual question: "I wonder what that would look like on semi-log paper?" These demands on a person's time are compounded if the data set is large.

The time required to produce such a graph is dependent on the two steps. The time for the first step, the creative process of choosing scales, may be considered constant. The time for the mechanical portion depends on the number of points. As the number of data points increases, the anticipated time to complete the graph increases. At some number of data points the investigator will decide that it is not worthwhile to draw the graph by hand. There are several options available when the anticipated graphing time exceeds that which one is willing to commit: l) the technician may be employed to prepare the graph; 2) the apparent number of data points may be reduced by plotting representative points such as every fifth or tenth one; and 3) the data may be summarized and appropriate averages plotted. These techniques may be useful if the purpose of the graph is communication. However, if the purpose is analysis, these techniques may cause the investigator to overlook some fact not obviously apparent in summarized or tabular form.

The value of manual graph preparation is two-fold: the person primarily associated with the data is directly involved and the cost is low. There are three major disadvantages: first, the time required becomes large as the
size of the data set increases; second, it involves drudgery; and third, it is usually necessary to re-draw a polished copy for publication.

## COMPUTER AIDED GRAPH PREPARATION

There are several viable alternatives to manual graph preparation. They all apply the computer to the mechanical portion of the process. Most of them complicate the creative aspects of graph preparation.

None of the existing computer aided graph producing techniques is able to replace the first phase of the graphing procedure, the human judgement as to scale factors. To do that would require that this phase of the process be reduced to an algorithm. Several attempts have been made to do this by formulating rules and guidelines (8, 4). However, more realistic authors contend that there is no universal way of choosing axes and scale factors because each graph is unique $(20,30)$.

In 1943 the American Society of Mechanical Engineers attempted to standardize graphing techniques through the publication: "American Standard for Engineering and Scientific Graphs for Publication". This standard is quite specific and detailed as to the choice of scale factors, etc. For example:
(d) For arithmetic scales, the scale numbers shown on the graph and space between coordinate rulings should preferably correspond to 1,2 or 5 units of measurement, multiplied or divided by $1,10,100$, etc. (3, p. 14).

In 1959, this body published revised standards (1) which abandoned detailed codification in favor of a series of examples of good and poor graphs. Human judgement is recognized as a key factor in successful presentation of graphs.

Production of graphs with a computer will always involve an interaction between the user and the computer. The utility of computer aided graphing procedures should be judged by three criteria: convenience, speed, and quality. The method of determining and modifying scale factors should be convenient; it should approximate the manual procedure. The results should be available quickly; the computer should draw a graph faster than the user can. The quality should be excellent; there should be no reason to re-copy a computer-produced graph for publication.

No computer aided graphing system meets all these goals. Each system is deficient in one or more of these areas. That means that the user must choose the system that will meet his particular need. The system which prepares graphs of publication quality is probably not the
system of choice for analyzing a set of data.
For purposes of comparison, the major systems are condensed into four types: mechanical (either incremental or vector) plotters, conventional on-line printers, traditional cathode ray tube terminals, and storage tube CRT devices.

## MECHANICAL PLOTTERS ${ }^{1}$

This category includes devices such as the Cal Comp flat bed and drum plotters which are designed specifically to produce hard copy computer controlled graphic output by mechanically positioning a writing instrument on some type of paper. They excel at preparing high resolution drawings for blueprints, printed circuit layouts, etc.

Several steps are required to cause a mechanical plotter to prepare a graph. The data are translated into commands which position the plotter pen by a program operating in the main computer. These commands are transferred to the plotter, usually as a file on magnetic tape, although some mechanical plotters operate on-line. The plotter then follows the commands to produce the graph. An

[^0]example, produced by a Cal Comp plotter, is shown in Figure 2.

This process is rather difficult for the user because of the time delay (turnaround times of several hours to a day or more are common) and because most plot preparation programs require more than casual familiarity with computer programming techniques. Because of the high quality of the output, many people accept the inconvenience of obtaining the services of a computer programmer whenever a series of graphs is needed.

ON-LINE PRINTERS
Line printers and teletypes are used as graph printing devices when low cost and rapid turnaround is important. Although such graphs lack precision and clarity as shown in Figure 3, they are sometimes helpful in analysis of data.

Any computer with printed output can be programmed to produce such graphs at the same cost as normal output. This type of graph is frequently incorporated in the output of routine data analysis programs in which the axes and scale factors remain fixed. Some computer installations provide interactive user-oriented graph producing packages



FIGURE 3. Graph of hypothetical data printed by a teletype.
in conjunction with time sharing operation of teletype terminals. ${ }^{2}$

Graph production on this type of device requires different logic from that outlined for manual graph production. Since the paper moves one line at a time in only one direction, the graph must be printed in that sequence. Thus, the computer program must store at least a portion of the 2

Three such plot routines are described in: CSCX BASIC Library, (Computer Sciences Corp., Los Angeles, 1969). They are: Scatter, Line-Plot, and Histogram. These subroutines of ***STATPK (discussed on pp. E00004-00.123-00 through E00004-00.125-00) are easy to use, but the user has no control over scale factors. Figure 3 was made with Line-Plot.
graph and scan it for printing. The programmer is focused to think in terms which are unfamiliar to the person accustomed to preparing graphs manually.

A new type of line printer, classified as nonimpact devices, operates by drawing the characters rather than printing them by impact (37). Although these devices require special paper and cannot produce multiple copies, they are quiet, inexpensive and fast. In large computer installations they tend to be used as remote terminals. They are often the only printing device attached to minicomputers.

Several of these printers have true graphic capability. If the printer can draw letters, it should also draw lines. The graphic capabilities of this class of printers are presently underexploited. The logic required to draw a graph suffers from the same handicap as with impact line printers. Storage of a display may tax the capacity of a minicomputer memory. Given the proper software, this type of printer could make a valuable contribution to the art of data analysis.

## CATHODE RAY TUBE (REFRESHED)

The term computer graphics is usually associated with the type of CRT found in television receivers. Because of
the short (millisecond) persistence of the phosphor on the screen, the display must be re-written several times each second. In return, the pattern on the screen may be caused to change dynamically. This requires that the computer store the contents of the entire screen which may consist of several hundred thousand raster positions. The usual practice is to operate the graphics terminal through a computer dedicated to that purpose.

The initial cost of a CRI terminal and associated computer is nigh ( $\$ 100,000$ or more) and the operating cost is high because of the requirement that the computer exclusively service the graphics terminal. Consequently, this system is seldom used for the pedestrian task of graphing data. The primary use of refreshed CRT terminals is in computer aided design. In this capacity, effective use has been made of the computer's ability to rotate displays, add or delete portions on command, recall diagrams of component parts from a data bank and assemble the parts on the screen (15, 22, 23).

The usual method of obtaining a hard copy of the display on the screen is either through photography or by directing the display file to an off-line mechanical plotter.

## CATHODE RAY TUBE (STORAGE TUBE)

This relatively new type of device differs from the conventional CRT in that the image is viewable for long periods of time (an hour or more if necessary) (31, 35). Graphic output may be written a dot at a time; however, the entire screen must be erased if the display is to be changed. In exchange for the loss of ability to dynamically alter the display, this system drastically reduces the cost of CRT graphics. The initial cost is moderate (under $\$ 10,000$ ), and the operating cost is comparable to that of other time sharing terminals.

A hard copy device is available which produces good quality copies on photosensitive paper. The figures in this dissertation were obtained from such a device.

Software is available which is similar to that for off-line mechanical plotters (32). Through calls to FORTRAN sub-routines the user's program creates a series of commands which position the electron beam on the screen. Because the process is much quicker than that described for off-line mechanical plotters, storage tube CRT terminals are often used as preview devices. The user can adjust parameters until he is satisfied with the display, then cause the same display to be plotted mechanically.

## COMPARISON OF COMPUTER GRAPHING SYSTEMS

The characteristics of the four systems are summarized in Table. I.

TABLE I. CHARACTERISTICS DF COMPUTER AIDED GRAPH PRODUCING SYSTEMS

| Type of System | Mechanical <br> Plotter <br> (Off-Line) |  | On-Line Printer <br> Or TTY |  | CRT <br> (Refreshed) |
| :--- | :--- | :--- | :--- | :--- | :--- |

[^1]The choice of a computer aided graph drawing system depends on the purpose of the graph and the needs of the user. Mechanical plotters are preferred when there is ample time and high quality output is important. On-line printers, which combine low cost with speed, are useful adjuncts to data analysis. Investigators with access to traditional computer graphics terminals will continue to insist on the convenience of dynamic interaction with the display as long as they can afford the cost of operating such devices. Display systems built around storage tube

CRT's offer a compromise, combining the convenience of a visual display with moderate cost.

A general purpose graph-drawing system should produce graphs good enough for effective communication at a cost (of time and money) low enough to promote its use in analysis of data. With this principle in mind, a strategy was developed to effectively use a Tektronix 4010 storage tube CRT terminal as an interactive graph drawing tool.

## III. STRATEGY

The effectiveness of a computer application depends on the balance with which the resources of computer technology are applied to the problem at hand. The result must be both cost effective and user effective. Three strategic aspects of program development were considered in designing EZPLOT:

- Computer environment
- Programming language
- Techniques of interactive programs.

Analysis of these factors and discussions with a group of scientific investigators who expressed interest in using computer aided graph drawing resulted in a set of specific goals for EZPLOT which satisfy many user needs at a minimum cost.

COMPUCIER ENVIRONMENT
Understanding of the hardware configuration, shown in Figure 4, is necessary before software strategies can be discussed.

The Univac 1108 is located at a computer center operated by Computer Sciences Corporation several miles from the Tektronix 4010 terminal. They are connected by a voice-grade telephone line through a standard acoustical coupler. This isolation frees the user from consideration

## HARDWARE Used by EZPLOT



FIGURE 4. Relationship between hardware components used by EZPLOT
of physical aspects of the 1108 and allows him to concentrate on the particular problem at hand. The main disadvantage of the separation of users from computer operations is that users have little ability to influence the operating system design of the main computer. As will be shown later, the
way in which the 1108 interfaces with the Tektronix 4010 placed interesting constraints on EZPLOT.

The graphic terminal and hard copy unit are described elsewhere (33, 34) and will be only briefly discussed here. The Tektronix 4010 alphanumeric-graphic terminal has a direct view storage CRT (visible portion 19 by 14.3 centimeters) for computer output and a typewriter keyboard for user input. The visible portion of the screen is composed of 780 by 1023 raster dots, these are individually addressable for graphic output. For alphanumeric output, the terminal contains logic to display characters with a $5 \times 7$ matrix of raster units, 72 of these characters fill a line and 35 lines fill the screen.

It is easy to draw characters of various sizes and orientations through the graphics mode of the terminal. However, it takes much longer to display a character this way than through the alphanumeric mode. The first strategic decision was to restrict all alphanumeric display to the fixed size characters generated automatically by the terminal. This limits output flexibility but saves execution time.

The hard copy unit, a Tektronix 4610, is located adjacent to the terminal. Copies are available in a few
seconds at the users command. Since copy making temporarily inhibits the input/output ability of the terminal, special consideration is made to allow pauses in program execution for static display that the user may wish to copy. In EZPLOT, this condition is signaled by the appearance of a question mark on the screen.

The Univac 1108 is committed to large scale data processing, involving long runs updating several magnetic tapes. In addition, it must serve the needs of a scientific community interested in computational ability. This dual purpose is accomplished through the operating system. The computer is essentially divided in two; there are two operating systems sharing the core. Users at remote terminals have access to either. The batch mode system, CRJE (Conventional Remote Job Entry), has access to 196,608 words ( 36 bits per word) of memory plus drum and tape storage with turnaround time depending on workload and priority. The time sharing mode, CSCX (12), gives the user access to a fixed size work area of 32,000 words. There are powerful editing routines available in this system as well as the interactive language, BASIC. Turnaround time under CSCX is immediate because the user has access to a specific physical portion of the computer rather than sharing it with
others. In exchange for rapid turnaround, the user must sacrifice ability to use magnetic tapes and is limited in the size of his program and data arrays. In addition, there is a premium cost attached to this mode of operation. In conjunction with the acquisition of the Tektronix terminal, a group of FORTRAN packages for the production of graphic output was secured (32). These are very flexible and an interactive program similar to EZPLOT could easily be built around one of them. However, FORTRAN programs may run only on CRJE in our computer environment. A survey of potential users indicated that waiting, often several hours, for results was unacceptable. A major strategic decision was to write the general purpose graph drawing program in BASIC.

BASIC
BASIC (Beginner's All Purpose Symbolic Instruction Code) is a language designed for novice computer programmers operating in a time sharing environment (16, 29). In contrast to batch oriented languages such as FORTRAN or COBOL, BASIC anticipates and encourages programmer/computer interaction during program development and debugging (6, 28).

The emphasis of the language is on simplified input and output. For example: there is no distinction between fixed and floating point numbers, format statements are not needed, and arithmetic statements may appear anywhere one would expect to use them (i.e., PRINT X * $(A+B)$ causes the results $Y$ of the computation $Y=X *(A+B)$ to be printed).

BASIC was designed as a flexible interactive language. When it was developed at Dartmouth it was anticipated that the typical BASIC program would be small and that larger programs would be written in another language such as FORTRAN. Therefore, the designers of the language, in optimizing for novice user convenience, adopted restrictions which compound the task of developing large BASIC programs.

Mnemonic naming of variables cannot be used to improve program clarity because variable names are restricted to one letter, optionally followed by one digit, while array names may only be single letters. This naming convention limits the number of variables to 286 and the number of arrays to 26.

Conditional branching is allowed, but conditional replacement statements are not; so that logical flow of the program is interrupted by IF (something) GO TO (line number) and GO TO (line number) statements.

Program documentation through the use of REMARK statements is a feature of the language. However, because REMARK statements are executable in the sense that FORTRAN CONTINUE statements are, they contribute to the storage requirements for the program. Programmers who anticipate that their program and data will approach the maximum allowable size are forced to minimize the use of REMARK statements.

In spite of these difficulties, which only affect the programmer, BASIC is a good language for EZPLOT because it minimizes user frustration. The flexibility of input format inherent in BASIC allows novice users to enter data conveniently. Most BASIC compilers allow for user correction of input errors during execution without re-running the entire program.

BASIC AT CSC
A serious limitation of BASIC is the lack of uniformity among its implementations (21, 26). Each compiler writer has added modifications to the original version. Enhancements to BASIC in the CSC version (11) are used throughout EZPLOT. It may be difficult to transfer it to another computer which has a different version of the language.

Some of the enhancements in the CSC implementation include:

- Ability to handle file input/output
- The verb: GET, which allows keyboard input of string variables without enclosure in quotation marks.
- ON (expression) GO TO (line number list) with drop-through on out of range expression
- PRINT USING an image or an implied image
- String manipulation statements: LEN, and STR.

The CSC version features an incremental compiler; each line of code is interpreted at run time. This feature allows debugging at run time; it is possible to interrupt the computer, change some instructions, and continue execution without changing the contents of data arrays. EZPLOT uses this feature by inviting the user to interrupt execution to add statements which compute functions the user wants to display.

Another advantage of this type of compilation is ability to easily recover form error conditions. If bad input is detected (for example, if the user enters two decimal points with a number) a message appears, execution stops, and the user is allowed to either exit or re-enter
the value after giving the BASIC command CONTINUE. Values entered successfully prior to that point are preserved. TECHNIQUES FOR INTERACTIVE PROGRAMS

The ordinary problems of a computer programmer are compounded when he writes programs for interactive use. Not only must the program conform to the requirements of the compiler and produce correct results, but it must also interface with the most unpredictable of phenomena, human beings.

The programmer must rely on the human user to supply critical program parameters in addition to data to be manipulated. He must devise tests of these input parameters to avoid out-of-range conditions within his program. In addition, he must make the user comfortable by avoiding delay in response and by asking understandable questions.

The development of EZPLOT occupied several months, much of which was devoted to analysis of user difficulties. The results of this attention to user complaints are summarized in the form of flexible guidelines which are applicable to all interactive programs.

- FOLLOW LOGIC OF THE MANUAL PROCEDURE. The user is familiar with a logical way of doing things. The interactive program should follow this pattern at
the expense of efficiency. For example, EZPLOT asks the user questions about the data, the type of axis, the scale of the $x$-axis, the scale of the y-axis, and then about the titles. This follows the pattern of the manual procedure for preparing graphs.
- KEEP QUESTIONS SHORT. Do not bore the user with lengthy questions, remember that he may repeat the sequence of questions several times at each session. Short abrupt statements are used as questions in EZPLOT. "What is the form of your input?" is reduced to "Input type?".
- PROVIDE DETAILED QUESTIONS IF REQUESTED. Neophyte users will not always understand the condensed questions. These users are the exception; therefore, a detailed form of the question should be available on request. This is accomplished in EZPLOT by the convention that a response of the number 0 to any question will cause a detailed question to appear.
- STANDARDIZE THE RESPONSE EXPECTED FROM THE USER. Do not expect a numeric answer one time and an alphabetic one the next. The user is more comfort-
able when he can anticipate the type of response required. Questions in EZPLOT either refer to a menu of options or ask for data input. The user always enters a single number, followed by a carriage return, in response to a menu-type question.
- KEEP MEANING OF RESPONSES CONSISTENT. Let the pattern of the responses be consistent. If l indicates a positive response to one question, do not have it mean a negative response to the next. In general, the following pattern in used in EZPLOT: $0=$ print the menu for this question, $l=$ a positive response, $2=$ a negative response, and 3, 4, 5, etc., are used if there are more than two items on the menu.
- BE FLEXIBLE. The users will discover ambiguities in the questions no matter how carefully they are prepared. More than half of the questions in EZPLOT have been re-written after analysis of user difficulties.


## GOALS OF EZPLOT

The final element of strategy was to adopt reasonable goals for the program. The major aim was to develop a
program that worked; embellishments could come later. Therefore, the goals are rather modest. Many things which are technically possible, such as rotating the display, "zooming in" on a portion of the graph, splitting the screen to display more than one graph, and using the graphic input thumb wheels to manipulate data elements, were rejected as unnecessary and undesirable complications to the program. The second major decision was to limit EZPLOT to general cases. This was the reason for rejection of special axes such as a time scale in days or months, preselected scales (i.e., 100 by 100 or 10 by 10), and other ideas suggested by users. Data reduction, regression analysis, and other statistical manipulations are available in other programs so they are omitted from EZPLOT. Finally, data input to EZPLOT is restricted to a keyboard entry routine or from a user prepared BASIC file. Editing capabilities to extensively rearrange data files are not the province of EZPLOT; they are available through CSCX.

The initial goals were:

- Keyboard data entry
- Several sets of data on one graph
- Linear scales
- Data modification
- Titles and numeric scale identification.

Soon some requests by users were added to make EZPIOT more general purpose:

- Logarithmic scales
- Functions as well as data
- Data input from computer file
- Dynamic modification of parameters to re-display graph.

User suggestions which may be added in the future include:

- Split screen display of two sets of axes
- Interchange of x and y axis
- Revised data format to allow several dependent variables for each independent variable
- Interface with output of existing BASIC regression programs.
IV. IMPLEMENTATION

To make the goals of EZPLOT a reality, a program was written combining three operational elements:

- User activated decision points
- Conversational routines in which the user supplies information
- Internal routines with no user participation. The intermingling of these program elements is illustrated in the general flow chart presented as Figure 5. On this abbreviated chart, diamonds represent questions asked at decision points within the program. These seven questions require that the user select options from a menu. The sequence of questions depends on previous responses.

The hexagons on the chart represent conversational routines. The number of questions asked in each is a function of the responses and the data. The rectangles represent internal routines. Many of these also contain logic not shown on the chart which can alter the sequence of questions presented to the user.

Two appendices included in this dissertation are for readers interested in details of program operation. A computer programmer may wish to compare the flow chart with the text of EZPLOT found in Appendix A. Potential users will be more interested in the EZPLOT Users Manual found in Appendix B.



As indicated on the flow chart, the pivotal point of the program is the question WHAT NEXT? This question divides operation of EZPLOT into two phases: l) the user interacts with the program to supply data, scale factors, titles, and other parameters, then 2) the computer draws a two dimensional graph on the CRT screen. The user may cycle through these phases until he is satisfied with the resulting display.

Implementation of the program will be discussed in terms of these two phases. The second, in which the graph is generated, will be treated first. The interactive phase is more straightforward and will be discussed later.

## TEKPLOT SUBROUTIINES

The graphics portion of EZPLOT was derived from a set of FORTRAN subroutines distributed by the terminal manufacturer (32). These plot driving TEKPLOT subroutines are designed to be machine independent; they are written in FORTRAN II and avoid the use of COMMON or LABELED COMMON. This reduces the problems of installing TEKPLOT on different computers, but requires the use of several subroutines devoted to keeping track of scale factors, rotation factors, and other parameters. These terminal status values are not available to the main program. Only two subroutines need
be written to adapt TEKPLOT to a new computer: one, CHIN, to define character transmission between the terminal and the computer, and the other, CHOUT, to translate in the reverse direction.

After installing TEKPLOT on the UNIVAC ll08, Computer Sciences personnel coverted a major portion of it to BASIC, calling the resulting graphics package **PLT ${ }^{5}$. This series of 29 subroutines provides the full range of graphics output supported by TEKPLOT, although hardware restrictions do not allow use of graphics input. Thus, the cross hair cursor on the terminal is unavailable to EZPLOT.

BASIC subroutines differ from FORTRAN subroutines; there is no parameter list associated with the call statement. The technique for passing data to a GO SUB in **PLT is to place the data in dummy variables used by the subroutine.

BASIC subroutines are not independent and all variables are essentially in COMMON. This means that the terminal status values are available to a BASIC program using **PLT whereas they are not in FORTRAN using TEKPLOT.

[^2]The large size of **PLT (approximately 1200 BASIC statements) limits size of the main program. Early in development of the interactive portion of EZPLOT this maximum was reached, the program plus **PLT exceeded the fixed portion of computer memory allowed each user. Serious consideration was given to splitting the graphics program into two parts, one to prepare the data, the other to obtain the scale factors and draw the graph. This proved to be too complicated for novice users.

Therefore, the graphics support package, **PLT, was reduced to eight subroutines consisting of about 250 BASIC statements. This was achieved by discarding those subroutines not necessary to support the goals of EZPLOT. Features which were discarded outright include:

- the software character generator and it's 400 data elements
- the pause (not needed in BASIC)
- all references to point or incremental mode graphics
- the axis generator, replaced by an EZPLOT subroutine
- the grid generator, replaced by an EZPLOT subroutine.

Elimination of subroutines associated with these features also allowed reduction in size of those remaining by removing linkages to the deleted subroutines. Some of the bookkeeping subroutines, TEK001 through TEK007 were eliminated, others were modified. The most often called subroutine, TPLOT, was replaced with a much smaller version tailored only to the needs of EZPLOT.

The eight graphics support subroutines derived from **PLT and their line numbers in EZPLOT are:

1100 BEGIN, which sets transmission rate and initializes bookkeeping.

1200 ERASE, which transmits the erase code and delays processing until erase is complete.

1500 VECTOR, which sets graphic mode.
2100 SCALE, which updates scale factor bookkeeping.
2300 WINDOW, which edits window limits for legality and updates bookkeeping.

4500 CHOUT, which transmits a coded character to the terminal.

4400 TEK002, which plots current $x, y$ points
3900 TEK003, which partitions $x, y$ points into bits to pass to terminal.

These could be further reduced if necessary. However, since
they represent less than $20 \%$ of EZPLOT, they are no longer a major hindrance to expansion of the program.

## EZPLOT SUBROUTINES

There are eight graphics support subroutines included in EZPLOT. These serve as links between the interactive portion of the program and the modified plot driver, **PLT. The main EZPLOT subroutine, called MY OWN TPLOT, is located at line 9000. The 15 lines of this subroutine replace approximately 100 lines of TPLOT. The major saving is the result elimination of software plot symbol generation. TPLOT and **PLT provide eight optional symbols, such as dots, arrows, circles, or boxes. In EZPLOT, all plot symbols are hardware generated keyboard characters, with the exception of the diamond which is drawn by vector mode techniques. The task of MY OWN TPLOT is then reduced to sending TEK002 the coordinates of the next location on the screen and a flag to indicate whether or not the vector is to be visible.

The ABSOLUTE SCALE subroutine is located at line 4240. It sends the proper values to the SCALE and WINDOW subroutines to set the scale so that screen raster location corresponds to program logical location. EZPLOT operates in absolute scale while displaying the top and bottom captions.

The USER'S SCALE subroutine starts on line 4350. It
sets the scale so that translation from user's units to raster locations is automatic. EZPLOT operates in user's scale while drawing linear graphs and modifies the scale before drawing log plots.

Considerable attention was given to the EZPLOT axis drawing routines. The **PLT ones were unacceptable because they represented the philosophy that the user must choose standard size axes just as if he were selecting graph paper from a drawer. Flexible axis definition is an essential concept of EZPLOT. The AXIS subroutine at line 5340 and the auxiliary LOG X TIC and LOG Y TIC subroutines at lines 9700 and 10000 cause a neatly labeled box to be drawn defining whatever size "graph paper" the user specifies.

The outline around the graph is drawn in this order: First the top and bottom horizontal borders (including tic marks and numeric labels where appropriate) are drawn, then the left and right vertical ones. This method reduces the execution time by eliminating redundant calculation of the tic mark location, as shown in Figure 6, a flow chart of the horizontal axis portion of the AXIS subroutine. Note that drawing visible grid lines is a simple matter of interrogating a switch variable between drawing of the lower and upper tic marks.


FIGURE 6. Logic of horizontal axis drawing portion of EZPLOT.

An alternate axis drawing scheme which progressed around the box counter-clockwise proved to be slower and did not allow a simple method of adding a grid to the display.

Calculation of tic mark location in the AXIS subroutine is a simple mathematical procedure. If the user wants a total of 12 tic marks, the location of the next tic to the right of the present one is $1 / 12$ th of the range of the axis added to the $x$-coordinate of the present location. Because of the way the user defines tic mark location on a log axis, this method cannot be used in that case. Rather than clutter up the AXIS subroutine with branching logic to treat log axes differently, two other subroutines are used.

The axis on a log scale is drawn by first "tricking" the AXIS subroutine into thinking that the user wants only one tic mark. This produces an axis properly labeled at either end with no intervening tic marks. A call to LOG X (or Y) TIC adds the tic marks and labels at the locations designated by the user.

The two remaining EZPLOT graphics subroutines, VERTICAL GRID and HORIZONTAL GRID, at lines 4470 and 4630, are called if the user elects to design his own grid scheme. They are quite simple because the user has supplied the
program with the specific location of each grid line.

## EZPLOT LOGIC

The logical flow of the interactive portion of EZPLOT is shown in Figure 5. Three areas are worthy of discussion here: two because of the difficulty they caused, and one because it was so easy to implement due to the nature of BASIC as enhanced by CSC.

The two difficult areas are associated with the transformation to logarithmic scaling. First there was the problem of labeling the log axis, second, the problem of transforming data to the new scale. Equally spaced tic marks are necessary on a linear plot, but how does one calculate their position on a $\log$ scale? If the linear axis runs from 10 to 20 with tic marks at $10,12,14,16,18$ and 20, a simple log transformation will suffice. However, if the linear axis runs from 0 to 10 , with tics at $0,2,4,6$, 8 and lo, a log transformation is impossible because the log of 0 (or a negative value) is undefined in BASIC.

Even with properly defined end points of the axis, computational techniques for spacing the tic marks are complicated. For example, the axis may run from 75 to 125 ; that is, it may include portions of two decades, or it may include a full decade and a portion of two others, i.e., 75
to 1500. The programming challenge of such a problem is great.

This challenge was not accepted; log axis tic mark location is decided by the user of EZPLOT, not by the program. Rather than deciding how far apart he wants the marks, as he does for linear axis, the user must explicitly define each tic mark location on a log axis. Thus, the programming problem is solved by asking the user to supply the logic rather than attempting to do it for him.

That solution could not be applied to the other problem associated with log scaling, that of negative numbers. Suppose a user has a data file with 100 data pairs of which a few have zero or negative values for one or both of the coordinates. He obtains a linear graph and decides to transform one of the axes to logs. It is simple enough to have the program skip the transformation and display of illegal points, but what information should be given the user?

Several ideas were tried in the development stages of EZPLOT. At first the user was told: YOU CANNOT PLOT NEGATIVE VALUES ON A LOG SCALE, PLEASE EDIT YOUR DATA FILE. The users objected because they had to use the slow (in a real time sense) interactive editing routine to clean up the
data.
The second version listed the data as follows:
YOU CANNOT PLOT THE FOLLOWING ON A LOG SCALE
1,0
20,-0.5
-1,4
$-3,-0.003367$
DO YOU WANT THE PLOT ANYWAY?
Experience with this version indicated that the user always wanted the plot anyway and was annoyed at having to answer what to him was a redundant question.

In the final version the data is listed thus:
WILL SKIP I,0
WILL SKIP 20,-0.5
WILL SKIP -I, 4
WILL SKIP -3,-0.003367.
These messages appear between the time the user requests a log scale and the time he defines the scale factors. This allows him to change his mind when WHAT NEXT? is asked before the graph is drawn if he realizes that his graph is meaningless without the negative data.

The third problem in developing the logic of EZPLOT was how to add functions to the graph. Implementation of this was planned in two steps. First a routine for graphic display of the function was written, then would come a routine to translate the $u s e^{\prime}$ s input into a function.

The graphic display of a function was accomplished by simply dividing the range of the horizontal axis into 100 increments and evaluating the vertical component of the function at each one of those points. To debug this routine. a test function was written into the program. Further testing required program interruption for modification of the function. This technique worked well and is a simple way for the average user to input his functions.

Thus, rather than using a translation routine to determine the function the user wants, EZPLOT allows him to interrupt execution and replace dummy functions in the program with BASIC statements.

## EXAMPLE OF USE

The use of EZPLOT is best explained through an example. Assume that you are investigating some phenomenon such as growth rate of plants or animals, strength of metals, or decay of radioactivity. Further assume that you are comparing the behavior of two cases (two plants, two metals, or
two radionuclides), you have summarized your results as shown in Table II, and wish to use EZPLOT to produce graphs of different aspects of this data.

You complete the procedure to activate communication between the terminal and the computer, then enter the interactive phase of EZPLOT.

In the keyboard data entry portion of the program, you type the data as a series of $x-y$ pairs identified by a plot symbol (one of the keyboard characters; in this case, an asterisk (*) for one case and the letter $x$ for the other). The program then displays the data as shown in Figure 7. At this point you may correct mistakes, insert forgotten points or change plot symbols, until you are satisfied that the computer has stored your data correctly.

To obtain a graph quickly, you choose the default options, allowing the computer to determine scale factors to accommodate the range of the data. After supplying the top and bottom descriptive lines to the program, you request and obtain the display shown in Figure 8.

The results are accurate but not pleasing to the eye. Since you intend to use this graph in subsequent discussions with your associates, you elect to re-enter the interactive phase of EZPLOT and choose scale factors more appropriate to

## TABLE II

HYPOTHETICAL DATA TO ILLUSTRATE EZPLOT

| INDEPENDENT <br> VARIABLE | DEPENDENT VARIABLES |  |
| :---: | :---: | :---: |
| 5 | 0 | 0 |
| 10 | 8.2 | 10.5 |
| 15 | 10.4 | 20.2 |
| 20 | 19.2 | 26.1 |
| 25 | 24.9 | 32.9 |
| 30 | 27.6 | 36.3 |
| 35 | 32.1 | 40.0 |
| 40 | 37.2 | 42.1 |
| 45 | 40.8 | 43.5 |
| 50 | 42.0 | 46.3 |
| 55 | 45.2 | 46.9 |
| 60 | 49.1 | 48.2 |
| 65 | 52.0 | 51.3 |
| 70 | 55.2 | 52.6 |
| 75 | 57.7 | 53.7 |
| 80 | 60.5 | 55.9 |
| 85 | 62.4 | 58.2 |
| 90 | 64.9 | 58.7 |
| 95 | 67.3 | 58.9 |
| 100 | 69.2 | 60.4 |



FIGURE 7. Display of data file for EZPLOT example.
hypothetice bita to illustpate ejplot


FIGURE 8. Graph of hypothetical data using automatic scaling option.
hipothetical dath to illustrate ezplit


FIGURE 9. Graph of hypothetical data obtained by using manual scaling routine.
the data. The results shown in Figure 9 are much more pleasing. The dialogue leading to Figure 9 is shown in Figure 10.

You re-enter the interactive phase again because you have previously obtained some functions which fit the data reasonably well. To include these in the display you have to formulate the equations in BASIC, which is almost as natural as ordinary algebraic notation. Figure 11 shows the data with the two functions superimposed.

Since one of the functions contained an exponential expression, you know that a plot on semi-log paper would yield a straight line. To illustrate this aspect of your investigation, you select the appropriate semi-log option of EZPLOT. Again, you choose to dictate the choice of scale factors because you want the plot to be easily understood by your colleagues. The resulting semi-log plot, Figure 12, illustrates that EZPLOT quickly and accurately transforms the data, re-plotting it as it were on a new type of graph paper.

This example, which included relatively slow keyboard input of 40 pairs of points and output of four graphs, was completed within 30 minutes. This time may be reduced if the data are prepared previously on a data file stored in


```
TYYE DF (GAPMOG)
1 = LINEAR
2 = LOG Y VS LINESP X
3 = LINEAR Y VS LOG X
4 = LOG Y VS LOG }
TYPE OF GEAPHT1
AUTD SCALET?
YOU IILL NEXT DEFINE THE SIZE GRAPH YOU WANT
B,0 CSN BE OFF THE SCREEN
X-Ax|S:
    MIN X MAX X
DATA 5 10%
AXIS O
M|fINU:& VALJE-7*
MAXI:AIJ VALJE - ? 1W%
X-4XIS GOES FHO: O TO 120
WITHIN IHIS RANGE OF THW UNITS
HO* MANY UNITS OO YOU WANT BET:UEEV TIC MARKS?S
THAT 'ILLL HEAN 2A TIC MAPXS ON THE AXIS
LABEL FACTOF?2
x ax:S Jn?l
    Y axIS
OATA 
BINIMUM VALUE-?D
HAXIMUH VALUE -775
Y-4XIS GOES Fru.1 \ TO 75
WITHIN THIS RANGE OF 75 UNITS
HOW VANY UNIIS CO YOU YA:NT BETWEEN TIC MARKSTS
THLT WILL MEAN: .15 TIC MARKS ON THE AXIS
LABEL FACTOR?5
Y EXIS OH?1
GF1DR2
TOP TITLE O*?0
YOU MAY: (1) HAVE:HYPOTHETICAL DATG TO ULLISTRATE EZPLOT DISPLAYED AT TOP OF G
                RAFH
OR
    (2) ENTER A NEX TITLE FOR THE TOP OF THE GHAFH
TOF THLE OK?1
ENTER DESCSIPTIVE LINE FOR BOTTOH OF GRAPH
}EXAAPLE OF SESCRIPTIVE LINE AT BOTTDA OF GRAF̈H
BOTTGM LIME ON?!
FIGURE 10. Interactions between EZPLOT and user which preceeded display of Figure 9.
```

hiforhetical gita to immitate ezplot


FIGURE 11. Graph of hypothetical data with superimposed functions.


FIGURE 12. Graph of hypothetical data with superimposed functions on semi-log axes.
the computer. Investigators with little training in computer technology are currently using EZPLOT in the manner described in the foregoing example.

## CONVERSION CONSIDERATIONS

Implementation of EZPLOT on a Univac 1108 operating under the CSCX operating system in Richland, Washington, has been described. It is appropriate to discuss the possibility of using it on other computers.

EZPLOT has been successfully tested on a similar computer configuration located in Los Angeles ${ }^{6}$. This time sharing computer service is available nation wide through telephone lines. Users with access to it will experience little difficulty installing and operating EZPLOT.

Users who do not have access to this system may consider converting EZPLOT to run on their own computer system. The success of such conversion will depend on whether their computer supports BASIC and, if it does, on whether their BASIC is interpreted or compiled.

If BASIC is available, it must support graphic output to the Tektronix terminal. This means that there must be some method of character string manipulation so that

[^3]appropriate commands may be sent to the terminal. Some BASIC implementations do not provide this capability. Another problem is that some computers do not allow BASIC files as large as EZPLOT. In that case, some features of the program will have to be discarded to reduce its size. A minor consideration is differences in internal representation of keyboard characters among computers which may require conversion of portions of the program.

Assuming that EZPLOT is installed on the new computer, user convenience in operation of it will depend on whether BASIC is interpreted or compiled. Much of the user enthusiasm toward EZPLOT in Richland depends on the interpretive nature of CSCX-BASIC. This allows the user to interrupt program execution without "loss of previously entered data. The interruption feature is essential to the simple way that the user inputs functions to be plotted with his data.

If the new BASIC is compiled rather than interpreted, EZPLOT will be much less convenient to use. If functions are desired, they will have to be inserted into the program prior to execution. If display of them indicates modifications are necessary, the user will have to stop the program, modify the functions, then re-initiate the program including re-entry of data and scale parameters.

If the new computer does not support BASIC, or if the new BASIC will not support graphic terminal output, EZPLOT will have to be converted to another language. Since the logical flow of the program has been thoroughly tested, language conversion would be relatively straight-forward. However, since most other languages, such as FORTRAN, are compiled, it will be inconvenient for the user to input and modify functions.

User convenience would suffer in another way because the new language would probably require more computer sophistication on the part of the user. For example, most FORTRAN versions do not allow the extent of free format input supported by BASIC. Further, it may be more difficult for the user to correctly input his functions if he has to write them in another language.

As an alternative to having the user input his functions directly into the program, a converted EZPLOT could employ some form of formula translator to construct the appropriate functions based on user responses. This would be an extensive modification to what is presently a relatively simple program.

In conclusion, EZPLOT could be converted to either a compiled version of BASIC or to another language such as FORTRAN. Both conversions would be much less convenient for the user. EZPLOT was designed to take advantage of an interpreted BASIC language, and from a user's standpoint, it should remain in that configuration.

## V. APPLICATIONS

Two types of investigators utilize EZPLOT at Battelle Northwest. One group consists of those who interact with the program to produce graphs of their data. They were trained by the author in the use of both the CRT terminal and EZPLOT, and were given a copy of the Users Manual (Appendix B). Further contact with them is limited to complaints about hardware or software failures. Therefore, discussion of their applications of EZPLOT is not included in this dissertation.

Other investigators prefer to involve the author or another statistician in the analysis of their data. To them, EZPLOT appears as a tool of the statistician. Several examples of this type of application are presented here. In each case, the investigator has given permission that his results in graphical form be included in this dissertation along with a brief description of his experiment.

## ANT ACTIVITY

In a study of the behavior of Harvester Ants (Pogonomyrmex occidentalis), Lee Rogers made a series of intensive observations at one ant colony for three days in the summer of 1971 (27). He counted the number of ants leaving and returning to the colony, recording the tally at five minute intervals. Other variables such as air and soil
temperature, quantity of solar radiation, and relative humidity were also recorded throughout the day.

Later a statistician was asked to help incorporate these observations into a simulation of an ecosystem. An equation was needed which would relate the number of active ants to soil temperature; that is, at a given soil temperature how many ants could be expected to be outside the colony? No restrictions were placed on the type of equation to be fit to the data because there was no evidence that this aspect of ant behavior followed any particular model. A search of the literature led Lee to speculate that the relationship would be linear if indeed a relationship could be demonstrated.

The observations were keypunched and the two parameters of immediate interest, soil temperature and ant activity, were placed on a computer file. The statistician used EZPLOT to produce a preliminary plot of this data file. This graph, Figure 13, showed that there was no ant activity when the soil surface temperature was below 25 or above $50^{\circ} \mathrm{C}$. Other than that, no particular pattern was evident.

In cases such as this, when the investigator gives no indication that the data should fit a particular model, the polynomial model is often applied. It is a simple

LEEE ROGERS GNT DATA $X=T E M P \quad Y=A C T I V E$ ANTS


FIGURE 13. Number of active ants at a given soil surface temperature, composite of 3 days of observation.
regression process to compute the parameters of an equation of the form:

$$
y=A+B x+C x^{2}+D x^{3}+e t c
$$

which give the closest fit to the data. Other models are more difficult to apply because they require that the statistician supply partial derivitives and estimates of the parameters.

The data file was used in conjunction with an interactive polynomial curve fitting routine (10, program no. 03-1823). This illustrates the concept of keeping EZPLOT a graph drawing program only. The ability to perform interactive curve fitting already existed, there was no need to incorporate it into the plot program. Some of the results of the polynomial fitting are shown in Figure 14 and 15.

None of the resulting equations fit the data very well. Polynomial equations of order 1 through 8 were tried, but the coefficient of determination was in no case greater than 0.6 ( 1.0 indicates exact correspondence between the equation and the points). Clearly a conference between the statistician and the investigator was necessary to find some aspect about the data which would allow better curve fitting. Without EZPLOT, the statistician would have shown

```
ENTER LOWEST DEGREE TS BE FIT?I
LEASI SQUARES PJLYNOMIALS
MMBER GF PJINTS = 119
                                    MEAN VALUE of
                                    MEAN VALUE gF Y = 37.9916
            STD DEV OF Y = 51.9037
NOTE: CDDE FOR 'WHAT NEXT?` IS :
    O = STGP PRJGRAM
    1 = C3EFFICIENTS gNLY
    2_= ENIIRE SUMMARY
    3 = FIT NEXI HIGHER DEGREE
PSLYFIT OF DEGREE 1 ; CSEFF IF DETERM = 1.67401E-2
UHAT NEXI?1
\begin{tabular}{ll} 
TERM & CSEFFICIENT \\
0. & 8.4644 \\
1 & .751617
\end{tabular}
WHAT NEXI?3
POLYFIT OF DEGREE_2_CEEFF OF DETERM=.325892_
WHAT IEXT?I
                                    CBEFFICIENT
\begin{tabular}{ll}
\hline 0 & -681.639 \\
1 & -38.6166 \\
2 & -491486
\end{tabular}
WHAT NEXTT3
POLYFIT OF DEGREE 3 :CBEFF EF DETERM \(=.562545\)
WHAT MEXTZ 1
\begin{tabular}{|c|c|}
\hline TERM & CBEFFICIENT \\
\hline 0 & 2437.44 \\
\hline 1 & -226.177 \\
\hline 2 & 6.7697 \\
\hline 3 & -6.44031 E-2 \\
\hline
\end{tabular}
```

FIGURE 14. Printout of a portion of the interactive polynomial regression analysis of ant activity data.

| X-ACTUAL | Y-ACTUAL | Y-CALC | DIFF | PCT-DIF |
| :---: | :---: | :---: | :---: | :---: |
| 26.7 | 1 | 8.9375 | -7.9375 | -88.8112 |
| 27.2 | 2 | 10.0312 | -8.03125 | -80.0623 |
| 28.9 | 0 | 11.1562 | -11.1562 | -100 |
| 28.9 | 5 | 11.1562 | -6.15825 | -55.1821 |
| 30 | 21 | 12.3906 | 8.10937 | 62.9091 |
| 31.1 | 29 | 17.2344 | 11.7636 | 68.2684 |
| . 30.5 | 18 | 15.3125 | 2.5875 | 17.551 |
| 32.2 | 14. | 24.375 | -10.375 | -42.5841 |
| 33.3 | 40 | 33.9531 | 6.04687 | 17,3095 |
| 34.4 | 46 | 43.2556 | 2.73437 | 6.31997 |
| 35.6 | 101 | 53.7344 | 47.2555 | 87.9516 |
| 30..1 | 36 | 58.2187 | -22.21\%\% | -37.1643 |
| 36.7 | 25 | 61.8437 | -38.3437 | -59.5755 |
| 37.5 | 55. | 70.6562 | -15.6562 | -22.1533 |
| \$7.2 | 47 | 67.0312 | -20.0312 | -29.3834 |
| 33 | 38 | 49.7344 | -11.7344 | -23.5941 |
| 35 | 46 | 49.7314 | -3.73437 | -7.50854 |
| 35.6 | 71. | 53.7344 | 17.2 .556 | 32.1314 |
| 40.5 | 101 | 88.4062 | 12.5937 | 14.2453 |
| 41 | 73. | 92.6552 | -19.6562 | -21.2142 |
| 43 | 77 | 108.875 | -31.375 | -29.2767 |
| 36.7 | 36 | 61.3437 | -25.8437 | - 41.7888 |
| 33.3 | 41 | 33.9531 | 7.04687 | 20.7547 |
| 39 | 100 | 75.7969 | 24.2031 | 31.9316 |
| 42 | 124 | 101.469 | 22.5312 | 22.2051 |
| 40 | 89 | 84.375 | 4.525 | 5.48!48 |
| 37.2 | 112 | 67.0312 | 44.9587 | 67.0862 |
| 41. | 99 | 92.6552 | 6.34375 | .. 6.84654 |
| 49 | 7 | 31.7344 | -24.7344 | -77.9419 |
| 49 | $?$ | 31.7344 | -23.73.44 | -33.6977 |
| 49 | 1 | 31.7344 | -30.7344 | -96.8488 |
| 50 | 0 | -2.89062 | 2.59062 | -100 |
| 50 | 0 | -2.89062 | 2.89062 | -100 |
| 50 | 0. | -2.89062 | 2.89062 | -100 |
| 49 |  | 31.7344 | -24.7344 | -77.9419 |
| 45.5 | 180 | 119.359 | 60.1406 | 50.178 |
| 45.5 | 160 | 119.859 | 40.1406 | 33.4838 |
| 46 | 65 | 112.047 | -47.0463 | - 41.9886 |
| 45 | 90 | 120.703 | -30.7031 | -25.4359 |
| 35.6 | 36. | 53.7344 | $-17.7344$ | -33.0038 |
| 28.9 | 7 | 11.1562 | -4.15625 | -37.2543 |
| 26.7 | 2 | 8.3375 | $-6.9375$ | -77.5224 |
| 24.4 | 1 | . 28125 | . 71875 | 255.558 |
| 24.4 | 0 | .28125. | -2.3129 | -100. |
| 25.6 | 4 | 5.82812 | $-1.82812$ | -31.3573 |
| 26.7 | 3 | 8.9375 | -5.9375 | -62.4336 |
| $2 \% .9$ | 5 | 11.1562 | -6.15625 | -55.1821 |
| 35.5 | 13 | 53.7344 | -40.7344 | -75.3069 |
| 26.7 | 6 | 8.9375 | -2.9375 | -32.8671 |
| 24.4 | 0 | . 28125 | -. 23125 | -100 |
| 24.4 | 0 | . 28125 | -.28125 | -100 |
| 24.4 | 2 | . 28125 | 1.71875 | 611.111 |
| 23.3 | 1 | 4.84375 | -3.84375 | -79.3548 |
| 25.6 | 27 | 5.82812 | 21.1719 | 363.271 |
| 30.8 | 21 | 15.1094 | 5.89062 | 38.9866 |

FIGURE 15. Detailed printout of portion of third degree polynomial fit to ant activity data.

Figures 14 and 15 to the investigator. It is difficult to use such tabular data to explain why the computer ( a device equated to God by many non-mathematical investigators) could not fit the data. However, the investigator was shown Figure 16 in which the third and fourth degree polynomials, which came closest to fitting the data, are shown superimposed on the 119 data points.

Lee Rogers saw clearly from Figure 16 that the problem was in the erratic number of ants observed when the temperature was between 40 and 50 degrees. Examination of the complete set of observations showed that one of the neglected variables, time of day, was needed to fully understand the observations.

A general pattern was apparent when the observations were displayed chronologically. The ants started emerging from the colony in mid-morning when the soil temperature rose to 25 or more degrees. As the soil warmed, the number of active ants increased until the temperature reached 40 degrees. Between 11 AM and noon, as the soil temperature rose from 40 degrees to 50 degrees, the number of active ants decreased. After noon, there was a period when no ants were active. The ants remained in the colony until the soil temperature started to drop. When the soil surface was cool enough a

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FIGURE 16. Number of active ants at given temperature with 3rd and 4 th degree polynomial fits superimposed.
large number of ants emerged from the colony, then the number of active ants steadily decreased as the afternoon progressed.

This suggested that two equations were needed to relate ant activity to soil temperature, one for morning, and another for the afternoon. The data file was split into two portions, and the polynomial regression analysis was repeated. The resulting curves shown in Figure 17 and 18 fit the observations much better.

The success of this approach suggested that the linear model may also fit the data. Figures 19 and 20 show results of this approach. The linear regressions fit almost as well as the third and fourth degree polynomials and have the additional advantage of simplicity.

The ability to graph and re-graph the large number of observations made it much easier for the statistician to communicate with the investigator. The goodness of fit of the various regression equations was readily apparent to the investigator when presented in graphic form. He, in turn, was able to show the analysis of his observations to his co-workers in simple graphic form.

This analysis required two sessions at the computer terminal. First the interactive curve fitting routine was
active mits ogserved after hoon by cee rocers


FIGURE 17. Number of active ants observed after noon at a given temperature, with polynomial regression fit superimposed.


FIGURE 18. Number of active ants observed before noon at a given temperature, with polynomial regression fit superimposed.


FIGURE 19. Number of active ants observed after noon at a given temperature, with linear model superimposed.


FIGURE 20. Number of active ants observed before noon at a given temperature, with linear model superimposed.
used and Figures 13 and 16 were prepared with EZPLOT. The elapsed time for this session was approximately $1 \frac{1}{2}$ hours. After these results were shown to the investigator, another computer session was planned. Dividing the data into morning and afternoon observations was done by manually separating the cards and transfering the two decks to new computer files.

The polynomial and linear curve fitting programs were run and graphs of the results prepared in about one hour. The savings of time and increase in communication ability due to EZPLOT are clearly evident in the analysis of Lee Roger's ant activity observations.

EINSTEINIUM 253 EXCRETION ANALYSIS
This application is another illustration of the simplification in communication between the statistician and investigator which results from the ability to automatically produce graphs of large data sets. In this case, the statistician wanted to show the effect of several data reduction techniques on the outcome of the regression analysis requested by the investigator. Neither the statistician nor the investigators would have plotted all 189 data points by hand, but analysis of such a graph, drawn by EZPLOT, allowed both of them to quickly understand ramifications of the
analysis.
The analysis involved a portion of a study of the toxicity of the trans-plutonium nuclide einsteinium-253, which is a pure alpha emitter. This material is being produced in anticipation of future use in radioisotope power sources, often called nuclear batteries, to be encapsulated and implanted in recipients of artificial hearts. Einsteinium-253 is an ideal candidate for this use because the short range of alpha particles limits the potential hazard to man to situations in which the encapsulation fails and the material is deposited in some radiosensitive organ of the body. Since this man-made nuclide has been available only in very small quantities, little information is available regarding its fate after it enters the body.
B. J. McClanahan and H. A. Ragan are investigating the metabolism of einsteinium-253 in a representative large laboratory animal species, miniature swine (25). A group of weanlings were injected with 3 micro Curies/kg of einsteinium-253 and held for observation. One important parameter, excretion rate, was monitored by collecting 24 hour urine and feces samples daily for the first ten days after injection and at frequent intervals thereafter.

Radiochemical analysis of the samples enabled the investigators to calculate the percent of injected dose excreted each day.

A graph of the mean percent excreted each day was prepared manually. This graph, on semi-log paper, showed the classic two compartment exponential excretion pattern (12). This is interpreted by assuming that two modes of metabolism contribute to the total excretion pattern. A portion of the injected material is quickly excreted via the urine; it is assumed that it passes directly from the blood to the kidney. Another portion is excreted over a long time period; it is assumed that this material is transfered from the blood to some intermediate site where it is retained and slowly released back to the blood from which part of it goes to the kidney.

If the two compartment model accounts for the observed einsteinium-253 excretion pattern, the parameters $A$ and $C$ of the equation:

$$
X=A e^{-B t}+C e^{-D t} \text { (where } t=\text { time) }
$$

indicate the proportion of the injected material deposited in each compartment, while $B$ and $D$ indicate the half-time
of residence in the compartment. The statistician was asked to evaluate these parameters for these observations.

The data from the individual pigs were transferred to a computer file and the mean percent excreted each day was re-evaluated to eliminate the possibility of mathematical error in the previous calculations. Graphs of the data and the summary statistics are shown in Figures 21 and 22. The statistician used several non-linear regression techniques to evaluate the fit of the model to the means of the observations and to various weightings of the means. Using EZPLOT, he displayed these evaluations of the model superimposed on the 189 data points. This helped him explain the effect of these statistical techniques to the investigators. They were able to help refine the curve fitting by identifying questionable data points which were contributing to the large variance on a few days.

Two of the graphs used in this analysis are shown as Figures 23 and 24. The first semi-log plot was used in a discussion of the problems associated with extrapolating beyond the duration of the experiment. Needless to say, converting a manual plot from a scale of 0 to 70 days into one from 0 to 200 days and displaying two functions accurately is too difficult to demand serious consideration just for
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\% excpeted us that 14 days
FIGURE 21. Percent of injected einsteinium-253 excreted in urine of miniature swine.


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FIGURE 22. Mean and $95 \%$ confidence interval of percent of injected einsteinium-253 excreted in urine.


FIGURE 23. Mean percent einsteinium-253 excreted with two nonlinear regression lines shown. Horizontal scale extended to 200 days.

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FIGURE 24. Mean percent einsteinium-253 excreted with outliers removed, illustrating rounded regression function.
the sake of a discussion. However, it is so easy for the computer to adjust the scale that the statistician didn't hesitate to specify this additional plot. The second graph, Figure 24, shows the refined fit to the urine data. It appears to fit the data well, and will be used in publication of the experimental results.

## PROBIT ANALYSIS

EZPLOT was initially used in this application to help a particular investigator understand the implications of a computer printout of an analysis of his data. Response by this and other investigators was so favorable that this use of graphic output to supplement numerical results is now routine.

Probit analysis (14) is a technique for interpreting the results of bioassay experiments in which groups of organisms are exposed to various concentrations of toxicant for an arbitrary time. The aim of a bioassay is to relate dose of toxicant to some observable end point such as death of the organism. Probit analysis provides a measure of the median lethal dose, that is, the concentration of toxicant necessary to kill half of the test population in a given time, called $\mathrm{LD}_{50^{\circ}}$

As with any statistical data reduction technique, probit analysis also determines the error associated with the predicted $\mathrm{LD}_{50}$. The technique is tedious and is best done by a computer program. Output from one such program is shown in Figure 25. Most of the information in the figure is of interest only to the statistician because it helps him understand the validity of the predicted $\mathrm{LD}_{50^{\circ}}$. The investigator is interested in the $\mathrm{LD}_{50}$ value and in some measure of the confidence in this value.

A problem in communication developed when one investigator asked the statistician how to use the values printed by the computer. The investigator found the $\mathrm{LD}_{50}$ value for the experiment, and assumed that he should summarize his experiment by reporting the $\mathrm{LD}_{50}$ and the standard deviation associated with that estimate. The statistician knew that the proper measure of confidence in the estimate is the upper and lower $95 \%$ fiducial limits, but he was unable to explain to the investigator's satisfaction why this was true.

The table of estimated concentrations needed to kill given percentages of the population, printed at the bottom of Figure 25, also includes fiducial limits for each estimate. These estimates along with the observed data were plotted as shown in Figure 26.

LD（5）TO LO（95）BY OIVISIONS OF 5 PERCENT FIDUCIAL LIMITS

| LO： | 51 | ＊ | 936.65218 | 842．55253 | 980.95522 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| L0： | 101 | － | 966．79555 | 890.19501 | 1005．8359 |
| LOI | 151 | ＊ | 957．67934 | 922．74031 | 1024．2110 |
| L0t | 201 | ＊ | ：004．59R4 | 948．37204 | 1040．2381 |
| LD： | 251 | ＝ | 1010.3442 | 969.74996 | 1055．4143 |
| LO1 | 301 | ＊ | 1032．7798 | 9R8．27144 | 1070.5123 |
| LOt | 351 | \％ | 1045.3703 | 1004.4963 | 1085．9975 |
| LOI | 401 | \％ | ： 057.4681 | 1016．9665 | 1102．1645 |
| Lot | 451 | ＊ | 1089．3041 | 1032.0926 | 1119.2079 |
| LO1 | 501 | ＊ | 1081．0859 | 1044.1079 | 1137．2805 |
| LOt | 551 | $=$ | ！197．0953 | 1055.6326 | 1156，5456 |
| LO1 | 601 | ＊ | 105．2311 | 1066.6820 | 1177．2250 |
| LOI | 651 | ＊ | －11P．0217 | 1077.6311 | 1199.6472 |
| LO： | 701 | $=$ | ：131．56i2 | 10AR．7794 | 1224．3145 |
| Lel | 751 | ＊ | 114F．567？ | 1100.484 A | 1252．02：0 |
| Lnt | 801 | \％ | 1147.7549 | 1113.7458 | 1284．0982 |
| LDI | 851 | ＊ | 11n3．3大力0 | 11こ7．4月9\％ | 1323．0165 |
| LO1 | 901 | \％ | 120ヶ4．4M？ | 1146.1276 | 1374．2176 |
| LO1 | 951 | ＝ | 1247．74：5 | 1173．0604 | 1454．5687 |

THSS is SET QIARAER＝ 1


FIGURE 25．Output of probit analysis computer program．

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FIGURE 26. Graph of output of probit analysis program with partially erased grid lines used to highlight the $\mathrm{LD}_{50}$ point.

The investigator was able to be more at ease with the fiducial limit concept after seeing this graph. The non-symetrical nature of the limits is apparent in the figure. It is also clear how the closeness of the predicted survival curve to the observed data is reflected in the fiducial limits.

However, the investigator was more impressed with the ability to convey so much information about his experiment in a single graph. Previously he had pubiished tables of $L D_{50}$ values relating his investigations. Now he plans to publish graphs similar to Figure 26.

## ZINC-65 IN ALGAE

The previous examples illustrate the use of computer generated graphs as a means of communication. This application of EZPLOT demonstrates that graphs often reveal relationships not obviously apparent in tabular data. The statistician and the investigator were led to reevaluate both the purpose and the procedure of the experiment after analyzing the graphs produced by EZPLOT.

Zinc-65 was formerly released in large quantities into the Columbia River from the nuclear reactors on the Hanford Project. The movement of this or other radionuclides through the aquatic food chain is a potential hazard to
people who eat fish from the river. Burt Cushing is investigating one aspect of this problem, the kinetics of zinc-65 in river bottom phytoplankton (13).

Algae colonies are allowed to form on glass plates submerged in the Columbia River. The plates are brought into the laboratory and attached to Geiger-Muller tubes in a trough of running water pumped from the river. Ordinarily, the water passes through the trough once, but it can be made to re-circulate. Reactor operation is simulated by placing the trough in the re-circulate mode and adding a small quantity of zinc-65 to the water. Some of the radionuclide adheres to the algae, some is incorporated into the structure of growing algae, and most of it remains in the water. After a given time, removal of the reactors is simulated by disposing of the contaminated water and introducing fresh water.

Count rates from the G-M tubes were automatically recorded every 30 minutes. The statistician ${ }^{7}$ was asked to analyze these data in order to relate decline in radioactivity after addition of fresh water to the growth rate and life span of members of the algae colony. A computer

John Thomas was the statistician in this case. The author
worked with him to produce the worked with him to produce the graphs.
file of the data was constructed for use with an interactive non-linear regression analysis program. Two models were proposed, one based on exponential growth of the colony, the other based on a power function.

The interactive regression programs require that the user supply reasonable estimates of the parameters of the model. The statistician needed a graphic representation of the data in order to make these estimates. To save time, he manually plotted representative data by choosing every tenth point. After adjusting his estimates until the regression program converged, he used EZPLOT to draw the functions superimposed on all the data values, shown in Figure 27. His attention was immediately drawn to the apparent sinusodial pattern in the data about the exponential fit. This was unexpected and would have gone undetected if only manual data display techniques were available. The cause of the pattern could be either measurement error or some unexpected behavior of the algae.

A conference with the investigator confirmed the automatic nature of the recording apparatus. Since the period of the apparent sine wave was approximately 24 hours, the lighting conditions in the laboratory became suspect. A check with the building manager confirmed that the fluores-


FIGURE 27. Radioactivity observed in algae colony after fresh water replaced zinc-65 labeled water. Results of two nonlinear models are superimposed on the data.
cent lights were on at all times as requested by the investigator. There emerged from that conference the strong suspicion that the algae "remember" the diurnal pattern of natural light in the river. Circadian rhythm has not been reported for this type of algae, but is observed in other plant species (23).

The apparent fluxuation in algae growth was further analyzed by using the regression analysis program to fit the residuals from the exponential fit of the radioactivity observations to a sine function model. The results, plotted in Figure 28, indicate that the period exhibited by the algae colony is not constant, but becomes longer as time progresses. This may be due to a loss of "memory" after the colony is removed from natural lighting conditions. It may also be due to dilution of the colony by growth of new members in the laboratory.

These findings prompted re-evaluation of the experimental technique. In addition, they changed the direction of the investigation. Further tests are planned to demonstrate the reproducibility of the apparent sinusodial pattern of radioactivity. A test is envisioned with an artifical algae colony (a partial roll of toilet paper or a swatch of cloth) to observe the count rate pattern under


FIGURE 28. Residuals from the modeling of zinc-65 activity in algae after freshwater added, fit to a sine function. This illustrates the circadian rhythm discovered in the algae.
conditions of adsorption only. Experiments are also planned to test the effect of variation in the time between removal from the river and introduction of the radionuclide.

In general, the investigation now focuses on the kinetics of algae growth more than it does on the kinetics of zinc-65in the system.

## VI. SUMMARY AND CONCLUSIONS

Graphs were discussed as instruments of communication within the scientific community and as tools for revealing relationships not readily apparent in tabular data. Manual methods of graph preparation are tedious. None of the computer aided techniques examined were entirely satisfactory to the researcher who is not also a computer programmer. Such users tend to avoid computerized methods of graph drawing because they are either expensive, complicated to initiate, or involve lengthy turnaround times.

A relatively new type of graphics display, utilizing storage type $C R T^{\prime \prime} s$, was shown to offer acceptable compromises between output quality and user convenience. Other systems using such terminals have been described (7, 15, 17, 22) Which successfully meet the needs of more sophisticated users at reasonable cost. Strategy for development of an unsophisticated, interactive, computer graphics system using these terminals was discussed. User convenience was the main element in that strategy. The system was designed for investigators in fields such as biology and ecology who have neither the inclination nor the time to become sophisticated in computer techniques.

Hardware for the system consists of: Tektronix 4002 or 4010 graphic terminals and optional hard copy generators,
connected to a Univac 1108 computer running under the CSCX operating system. Software was written in BASIC because of the immediate response available under this operating system and because BASIC is very forgiving to unsophisticated users. Prior to software implementation, careful consideration was given to techniques of interactive programming which would maximize user convenience. The menu picking technique was adopted with display of the menu only at the user's request. Goals for the system were developed through close contact with a group of potential users. These goals appear rather modest in light of hardware capabilities, because emphasis was placed on usable output within a reasonable implementation time rather than on exotic results after several man-years of development. These goals were implemented a few at a time so that user experience could influence program development.

Implementation of the system required extensive modification of the plot driving package TEKPLOT to meet the program size limitation imposed by CSCX. Interface with this minimum plot driving package required development of routines to generate the type of graph format requested by the users. Finally, the interactive portion of the program was modified several times in response to user feedback.

Four applications of EZPLOT were discussed in detail to show the improvement in communication between investigators achieved through easily obtained graphs. These applications also illustrate the importance of a creative human effort in the pictorialization of output from data analysis.

The main conclusions which may be drawn from this work are:

- Inclusion of user input in the design phase and establishing reasonable goals, which were implemented a few at a time, were responsible for the fairly rapid implementation of the system.
- Allowing the user to supply logic at run time, as in the case of labeling of logarithmic axes, not only reduced program size and execution time, it also met with user enthusiasm. Never underestimate the user!
- The ability of the user to see his graph immediately encourages his creativity by inviting modification of scale parameters "just to see how it would look this way".
- Restricting EZPLOT to the task of graph preparation rather than including data analysis (i.e., regression) has not been a hardship to users. It encouraged development of a reliable general purpose tool rather than a graphic appendage to an analysis package.
- This system of interactive computer graphics has provided a group of investigators who are not interested in computers with a valuable and useful research tool.


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APPENDICES

## APPENDIX A

This appendix contains a brief survey of the BASIC statements used in EZPLOT, a key to array names and their function in the program, a key to variable names and their function in the program, a detailed key to the array named $P$ showing the effect of possible values stored in that array, and finally, it contains a listing of the program.

The program was not written as a work of art, but as a functional research tool. Do not be distracted by poor programming practices hastily appended to existing logic. The program listing reflects one stage of a graphics system which is still being refined.

A brief survey of BASIC statements used in EZPLOT:

| Statement | Fortran Equivalent | Description |
| :---: | :---: | :---: |
| ' (apostrophe) | None | Remainder of instruction line is remark |
| DIM | DIMENSION | Declares maximum bounds of arrays and lengths of string variables |
| END | END | Terminates program execution |
| FILES | None | Closes or opens files |
| FOR | DO | Initiates DO loop, must be terminated by a iNEXT statement |
| GOSUB | CALL | Transfers program control to a subroutine |
| GOTO | GO TO | Transfers program control to a statement other than the next sequential one |
| IF | IF ( ) GO TO | Tests logical expression and transfers a TRUE condition |
| : (image) | FORMAT | Provides a format for a single line, used with PRINT USING or OUTPUT USING |
| INPUT | READ | Causes "?" to appear at terminal then accepts data |
| NEXT | None (Continue) | Terminator of DO loop |
| ONS (N) GO TO, , , | $\mathrm{GO} \mathrm{MO}(,,)$, | Transfers control according to integer value of an expression |
| OUTPUT | None | Prints line at terminal |
| OUTPUT USING | $\begin{aligned} & \text { WRITE }(6,101) \\ & \text { Text } \end{aligned}$ | Prints formated lines |


| Statement | Fortran Equivalent | Description |
| :---: | :---: | :---: |
| PRINT |  | Same as OUTPUT |
| PRINT USING |  | Same as OUTPUT USING |
| REM | C | Adds remark to program listing |
| RETURN | RETURN | Returns program control from a subroutine |
| $<$ | .LT. | Less than |
| $=$ | .EQ. | Equal to |
| > | - GT. | Greater than |
| <> | . NE. | Not equal |
| <= | . LE. | Less than or equal to |
| $>=$ | - GE. | Greater than or equal to |
| Since array and variable names are limited to a |  |  |
| single letter or a letter and a number by BASIC, the follow- |  |  |
| ing key to variable names is necessary for understanding of |  |  |
| the program listing. |  |  |


| ARRAY | DIMENSION | FUNCTION IN EZPLOT |
| :---: | :---: | :---: |
| B | 200 | Storage of $x$ coordinate of data points <br> after possible internal transformation <br> by EZPLOT |
| C | 200 | Storage of y coordinates of transformed <br> data. <br> O $=$ th point may be plotted on log axis. <br> Q |
| Q | 20 | Storage of user responses to menu-type <br> questions. |
| R | $100 *$ | Storage of internal switches and some <br> user responses to non-menu type questions. <br> Used by TEKPLOT subroutines (line numbers <br> $l l 000$ through 45160$)$ |


| ARRAY | DIMENSION | FUNCTION IN EZPLOT |
| :---: | :---: | :---: |
| S | 100* | Used by TEKPLOT subroutines. |
| T | 100* | Used by TEKPLOT subroutines. |
| X | 200 | Storage of x -coordinate input data. |
| Y | 200 | Storage of y -coordinate input data. |
| Z \$ | 200 | String array to store plotting symbols. |
| B \$ | 55 | String array to store 55 character bottom line. |
| M \$ | 55 | String array to store 55 character line displayed at the top of the completed graph. |

*These arrays could be greatly reduced if necessary.

| VARIABLE | VARIABLE |  |
| :---: | :---: | :---: |
| RELATED | RELATED |  |
| TO | TO |  |
| X-AXIS | Y-AXIS | FUNCTION IN EZPLOT |
| F | F | $F=$ number of $x-p$ pairs to be plotted. |
| A1 | B1 | Minimum axis value in user's frame of reference. |
| A2 | B2 | Maximum axis value in user's frame of reference. |
| A3 | B3 | Range of axis in user's terms (ie. A3 = A2-A1) |
| A4 | B4 | Scale factor ( $n r$. of raster units/user's unit) |
| A5 | B5 | Screen location of minimum axis value. |
| A6 | B6 | Number of units between tic marks. |
| A 8 | B8 | Margin factor ( nr . of user's units viewable beyond the defined plot area, set at $1 / 75$ of the $x$-axis range and $1 / 50$ of the $y$-axis range) |
| A9 | B9 | Number of tic marks on axis. |



| VARIABLE | CONTENTS | MEANING |
| :---: | :---: | :---: |
| P (5) |  | AUTO SCALE? |
|  | 1 | Yes |
|  | 2 | No |
| $P(6)$ |  | GRID? |
|  | 1 | Yes, grid line at every tic mark |
|  | 2 | No grid at all |
|  | 3 | User will supply grid locations |
| $P(7)$ |  | TOP TITLE OK? |
|  | 1 | Yes |
|  | 2 | No |
| P(8) |  | BOTTOM LINE OK? |
|  | 1 | Yes |
|  | 2 | No |
| P(9) |  | WHAT NEXT? |
|  | 1 | Plot data |
|  | 2 | Change type of graph |
|  | 3 | Change Scale |
|  | 4 | Edit data |
|  | 5 | Add functions |
|  | 6 | Get new set of data |
|  | 7 | Quit |
| $P(10)$ |  | X-AXIS OK? |
|  | 1 | Yes |
|  | 2 | No |
| P(11) |  | Y-AXIS OK? |
|  | 1 | Yes |
|  | 2 | No |


| VARIABLE | CONTENTS | MEANING |
| :---: | :---: | :---: |
| P (12) |  | EDIT OPTION? |
|  | 1 | Display data |
|  | 2 | Change 1 or more items |
|  | 3 | Insert items |
|  | 4 | Switch a pair of items |
|  | 5 | Delete an item |
|  | 6 | Change Plot symbol |
|  | 7 | Data ok |
| P(15) |  | INPUT EXPERT? |
|  | 1 | Yes |
|  | 2 | No |

```
*E7PLT 10:30 09/02/73
100 DIM P(100),T(100),S(100)
110 DIM Z(200)$(1),x(200),Y(2.00)
120 DIM A(200),B(200),C(200)
130 DIM P(20)
140 DIM M$(55) ,B$(55)
150 DIM Q(20)
160 LI = 0.43429448
170 A$ = "CRWTMP"
180 G8SUB 11000 * CALL BEGIN
190 GOSUB 12000 E ERASE
200 PRINT "EZPLIOT VERSION 2 5/3/73"
210 PRINT "FgR DETAILS ABOUT ANY QUESTION ANSWER O, THERWISE"
220 PRINT "ANSWER ALL QUESTIgNS WITH SINGLE DIGIT I-9"
225Q(2) = D9 = 0
230 PRINT "INPUT TYPE";
240 INPUT P(1)
250 ON P(1) GOTO 330,7000,320,310
270 PRINT " (1) FILE IN USERS LIBRARY*
280 PRINT " (2) WANT TG ENTER DATA FRgM KEYBGARD*
290 PRINT "* (3) FILE AND WANT QUICK LOGK AT LINEAR GRAPH*
295 PRINI " (4) NO DATA, WANT ID DRAW FUNCTIgNS GNLY"
300 G8T0 230
310 F = 1
311X(1) = Y(1) = 1
312 X(2)=Y(2)=999
313 G0T0 800
320 P(4) = P(5) = 1
330 PRINT "WHAT NAME DID YOU GIVE IT";
340 IMPUT A今$
350 FILES AS
360 GET #1,M$
370 PRINT MS
380 GETg 430
390 PRINT "IS THIS:"
400 PRINT " *ap* (1) THE PROPER FILE*
420 PRINT "*R" (2) SHALL WE TRY ANBTHER FILE NAME"
430 PRINT "CBRRECT FILE";
440 INPUT P(2)
450 ON P(2) GET0 460,230
455 G9T0 390
4 6 0 ~ I F ~ P ( 1 ) ~ = ~ 3 ~ G 0 T 0 ~ 4 7 0 ~
461 PRINT " LIST AND/OR EDIT DATA";
4 6 2 ~ I N P U T ~ P ( 3 )
463 gN P(3) G0T0 470,470
464 PRINT "1 = YES, 2 = Ng"
465 GOT0 461
470 C6 = C8 = +999999
480 C7 = C9 = -999999
490 F = 0
500 FOR I = 1 T0 200
510 IFQ(2)=1 GGTg 530
515 IFP(1) = 2G0T0 530
520 INPUT #1,X(I),Y(I),Z(I)$
530 IF X(I) = 999 G0T0 641
540 IF X(I) = 888 G0T0 630
550 IF X(I) >C6 GgTg 570
```

```
5KOCK= C1 = X(I)
570 IF X(I) <C7 GOT0 590
580 C7 = C2 = X(I) 
600 C8 = DI = Y(I)
610 iF Y(I) < C9 G8T0 630
620 C9 = D2 = Y(I)
630 F = F + I
635 C(I) = 0
640 NEXT I
641 IF P(3) <>1 GOT0 650
642 P(1) = P(3)=2
643 G8T0 7990
650 IF Q(2) <>I GOT0 670
660 BN P(9) EBIO 3120,800,1270
6 7 0 ~ I F ~ P ( I ) ~ = ~ 3 ~ G 0 T 0 ~ 8 2 0 ~
680 PRINT USING "NQW HAVE ### ITEMS ",F
690 PRINT " MINX MAXX MINY MAX Y"
700 PRINT C6,C7,C8,C9
710 FILES
800 PRINT " TYPE GF GRAPH**
805 Q(17) = Q(18) = 0
810 INPUT P(4)
820 ON P(4) GOTO 1060,1060,920,920
840 PRINT "2 = LOG Y VS LINEAR X"
850 PRINT "3 = LINEAR Y VS LOG X*
860 PRINT " 4 = LQGY Y VS LQG X"
8 7 0 ~ G O T O ~ 8 0 0 ~
920 REM L0G 0F X ValuES
930 FOR I = 1 T0 F
940 IF X(I) <> 888 G0T0 970
950 A(I) = X(I)
960 G日Tg 1040
970 IF X(I) = 999 GDTD 1040
980 IF X(I) >0.0 GOT0 1030
990 PRINT "WILL SKIP:";
1000 PRINT X(I),Y(I)
1010 C(I) = 1
1020 G0T0 1040
1030 A(I) = LI * L|G (X(I))
1040 NEXT I
1050 G0T0 1090
1060 FOR I = 1 Tg F
1070 A(I) = X(I)
1080 NEXT I
1090 ON P(4) GgTg 1240,1100,1240,1100
1IOO REM LOG OF Y VALUES
1110 FOR I = 1 T F
1120 IF Y(I) <> 888 G0T0 1150
1130 B(I) = Y(I)
1140 GOT0 1220
1150 IF Y(I) = 999 G8T0 1220
1160 IF Y(I) > 0 GOIO 1210
1170 C(I) = I
1180 PRINT "WILL. SKIP: ";
1190 PRINT X(I),Y(I)
1200 GOT0 1220
1210 B(I) = L1 * LOG (Y(I))
122.0 NEXT I
1230 G0T0 1270
1240 FOR I = 1 T0 F
1250 B(I)= Y(I)
1260 NEXT I
1265 IFP(I) = 3 GBT0 1420
1269 REM ON NEG 1.&G AXIS. FGRCE USER INTO MANUAL SCALE
```

```
    1270 ON P(4) G8T\ddot{0 1279,12́71,1273,1271}
    1271 IF C&<0 G0Tg 1275
    1272 IF P(4) <>4 GOT0 1279 104
    1273 IF C6<0 GBTg 1275
    1274 G0T0 1279
    1275 P(5) = 2
    1276 GBTQ }175
    1279 PRINT "AUTD SCALE";
    1280 INPUT P(5)
    1290 NN P(5) GOT0 1420,1750
    1300 PRINT "1 = AUTGMATIC SCALE T0 FIT DATA"
    1310 PRINT "2 = USEP. WILL SUPPLY SCALE FACT0RS"
    1320 GBTA 1270
    1420 REM AUTO SCALE
    1422 A1 = C5
    1424 A2 = C7
    1426 B1 = C8
    1428 B2 = C9
1470 ON P(4) G0T0 1500,1500,1480,1480
1480 Cl = LI * LOG(AI)
1490 C2 = L1 * LOG(A2)
1500 C3 = C2 - C1
1505 A3 = A2 - A1
1510 AS = A3/10
1560 ON P(4) GOTg 1590,1570,1590,1570
1570 DI = LI * LBG(B1)
1580 D2 = L1 * LOG(B2)
1590 D3 = D2 -D1
1595 B3 = B2 - B1
1600 B6 = B3/10
1610Q(7) = Q(8) = 2
1620 A9 = B9 = 10
1630 REM ALL LINEAR SCALES CQME HERE
1640 A4 = 900/C3
1650 A5 = i00 - (CiN&4)
16к0 B4 = 600/D3
1670 B5 = 100-(D1*B4)
1680 A8 = C3/75
1690 B8 = D3/50
1700 G8TB 2610
1710 REM MANUAL SCALE FACTORS
1750 PRINT "YOU WILL NEXI DEFINE THE SIZE GRAPH YOU WANT"
1760 PRINT "O,0 CAN BE GFF THE SCREEN"
1850 PRINT "X-AXIS:"
1852 PRINT " MIN X MAX X"
1854 PRINT "DATA
1856 PRINT C6,C
1857 PRINT "AXIS
1858 PRINT AI,A2
1880 PRINT USINNG 1890;
1890 :MINIMUM VALUE-
1900 I NPUT Al
1910 PRINT USING 1920;
1920 :MAXIMUM1 VALUE -
1930 INPUT A2
1940 IF A2<AI G&T& 1850
1942 ON P(4) G0T0 1950,1950,1944,1944
1944 IF AI > O G0T0 1950
194K PRINT "CANNgT HAVE NEGATIVE VALUES IN LOG SCALE"
1948 G0T0 1850
1950 A3 = C3 = A2 - A1
1960 C1 = A1
1970 C2 = A2
1980 PRINT " X -AXIS G0ES FROM ";
1990 PRINT A!;
2000 PRINT "Tg ":
```

```
    2010 PRINT A2
-2011 ON P(4) G0T0 202.9,2029,2012,2012.
    2012 AG = A3
    2013 A9 = 1
    2014 PRINT "IN ADDITION T0 THESE 2 ENDPQINTS"
    2015 PRINT "HOW MANY GTHER TIC MARKS ARE WANTED (MAX 10)";
    2016 INPUT Q(17)
    2017 FGR I = 1 TQ Q(17)
    2018 PPINT "X VALUE FOR ";
    2019 PPINT I;
    2020 INPUT L(I)
    2 0 2 1 ~ N E X T ~ I ~
    2022. Q(7) = 1
    2023 GBT0 2091
    2029 PRINT "WITHIN THIS RANGE QF *;
    2030 PRINT A3;
    2040 PRINT "UNITS"
    2050 PRINT "HOW MANY UNITS DD YBU WANT BETWEEN TIC MARKS";
    2060 INPUT AG
    2070 B9 = A3/AG
    2080 Q(3) = 1
    2090 GDT| 2380
    2091 PPINT "X AXIS 0K";
    2092 INPUT P(10)
    2093 ON P(10) GOTg 2100,1850
    2094 PPINT "1 = YES, 2= NO"
    2095 G0T0 2091
    2100Q(3)=0
    2105 gNP(4)GBT8 2110,2110,2140,2140
    2110Q(7) = Q(9)
    2120 A9 = B9
2130 G0T0 2170
2140 C1 = LI * L0G(AI)
2150C2 = L1 * LBG (A2)
2160 C3 = C2 - C1
2170 G8SUB 12000
2172 PRINT " Y AXIS*
2174 PRINT "DATA ";
2176 PRINT C8,C9
2177 PRINT "AXIS ";
2178 PRINT B1,B2 
2210 INPUT B!
2220 PRINT USING 1920;
2 2 3 0 ~ I N P U T ~ B 2 ,
2240 IF B2&B1 GOTO 2170
2242 0N P(4) G0T8 2250,2244,2250,2244
2244 IF BI > O GgT0 2250
224G PRINT "CANN@T HAVE NEGATIVE VALUES ON LBG SCALE"
2248 GOTg 2170
2250 B3 = D3 = B2 -B1
2260 D1 = B1
2270 D2 = B2
2280 PRINT "Y-AXIS GOES FRgM ";
2290 PRINT BI;
2300 PRINT " To";
2310 PRINT B2
2311 GN P(4)GB T0 2329,2312,2329,2312
2312 B6 = B3
2313 B9 = 1
2314 PRINT "IN ADDITION T0 THESE 2 ENDPOINTS,*
2315 PRINT "HOW MANY GTHER IIC MARKS ARE WANTED (MAX 10)";
2316 INPUT Q(18)
2317 FOR I = 1 TOQ(18)
2318 PRINT " Y VALUE FOR TIC ";
2319 PRINT I:
```

```
        2320
    2321 NEXT I
    2322 Q(8) = 1
    2324 GOT0 2520
    2329 PPINT "WITHIN THIS RANGE OF **
    2330 PRINT B3;
    2340 PRINT "UNITS"
    2350 PRINT "HDW MANY UNITS DO YOU WANT BETWEEN TIC MARKS";
    2360 INPUT BG
    2370 B9 = B3/B6
    2380 PRINT USING "THAT WILL MEAN ### TIC MARKS ON THE AXIS",B9
    2390 IF B9 <1 GGT0 2530
    2400 IF B9 >51 G0T0 2530
    2410 GOTg 2460
    2420. PRINT "1 = EVERY TIC WILL BE LABELED*
    2430 PRINT " 2 = EVERY OTHER TIC WILL BE LABELED*
    2440 PRINT * 3 = EVERY TMIRD TIC LABELED*
    2450 PRINT " ETC."
    2460 PRINT "LABEL FACTOR";
    2470 INPUT Q(9)
    2480 IF Q(9) <1 G0Tg 2420
    2490 IF Q(9) > B9 G0T0 2420
    2500 IF Q(3)=1 G0T0 2.091
    2510 Q(8) = Q(9)
    2520 PRINT "Y AXIS 0K";
    2521 INPUT P(11)
    2522 0N P(11) GOT0 2560,2170
    2523 PRINT "1 = YES, 2 = Ng"
    2524 G0Tg 2520
    2530 PRINT "T0O FEW GR TOO MANY"
    2540 IF Q(3) = 1 G9T8 2050
    2550 GOT8 2350
    2560 ON P(4) G0T0 1640,2570,164C,2570
    2570 DI = LI * LgG(BI)
    2580 DP = !! * LaG(B2)
2590 D3 = D2 - D1
2600 G8TG 1640
2610 REM
2620 IF P(1) = 3 GIT0 2970
2K21 PRINT "GRID";
2622. INPUT P(6)
2623 日N P(6) G0T0 2630,2630,2790
2624 PRINT "1 = AUTOMATIC GRID AT EACH TIC"
2625 PRINT "2 = N% GRID AT ALL"
2626 PRINT "3 = USER WILL SUPPLY GRID LBCATIONS"
2627 G0T0 2621
2630 PRINT "TgP TITLE OK";
2640 INPUT P(7)
2650 NN P(7) GBT& 2760,2740
2660 PRINT "YOU MAY:"
2670 PRINT " (1) HAVE:";
2680 PRINT MS;
2690 PRINT " DISPLAYED AT TBP OF GRAPH*
2700 PRINT "gR"
2710 PRINT "(2) ENTER A NEW TITLE FGR THE TQP OF THE GRAPH"*
2.740 PRINT "ENTER TITLE FQR THIS DATA (MAX 55 CHARACTERS)"
2750 GET M$
2755 G9T0 2630
2760 IF P(6) = 1 GeTO 2950
2770 Q(6) = 0
2780 G0T0 2960
2790 PRINT "HOW MANY VERTICAL GRID LINES (O=NgNE,MAX IS 10)*;
2800 INPUT Q(4)
2810 IF Q(4)<1 G0T0 2860
2815 IF Q(4) > 10 GBTO 2860
```

```
2820 FOR I = 1 TO Q(A)
2830 PRINT USING "WHAT X VALUE FOR GRID LINE ##",I;
2840 I NPUT K(I)
2850 NEXT I
2860 PRINT "HOW MANY HORIZONTAL GRID LINES (O=N8NE, MAX IS 10)";
2870 INPUT Q(5)
2880 IF Q(5) <1 G0T0 2960
2885 IF Q(5) > 10 GBT0 2960
2890 FGR I = 1 T0 Q(5)
2900 PRINT USING "WHAT Y VALUE FER GRID LINE *",I;
2910 INPUT J(I)
2 9 2 0 ~ N E X T ~ I ~
2930 G0T0 2630
2940 REM----SET UP AUT% GRID
2950 Q(6) = 1
2960 IF Q(2) = 1 G9T0 2990
2970 PRINT "ENTER DESCRIPTIVE LINE FER BGTTQM OF GRAPH"
2980 GET B$
2990 PRINT "BOTTOM LINE OK";
2992 INPUT P(8)
2994 ON P(8) G9TO 3090,2970
3000 PRINT "ARE Y&U:"
3010 PRINT "(1) SATISFIED WITH: ";
3020 PRINT B$
3030 PPINT " OR DO YOU*
3040 PRINT "(2) WANT A DIFFERENT B0TTGM LINE*
3050 G@T0 2990
3090 Q(1) = 1
3100 IF Q(2) =1 GOTb 4180
3110 IF P(1) = 4GgT0 5160
3120 Q(2) = 1
3145 REM-------------PLOT GRAPH HERE
3150 GGSUB 12000 'PAGE
3160 G0SUB 4350 'USERS SCALE
JiTO GnSUB i 5000 :VECTOR MODE
3180 GZSUB 5340 'DRAW AXIS
3181 IF Q(17) = 0 G8T0 3184
3182 GQSUB 9700 'LQG X TIC MARKS IF ANY
3184 IF Q(18) = O G0T0 3190
3186 GOSUB 10000 LGG Y TIC MARKS IF ANY
3190 IF Q(4) < 1 G0T0 3210
3200 GQSUB 4470 vERTICAL GRID
3210 IF Q(5)<1 G日T0 3230
3220 GOSUB 4630 HORIZONTAL GRID
3225 IF P(1) = 4 G@T0 3870
3230 FOR I = 1 TOF
3240 IF Z(I)$ = " '* G0T0 3860
3250 IF C(I) = 1 GOT0 3860
3260 J = 0
3270 IF Z(I)$ = "-" G0T| 3330
3280 J = 0
3290 IF Z(I)S = "D" GETg 3340
3300 IF Z(I)$ = "."G8TD 3340
3310 K=2
3320 G&T0 3350
3330 J = 1
3340 K = 1
3350 IF A(I) <>888 GBT0 3420
3360 IF B(I) <> 888 G0TO 3420
3370 X1 = A(I+1)
3380 X2 = B(I+1)
3390 X3 = 0
3400 GgSUR 9000
3410 G0T0 3860
342.0 X1 = A(I)
3430 X2 = B(I)
```

```
    3440 IF I >1 GOT0 3470
    3450 X = =0
    3460 GB T0 3490
    3470 <3 = J
    3490 GOSUB 9000
    3500 IF K<>2 GOTg 3580
    3510 REM ADJUST KEYBOARD SYMBGLS TO CENTER PROPERLY
    3520 X1 = A(I) -3/A4
    3530 X2 = B(I) -4/B4
    3540\times3=0
    3550 GgSUB 9000 'DARK TG DATA PBSITIGN
    3560 PRINT Z(I)$
    3570 GOT0 3860
    3580 IF Z(I)$ = "D" G0Tg 3650
    3590 X1 = A(I)
    3600 X2 = B(I)
    3610 X3 = 1
    3630 GOSUB 9000
    3640 GaT 3860
    3650 REM DRAU DIAMGND CENTERED ON ACTUAL DATA POSITIGN
    3660 XI = A(I) + 4/A4
    3670 X2 = B(I)
    3680 <3 = 0
    3690 GBSUB 9000
    3700 %1 = A(I)
    3710 X2 = B(I) -6/E4
    3720 X3 = 1
    3730 GOSUB 9000
    3740 X1 = A(I) - 4/A4
    3750 X2 = B(I)
    3760 X3 = 1
    3770 G9SUB 9000
    3780 XI = A(I)
    3790 X2 = B(I) + 6/B4
    3800 K3 = 1
    3810 G0SUB 9000
    3820 X1 = A(I) +4/A4
    3830 X2 = B(I)
    3840 X3 = 1
    3850 GOSUB 9000
    3860 NEXT I
    3870 IF D9 <> 9 GOTD 3890
    3880 G9SUB 4810
    3890 FgR I = 1 TG 5
    3900 X1 = 7
    3910 GgSUB 45000 'RING BELL
    3920 X1 = 0
--3930 G0SUB 45000
    3940 NEXT I
    3950 G2SUB 4240 *ABS8LUTE SCALE
    3960 K1 = 200
    3970 X2 = 780
    3980 <3 = 0
3990 GOSUB 9000
3992. XI = 200
3993 X2 = 780
3994 X3 = 0
4010 X1 = 200
4020 X2 = X3 = 0
4030 GBSUB 9000
4040 OUTPUT B$
4041 X1 = 200
4042. }\times2=76
4043 X3 = 0
4 0 4 4 ~ G 0 S U B ~ 9 0 0 0 ~
4045 RUTPUT M$
```

```
4050 X1 = X3 = 0
4060 X1 = X2 = x3 = 0
4070 G0SUB 9000 'G8T0 UPPER LEFT 109
4071 X1 = X3 = 0
4072 X2 = 780
4 0 7 3 \text { G0SUB 9000}
4080 GUTPUT "?";
```



```
4l00 GBSUB 12000 'PAGE
4 1 0 5 ~ P ( 1 ) ~ = ~ 0 ~ 0
4110 GOTg 4180
4120 PRINT " I = PLGT DATA AS IT IS"
4l30 PRINT " 2 = CHANGE TYPE OF GRAPH*
4I40 PRINT " 3 = CHANGE SCALE"
4150 PRINT " 4 = EDIT DATA*
4160 PRINT " 5 = ADD FUNCTIGNS"
4165 PRINT " 6 = GET NEU DATA FILE*
4170 PRINT " 7 = QUIT"
4180 PRINT "HHAT NEXT";
4190 INPUT P(9)
4210 ON P(9)G日T0 3120,470,470,7990,5160,225,4220,4120
4211 G0T0 4120
4 2 2 0 ~ E N D
4 2 3 0 ~ R E M
```



```
4250 X1 = X2 = 1
4260 X3 = 0
4270 GOSUB 21000
4280 X1 = 0
4 2 9 0 \times 2 = 0
4300 X3 = 1020
4310 X4 = 780
4320 GBSUB 23000
4 3 3 0 ~ R E T U R N
434Ö REM
4350 REM ............ SUBROUTINE T0 SET SCALE TQ USERS CHgICE
4360 X1 = A4
4370 X2 = B4
4380 X3 = A5
4390 X4 = B5
4400 GBSUB 21000
4410 X1 = C1 - 20*AB
4420 <2 = D1 - 20*B8
4430 X3 = C2 + 10*A8
4440 X4 = D2 + 10*B8
4450 GeSUB 23000
4460 RETUPN
4470 REM --.-- SUBRQUTINE FGR VERTICAL GRID LINES
4480 FOR I = 1 TO Q(4)
4490 GN P(4) G8T8 4520,4520,4500,4500
4500 XI = G = LI * LOG(K(I))
4510 G0T0 4530
4520 XI = G = K(I)
4530 X2 = B1
4540 X3 = 0
4550 G0SUB 9000
4560 <1 =G
4570 X2 = B2
4580 X3 = 1
4600 G8SUB 9000
4610 NEXT I
4 6 2 0 ~ R E T U R N
4630 REM =---- SUBROUTINE FGP HORIZQNTAL GRID LINES
4640 FOR I = 1 TO Q(5)
4650 X1 = A1
AKKO ON P(4) GOTO 4K90.4670.4690.4670
```

```
    4 6 7 0 \times 2 = G = L 1 ~ * ~ L D G ( J ( I ) ; ~
4680 G0T0 4700
4690 X2 =G = J(I) 110
4710 G0SUB 9000
4720 X1 = A2
4730 X2 =G
4740 X3 = 1
4760 G8SUB 9000
4 7 7 0 ~ N E X T ~ I ~
4 7 8 0 \text { RETUPN}
4790 REM
4800 REM ...................................
4810 PEM SUBROUTINE FOR USER FUNCTIGNS (MAX 5)
4820 D8 = Y
4830 D7 = X
4 8 4 0 ~ F Q R ~ J = 1 ~ T O ~ D G ~
4850 X1 = C1
4860 X2 = D1
4870 X3 = 0
4 8 8 0 ~ G Q S U B ~ 9 0 0 0 ~ ' D A P K ~ T O ~ O R I G I N
4 8 9 0 ~ F G R ~ I ~ = ~ A 1 ~ T O ~ A 2 ~ S T E P ~ A 3 / 1 0 0 ~
```



```
4910 IF I <>0 G0Tg 4930
4920 X = 0.0000001
4930 ON J G0T0 4950,4970,4990,5010,5030
4940 REM USER XTATEMENTS NEXT
4 9 5 0 ~ Y ~ = ~ X ~
4960 G0T0}504
4970 Y = X - . 5
4980 GET0 5040
4990 Y = DI
5000 GOTD 5040
5010 Y = DI
5020 G0TA 5040
5030 Y = DI
5040 ON P(4) GOTO 5045,5045,5050,5050
5045 X1 = X
5047 G0T0 5060
5050 X1 = L.1 * L0G(X)
5060 ON P(4) GOTO 5065,5070,5065,5070
5065 X2 = Y
5067 G0T0 5080
5070 X2 = L1 * LOG(Y)
5080 X3 = 1
5081 IF I <>CI GOT0 5100
5082 X3 = 0
5100 G0SUB 9000
5110 NEXT I
5120 NEXT J
5130 Y = D8
5140 X = D7
5150 RETURN
5160 PRINT "YOU MUST ENTER YOUR FUNCTION AS A BASIC STATEMENT"
5170 D9 = 9
5180 PRINT "ENTER NUMBER OF FUNCTIONS YOU WISH TO DISPLAY (LIMIT 5)";
5190 INPUT DG
5200 0N DG G0T0 5220,5220,5220,5220,5220
5210 GOT0 5180
5220 PRINT "INSERT FUNCTIONS AT 4950,4970,49690,5010,5030"
5250 PRINT "EXAMPLE: 4950 Y = SIN(Y)"
5260 PRINT *T0 SEE THE RESULTS, TYPE "mGg T| 9600"mo
5270 PRINT "HIT CONTROL-SHIFT-K NOWI!"
5280 GET A$
52.90 GOT0 4180
5300 GOT0 2960
```

```
    5340 REM -----AXIS SUBRqUTINE
    5345 GOSUB 15000
    5350 REM HQRIZONTAL TIC MARKS TOP AND BOTTQM 111
    5360Q(9) = 0
    5 3 7 0 ~ F O R ~ I ~ = ~ O ~ T O ~ A S ~ A
    5380 G = G1 = A1 + AG*I
    5390 0N P(4) G0T0 5410,5410,5400,5400
    5400 G = L1 * L8G (G)
    5410 IF Q(9)<>0 GgTD 5468
    5420 XI = G - 3*A8
    5430 X2 = D1 - 5*B8
    5440 X3 = 0
    5450 G8SUB 9000
    5460 PRINT GI
    5464 X2 = D1 - B8
    5466 G0T0 5470
    5468 X2 = D1 - B8/2
    5470Q(9)=Q(9)+1
    5480 IF Q(9) <> Q(7) G0T0 5500
    5490 Q(9) = 0
    5500 X1 = G
    5520 X3 = 0
    5530 GESUB 9000
    5540 X1 = G
    5550 X2 = D1
    5560 X3 = 1
    5570 G8SUB 9000
    5580 X1 = G
    5590 X2 = D2
    5600 IF I = O GPT& 5640
    5610 IF I = Ag GOT0 5640
    5620 X3 = Q(6)
    5630 GETO 5650
5640 X3 = 1
5650 G0SUB 9000
5660 X1 = G
5670 X2 = D2 + B8/2
5680 X3 = 1
5690 G0SUB 9000
5 7 0 0 ~ N E X T ~ I ~
5 7 1 0 \text { PEM Y AXIS TIC MARKS AND OPTIONAL GRID}
5715 GBSUB 15000
5720 Q(9) = 0
5730 FGR I = 0 TO B9
5740G=G1=B1 + B6*I
5770 GN P(4) G0Tg 5790,5780,5790,5780
5780 G = LI * L|G(G)
5790 IF Q(9) <> O GgT0 5848
5800 X1 = C1 - 10*A8
5810 X2 = G -B8/2
5820 X3 = 0
5830 G9SUB 9000
5840 PRINT GI
5844 X1 = C1 - A8
5846 G0T0 5850
5848 X1 = C1 - A8/2
5850 Q (9) = Q(9) +1
5860 IF Q(9) <> Q(8) G0T0 5890
5870 Q(9) = 0
5890 X2 = G
5900 X3 = 0
5910 G0SUB 9000
5920 X1 = C1
5930 <2 =G
5940 X3 = 1
5950 GBSUR 9000
```

```
    5960 Xi = C2
    5970 X2 = G
    5980 IF I = 0 GOT0 6020
    5990 IF I = B9 GOIO 6020
    6000 X3 = Q(6)
    6010 G0T0 6030
    6020 X3 = 1
    6030 G&SUB 9000
    6040 X1 = C2 + A8/2
    6050 X2 = G
    6060 X3 = 1
    6 0 7 0 \text { G0SUB } 9 0 0 0
    6 0 8 0 ~ N E X T ~ I ~
    6 0 9 0 ~ R E T U R N
    7000 REM ------ SUBR@UTINE TO INPUT DATA FR@M KEYBgARD
    7010 K = 1
    7020 GgT0 7120
    7040 PRINT "IF YOU CHOOSE TG CONNECT YOUR DOTS WITH A LINE,"*
    7050 PRINT "REMEMBER THAT THEY WILL BE CONNECTED IN THE ORDER"
    7060 PRINT "IN WHICH YOU ENTER THEM. ENIER 1 IF YOU WANT THEM CONNECTED"
        PR
    7070 PRINT " 2 IF NOT";
    7080 INPUT K!
    7090 IF KI = 2 G9T0 7110
    7100 H$ = "-"
    7110 GBTO 7300
7120 PRINT
7!21 PRINT "ENTER DESCRIPTIUE LINE FgR THIS DATA"
7122 GET MS
7125 PRINT "INPUT EXPERT";
7126 INPUT P(15)
7127 IF P(15) =1 G&T0}725
7130 PRINT "DATA WILL BE ENTERED AS X,Y PAIRS"
7140 PRINI "EACH SET OF DATA POINTS MUST BE PRECEEDED BY A PLOT SYMBOL"
7150 PRINT "TO HAVE DATA POINTS CONNECTED ENTER KEYBOARD PERI@D AS PLOI
        SYMB01"
7160 PRINT "THE KEYBOARD "*D"" WILL RESULT IN A SMALL DIAMOND *
7180 PRINT "OTHER KEYBEARD CHARACTERS WILL BE CENTERED AT THE DATA"
7190 PRINT "LOCATIQN, BUT MAY PRINT GFFSET BECAUSE OF THEIR SHAPE"
7200 PRINT "I SUGGEST YOU USE SYMETRICAL KEYBOARD CHARACTERS"
7210 PRINT "SUCH AS: 0,*,0,@,X,+,#, AND Q."
7220 PRINT "MAXIMUM NUMBER OF'POINTS IS 200"
7230 PRINT "WHEN LAST ITEM IS ENTERED, ENTER 999,999 T% SIGNAL END OF DA
7240 PRINT "WHEN YgU WISH TO CHANGE. PLOT SYMBQL ENTER 888,888"
7250 PRINT USING "ENTER gNE KEYB@ARD CHARACTER TO BE USED WITH DATA SET
        ## ",K;
7260 INPUT H$
7270 IF HS <> "-" GOIO 7290
7280 H$ = "."
7290 IF H$ = "."G0T0 7040
7300 PRINT
7310 PRINT USING *NTER
7320 FOR I = 1. TO 200
7330 MAT INPUT H(1,2)
7340
7350 X(I) = H(1,1)
7360 Y(I) = H(1,2)
7370 IF X(I) = 888 GO TO 7410
7380 Z(I)$ = H$
7 3 9 0 ~ I F ~ X ( I ) ~ = ~ 9 9 9 ~ G 0 ~ T 0 ~ 7 5 6 0 ~
7400 GG T0 7570
7410 K= K + 1
7420 Z(I)$ = "1"
7430 PRINT USING "ENTER NEW SYMBOL FOR DATA SET ##.K:
```

```
7440 INPUT H$
7450 IF H$ = "-"G0T0 7470
7460 GOT0 7480
7470 K$$="""** GOTD 7510
7490 PRINT USING "ENTER M&RE PAIRS FOR DATA SET ## ",K
7500 G8T8 7570
7510 PRINT "DG Y&U WANT THESE DOTS CONNECTED WITH A LINE (1) QR NGT(2)";
7520 I NPUT KI
7530 IF K1 = 2 GOTO 7490
7540 H$ = "-"
7550 G0T0 7490
7560 IF Y(I) = 999 G0 T0 7590
7 5 7 0 ~ N E X T ~ I ~
7580 PRINT "YOU HAVE EXCEEDED 200 DATA PQINTS, WILL PLOT WHAT YOU HAVE E
                NTERED"
7590 REM
7600 F =I
7610 G = 1
7640 REM ------\Gamma gUTINE TO EDIT DATA
7650 G0T0 7990
7660 GOSUB 12000 'PAGE
7670 PRINT " YOUR DATA IS:*
7680 PRINT "ITEM NUMBER X-VALUE Y' VANT "IEME SYMB0L"
7700 G = = 1 = 1 IO F
7 7 2 0 ~ I F ~ X ( I ) = 8 8 8 ~ G 0 ~ T 0 ~ 7 7 4 0
7730 G0T0 7800
7740 PRINT I;
7750 PRINT " DATA SET ";
7760 G = G + 1
7770 PRINT G;
7780 PRINT "'FBLLBWS*
7790 GOTg 7900
7800 PRINT I, X(I),Y(I),Z(I)$
7810 IF I = 32 G0T0 7870
7820 LF I = 66 G0Td 7870
7830 IF I = 100 G8T0 7870
7840 IF I = 134 G0T0 7870
7850 IF I = 168 G0ID 7870
7860 GBTD 7900
7870 PRINT "?";
7880 GET B$
7890 GgSUB 12000 'PAGE
7 9 0 0 ~ N E X T ~ I ~
7 9 1 0 ~ G 8 T O ~ 7 9 9 0 ~
```



```
8027 G0T\ 4180
8030 PRINT "ENTER NUMBER OF ITEM TG CHANGE";
8 0 4 0 ~ I N P U T ~ K I ~
8050 PRINT USING "NEW X FOR ITEM ###",KI;
8 0 6 0 ~ I N P U T ~ X ( K I )
```

```
8070 PRINT USING "NEW Y FOR ITEM ###",KI;
```



```
8090 G8T0 7990
8100 REM
8340 PRINT "WHAT ITEM # PRECEEDS THE ITEM YOU WISK TO INSERT";
8 3 5 0 ~ I ~ N P U T ~ K 3 ~
8360 FOR I = FTO K3 + 1 STEP - 1
8370 X(I+1 ) = X(I)
8380 Y(I+1) = Y(I)
8390 Z(I+1)$=Z(I)$
8400 NEXT I
8410 F=F + 1
8420 PRINT "C OMPUTER HAS RENUMBERED YOUR. ITEMS"
8 4 2 5 ~ I F ~ P ( 1 2 ) ~ = ~ 5 ~ G 9 T 0 ~ 7 9 9 0 ~
8430 K1 = K3 +1
8440 G0T0 8050
8450 PRINT "WHAT ITEMS Dg YOU WISH SWITCHED"
8460 PRINT "FIRST ITEM";
8470 INPUT K4
8480 PRINT "SECBND ITEM";
8490 INPUT K5
8500 D = X(K4)
8510 X(K4) = X(K5)
8520 X(K5) = D
8530 E = Y(K4)
8540 Y(K4) = Y(K5)
8 5 5 0 ~ Y ( K 5 ) ~ = ~ E ~
8560 G$ = Z(K4)$
8570 Z(K4)$=Z(K5)$
8580 Z(K5)$ = G$
8590 : ITEM ## IS NQU ITEM ##
8600 PRINT USING 8590,K4,K5
8610 PRINT USING 8590,K5,K4
8620 GBT0 7990
8630 PRINT "SYMBGL CHANGE*
8640 PRINT "FIRST ITEM NUMBER";
8650 INPUT K7
8660 PRINT "LAST ITEM NUMBER ";
8 6 7 0 ~ I N P U T ~ K 8 ~
8680 PRINT "ENTER NEW SYMBBL";
8 6 9 0 ~ I N P U T ~ H S ~
8700 FBR I = K7 T0 K8
8710 Z(I)$ = H$
8 7 2 0 ~ N E X T ~ I ~
8730 GGTg 7990
8740 PRINT "WHAT ITEM # TO DELETE*;
8 7 5 0 ~ I N P U T ~ K 6 ~
8760 FOR I = K6 +1 T0 F
8770 X(I-1)= X(I)
8780 Y(I-1) = Y(I)
8790 Z(I-1)$ = Z(I)$
8 8 0 0 ~ N E X T ~ I ~
8810 F = F -1
8820 G0T0 8420
9000 REM --------- MY OWN TPLBT SUBROUTINE
9010 X4=0
9020 T(58) = X1
9030 T(59) = X2
9040 T(60) = X3
9050 T(61) = X4
9060 S0 = T(61)
9070 R(2) = T(58)*R(6) + R(8)
9080 R(3) = T(59) * R(7)+R(9)
9090 S1 = R(1)
9100 IF T(60) = 0.G0T8 9140
9110 K1 = 0
```

```
9120 GBSUB 44000
9130 GuTg 9300
9140 G0SUB 15000
1 1 5
9150 SO=0
9300 RETURN
9600 G0Tg 4180
9700 REM X AXIS LQG IIS MARKS
9710 FOR I = 1 T| Q(17)
9720 <0 = L1 * LGG(L(I))
9730 X1 = X0 - 3*A8
9740 X2 = D1 - 5*B8
9750 X3 = 0
9 7 6 0 \text { GBSUB 9000}
9770 PRINT L(I)
9780 X1 = X0
9790 X2 = D1 - B8
9799 X3 = 0
9800 G0SUB 9000
9810 X1 = X0
9820 X2 = D1
9830 X3 = 1
9840 G8SUB 9000
9850 X1 = x0
9860 X2 = D2
9870 X3 = 0
9880 G0SUB 9000
9890 X1 = X0
9899 X2 = D2 + B8/2
9900 <3 = 1
9910 GOSUB 9000
9920 NEXT I
9940 RETURN
10000 REM----- Y AXIS TIC MARKS IF LOG
10010 FgR I = 1 T8 Q(18)
10020 XO = L1 * LOG(M(1))
10030 X1 = C1 - 10*A8
10040 x2 = x0
10050 x3 = 0
10060 GBSUB 9000
10070 PRINT M(I)
10080 X1 = C1 - A8
10090 X2 = x0
10100 X3 = 0
10110 G8SUB 9000
10120 X1 = Cl
10123 x2 = x0
10130 X3 = 1
10140 G0SUB 9000
10150 X1 = C2
10160 X2 = x0
10170 X3 = 0
10180 G9SUB 9000
10190 X1 = C2 + A8/2
10199 x2 = x0
10200 X3 = 1
10210 GBSUB 9000
102.20 NEXT I
10230 RETURN
11000 REM ------- BEGIN
11015 T(1) =300
11020 F0R T=1 T0 22
11030 R(T) =0.
11040 NEXT T
11050 R(6)=1.
11060 R(7) =1.
11070 R(14)=1023.
```

```
    11080 R(15)=761.
    11090 R(17)=1024.
    11100 R(18)=762.
    11110 R(22)=1
    11120 GOSUB 15000
    11140 REM COMPUTE CHARACTERS PER .5 SECOND
    11150 REM AT SPECIFIED BAUD RATE
    11160 R(23)=T(1)/16.
    11170 RETURN
    11180 REM
    12000 REM ERASE
    12005 X1=27
    12006 GOSUB45000
    12007 X1=12
    12008 GOSUB45000
    12010 < = =24
    12020 GBSUB 45000
    12030 REM GUTPUT A CANCEL CBDE
    12040 I=R (2.3)
    12050 REM FETCH CHARACTERS PER . }5\mathrm{ SECOND
    12060 FgR T1 =1 T0 I+1
    12070 XI=0
    12080 G0SUB 45000
    12090 NEXT Tl
    12100 REM GUTPUT . }5\mathrm{ SECGNDS WGRTH OF NULLS
    12120 RETURN
    12130 REM
    15000 REM VECTOR
    15010 X1=31
    15020 GOSUB 45000
    15030 REN gUTPUT A US FIRST AS INSURANCE.
    15040 IF P(10)=0 G0Tg 15080
    15050 XI=25
    15060 GOSUB 45000
```



```
    15080 R(1)=1
    15090 REM SET THE R ARRAY TO VECTOR STATUS
    15100 X1=1
    15110 GOSUB 44000
    15120 REM DARK VECTOR TO THE CURRENT POSITION.
    15130 RETURN
    15140 REM ------------------------------------------------------------------
    21000 REM SCALE
    21010 S9=3
    21020 T(3)=X1
    21030 T(4) =X2
    21040 T(5) = X3
    21050 T(6) =X4
    21060 R(6)=T(S9)
    21070 R(7)=T(S9+1)
    21080 R(8) =T(S9+2)
    21090 R(9)=T(S9+3)
    21100 PETURN
21110 REM
23000 REM WINDGW
23010 S=10
23020 T(10)=x1
23030 T(11)=X2
23040 T(12) =X3
23050 T(13) = X4
23060 FOR T=1 T0 4
23070 R(T+30) =R(T+5)
23080 NEXI T
23090 REM FETCH CURRENT SCALING FACTGRS AND GRIGIN.
23100 R(35)=T(S)*R(31)
23110 R(36)=T(S+1)*R(32)
```

```
    23120 R(37) =T(S+2)*R(31)
    23130 R(38)=T(S+3)*R(32)
```



```
    23320 T1=1
    23330 F0R T2=1 T0 2
    23340 FRR T3=3 T0 4
    23350 R(T1+34)=R(T1+34)+R(T3+30)
    23360 T1 =T1+1
    23370 NEXT T3
    23380 NEXT T2
    23390 REM ADD IN THE RRIGIN
    23400 REM NOW TEST THAT MINIMUM VALUES ARE LESS THAN MAXIMUM VALUES.
    23410 FGR T1=1 TG 2
    23420 T2=T1+2
    23430 IF R(T1+34)<=R (T2+34) 60T0 23480
23440 T3=P(T2+34)
23450 P(T2+34)=R(T1+34)
23460 R(T1+34)=T3
23470 REM EXCHANGE MIN AND MAX.
23480 IF R(Tl+34)>=0 G@TB 23510
23490 R(TI+34)=0
23500 REM MAKE SURE MIN VALUE >= 0
23510 NEXT TI
23520 IF R(37)<=1023. G0T0 23550
23530 R(37) =1023.
23540 REM MAKE SURE XMAX <= 1023
23550 IF R(38)<=761. G9T0 23590
23560 R(38)=761.
23570 REM MAKE SURE YMAX <= 761
23580 REM NOW RECgMPUTE THE OLD OFF-SCREEN FLAG
23590 T1 =R (4)
23600 T2=R(5)
23610 REM FETCH LAST (X,Y) AND RECBMPUTE THE FLAG.
23620 T3=0
23030 IF Ti>=R(35) G0T自 23650
23640 T3=1
23650 IF R(37)>=T1 G0T0 23670
23660 T3=2
23670 IF T2>=R (36) GOT| 23690
23680 T3 =T3+4
23690 IF R(38)>=T2 GgT0 23710
23700 T3 =T3+8
23710 R(19)=T3
23720 REM SAUE THE GFF-SCREEN FLAG.
23730 F0R T1=1 Tg 4
23740 T2 =11+T1
23750 R(T2) =R (T1+34)
-23760 NEXT TI
23770 REM STORE WINDOW LIMITS BACK TO R ARRAY.
23780 RETURN
23790 REM
39000 REM
                                TEK003
39010 R9=67
-. 39020 T(67) =X1
39030 T(68) = X2
39040 T(69) =x3
39050 IF T(R9+2) =0 G0T0 39090
39060 R(51)=1000
39070 R(52) =1000
39080 IF T(R9+2)<0 G0T0 39270
39090 R(53) =INT(T(R9)/32)
39100 R(54) =INT (T (R9+1)/32)
39110 R(55)=T(R9)-R(53)*32+64
39120 R(56)=T(R9+1)-R(54)*32+96
39130 IF R(54) =F(52) G0T0 39180
39140 R(52)=R (54)
```

```
    39150 R(54)=R(54)+32
    39160 <1=P(54)
    39170 G0SUB 45000
    39180 <1=R(56)
    39190 G0SUB 45000
    39200 IF R(53) =P(51) G0T0 39250
    39210 R(51) =R(53)
    39220 R(53)=R(53)+32
    39230 <1=R(53)
    39240 G0SUB 45000
    392.50 <1=R (55)
    39260 G0SUB 45000
    39270 RETURN
    39280 PEM
    44000 REM TEK002
    44010 R=66
    44020 T(66) = X1
    44030 R!=R (2)
    44040 R2=R (3)
    44050 R3=R(16)
    44100 RO=0
    44110 R4=R(4)
    44120 R5=R (5)
    44:30 REM FETCH CURRENT WINDOW LIMITS
    44140 FOR RG=1 T0 4
    44150 R(R6+30) =R (R6+11)
    44160 NEXT RG
    44170 IF R1>=R(31) G0T0 44200
    4 4 1 8 0 ~ R O = 1
    44190 GET0 44220
44200 IF R(33)>=R1 G0T0 44220
44210 RO=2
44220 IF R2>=R (32) G0ID 44250
4 4 2 3 0 ~ R O = R ~ 0 + 4 ~
```



```
44250 IF R(34)>=R2 G0T0 44270
44260 RO=RO+8
44270 R.7=1NT(R(19))
44280 IF RO+R7=0 G0T0 44860
44290 R(35) =INT(R0/4)
44300 R(36)=INT(R7/4)
44310 R(37) =R 0-R(35)*4
44320 P(38)=R7-R(36)*4
44330 IF RO=0 GOTD 44390
44340 IF R7=0 G日T0 44390
44350 IF R(35)*R(36)=0 GRT0 44370
44360 IF R(35)-R(36)=0 GBT8 44950
44370 IF R(37)*R(38)=0 GOT0 44390
44380 IF R(37)-R(38)=0 GOT0 44950
44390 IF R(1)<=1 GET0 44420
44400 IF RO=0 GOT0 44860
44410 G8T0 44950
44420 R8=R1-R4
44430 IF R8=0 GRT0 44450
44440 R(81)=(R2-R 5)/R8
44450 IF R7=0 GOT0 44680
44460 IF R(36)=0 G8T0 44540
44470 R6=2*R(36)
44480 R3=R (R6+30)
44490 R6=R4
44500 IF R8=0 GDT0 44520
44510 R6=R 6+(R3-R 5)/R (81)
44520 IF R(33)<RG GBTG 44540
44530 IF RG> =R (31) GBTD 44600
44540 IF R(38)<=0 GBT0 44950
44550 R6=2*R(38)-1
```

```
    44560 R6=R(R6+30)
    44570 R3=R5+R(81)*(R5-R4)
        1 1 9
    44580 IF R(34)<R3 GDI0 44950
    44590 IF R3<P(32) G0ID 44950
```



```
    44610 P.5=R 3
    44620 X1=29
    44630 G0SUB 45000
    44640 XI=INT(R4)
    44650 X2=INT(R5)
    4 4 6 6 0 ~ X 3 = T ( R )
    44670 GBSUB 39000
    44680 IF PO=0 GBT0 44860
    44690 IF R(35)=0 G0T0 44770
    44700 R3=2*R(35)
    44710 R3=R (R3+30)
    44720 R6=R4
    44730 IF R&=0 G0I0 44750
    44740 R6=R6+(R3-R5)/R(81)
    44750 IF R(33)<R6 G3T0 44770
    44760 IF R6>-R(31) G偣 44830
    44770 IF R(37)<=0 GET0 44950
    44780 R6=2*R(37)-1
    44790 R6=R(R6+30)
    44800 R3=R 5+R(81)*(P6-R 4)
    44810 IF R(34)<P3 G0T0 44950
    44820 IF R3<P(32) G0TG 44950
    44830 X1=INT(R6)
    44840 X2=INT(R3)
    44850 G8T0 44880
    44860 X1=INT(RI)
    44870 X2=INT(R2)
    4 4 8 8 0 ~ I F ~ T ( R ) = 0 ~ G 0 T 0 ~ 4 4 9 3 0
4 4 8 9 0 ~ R ( 3 9 ) ~ = ~ X 1 ~
44900 Xi=29
44910 GBSUB 45000
4 4 9 2 0 ~ X 1 = R ( 3 9 ) ~
4 4 9 3 0 ~ X 3 = T ( R )
44940 GBSUB 39000
4 4 9 5 0 ~ R ( 4 ) = R . 1
44960 R(5)=R2
44970 R(19)=R0
4 4 9 8 0 ~ R E T U R N ~
```



```
4 5 0 0 0 ~ R E M ~ C H O U T
45010 R(90) =0
4 5 0 2 0 ~ R ( 9 1 ) = 1
45030 R(92) =I(63) = X1
45040 R(93)=INT(R(92)/8)
45050 R(90) =R (90)+(R(92)-R(93)*8)*R(91)
4 5 0 6 0 ~ I F ~ R ( 9 3 ) = 0 ~ G O T 0 ~ 4 5 1 0 0 ~
45070 R(92)=R(93)
45080 R(91) =R (91)*10
45090 GETG 45040
45100. AT THIS POINT R(90) =T@ AN OCTAL NUMBER I P PLACE
45110 ' IN THE QUTPUT STRING I$
4512.0 T$="@@@000"
45130 S$=STR(R(90))
45140 T$(8-LEN(S$))=S$(2,LEN(S$)-1)
45150 PRINT T$
45160 RETURN
READY
```


## APPENDIX B

This appendix contains the EZPLOT Users Manual which is currently in use by research scientists at Battelle-Northwest.

## EZPLOT

USERS IIAMUAL

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The best manual for EZPLOT is experience. The program is interactive and easy to use. Sit down at the terminal and make some graphs. You will learn about features that I haven't mentioned in this report; you may learn about features I didn't know I had built into the program.

I suggest you use this manual in two ways: first, read it through to get a general idea of how EZPLOT is used; second, keep it handy as a reference while you are using the program. I find that I forget details about the various options and their results. A quick look in the manual can save quite a bit of computer time.

Feel free to make suggestions about both the program and this users manual; they are dynamic research aids. I hope to continue improving EZPLOT to make it more responsive to your needs. Suggestions of new features and ways of improving old ones are always welcomed. EZPLOT is designed for you, not for me, so let me know how well it is meeting that goal.

Chuck Hatson

## LIST OF FICURES

1. CRT Display after User's Interactions with EZPLOT to Define Linear
Graph and Add Two Functions. . . . . . . . . . . . . . . . . . . . . . 1
2. Features of the Tektronix 4010 Keyboard. . . . . . . . . . . . . . . . . . . 4
3. Data File for Use by EZPLOT. . . . . . . . . . . . . . . . . . . . . . . . . 10
4. Editing Option to Display Data . . . . . . . . . . . . . . . . . . . . . . . 13
5. CRT Display after Editing to Change Plot Symbol of Second Set of Data. . . . 14
6. CRT Display after Selection of Automatic Scaling for a Linear Graph. . . . . 18
7. CRT Display after Input of User's Scale Factors for a Linear Graph . . . . . 18
8. CRT Display after Selection of Automatic Scaling for a Semi-Log Plot . . . . 19
9. CRI Display after Input of User's Scale Factors for a Semi-Log Plot. . . . . 21
10. CRT Display after Input of User's Scale Factors which are Smaller than
Range of Data on Semi-Log Plot . . . . . . . . . . . . . . . . . . . 21
11. CRT Display after Selection of Automatic Grid Feature. . . . . . . . . . . . 22
12. CRT Display after Input of User's Choice of Grid Line Locations. . . . . . . 23
13. CRT Display Illustrating Use of Grid Lines to Call Attention to Data

Feature. . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . 24
-1-

## IHTRODUCTION

This manual explains how to use EZPLOT, a BASIC computer program available on the UilIVAC 1108, to prepare graphs of your data. The program operates through Tektronix 4010 or 4002 cathode ray tube (CRT) computer teminals. Figure 1 (reduced in size for this publication), illustrates the quality of the graphs and demonstrates the optional feature of including functions as well as data. EZPLOT allowed the user to modify scale parameters and obtain the desired graph in a few minutes.


FIGURE 1. CRT Display after User's Interactions with EZPLOT to Define Linear
Graph and Add Two Functions.

EZPLOT is oriented toward the needs of scientific investigators. It serves tivo functions: it helps comunicate experimental results through visual display and it aids in the analysis of data through scale and axis transfomation. The main features and limitations of the program are:

- Dual modes

Data is easily entered via the terminal keyboard. Data files, stored in the user's. BASIC library, may also be used. In both cases, the total number of pairs of points cannot exceed. 200.

- Data editing routine

A simple procedure is included for editing data by deleting points, adding them, or changing values.

- Multiple data sets

Several sets of data may be plotted on a single set of axes, each identified by a different keyboard character.

- Transformation of axes

Either axis may be linear or logarithmic. An axis may be redefined and the data re-plotted within mirutes.

- Descriptive titles

Two alphanumeric lines (limited to 55 characters each) are displayed, one at the top and the other at the bottom of the graph.

- Optional grid

The user may select to have a grid superimposed on the graph.

- Functions

Up to 5 functions may be superimposed on the display. Functions such as $y=5 x^{2}+3 x+2$ or $y=27 e^{-1.4 x}+17.5 x$ which the user can express as BASIC statements are acceptable.

- Default mode

The user may elect to have the program select the scale factors for a quick display of the data.

## TEKTRONIX TERMINALS

Tektronix CRT terminals are very similar to teletype teminals with a CRT display added. Details of the operation of specific models. will be found in a manual located near the terminal. Some of the unusual keyboard features of the 4010 are illustrated in Figure 2.

Most Tektronix terminals have hard copy units a+tached. A copy of the display may be obtained by pressing the "MAKE COPY" button on either the keyboard or the hard copy unit. The copier should be allowed several minutes of warm-up before making a copy. Copy qual ity depends in part on the thermal history of the silver activated paper. It may also be altered by exposure to heat or strong light immediately after the copy anerges from the unit. A good procedure is to make Xerox reproductions as soon as practical after each session of terminal usage.

To increase the useful life of the CRT screen, the Tektronix terminal will automatically dim the display if there are no keyboard entries in a 90 second period. To re-activate the intensity of display without entering extraneous data to the computer, press the SHIFT key.

Information to be sent to the computer is stored in the temmal until the RETURIV key is depressed. If a mistake is made in entering a line of data, there are two methods of correcting it. Pressing the CONTROL and $X$ keys at the same time causes the entire line to be disregarded. Pressing the SHIFT and 0 keys causes a backspace so that the last character may be re-entered.


SIGN-OH PROCEDURE

To activate EZPLOT, the following steps should be followed:

1. Turn on power to terminal, hard copy unit, and acoustic coupler (terminal power switch is located on the pedestal near your right knee).
2. Clear the screen with the PAGE key.
3. Dial the number of the UNIVAC 1108. This phone number depends on the particular terminal location and should be posted near the phone.
4. When you hear the computer whistle, place the handset on the cradle of the acoustic coupler.
5. A greeting from the UNIVAC should appear at the upper left corner of the screen:

ON AT 14:15:59 30 SEP 73 SUIDAY RIG83J 067 ASSISTANCE: RUN **NEWS USER ID,PASSIORD,PROJECT ID-
6. Respond with: your USER ID (CUB \#), your PASSWORD (if any), and TO. The addition of the $T$ and zero to the normal sign on procedure tells the computer you are using a CRT. UNINTELLIGIBLE OUTPUT WILL RESULT if you omit these two letters.
7. The computer will respond with:
SYSTEM —
8. Respond by pressing three keys at once:

COITREL SHIFT D
9. The computer will respond with:

VERSION 14 OCT 71 20:07 ready
10. Enter: RUN *EZPLOT; then hit RETURN.

Successful complation of the sign-on procedure will result in a flash as the screen erases itself. The following greeting will appear at the upper left corner of the screen:

```
EZPIOT VERSION 2 5/3/73
FOP DEIAITS ABCUT ANY QUESTION ANSWER 0, OIHEPNISE ANSWER AL工 QUESTIONS WITH SINGIE DIGIT 1-9 INPUT TYPE?
```

Don't panic! This greeting serves three functions, telling you that:

- You have activated the correct BASIC program - EZPLOT.
- The primary mode of operation is numeric user responses. Zero will cause the display of the menu of options associated with a given question.
- The first question is: INPUT TYPE?

If you are familiar with EZPLOT you may have memorized each list of options or you may operate with this manual in hand. If you know the option you want, simply enter the option number and hit the RETURI key. If you are unsure of the option, entering zero will display the choices. If you are unsure what the options mean, the section of this manual, "Explanation of Questions", provides details about each choice.

The program operates by asking you a series of questions about your data. Then, it draws the graph you have specified. You may then change some of the specifications and obtain a new graph. The program asks these questions in a logical order, much as you would ask yourself questions before preparing a graph by traditional manual methods.

The first series of questions deal with defining the data that you wish to plot. Input may come from a file you have specially stored in the computer or you may enter the data points through the terminal keyboard.

The next logical thing to do is define the type of graph paper on which you wish to plot the data. Rather than choosing from various sized linear and logarithmic paper, you are allowed to define the way in which the computer treats the CRT screen.

You are also given great latitude in the choice of scale units for the two axes. Each will be given a number of "tic" marks according to your specifications. These marks will be clearly labeled on output. You may wish to see the graph with or without a grid superimposed on the data, so the program wi!? ask for your preference.

The final information needed to prepare your graph is descriptive labels for both the top and bottom of the graph.

Once you have selected all these parameters, the program will erase the screen and draw the graph. After giving you a chance to make a hard copy of the results, the program will allow you to re-enter the interactive phase of establishing parameters. This allows completion of several graphs of the same data.

## EXPLAMATION OF QUESTIOAIS

Each of the major questions asked by EZPLOT is associated with a list of logical options. The question, the options, and advice about the choices are presented on the following pages. It is a good procedure to have these pages available while using EZPLOT.

Some of the questions lead to conversational routines. These are (hopefully) self-explanatory and will not be discussed in detail here.

The sequence of questions depends on your responses. The order in which they appear in the following pages is typical of a session in which the user elects to use all of the features of EZPLOT. User response must always terminate with the RETURN key.

Users who are also BASIC programmers will appreciate the inclusion of program line numbers with each question. These line numbers may facilitate error recovery and/or allow a programer to modify EZPLOT. They are not needed in normal usage.

## QUESTION: INPUT TYPE?

LIME NUMBER: 230
MEIN: INPUT TYPE?O
(1) FIIE IIJ USERS LIBRARY
(2) WANT TO ENIER DATA FROM KEYBOARD
(3) FIIE AND WANT QUICK LOOK AT LITEAR GRAPH
(4) NO DATA, WANI TO DRAW FUICTIONS ONUY

INPUT TYPE?
ADVICE:

- Option 1 - This implies that you have prepared your data in the proper form and have saved it in a BASIC library file. Figure 3 illustrates the proper data format.
- Option 2 - This implies that you have the data in hand and are ready to enter it over the terminal. Be prepared to enter $X, Y$ pairs rather than a series of $X$ values and then a series of $Y$ values. Remember that numbers must be separated by either a space or a corma.
-Option 3 - This provides a quick look at the data previously stored in the user's library and is very useful in early stages of data analysis.
- Option 4 - To display functions only, you must also enter scale factors in a later question. Therefore, be sure that you choose a scale which will include the values of your function(s).


FIGURE 3. Data File for Use by EZPLOT

QUESTIOH: LIST ARD/OR EDIT DATA?

LINE NUHBER: 467

MEIV: LIST AND/OR EDIT DATA?O
$1=\mathrm{YES}, 2=\mathrm{NO}$
LIST AND/OR EDIT DATA?

ADVICE:

- Option 1 - This will lead you to the editing routine which is described later.
- Option 2 - If you skip editing or listing data at this point and you later see errors in the plot of the data, you may return to this question as one of the options to a later question: WHAT HEXT?
- Remember - Respond with a number, either 1 or 2. A response of YES or 110 results in a computer detected error condition.


## QUESTION: EDIT OPTION?

## LIHE RUMBER: 7990

MENU: EDIT OPTION?O
OPTIONS REASONS

1 DISPIAY DATA
2 CHANGE 1 OR MORE ITEMS
3 INSERT ITEMS
4 SWITCH A PAIR OF ITEMS
5 DELEIE AN ITEM
6 CHANGE PLDT SMMBOL FOR A SET
7 DATA OK, PROCEED
EDIT OPTION?

## ADVICE:

- Option 1 - It is almost essential that you display the data at least once if you plan to edit it. The editing depends on item numbers assigned to the pairs of points as shown in Figure 4.
- Options 2 through 6 - These lead you to interactive routines in which you will be asked which items to change, switch, delete, etc. After completing the data changes, these editing options return to the question EDIT OPTION? It is a good idea to respond with 1 to see if the edited data is correct.
- Option 6 - This option is illustrated in Figure 5 where plot symbols are changed to display the data points connected by line segments rather than as individual symbols.
- Option 7 - This returns you to the main sequence of questions. You may re-enter the editing sequence later as option 4 of the question HHAT NEXT?

The following is an example of the display generated by option 1 . Subsequent editing depends on the item numbers. For example, the first pair of points in the second data set must be referred to as item 22.

YOUR DATA IS:


FIGURE 4. Example of Editing Option to Display Data

The example below illustrates a change from the plot symbol $x$ to the special plot symbol -. The program will connect your data points when the plot symbol is a dash (-). In that case, the results will look funny if the data is not ordered properly, because data is not sorted by EZPLOT.

```
EDIT OPTION?6
SYM
FIRST ITEM NUMBER?22
LAST ITEA MMBER?41
ENIER NEN SYMBOL? -
EDIT OPTION? 7
```

Further interactions resulted in Figure 5.


FIGURE 5. CRT Display after Editing to Change Plot Symbol of Second Set of Data.

QUESTIOH: TYPE OF GRAPH?
LIHE NUMBER: 800
MEIU: TYPE OF GRAPH?O
$1=\operatorname{LINEAR}$
$2=$ LOG Y VS LINEAR X
3 = LINEAR Y VS LOG X
$4=\operatorname{LOG} Y$ VS LOG X
TYPE OF GRAPH?
ADVICE:

- Option 1 - Figure 1 used this option.
- Log Scales (Options 2, 3, or 4) - The program uses log to the base

10. Any data items less than or equal to zero will be ignored. You will get a message to this effect prior to the drawing of the graph, but the graph itself will show no trace of such out-of-range data.

- Option 3 - Figures 9 and 10 used this option.
- General - This question is a powerful tool in the analysis of data. Use it freely to explore alternate ways of displaying graphs of the data. After display of one type of graph, you may return to this question with option 2 of the question, WHAT NEXT?


## QUESTIOH: AUTO SCALE?

LIME NUMBER: 1270
MEHU: AUTO SCALE?O
$1=$ AUTOMATIC SCALE TO FIT DATA
$2=$ USER WILL SUPPLY SCALE FACTORS
AUIO SCALE?
ADVICE:

- Option 1 - The program will adjust the scale of the graph to fit your data by setting the endpoints of each axis to the minima and maxima of your data. The axes will be subdivided into ten equal parts. Usually the results are not pleasing to the eye although they are mathematically correct. For example, if the range of the data is from 1 to 10 , the "tic" marks on the axis will be located at 1.0, 1.9, 2.8, 3.6, 4.5 , etc. Figure 6 illustrates automatic scaling of a innear graph. Automatic scaĩing of iog piots is discussed on page 19.
- Option 2 - User supplied scale factors give nicer looking results (Compare the example of automatic scaling in Figure 6 with the user supplied scale in Figure 7.), but requires more time by the user. In general, use auto scale in analysis of data and use your own scale factors when preparing graphs to communicate results to others.

The following example illustrates the interactions between the program and the user in defining the scale factors for one axis of the graph (user responses underlined).

X-AXIS:

|  | MIN X | MAX X |
| :---: | :---: | :---: |
| DATA | 5 | 100 |
| AXIS | 0 | 0 |

MINIMUM VALUE-? 0
MAXIMMM VALUE-? 100
X-AXIS GOES FROM 0 TO 100
WITHIN THIS RANGE OF 100 UNITS
HOW MANY UNIIS DO YOU WRNT BETTEEE TIC MARKS?5
THAT WIIL MEAN 20 TIC MARKS ON THE AXIS
LABEL FACTOR?2
After setting the endpoints at zero and 100, the user specified that at every 5 units there would be a tic mark. The last question, $\operatorname{LABEL}$ FACTOR?, allows the user to choose which of the tic marks will be labeled. In this case the user asked that every other tic be labeled.

```
Y-AXIS:
```


## MIN Y <br> MAX Y

DATA
0 69.2

AXIS
0 0

MINIMIM VALUE? 0
MAUTMUM VALUE? 75
Y AXIS GOES FROM 0 TO 75
WITHIN THIS RANGE OF 75 UNITS
HON MAITY UNIITS DO YOU WANI BEINEEN TIC MARKS? 5
THAT WIIL MEAN 15 TIC MARKS ON THE AXIS
IABEL FACTOR?5

The result of these selections is shown in Figure 7 and is to be compared with Figure 6.
-18-



FIGURE 6. CRT Display after selection of Automatic Scaling for a Linear Graph.


FIGURE 7. CRT Display after Input of User's Scale Factors for a Linear Graph.

- Option 1 with LOG SCALES - The logic for automatic scaling of $\log$ axes is the same as that for linear ones. As shown in Figure 8, this results in plots which are mathematically correct, although the axis divisions are uncoriventional
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FIGURE 8. CRT Display after Selection of Automatic Scaling for a Semi-Log Plot.

- Option 2 with LOG SCALES - The procedure for scaling log axes is different than that for linear ones. You witil be asked for the location of each tic mark along the axis. To place these properly, think of the axes in terms of decades. For example, if the endpoints are at 1 and 100 you have 2 decades. In that case, the tics would look appropriate at $2,4,5,8,10,20,40,60$, and 80 .

Remember that the axis cannot include zero or negative values on a log scale.

An example of user supplied scaling factors for a $\log$ axis follows.

X-AXIS:
MIN X MAX X
DATA
AXIS
5
100

MINIMCM VALUE-?5
MAXIMLM VALUE-? 100
X-AXIS GOES FROM 5 TO 100
IN ADDITION TO THESE THO ENDPOINTS
How MANY OTHER TIC MARKS ARE WANTED (MAX. 10)?6
X VALUE FOR TIC 1?7.5
X VALUE FOR TIC 2 ? 10
X VALUE FOR TIC $3 ? 20$
X VALUE FOR TIC 4340
$X$ VALUE FOR TIC $5 ? 60$
X VALUE FOR TIC 6?80
The resulting graph is shown in Figure 9. Figure 10 is an example of a semi-log scale which is smaller than the data range. The user elected to restrict the x -axis to run from 10 to 100. The excluded data points (at $X=5$ ) are shown on the left margin of the screen.
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FIGURE 9. CRT Display after Input of User's Scale Factors for a Semi-Log Plot.
hipotheticgl data to illustrate ezplot

example of schle shaller thait railge of oafhe
FIGURI 10. CAT Disphay after Input of User's Scale ranctors which are maller than Range of Data on Scmi-log plot.

## QUESTION: GRID?

## LINE NUMBER: 2621

MENU:
GRID?O
$1=$ AUTOMATIC GRID AT EACH TIC
$2=$ NO GRDD AT ALL
3 = USER WILL SUPPLY GRID LOCATIONS
GRID?

## ADVICE:

- Option 1 - Try to visualize how the graph will look with grid lines at each tic location. Remember that the program has no control over the intensity of the image on the screen. If there are more than a few tic marks, a graph with full grid usually obscures the data.
hifothetical. oata to illusteate ezflot
75

59

25

0


FIGURE 11. CRT Display after Selection of Automatic Grid Feature.

- Option 2 - Most of the time you will elect to skip the grid feature. To locate specific data points it is usually possible to use a straight edge with reasonable accuracy.
-Option 3 - As shown in Figure 12, user selected grids are often useful enhancements to the graph. You will supply each location, for example, in Figure 12 horizontal grid lines were requested at $y=25$ and $y=50$ and vertical lines at $x=20, x=40, x=60$ and $x=80$.
hypothetichl uhta to illustrate ezplot


FIGURE 12. CRT Display after Input of User's Choice of Grid Line Locations.

- Alternate uses of grid - The grid option 3 allows you to do things not usually associated with a grid. For example, if your $\gamma$-axis runs from -10 to +10 , you might want a horizontal line across the graph at $Y=0$. This is easy under option 3; simply ask for one horizontal grid line $\gamma=0$.

Another use of the grid feature is to highlight interesting aspects of your data. For example, you may wish to call attention to the intersection of two curves by using a pair of grid lines which also intersect there as shown in Figure 13.


FIGURE 13. CRT Display Illustrating Use of Grid Lines to Call Attention to Data Feature.

QUESTION: TOP TITLE OK?
LINE NUMBER: 2630
MEINU: TOP TITLE OK?O
YOU MAY:
(1) HAVE:*** YOUR PREVIOUSLY ENTEPED TIITE GIIL PRINT HERE *** DISPIAYED AT TOP OF GRAPH
OR
(2) ENTER A NEW TITLE FOR THE TOP OF THE GRAPH TOP TITILE OK?

ADVICE:

- General - The choice of wording of the top title is up to the user. Most people make the top line a general description of the data, using the bottom line to identify the variables.
- Option 2 - If you decide to re-enter the top title, the program will solicit your new title, then ask again TOP TITLE OK?. It is good practice to respond with zero so that the program will display the linc you have just entered. This will heip avoid misspellings or lines that were too long to fit on the graph.


## QUESTION: BOTTOM LIME OK?

LIAIE NUMBER: 2990
MENU: BOTTOM LINE OK?O
ARE YOU:
(1) SATISFIED WITH:*** YOUR PREvIOUSLY ENTERED LINE WILL PRINT HERE ***
OR DO YOU
(2) WANL A DIFFERENT BOTTOA LINE BOTTOM LINE OK?

ADVICE:

- General - Most investigators use the bottom line to identify the axes units. For example:

UPTAKE (IN MG PER L) VS TIME (IN HOURS)

- Option 2 - As with the top title, it is a good practice to ask the program to display your ne:l bottom line by responding with zero when it asks BOTTOM LIAE OK? after you entered the new bottom line.


## QUESTIOH: WHAT HEXT?

LINE RUMBER: 4180
MENU: WHAT NEXT?O
$1=$ PLOT DATA AS IT IS
$2=$ CHANGE TYPE OF GRAPH
$3=$ Chavge scale
$4=\operatorname{EDIT}$ DASA
$5=\mathrm{ADD}$ FUNCTIONS
$6=$ GET NEN DATA FILE
7 = QUIT
WHAT NEXT?
ADVICE:

- Option 1 - The screen will erase, and your graph will be drawn. At the conclusion of the drawing, two question marks will appear at the upper left corner of the screen. The display will then remain on the screen until you hit the RETURIN key. Then the screen will erase and you will be asked WHAT MEXT?
- Option 2 - This takes you back to the question TYPE OF GPAPH?
- Option 3 - This takes you back to the question AUTO SCALE?
- Option 4 - This will take you to the question EDIT OPTIOH? After editing the data you will be asked UHAT NEXT? so that you do not have to re-set the scale parameters.
- Option 5 - This will lead to an interactive routine in which you are invited to interrupt program execution to add as many as 5 functions. The program will return to UHAT HEXT?

Two functions were added to the program to produce the graph shown in Figure 1. The follo:1ing example illustrates how two such functions can be added. For help in expressing your functions in BASIC consult the CSC BASIC REFERENCE MANUAL or find a BASIC programmer who can help you.

YOU HUST EHTER YOUR FUHCTIONS AS BASIC STATEHENTS ENTER THE NUHBER OF FUNCTIOIIS YOU :IISH TO DISPLAY (LIMIT 5)?2
IISSERT FUIICTIOAS AT 4950, 4970, 4990, 5010, 5030
EXAMPLE: 4950 Y $=\operatorname{SIN}(X)$
TO SEE THE RESULTS, TYPE "GO TO 9600" HIT COHTROL-SHIFT-K HOW:?!

ATTENTION READY
$4950 Y=(\operatorname{SQRT}(2 * x / 5)) * 2$
$4970 Y=4.56 * \operatorname{EXP}(1.223 * X)-7.5 E-4 * X+0.003429$
GO TO 9600
When the user enters COMTROL-SHIFT-K the program EZPLOT is inoperative. Control is returned to the BASIC system. This allows the user to insert BASIC statements at the correct locations. Upon return to EZPLOT (via GO TO 9600) the functions may be dravn.

The logic for drawing functions is to step across the screen with increasing values of $X$. This means that functions such as the equation of a circle are not valid for EZPLOT.



- Option 6 - This will go back to INPUT TYPE? All parameters will be cleared and you will be asked all questions over again.


## III CASE OF ERROR

Suppose that you make a mistake in entering your response. Even though you are not a computer programmer, a few simple rules will enable you to recover from error conditions without the loss of previously entered information. Three types of mistakes are common; each has an associated error recovery technique.

1) Error detected before RETURN key is depressed

Simultaneous pressing of the SHIFT and 0 (letter 0 ) keys results in a backspace, allowing entry of the correct response. Underlined characters (-) will appear on the screen to indicate a logical backspace each time the SHIFT/O key is depressed.

Simultaneously pressing the CONTROL and $X$ keys causes the entire line of information to be deleted, allowing re~entry of the correct information. The word DELETED will appear followed by a line feed to indicate that the computer is ready for the new line.
2) Error detected after RETURN key is depressed

You may proceed but will obtain a display that is not correct. At that point EZPLOT allows you to change parameters and obtain a modified graph. This method wastes time but is simple.

A more economical method is based on interrupting execution of the program and directing it to ask the question again. Each step of the program has a unique line number. Line numbers of the menu selecting questions are listed in the Summary section of this manual.

To interrupt the program, enter CONTROL-SHIFT-Z. The computer will respond with: READY To direct the program to repeat the question, enter:

GO TO line number; then hit RETURII.

CAUTION: Do not use this method of error correction unless you detect the error immediately after it is made. Strange things may havpen if you attempt to skip back several questions.
3) Error detected by the computer

Errors such as entry of alphabetic information when the computer expects a number result in interruption of program execution. The computer will display a message of some sort, followed by READY-
At this point you may enter GO TO line number to cause the question to be repeated.

Another procedure is to enter the word:
continue
This will cause the last line prior to the error to be repeated. Usually this will result in the display of a solitary question mark. Respond as if the previous question had been repeated.
Sometimes the computer itself makes mistakes. These usually appear as strange strings of characters in the middle of your graph. The problem is most often in telephone transmission of information from the computer to your remote terminal. Try to have the graph re-displayed. If it is still faulty, try the entire procedure over again, including hanging up and re-dialing the computer.

If things get too bad, it is possible to terminate a computer session any time the READY- condition exists. To terminate, respond with OFF.

## SIGH-OFF PROCEDURE

To terminate a computer session, the following steps should be followed:

1. Type OFF when the Univac says READY-.
2. Erase the screen with the PAGE key.
3. Turn off power to: Teminal

Hard Copy Unit
Acoustic Coupler
4. Hang up the telephone.
5. Place bad copies in waste basket; take good ones with you.

## SUMMARY OF OUESTIONS

In summary, the EZPLOT BASIC computer program can be operated by responding to a series of questions about your data. The following is a guide to the major questions asked by EZPLOT.

| Line Number | Question | Options |
| :---: | :---: | :---: |
| 230 | INPUT TYPE? | 1 File <br> 2 Keyboard <br> 3 File \& Quick Linear <br> 4 Functions Only |
| 461 | LIST AND?OR EDIT DATA? | $\begin{array}{ll} 1 & \text { Yes } \\ 2 & \text { No } \end{array}$ |
| 7990 | EDIT OPTION? | $\begin{array}{ll}1 & \text { Display Data } \\ 2 & \text { Change Data } \\ 3 & \text { Insert } \\ 4 & \text { Switch } \\ 5 & \text { Delete } \\ 6 & \text { Symbol Change }\end{array}$ |
| 800 | TYPE OF GRAPH? | ```1 Linear 2 Log Y Linear X 3 Linear Y Log X 4 Log Y Log X``` |
| 1270 | AUTO SCALE? | 1 Yes, Automatic Scale <br> 2 User Supplied Scale |
| 2621 | GRID? | 1 Automatic Grid <br> 2 Ho Grid <br> 3 User Supplied Grid |
| 2630 | TOP TITLE OK? | $\begin{array}{ll} 1 & \text { Yes } \\ 2 & \mathrm{Ho} \end{array}$ |
| 2990 | BOTTOM LIHE OK? | $\begin{array}{ll} 1 & \text { Yes } \\ 2 & \mathrm{No} \end{array}$ |
| 4180 | WHAT MEXT? | 1 Plot <br> 2 Change Type <br> 3 Change Scale <br> 4 Edit <br> 5 Add Functions <br> 6 New Data <br> 7 Quit |


[^0]:    $\overline{1}$ For a comprehensive machine by machine review of this type of plotter see: Auerbach on Digital Plotters and Image Digitizers; Auerbach Publishers, Princeton, l972.

[^1]:    *These systems can be used to preview displays to be drawn off-line on an incremental plotter.

[^2]:    5 Unpublished information from Larry Gannon, Computer Sciences Corp., Richland, Washington.

[^3]:    INFONET, an expanded version of CSCX, uses several UNIVAC $l l 08$ computers. It is available through Computer Sciences Corporation, Los Angeles, California.

