# SKYLINE ANALYSIS WITH LOG DRAG 

by

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## LEGEND OF TERMS

A = Choker angle
$B \quad=$ Angle between $\log$ and ground
$B_{1}=$ Angle between $\log$ and ground
$C \quad=$ Clearance between the top of the front end of the $\log$ and the ground
$C_{1}=$ Clearance between the carriage and the ground
$C_{2}=$ Carriage type
$C_{5}=$ Previous $C_{6}$
$C_{6}=$ Fraction of $W_{4}$ in $V_{4}$
$C_{7}=$ Fraction of $W_{4}$ in $\mathrm{H}_{4}$
$C_{8}=$ Fractional distance from the end of $\log$ to the center of gravity
$D()=$ Array of horizontal distances from the headspar to the carriage
D = Horizontal distance from the headspar to the carriage
$D_{1}=$ Horizontal distance from the carriage to the end of the log
$D_{2}=X$ coordinate of carriage with the end of the log at $X(I+1)$
$D_{3}=\begin{gathered}\text { Distance from the end of the } \\ \text { attached }\end{gathered}$
$D_{5}=$ Horizontal distance from the end of the $\log$ to the front of the log
$\mathrm{E}=$ Constant in the elliptical path equation
$E_{3}=$ Previous value of $T$
$E_{4}=$ Current value of $T$
$E_{5}=$ Reciprical of the fractional distance from the center of gravity of the log to the point of choker attachment divided by the distance from the end of the log to the point of choker attachment
$F=$ Number of terms in the $D(), P(), S()$, and $V()$ arrays
$F_{1}=$ File yarder is to be loaded from
$F_{3}=$ Previous value of the function
$F_{4}=$ Current value of the function
$G_{1}=$ Minimum $Y$ coordinate
$G_{2} \quad=$ Maximum $Y$ coordinate
$G_{3}=$ Maximum difference in values of the $X$ coordinates
$G_{4}=X$ graph limit for plotting profiles
$\mathrm{G}_{5}=\mathrm{Y}$ graph limit for plotting profiles
$G_{6}=X$ offset for plotting profiles
$G_{7}=Y$ offset for plotting profiles
H = Vertical distance from the top of the tailspar to the top of the headspar
$H_{1}=$ Horizontal component of the force in line 1 at the carriage
$H_{2}=$ Horizontal component of the force in line 2 at the carriage
$H_{3}=$ Horizontal component of the force in line 3 at the carriage
$H_{4}=$ Horizontal component of the force in the choker at the carriage
$H_{6}=$ Headspar height
$H_{7}=$ Tailspar height
I $=$ Terrain point number
$\mathrm{I}_{1} \quad=$ Input control parameter
$I_{5}=$ Integer value of headspar terrain point plus 1
$I_{6} \quad=$ Integer value of tailspar terrain point
K = Constant
$\mathrm{K}_{1} \quad=$ Constant which equals $Y / D$
$\mathrm{K}_{2}=$ Constant which equals (Y-H)/(L-D)
$\mathrm{K}_{7}=$ Constant
$K_{8}=$ Constant
$\mathrm{L} \quad=$ Span length which equals the horizontal distance from the headspar to the tailspar

```
\(\mathrm{L}_{1}=\) Length of choker from the carriage to the top of the \(\log\)
\(L_{2}=\) Distance from the choker to the end of the \(\log\)
\(L_{3}=\) Length of the \(\log\)
\(L_{4}=\) Distance from point of choker attachment to ground below the end
        of the log
\(L_{5}=\) Required rigging length
M = Constant
\(M_{1}=\) Constant
\(M_{2}=\) Constant
\(M_{3}=\) Constant
\(M_{4}=\) Constant
\(\mathrm{N}=\) Constant
\(N_{1}=\) Number of terrain points
\(N_{5}=\) Plot parameter which causes the \(\log\) to be plotted every third point
\(0=\) Constant
\(P(\) ) = Array of slope angles
P = Slope angle
\(P_{1} \quad=\) Profile number and file profile is stored in
\(P_{5}=\) Profile plot parameter
\(R \quad=\) Type of skyline
\(R_{1}=\) Total weight in line 1
\(R_{2}=\) Total weight in line 2
\(R_{3}=\) Total weight in line 3
\(R_{4}=\) Running skyline parameter
\(R_{5}=R c / R m\)
\(R_{6}=R s / R m\)
\(R_{c} \quad=\) Distance from the center of the drum in the carriage to the dropline
```

$R_{m}=$ Distance from the center of the drum in the carriage to the mainline
$R_{s}=$ Distance from the center of the drum in the carriage to the slackline
$S($ ) = Array of terrain points
$S_{1}=$ Headspar terrain point
$S_{2}=$ Tailspar terrain point
$S_{3}=$ Terrain point of inner yarding limit
$S_{4}=$ Terrain point of outer yarding limit
$S_{5}=$ Terrain point step size
$S_{6}=$ Terrain point step size
$S_{7}=$ Step size between terrain points
$\mathrm{S}_{8} \quad=$ Step size between terrain points
$S_{9}=$ Terrain point number
T = Allowable haulback plus slackline tension
$T_{0}=$ Allowable slackline tension
$T_{1}=$ Maximum allowable skyline tension
$\mathrm{T}_{2}=$ Maximum allowable haulback tension
$T_{3}=$ Maximum allowable mainline tension
$\mathrm{T}_{6}=$ Tension in lines 1 and 2 at the carriage
$T_{7}=$ Tension at the headspar in line 1
$\mathrm{T}_{8}=$ Tension at the headspar in line 3
$T_{9}=$ Tension in the mainline plus the slackline at the carriage
$T_{m}=$ Tension in the mainline at the carriage
$\mathrm{T}_{\text {ma }}=$ Tension in the mainline at the headspar
$\mathrm{T}_{\mathrm{c}}=$ Tension in the choker at the carriage
$\mathrm{T}_{\mathrm{s}}=$ Tension in the slackline at the carriage
$U=$ Coefficient of friction between the $\log$ and the ground
$U_{4}=$ Minimum line length
$U_{5} \quad=$ Line length
$V()=A r r a y$ of the ground elevations below the carriage
$V_{1}=$ Vertical component of the force in line 1 at the carriage
$V_{2}=$ Vertical component of the force in line 2 at the carriage
$V_{3}=$ Vertical component of the force in line 3 at the carriage
$V_{4}=$ Vertical component of the force in the choker
W = Haulback plus the slackline weight per foot
$W_{0} \quad=$ Slackline weight per foot
$W_{1} \quad=$ Skyline weight per foot
$W_{2} \quad$ Haulback weight per foot
$W_{3}=$ Mainline weight per foot
$W_{4} \quad$ Maximum log weight
$W_{5}=$ Carriage weight
$W_{7} \quad=$ Maximum $\log$ weight with the skyline or haulback being limiting
$W_{8} \quad=$ Maximum log weight with the mainline being limited
$X()=$ Array of $X$ coordinates
$X_{1}=X$ coordinate of the top of the headspar
$X_{2}=X$ coordinate of the top of the tailspar
$X_{3}=X$ coordinate of the bottom of the headspar.
$X_{4}=X$ coordinate of the bottom of the tailspar
$X_{5}=X$ coordinate of the inner yarding limit
$X_{6}=X$ coordinate of the outer yarding limit
$x_{7}=X$ coordinate of the end of the log
$X_{8}=X$ coordinate of the carriage
$x_{9}=X$ coordinate of the ground below the carriage
$Y()=$ Vertical distance from the top of the headspar to the carriage
$\gamma_{1}=Y$ coordinate of the top of the headspar
$Y_{2}=Y$ coordinate of the top of the tailspar
$Y_{3}=Y$ coordinate of the bottom of the headspar
$Y_{4}=Y$ coordinate of the bottom of the tailspar
$Y_{5}=Y$ coordinate of the inner yarding limit
$Y_{6}=Y$ coordinate of the outer yarding limit
$Y_{7}=Y$ coordinate of the end of the log
$Y_{8}=Y$ coordinate of the carriage
$Y_{9}=Y$ coordinate of the ground below the carriage
Y\$ = Yarder name
$Z()=$ Array of $X$ and $Y$ coordinates which are loaded from tape

## ABSTRACT

This paper describes a mathematical formulation and a computer program in basic language for analyzing the load carrying capacity of skyline systems using the effects of $\log$ drag. The actual $\log$ and ground geometry are used in the analysis of the payload capacities for standing, live and running skylines. The paper uses an example problem to show the effects of the various parameters used in computing payload capacity using the effects of $\log$ drag (choker length, $\log$ length, $\log$ to ground clearance, point of choker attachment, center of gravity of the log, coefficient of friction, and type of carriage).

The method described in this paper was compared with an existing method which calculates skyline payloads for a fully suspended load. It was found that when logs have one end suspension, there can be considerable difference in the payloads calculated by the two methods.

## INTRODUCTION

An important step in planning skyline logging systems is the determination of the load-carrying capacity of the skyline system while anchored in a specific geometry and operating over a specific terrain. Several methods are now available to determine the load-carrying capacity of this type of system: graphical-tabular handbook approaches and mathematical solutions using hand held, desk top, and large computer systems. However, until recently none of these systems took into account the effect of log drag and the effect of the actual log to ground geometry. Recently, Gary Falk (6) developed a series of HP 67 programs which consider the effect of the actual log to ground geometry.

Most of the methods currently used assume a fully suspended load. The Skyline Analysis Program on the HP 9830 assumes a fully suspended load and increases the net load by 50 percent for a dragging log.

The effects of the forces due to log drag on the skyline and mainline depend on the angle the log makes with the ground, length of the log, length of the choker, carriage clearance, ground slope, weight of the turn, log diameter, point of choker attachment and the coefficient of friction between the $\log$ and the ground. Carson (2) developed equations for using the effects of $\log$ drag in determining the load carrying capacity of running skylines. The equations developed by Carson determine the forces at the carriage for a given angle between the $\log$ and the ground. The equations cannot be applied directly to a standing skyline where the angle the log makes with the ground varies as the load is brought in.

With a standing skyline, the length of the skyline is fixed during the yarding cycle. The length of the skyline is often fixed at a length
such that the $\log$ will have at least one end suspended at all points. This is done to eliminate the soil displacement damage caused by the plowing of the front end of the log. Once the length of the skyline is fixed, the angle the log makes with the ground along the skyline road varies according to the ground slope, length of the log, length of the choker and carriage clearance.

Desk top computer systems, such as the HP 9830, HP 9845, and the Techtronics 4051, provide one of the easiest and fastest methods for entering profile data and determining the load carrying capacity of skylines. These systems have the ability to enter profile data from a digitizer, keyboard, files, X, Y coordinates, or slope, \% slope data. The profile data can be stored for later use, analyzed, and plotted with these systems.

This paper describes a mathematical formulation, a computer program written in basic placed on the HP 9830 and the effects of the various parameters in using log drag for determining the load carrying capacity of live, standing and running skylines.

## OBJECTIVES

The purpose of this study is to analyze the effects of using log drag for determining the load carrying capacity of live, running and standing skylines, and to develop a working mode1 on the HP 9830 for determining the payload capacity of these skyline systems with the effects of $\log$ drag included in the model. The specific objectives will be as follows:

1. Develop a computer program written in basic and placed on the HP 9830 which will determine the load carrying capacity for a live, standing, and running skyline system given; the allowable mainline tension, the allowable skyline tension, log to ground geometry, the $\log$ length, choker length, log to ground coefficient of friction, yarder specifications, ground profile and cable system geometry.
2. Determine individually the effects of the various parameters used in the model (choker length, log length, log to ground clearance, point of choker attachment, center of gravity of the log, coefficient of friction, and type of carriage), and their effect on the load carrying capacity, mainline tensions, and skyline tensions.
3. Compare the results obtained using the HP 9830 Skyline Analysis Program with the results from the Skyline Analysis Program with Drag developed in this paper.

## MATHEMATICAL FORMULATIONS

The symbols used in the following formulations are all described in the Legend of Terms. The terms used are all terms which could be programmed into the HP 9830 and the equations shown are the ones used in the computer programs.

## Log Drag for a Live and a Running Skyline

For the purposes of this paper a live skyline will be defined as a system having two lines; a skyline and a mainline, where the skyline length - is varied to maintain a constant $\log$ to ground clearance ( $C$ ) as shown in Figure (1). A running skyline is a system where the haulback line runs through a sheave in the carriage, through a block at the tailspar, and is then connected to the carriage. It has one or two additional lines, a mainline and a slackpulling line, which run from the headspar to the carriage. In a running skyline the haulback line length will vary to maintain a constant log to ground angle ( $\mathrm{B}_{j}$ ).


Figure 1. Log to Ground Geometry for a Running and a Live Skyline.

The following values are known:

$$
C, P, X(I), Y(I), X_{7}, Y Y_{7}, X(I+1), Y(I+1), L 3, L 2, E 5, L 1
$$

We want to find: $C_{6}, C_{7}, C_{1}, X_{8}, Y_{8}$

For the geometry shown in Figure 1, Carson (2) developed the following equations for determining the horizontal and vertical forces at the carriage due to a dragging log:

$$
\begin{align*}
& H_{4}=W_{4}(U \cos P+\sin P)\left(\frac{\cos \left(P+B_{1}\right) / E_{5}}{\cos B_{1}+U \sin B_{1}}\right)  \tag{1}\\
& V_{4}=W_{4}[1+(U \sin P-\cos P)]\left(\frac{\cos \left(P+B_{1}\right) / E_{5}}{\cos B_{1}+U \sin B_{1}}\right) \tag{2}
\end{align*}
$$

However, we wish to find $C_{6}, C_{7}, C_{1}, X_{8}, Y_{8}$ so let:

$$
\begin{align*}
& C_{7}=H_{4} / W_{4}  \tag{3}\\
& C_{6}=V_{4} / W_{4}  \tag{4}\\
& K=\cos (P+B) /\left[E_{5}\left(\cos \left(B_{1}\right)+U \sin \left(B_{1}\right)\right)\right] \tag{5}
\end{align*}
$$

Then:

$$
\begin{align*}
& P=\operatorname{Tan}^{-1}[(Y(I)-Y(I+1)] /[X(I+1)-X(I)]  \tag{6}\\
& B_{1}=\sin ^{-1}\left(C / L_{3}\right)  \tag{7}\\
& E_{5}=L_{2} /\left(L_{2}-L_{3} / 2\right)  \tag{8}\\
& C_{7}=[U \cos (P)+\sin (P)] K  \tag{9}\\
& C_{6}=[1+(U \sin (P)-\cos (P)] K  \tag{10}\\
& A=90-\tan ^{-1}\left(C_{7} / C_{6}\right)  \tag{1}\\
& X_{7}=X_{8}+L_{2} \cos \left(P+B_{1}\right)+L_{1} \cos (A)  \tag{12}\\
& Y_{8}=Y_{7}+L_{2} \sin \left(P+B_{1}\right)+L_{1} \sin (A)  \tag{13}\\
& Y_{9}=Y_{7}+\left(X_{2}-X_{7}\right) \sin (P)  \tag{14}\\
& C_{1}=Y_{8}-Y_{9} \tag{15}
\end{align*}
$$

With this set of equations the geometry and fraction of the log weight that is in the vertical and horizontal components of the choker at the carriage can be determined for a given log length, choker length, point of choker attachment, location of the center of gravity, and the ground slope.

## Log Orag for a Standing Skyline

For a standing skyline the log to ground clearance (C) is unknown, but the carriage clearance $C_{1}$ can be found from the elliptical load path equations, the skyline length, and the cable system and ground geometry. So, referring to Figure 1, we are given: $\mathrm{C}_{1}, \mathrm{P}, \mathrm{X}(\mathrm{I}), Y(\mathrm{I}), X(\mathrm{I}+1)$, $Y(I+1), X_{8}, Y, X_{9}, Y_{9}, L_{2}, L_{3}, E_{5}, L_{1}$.
We want to find: $C_{6}, C_{7}, B_{1}, A$
Referring to Figure 2:

$$
\begin{align*}
& C^{\prime}=C_{1}-L_{1} \sin (A)+L_{1} \cos (A) \tan (P)  \tag{16}\\
& A=90-\tan ^{-1}\left(C_{7} / C_{6}\right) \tag{17}
\end{align*}
$$

Then from the law of sines and Figure 2:

$$
\begin{equation*}
\frac{L_{2}}{\sin (90+P)}=\frac{c^{\prime}}{\sin \left(B_{1}\right)} \tag{18}
\end{equation*}
$$

Substituting in equation (16) and simplifying yields:

$$
\begin{equation*}
\frac{L_{2}}{\cos (P)}=\frac{C_{1}-L_{1} \sin (A)+L_{1} \cos (A) \tan (P)}{\sin \left(B_{1}\right)} \tag{19}
\end{equation*}
$$



Figure 2. Log Geometry for a Standing Skyline.

Solving for $B_{1}$ :

$$
\begin{equation*}
B_{1}=\sin ^{-1}\left[\frac{\cos (P)}{L_{2}}\left(C_{1}+L_{1}(\cos (A) \tan (P)-\sin (A))\right]\right. \tag{20}
\end{equation*}
$$

Now, the following equations can be used to solve for $B_{1}, C_{6}, C_{7}$ and $A$ :

$$
\begin{align*}
& B_{1}=\sin ^{-1}\left[\frac{\cos (P)}{L_{2}}\left(C_{1}+L_{1}(\cos (A) \tan (P)-\sin (A))\right]\right.  \tag{20}\\
& K=\cos \left(P+B_{1}\right) /\left(E_{5}\left(\cos \left(B_{1}\right)+U \sin \left(B_{1}\right)\right)\right)  \tag{5}\\
& C_{7}=(U \cos (P)+\sin (P)) K  \tag{9}\\
& C_{6}=(1+(U \sin (P)-\cos (P)) K  \tag{10}\\
& A=90-\tan ^{-1}\left(C_{7} / C_{6}\right) \tag{17}
\end{align*}
$$

To solve for $C_{6}$ and $C_{7}$ these equations are transcendental (cannot be manipulated algebraically for direct solution), so an iterative type solution is needed. First, for an initial guess of $B_{1}$ we can assume $L_{1}$
and $L_{2}$ are a straight line as shown in Figure 3.


Figure 3. Geometry for an initial guess of $B_{1}$.

Using the law of sines for the geometry of Figure 3, we obtain:

$$
\begin{align*}
& \frac{L_{1}+L_{2}}{\sin (90+P)}=\frac{C_{1}}{\sin \left(B_{1}\right)}  \tag{21}\\
& B_{1}=\sin ^{-1}\left[C_{1} \sin (90+P) /\left(L_{1}+L_{2}\right)\right] \tag{22}
\end{align*}
$$

The iterative procedure is to first use equation (22) to arrive at an initial guess of $B_{1}$. Then this value is used in equations (5), (9) and (10) to solve for $C_{7}$ and $C_{6}$. Using these values of $C_{6}$ and $C_{7}$, the value of $A$ can be found from equation (17). This value can then be used in equation (20) to solve for a new value of $B_{1}$.

Then the new value of $B_{1}$ can be used in equations (5), (9) and (10) to solve for $C_{7}$ and $C_{6}$. This process is then continued until the value of $C_{6}$ changes by less than 0.001 . This is not a conventional type iterative procedure, but for this problem it tends to converge very rapidly.

## Live and Standing Skyline Loads and Line Tensions

The following analysis uses a rigid link assumption for the lines, and neglects line stretch. Figure 4 below shows the cable system geometry for this problem.


Figure 4. Cable System Geometry.

Figure 5 shows the geometry and forces acting on each line segment for this problem.


Figure 5. Free Body Diagram for a Standing and Live Skyline.

For each line segment the moments can be taken about the upper end. Since the system is assumed to be in static equilbrium, there has to be a moment force balance for each line segment. The following three equations are then obtained:

$$
\begin{array}{ll}
\Sigma M_{A}=0 & V 1=H_{1}(Y / D)-R_{1} / 2 \\
\Sigma M_{B}=0 & V 2=H_{2}[(Y-H) / L-D]-R_{2} / 2 \\
\Sigma M_{A}=0 & V 3=H_{3}(Y / D)-R_{3} / 2 \tag{25}
\end{array}
$$

The carriage is also assumed to be in static equilbrium, so the horizontal and vertical forces at the carriage must balance. The equations for the carriage force balance are:

$$
\begin{array}{ll}
\Sigma F_{x}=0 & H_{3}=-H_{1}+H_{2}+H_{4} \\
\Sigma F_{y}=0 & V_{1}+V_{2}+V_{3}=W_{5}+V_{4} \tag{27}
\end{array}
$$

Let:

$$
\begin{align*}
& K_{1}=Y / D  \tag{28}\\
& K_{2}=(Y-H) /(L-D) \tag{29}
\end{align*}
$$

Substituting equations (23), (24), (25), (28), and (29) into equation (27):

$$
\begin{equation*}
\mathrm{H}_{1} \mathrm{~K}_{1}-\mathrm{R}_{1} / 2+\mathrm{H}_{2} \mathrm{~K}_{2}-\mathrm{R}_{2} / 2+\mathrm{H}_{3} \mathrm{~K}_{1}-\mathrm{R}_{3} / 2=\mathrm{W}_{5}+\mathrm{V}_{4} \tag{30}
\end{equation*}
$$

Now using equation (26) to substitute in for $\mathrm{H}_{3}$ :

$$
\begin{equation*}
\mathrm{H}_{1} \mathrm{~K}_{1}-\mathrm{R}_{1} / 2+\mathrm{H}_{2} \mathrm{~K}_{2}-\mathrm{R}_{2} / 2-\mathrm{H}_{1} \mathrm{~K}_{1}+\mathrm{H}_{2} \mathrm{~K}_{1}+\mathrm{H}_{4} \mathrm{~K}_{1}-\mathrm{R}_{3} / 2=\mathrm{W}_{5}+\mathrm{V}_{4} \tag{31}
\end{equation*}
$$

Reducing:

$$
\begin{equation*}
\mathrm{H}_{2}\left(\mathrm{~K}_{1}+\mathrm{K}_{2}\right)+\mathrm{H}_{4} \mathrm{~K}_{1}-\left(\mathrm{R}_{1}+\mathrm{R}_{2}+\mathrm{R}_{3}\right) / 2=\mathrm{W}_{5}+\mathrm{V}_{4} \tag{32}
\end{equation*}
$$

Solving for $H_{2}$ yields:

$$
\begin{equation*}
H_{2}=\frac{\left(R_{1}+R_{2}+R_{3}\right) / 2+W_{5}+V_{4}-H_{4} K_{1}}{K_{1}+K_{2}} \tag{33}
\end{equation*}
$$

In the above equations $R_{1}, R_{2}$ and $R_{3}$ are the forces due to the weight of the cable in each line segment. These forces can be found from the following equations:

$$
\begin{equation*}
R_{1}=W_{1} \sqrt{D^{2}+Y^{2}} \tag{34}
\end{equation*}
$$

$$
\begin{align*}
& R_{2}=W_{1} \sqrt{(L-D)^{2}+(Y-H)^{2}}  \tag{35}\\
& R_{3}=W_{3} \sqrt{D^{2}+Y^{2}} \tag{36}
\end{align*}
$$

The skyline passes under sheaves in the carriage. Assuming a frictionless sheave, when a line passes under a sheave, the tensions in the line on both sides of the sheave are equal. So for lines 1 and 2, the tension in the cables at the carriage are equal. From this relationship the following equations can be formulated:

$$
\begin{array}{lll}
T_{6}=\sqrt{V_{1}^{2}+H_{1}^{2}} & = & \sqrt{V_{2}^{2}+H_{2}^{2}} \\
T_{6}^{2}=V_{1}^{2}+H_{1}^{2} & \stackrel{\text { or }}{=} & V_{2}^{2}+H_{2}^{2} \tag{38}
\end{array}
$$

From equation (33) the value of $\mathrm{H}_{2}$ can be found and using the relationship between $H_{2}$ and $V_{2}$ from equation (24), the value of $T_{6}$ can be found from the following equation:

$$
\begin{equation*}
T_{6}=\sqrt{H_{2}^{2}+\left(H_{2} K_{2}-R_{2} / 2\right)^{2}} \tag{39}
\end{equation*}
$$

Reducing yeilds:

$$
\begin{equation*}
T_{6}=\sqrt{\mathrm{H}_{2}^{2}\left(1+\mathrm{K}_{2}^{2)}-\mathrm{R}_{2} \mathrm{H}_{2} \mathrm{~K}_{2}+\mathrm{R}_{2}^{2} / 4\right.} \tag{40}
\end{equation*}
$$

Once the value of $T_{6}$ is found the value of $H_{1}$ can be found by using equation (38) and the relationship between $V_{1}$ and $H_{1}$ from equation (23) as follows:

$$
\begin{equation*}
T_{6}^{2}=V_{1}^{2}+H_{1}^{2}=H_{1}^{2}+\left(H_{1} K_{1}-R_{1} / 2\right)^{2} \tag{41}
\end{equation*}
$$

Reducing yields:

$$
\begin{equation*}
\mathrm{H}_{1}^{2}\left(1+\mathrm{K}_{1}^{2}\right)-\mathrm{H}_{1} \mathrm{~K}_{1} \mathrm{R}_{1}+\mathrm{R}_{1}^{2} / 4-\mathrm{T}_{6}^{2}=0 \tag{42}
\end{equation*}
$$

Since $H_{1}$ is the only unknown in this equation, the solution can be found from the quadratic equation as follows:

Let:

$$
\begin{align*}
& M=1+K_{1}^{2}  \tag{43}\\
& N=-K_{1} R_{1}  \tag{44}\\
& 0=R_{1}^{2} / 4-T_{6}^{2} \tag{45}
\end{align*}
$$

Then :

$$
\begin{equation*}
H_{1}=\frac{-N+\sqrt{N^{2}-4 M O}}{2 M} \tag{46}
\end{equation*}
$$

The value of $\mathrm{H}_{4}$ can be found from the $\log$ drag equations and the values of $H_{1}$ and $H_{2}$ can be found from the previously formulated equations. Once these values are found the value of $\mathrm{H}_{3}$ can be found from equation (26).

Now the tension in the lines 1 and 3 at the headspar can be found using equations (23), (25), (28), and (29) as follows:

$$
\begin{array}{ll}
T_{6}=\sqrt{V_{1}^{2}+H_{1}^{2}} & =\sqrt{\left(H_{1} K_{1}-R_{1} / 2\right)^{2}+H_{1}^{2}} \\
T_{M}=\sqrt{V_{3}^{2}+H_{3}^{2}} & =\sqrt{\left(H_{3} K_{1}-R_{3} / 2\right)^{2}+H_{3}^{2}} \tag{49}
\end{array}
$$

Then:

$$
\begin{align*}
& T_{7}=T_{6}+W_{1} Y=\sqrt{\left(H_{1} K_{1}-R_{1} / 2\right)^{2}+H_{1}^{2}}+W_{1} Y  \tag{50}\\
& T_{8}=T_{M}+W_{3} Y=\sqrt{\left(H_{3} K_{1}-R_{3} / 2\right)^{2}+H_{3}^{2}}+W_{3} Y \tag{51}
\end{align*}
$$

The relationships $T_{7}=T_{6}+W_{1} Y$ and $T_{8}=T_{M}+W_{3} Y$ are from the
catenary equation. This is one of the more simple and easy to use relationships from the catenary equations. This relationship will be used to convert tensions from the carriage to the headspar and from the headspar to the carriage. It will be used to convert the magnitude of the force, and the rigid link equations will be used to determine the direction of the force.

The previously formulated equations assumed the log weight was known. If the $\log$ weight is known, then from the previously formulated equations the mainline and skyline tensions can be found. However, it is useful to know what log weight will cause the mainline or skyline to be at its maximum allowable tension.

The following analysis is a method of determining the maximum allowable load which will cause the skyline to be at its maximum allowable tension.

First, assuming the skyline is at its maximum allowable load, then the value of $\mathrm{H}_{2}$ can be found using equation (24) in the following analysis:

$$
\begin{align*}
& T_{6}=T_{1}-W_{1} Y  \tag{53}\\
& T_{6}^{2}=H_{2}^{2}+V_{2}^{2}=H_{2}^{2}+\left(H_{2} K_{2}-R_{2} / 2\right)^{2}=\left(T_{1}-W_{1} Y\right)^{2} \tag{54}
\end{align*}
$$

Reducing yields:

$$
\begin{equation*}
H_{2}^{2}\left(1+K_{2}^{2}\right)-H_{2} K_{2} R_{2}+R_{2}^{2} / 4-\left(T_{1}-W_{1} Y\right)^{2}=0 \tag{55}
\end{equation*}
$$

To solve for $\mathrm{H}_{2}$ the quadratic equation must be used as follows:
Let:

$$
\begin{align*}
& M=1+K_{2}^{2}  \tag{56}\\
& N=-K_{2} R_{2}  \tag{57}\\
& O=R_{2}^{2} / 4-\left(T_{1}-W_{1} Y\right)^{2} \tag{58}
\end{align*}
$$

Then:

$$
\begin{equation*}
H_{2}=\frac{-N+\sqrt{N^{2}-4 M O}}{2 M} \tag{59}
\end{equation*}
$$

If the value of $\mathrm{H}_{2}$ is known, equations (3) and (4) can be used to substitute for the value of $H_{4}$ and $V_{4}$ in equation (33) and then the value of $W_{7}$ can be solved for in equation (33) as follows:

$$
\begin{equation*}
H_{2}=\frac{\left(R_{1}+R_{2}+R_{3}\right) / 2+W_{5}+C_{6} W_{7}-C_{7} W_{7} K_{1}}{K_{1}+K_{2}} \tag{60}
\end{equation*}
$$

Solving for $W_{7}$ yields:

$$
\begin{equation*}
W_{7}=\frac{H_{2}\left(K_{2}+K_{1}\right)-W_{5}-\left(R_{1}+R_{2}+R_{3}\right) / 2}{\left(C_{6}-C_{7} K_{1}\right)} \tag{61}
\end{equation*}
$$

With the above equations, the log weight can be found which causes the skyline to be at its maximum allowable tension. However, in some cases the mainline will be the limiting factor in determining the maximum log weight. The following analysis is a method of determing the log weight which will cause the mainline to be at its maximum allowable load.

From equation (26):

$$
\begin{align*}
& \mathrm{H}_{1}=\mathrm{H}_{2}-\mathrm{H}_{3}+\mathrm{H}_{4}  \tag{62}\\
& \mathrm{H}_{1}^{2}=\mathrm{H}_{2}^{2}+\mathrm{H}_{3}^{2}+\mathrm{H}_{4}^{2}-2 \mathrm{H}_{4} \mathrm{H}_{3}+2 \mathrm{H}_{4} \mathrm{H}_{2}-2 \mathrm{H}_{3} \mathrm{H}_{2} \tag{63}
\end{align*}
$$

Then from equations (38), (23) and (24):

$$
\begin{equation*}
\mathrm{V}_{1}^{2}+\mathrm{H}_{1}^{2}=\mathrm{V}_{2}^{2}+\mathrm{H}_{2}^{2} \tag{64}
\end{equation*}
$$

$$
\begin{align*}
& \left(H_{1} K_{1}-R_{1} / 2\right)^{2}+H_{1}^{2}=\left(H_{2} K_{2}-R_{2} / 2\right)^{2}+H_{2}^{2}  \tag{65}\\
& H_{1}^{2}\left(1+K_{1}^{2}\right)-H_{1} K_{1} R_{1}+\left(R_{1}^{2}-R_{2}^{2}\right) / 4-H_{2}^{2}\left(1+K_{2}^{2}\right)+H_{2} K_{2} R_{2}=0 \tag{66}
\end{align*}
$$

Substituting the values of $\mathrm{H}_{1}$ and $\mathrm{H}_{1}^{2}$ from equations (62) and (63) into equation (66) yields:

$$
\begin{align*}
& H_{2}^{2}\left(K_{1}^{2}-K_{2}^{2}\right)+H_{2}\left(2 H_{4}\left(1+K_{1}^{2}\right)-2 H_{3}\left(1+K_{1}^{2}\right)-K_{1} R_{1}+K_{2} R_{2}\right) \\
& +H_{3}^{2}\left(1+K_{1}^{2}\right)+H_{4}^{2}\left(1+K_{1}^{2}\right)-2 H_{4} H_{3}\left(1+K_{1}^{2}\right)+H_{3} K_{1} R_{1} \\
& -H_{4} K_{1} R_{1}+\left(R_{1}^{2}-R_{2}^{2}\right) / 4=0 \tag{67}
\end{align*}
$$

Now let:

$$
\begin{align*}
& V_{4}=C_{6} W_{8}  \tag{68}\\
& H_{4}=C_{7} W_{8}  \tag{69}\\
& M_{1}=\frac{W_{5}+\left(R_{1}+R_{2}+R_{3}\right) / 2}{K_{1}+K_{2}}  \tag{70}\\
& M_{2}=\left(C_{6}-C_{7} K_{1}\right) /\left(K_{1}+K_{2}\right)  \tag{71}\\
& M_{3}=K_{1}^{2}-K_{3}^{2}  \tag{72}\\
& M_{4}=1+K_{1}^{2} \tag{73}
\end{align*}
$$

Substituting (68), (69), (70), and (71) into equation (33) gives:
$H_{2}=M_{1}+M_{2} W_{8}$
$H_{2}^{2}=M_{1}^{2}+2 M_{2} M_{1} W_{8}+M_{2}^{2} W_{8}^{2}$

Substituting equations (68), (69), (72), (73), (74), and (75), into equation (67) yields:

$$
\begin{align*}
& \left(M_{1}^{2}+2 M_{2} M_{1} W_{8}+M_{2}^{2} W_{8}^{2}\right) M_{3}+\left(M_{1}+M_{2} W_{8}\right)\left(2 C_{7} W_{8} M_{4}-2 H_{3} M_{4}\right. \\
& \left.-K_{1} R_{1}+K_{2} R_{2}\right)+H_{3}^{2} M_{4}+C_{7}^{2} W_{8}^{2} M_{4}^{2}-2 C_{7} W_{8} H_{3} M_{4}+H_{3} K_{1} R_{1} \\
& -C_{7} W_{8} K_{1} R_{1}+\left(R_{1}^{2}-R_{2}^{2}\right) / 4=0 \tag{76}
\end{align*}
$$

Simplifying yields:

$$
\begin{align*}
& W_{8}^{2}\left(M_{2}^{2} M_{3}+2 M_{2} M_{4} C_{7}+C_{7}^{2} M_{4}\right)+W_{8}\left(M _ { 2 } \left(2 M_{3} M_{1}-2 H_{3} M_{4}-K_{1} R_{1}\right.\right. \\
& \left.\left.+K_{2} R_{2}\right)+2 C_{7} M_{4}\left(M_{1}-H_{3}\right)-C_{7} K_{1} R_{1}\right)+M_{1}\left(M_{1} M_{3}-2 H_{3} M_{4}-K_{1} R_{1}\right. \\
& \left.+K_{2} R_{2}\right)+H_{3}\left(H_{3} M_{4}+K_{1} R_{1}\right)+\left(R_{1}^{2}-R_{2}^{2}\right) / 4=0 \tag{77}
\end{align*}
$$

To solve for $W_{8}$ the quadratic formula must be used as follows: Let:

$$
\begin{align*}
& M=M_{2}{ }^{2} M_{3}+2 M_{2} M_{4} C_{7}+C_{7}^{2} M_{4}  \tag{78}\\
& N=M_{2}\left(2 M_{3} M_{1}-2 H_{3} M_{4}-K_{1} R_{1}+K_{2} R_{2}\right)+2 C_{7} M_{4}\left(M_{1}-H_{3}\right)-C_{7} K_{1} R_{1}  \tag{79}\\
& 0=M_{1}\left(M_{1} M_{3}-2 H_{3} M_{4}-K_{1} R_{1}+K_{2} R_{2}\right)+H_{3}\left(H_{3} M_{4}+K_{1} R_{1}\right)+\left(R_{1}^{2}-R_{2}^{2}\right) / 4 \tag{80}
\end{align*}
$$

Then:

$$
\begin{equation*}
W_{8}=\frac{-N+\sqrt{N^{2}-4 M O}}{2 M} \tag{81}
\end{equation*}
$$

The value of $\mathrm{H}_{3}$ to be used in the above equations can be found using equation (25) in the following analysis:

$$
\begin{equation*}
T_{M}^{2}=V_{3}^{2}+H_{3}^{2}=\left(H_{3} K_{1}-R_{3} / 2\right)^{2}+H_{3}^{2}=\left(T_{3}-W_{3} Y\right)^{2} \tag{82}
\end{equation*}
$$

Reducing yields:

$$
\begin{equation*}
H_{3}^{2}\left(K_{1}^{2}+1\right)-H_{3} K_{1} R_{3}+R_{3}^{2} / 4-\left(T_{3}-W_{3} Y\right)^{2} \tag{84}
\end{equation*}
$$

The solution to equation (84) can be found using the quadratic formula as follows:

Let:

$$
\begin{align*}
& M=1+K_{1}^{2}  \tag{85}\\
& N=-K_{1} R_{3}  \tag{86}\\
& O=R_{3}^{2} / 4-\left(T_{3}-W_{3} Y\right)^{2} \tag{87}
\end{align*}
$$

Then:

$$
\begin{equation*}
H_{3}=\frac{-N+\sqrt{N^{2}-4 M O}}{2 M} \tag{88}
\end{equation*}
$$

The solution procedure for finding the maximum allowable log weight, is to find the maximum $\log$ weight with the skyline being limited and then find the maximum log weight with the mainline being limited. The smaller of these values is then the maximum log weight. The limiting line will then be at its maximum allowable tension and the tension in the other line can be found from the formulas which give the tensions in the lines for a given log weight.

Running Skyline Loads and Line Tensions
The analysis method for a running skyline is essentially the same as for a standing and live skyline, only in place of line 2 are two lines with equal tensions. The mathematical formulation shown here for a running skyline will be reduced, just showing the essential equations and analysis. For more details on the analysis refer to the standing and live skyline analysis which is essentially the same with only a few changes in each equation. The cable system geometry for a running skyline is the same as shown in Figure 4. The geometry and forces acting on
each line segment are as shown in Figure 6.


Figure 6. Free Body Diagram for a Running Skyline.

For a running skyline, the equations for the moment and vertical force balance for each line segment remain essentially the same as equations (23), (24), (25), (28), and (29). These equations are as follows: Let:

$$
\begin{equation*}
K_{1}=Y / D \tag{89}
\end{equation*}
$$

$$
\begin{equation*}
K_{2}=(Y-H) /(L-D) \tag{90}
\end{equation*}
$$

Then:

$$
\begin{array}{ll}
\Sigma M_{A}=0 & V_{1}=H_{1} K_{1}-R_{1} / 2 \\
\Sigma M_{B}=0 & V_{2}=H_{2} K_{2}-R_{2} / 2 \\
\Sigma M_{A}=0 & V_{3}=H_{3} K_{1}-R_{3} / 2 \tag{93}
\end{array}
$$

The equations for the carriage force balance are the following:

$$
\begin{array}{ll}
\Sigma F x=0 & 2 H_{2}+H_{4}-H_{1}+H_{3}=0 \\
\Sigma F y=0 & V_{1}+2 V_{2}-V_{3}-W_{5}-V_{4}=0 \tag{98}
\end{array}
$$

Using these equations, the following equation for $\mathrm{H}_{2}$ can be formulated:

$$
\begin{equation*}
H_{2}=\frac{W_{5}+V_{4}+\left(R_{1}+2 R_{2}+R_{3}\right) / 2-H_{4} K_{1}}{2\left(K_{1}+K_{2}\right)} \tag{99}
\end{equation*}
$$

The equation for $R_{1}, R_{2}$ and $R_{3}$ are only changed by substituting for the different line weights as follows:

$$
\begin{align*}
& R_{1}=W_{2} \sqrt{D^{2}+Y^{2}}  \tag{100}\\
& R_{2}=W_{2} \sqrt{(L-D)^{2}+(Y-H)^{2}}  \tag{101}\\
& R_{3}=W \sqrt{D^{2}+Y^{2}} \tag{102}
\end{align*}
$$

The haulback on a running skyline also passes over a sheave in the carriage, so assuming a frictionless sheave, the tensions in lines 1 and 2
at the carriage will be equal which are also equal to the tension in line 2 at the carriage. From this relationship, the following equations can be formulated:

$$
\begin{align*}
& T_{6}=\sqrt{V_{1}^{2}+H_{1}^{2}}=\sqrt{V_{2}^{2}+H_{2}^{2}}  \tag{103}\\
& T_{6}^{2}=V_{1}^{2}+H_{1}^{2}=V_{2}^{2}+H_{2}^{2} \tag{104}
\end{align*}
$$

Substituting for the value of $V_{2}$ from equation (92) into equation (103) yields:

$$
\begin{equation*}
T_{6}=\sqrt{H_{2}^{2}+\left(H_{2} K_{2}-R_{2} / 2\right)^{2}} \tag{105}
\end{equation*}
$$

Once the value of $T_{6}$ is found, the following equation can be formulated from equations (104) and (91) to find the value of $H_{1}$ :

$$
\begin{equation*}
\mathrm{H}_{1}^{2}\left(1+\mathrm{K}_{1}^{2}\right)-\mathrm{H}_{1} \mathrm{~K}_{1} \mathrm{R}_{1}+\mathrm{R}_{1}^{2} / 4-\mathrm{T}_{6}^{2}=0 \tag{106}
\end{equation*}
$$

The solution to this equation for $H_{1}$ can be found from the quadratic formula as follows:

Let:

$$
\begin{align*}
& M=1+K_{1}^{2}  \tag{107}\\
& N=-K_{1} R_{1}  \tag{108}\\
& 0=R_{1}^{2} / 4-T_{6}^{2} \tag{109}
\end{align*}
$$

Then:

$$
\begin{equation*}
H_{1}=\frac{-N+\sqrt{N^{2}-4 M O}}{2 M} \tag{1.10}
\end{equation*}
$$

Once the values of $H_{1}$ and $H_{2}$ are found from equations (99) and (110), the value of $H_{3}$ can be found from equation (97). When the values of $H_{1}$ and $H_{3}$ are known, the tensions in lines 1 and 3 at the headspar can be found from the following equation:

$$
\begin{align*}
& T_{7}=\sqrt{H_{1}^{2}+\left(H_{1} K_{1}-R_{1} / 2\right)^{2}}+W_{1} Y  \tag{111}\\
& T_{8}=\sqrt{H_{3}^{2}+\left(H_{3} K_{1}-R_{3} / 2\right)^{2}}+W_{3} Y \tag{12}
\end{align*}
$$

The previously formulated equations are for determining the haulback and mainline tensions for a given log weight.

The following analysis is for determining the maximum allowable log weight with the haulback being limited by its maximum allowable load:

$$
\begin{align*}
& T_{6}=T_{2}-W_{1} Y  \tag{113}\\
& T_{6}^{2}=H_{2}^{2}+V_{2}^{2}=H_{2}^{2}+\left(H_{2} K_{2}-R_{2} / 2\right)^{2}=\left(T_{2}-W_{2} Y\right)^{2} \tag{114}
\end{align*}
$$

Reducing yields:

$$
\begin{equation*}
H_{2}^{2}\left(1+K_{2}^{2}\right)-H_{2} K_{2} R_{2}+R_{2}^{2} / 4-\left(T_{2}-W_{2} Y\right)^{2}=0 \tag{115}
\end{equation*}
$$

To solve for $\mathrm{H}_{2}$ the quadratic formula must be used as follows:
Let:

$$
\begin{align*}
& M=1+K_{2}^{2}  \tag{116}\\
& N=-K_{2} R_{2}  \tag{117}\\
& 0=R_{2}^{2} / 4-\left(T_{2}-W_{2} Y\right)^{2} \tag{118}
\end{align*}
$$

Then:

$$
\begin{equation*}
H_{2}=\frac{-N+\sqrt{N^{2}-4 M O}}{2 M} \tag{119}
\end{equation*}
$$

Once the value of $\mathrm{H}_{2}$ is known, equations (2) and (3) can be used to substitute in for the values of $V_{4}$ and $H_{4}$ and the resulting equation can be solved for $W_{7}$ yielding the following equation:

$$
\begin{equation*}
W_{7}=\frac{2 H_{2}\left(K_{2}+K_{1}\right)-W_{5}-\left(R_{1}+2 R_{2}+R_{3}\right) / 2}{C_{6}-C_{7} K_{1}} \tag{120}
\end{equation*}
$$

With the above equation, the log weight can be found which will cause the haulback to be at its maximum allowable tension. However, with a running skyline, the mainline will often be the limiting factor in determining the maximum log weight. The following analysis is a method of determining the $\log$ weight which will cause the mainline to be at its maximum allowable load.

First, by substituting equations (91), (92) and (97) into equation (104) and simplifying yields:

$$
\begin{align*}
& \mathrm{H}_{2}^{2}\left(4 \mathrm{~K}_{1}^{2}-\mathrm{K}_{2}^{2}+3\right)+2 \mathrm{H}_{2}\left(2 \mathrm{H}_{4}\left(1+\mathrm{K}_{1}^{2}\right)-2 \mathrm{H}_{3}\left(1+\mathrm{K}_{1}^{2}\right)+\mathrm{K}_{1} \mathrm{R}_{1}+\mathrm{K}_{2} \mathrm{R}_{2} / 2\right) \\
& +\mathrm{H}_{3}^{2}\left(1+\mathrm{K}_{1}^{2}\right)+\mathrm{H}_{4}^{2}\left(1+\mathrm{K}_{1}^{2}\right)-2 \mathrm{H}_{4} \mathrm{H}_{3}\left(1+\mathrm{K}_{1}^{2}\right)+\mathrm{H}_{3} \mathrm{~K}_{1} \mathrm{R}_{1}-\mathrm{H}_{4} \mathrm{~K}_{1} \mathrm{R}_{1} \\
& +\left(\mathrm{R}_{1}^{2}-\mathrm{R}_{2}^{2}\right) / 4=0 \tag{121}
\end{align*}
$$

Then let:

$$
\begin{align*}
& V_{4}=C_{6} W_{8}  \tag{122}\\
& H_{4}=C_{7} W_{8} \tag{123}
\end{align*}
$$

$$
\begin{align*}
& M_{1}=\frac{\left(R_{1}+2 R_{2}+R_{3}\right) / 2+W_{5}}{2\left(K_{1}+K_{2}\right)}  \tag{124}\\
& M_{2}=\frac{C_{6}-C_{7} K_{1}}{2\left(K_{1}+K_{2}\right)}  \tag{125}\\
& M_{3}=4 K_{1}^{2}-K_{2}^{2}+3  \tag{126}\\
& M_{4}=1+K_{1}^{2} \tag{127}
\end{align*}
$$

Substituting equations (122), (123), (124), and (125) into equation (99) yields:

$$
\begin{align*}
& H_{2}=M_{1}+M_{2} W_{8}  \tag{128}\\
& H_{2}^{2}=M_{1}^{2}+2 M_{2} M_{1} W_{8}+M_{2}^{2} W_{8}^{2} \tag{129}
\end{align*}
$$

Substituting equations (122), (123), (126), (127), (128), and (129), into equation (121) and simplifying yields:

$$
\begin{align*}
& W_{8}^{2}\left(M_{2}^{2} M_{3}+4 M_{2} M_{4} C_{7}+C_{7}^{2} M_{4}\right)+W_{8}\left(M_{1}\left(M_{1} M_{3}-4 H_{3} M_{4}-2 K_{1} R_{1}+K_{2} R_{2}\right)\right) \\
& +H_{3}\left(H_{3} M_{4}+K_{1} R_{1}\right)+\left(R_{1}^{2}-R_{2}^{2}\right) / 4=0 \tag{130}
\end{align*}
$$

To solve for $W_{8}$ in this equation the quadratic formula can be used as follows:

Let:

$$
\begin{equation*}
M=M_{2}^{2} M_{3}+4 M_{2} M_{4} C_{7}+C_{7}^{2} M_{4} \tag{131}
\end{equation*}
$$

$$
\begin{align*}
& N=M_{2}\left(2 M_{3} M_{1}-4 H_{3} M_{4}-2 K_{1} R_{1}+K_{2} R_{2}\right)+2 C_{7} M_{4}\left(2 M_{1}-H_{3}\right)-C_{7} K_{1} R_{1}  \tag{132}\\
& 0=M_{1}\left(M_{1} M_{3}-4 H_{3} M_{4}-2 K_{1} R_{1}+K_{2} R_{2}\right)+H_{3}\left(H_{3} M_{4}+K_{1} R_{1}\right)+\left(R_{1}^{2}-R_{2}^{2}\right) / 4 \tag{133}
\end{align*}
$$

Then:

$$
\begin{equation*}
W_{8}=\frac{-N+\sqrt{N^{2}-4 M O}}{2 M} \tag{134}
\end{equation*}
$$

The value of $\mathrm{H}_{3}$ to be used in the above equations can be found using equation (93) as follows:

$$
\begin{equation*}
T_{M}^{2}=V_{3}^{2}+H_{3}^{2}=\left(H_{3} K_{1}-R_{3} / 2\right)^{2}+H_{3}^{2}=\left(T_{3}-W_{3} Y\right)^{2} \tag{135}
\end{equation*}
$$

Reducing yields:

$$
\begin{equation*}
H_{3}^{2}\left(K_{1}^{2}+1\right)-H_{3} K_{1} R_{3}+R_{3}^{2} / 4-\left(T_{3}-W_{3} Y\right)^{2}=0 \tag{137}
\end{equation*}
$$

The solution to equation (137) can be found using the quadratic formula as follows:

$$
\begin{equation*}
H_{3}=\frac{K_{1} R_{3}+\sqrt{K_{1}^{2} R_{3}^{2}-4 M_{4}\left(R_{3}^{2} / 4-(T-W Y)^{2}\right)}}{2 M_{4}} \tag{139}
\end{equation*}
$$

The solution procedure for finding the maximum allowable log weight is to find the maximum log weight with the haulback being limited and then find the maximum log weight with the mainline being limited. The smaller of these values is then the maximum log weight. The limiting line will then be at its maximum allowable tension and the tension in the other line
can be found from the formulas which give the tensions in the lines for a given $\log$ weight.

## Standing Skyline Length and Carriage Clearance

A standing skyline has a fixed line length. For this analysis it is assumed that this line length is fixed such that the log will have a specified minimum amount of one and suspension at all points along the skyline. This line length is found by placing the $\log$, with its minimum required clearance along the terrain as described in the section "Terrain Point Step Size." The line length for each of these points along the terrain is then determined. The line length is then fixed at the shortest of these lengths.

The carriage clearance is found from the equations shown for $\log \mathrm{drag}$ of a live skyline. Once the carriage clearance $\left(C_{p}\right)$ is found, using Figures 1 and 4, the skyline length can be found from the following equations:

First, from the geometry of Figures 1 and 4:

$$
\begin{align*}
& Y_{8}=Y_{9}+C_{1}  \tag{140}\\
& Y=Y_{1}-Y_{8}  \tag{141}\\
& H=Y_{2}-Y_{1}  \tag{142}\\
& D=X_{8}-X_{1} \tag{143}
\end{align*}
$$

Then the skyline length can be found from the following equation:

$$
\begin{equation*}
U_{5}=\sqrt{D^{2}+Y^{2}}+\sqrt{(L-D)^{2}+(Y-H)^{2}} \tag{144}
\end{equation*}
$$

This analysis assumes straight line segments and neglects line stretch.

Once the line length is set, the vertical distance from the carriage to the top of the headspar ( $Y$ ) can be found from the elliptical load path equations developed by Carson (1). These equations were modified to use the variables from the rest of this analysis. These equations are as follows:

$$
\begin{align*}
& E=\frac{U_{4}}{\sqrt{L^{2}+H^{2}}}  \tag{145}\\
& M=E^{2}+H^{2}\left(E^{2}-1\right) / L^{2}  \tag{146}\\
& N=E(1-2 D / L)  \tag{147}\\
& 0=(1-2 D / L)^{2}-H^{2}\left(E^{2}-1\right) / L^{2}  \tag{148}\\
& N=\left(-N+A B S(H)^{\sqrt{\left.N^{2}-4 M O / H\right) / M}}\right.  \tag{149}\\
& Y=\left(H \left(1+E N+L^{\sqrt{\left.\left(E^{2}-1\right)\left(1-N^{2}\right)\right) / 2}}\right.\right. \tag{150}
\end{align*}
$$

Once the value of $Y$ is found, the carriage clearance can be found from the following equations:

$$
\begin{align*}
& Y 8=Y 1-Y  \tag{151}\\
& C_{1}=Y_{8}-Y_{9} \tag{152}
\end{align*}
$$

Once the value of $C_{1}$ is known the horizontal and vertical forces at the carriage from the choker can be found by using the analysis shown for $\log$ drag for a standing skyline. Then the formula for determining standing skyline loads and line tensions can be used to find the maximum allowable load for each terrain point and the resulting mainline and skyline tensions.

## Carriage Types

For a standing skyline, which is usually skyline limited, a single mainline type carriage is assumed in the computer program. For a running skyline, which is often mainline limited, and where mechanical slackpulling (MSP) and over/under wound type carriages (Rowley-Parker style) are often used, the computer program offers a choice of using a single mainline type carriage, a MSP type carriage or an over/under wound carriage. For a single mainline type carriage, the equations formulated for a running skyline analysis can be used as formulated in the section "Running Skyline Loads and Line Tensions." Figures 7 and 8 show a free body diagram for a MSP and an over/under wound carriage, respectively.


Figure 7. Free Body Diagram for a MSP Type Carriage, on a Running Skyline.


Figure 8. Free Body Diagram for a Over/Under Wound Type Carriage on a Running Skyline.

For a over/under wound carriage as shown above, it is assumed the dropline, mainline and slackpulling line drums in the carriage cannot lock, and therefore, the sum of the moments about the center of the drums must be in balance as shown in the following equation:

$$
\begin{equation*}
\Sigma M=0 \quad R_{m} T_{m}-R_{c} T_{C}-R_{s} T_{s}=0 \tag{153}
\end{equation*}
$$

The analysis for a MSP carriage is the same as for a over/under carriage only $R_{m}=R_{c}=R_{s}$.

Let $T$ be the maximum tension the mainline plus the slackpuling line can have at the headspar. If the value of $T$ is known, the equations derived for a running skyline can be used with $T$ in place of the maximum allowable mainline tension and with the mainline plus the slackpulling line weight substituted for the mainline weight. However, the value of T is generally not known and cannot be solved for directly, so an iterative type procedure is needed: The secant method was the iterative procedure chosen for this problem with the value of $T$ as the variable and the difference between the allowable mainline tension and the actual value of the mainline tension for the chosen value of $T$ as the function. The value of $T$ which makes the value of the function equal zero will then be the value of $T$ for which the mainline will be at its maximum allowable tension. For this problem, the value of mainline tension at the headspar can be found as follows:

First, rearranging equation (153) yields:

$$
\begin{equation*}
T_{m}=\frac{R c}{R m} T_{c}+\frac{R s}{R m} T_{s} \tag{154}
\end{equation*}
$$

Let:

$$
\begin{align*}
& R_{5}=\frac{R c}{R m}  \tag{155}\\
& R_{6}=\frac{R s}{R m} \tag{156}
\end{align*}
$$

Then substituting equation (155) and (156) into equation (154) yields:

$$
\begin{equation*}
T_{m}=R_{5} T_{c}+R_{6} T_{s} \tag{157}
\end{equation*}
$$

Solving for $T_{S}$ yields:

$$
\begin{equation*}
T_{s}=\frac{T_{m}-R_{5} T_{c}}{R_{6}} \tag{158}
\end{equation*}
$$

The value of $T, T_{s}$ and $T_{m}$ can be equated using the following equation:

$$
\begin{equation*}
T-W Y=T_{5}+T_{m} \tag{159}
\end{equation*}
$$

Substituting in equation (159) the value of $\mathrm{T}_{\mathrm{s}}$ from equation (158) yields:

$$
\begin{equation*}
T-W Y=\frac{T_{m}-R_{5} T_{c}}{R_{6}}+T_{m} \tag{160}
\end{equation*}
$$

Solving for Tm yields:

$$
\begin{equation*}
T_{m}=\left(T-W Y+\frac{R_{5} T_{c}}{R_{6}}\right) \frac{R_{6}}{T+R_{6}} \tag{161}
\end{equation*}
$$

If the value of the mainline tension at the carriage is known, the tension in the mainline at the headspar can be found as follows:

$$
\begin{equation*}
T_{\mathrm{ma}}=T_{m}+W_{3} Y \tag{162}
\end{equation*}
$$

$$
\begin{equation*}
T_{\text {ma }}=\left(T-W Y+\frac{R_{5} T c}{R_{6}}\right) \frac{R_{6}}{1+R_{6}}+W_{3} Y \tag{163}
\end{equation*}
$$

The value of $T_{c}$ can be found from the following equation:

$$
T_{c}=W_{8} \sqrt{C_{6}^{2}+c_{7}^{2}}
$$

The equation for the function can now be written as follows:

$$
\begin{equation*}
F_{4}=T_{3}-T_{m a}=T_{3}-\left(T-W Y+\frac{R_{5} W_{8} \sqrt{C_{6}{ }^{2}+C_{7}^{2}}}{R_{6}}\right) \frac{R_{6}}{1+R_{6}}-W_{3} Y \tag{164}
\end{equation*}
$$

In the above equation, the value of $W_{8}$ is found from the equations for determining the maximum allowable load with the mainline being limited. Using the secant method, the equation for choosing a new value of $T$ is the following:

$$
\begin{equation*}
T=E_{4}-F_{4} \frac{E_{4}-E_{3}}{F_{4}-F_{3}} \tag{165}
\end{equation*}
$$

In this equation $E_{4}$ is the current value of $T, E_{3}$ is the last value of $T, F_{4}$ is the current value of the function, $F_{3}$ is the last value of the function, and $T$ is the new guess for a value of $T$.

The iterative procedure is then to choose two initial values for $E_{3}$ and $E_{4}$ and find the values of $F_{4}$ and $F_{3}$ for these values of $T$. Then equation (165) is used to determine a new guess of $T$. The value of $F_{4}$ is then found for this new value of $T$ using the equations for finding $W_{8}$ given the value of $T$ and equation (164). This procedure is continued until the value of $F_{4}$ is within an acceptable tolerance of zero.

Portions of the preceeding analysis and figures used the methods devised by Carson (2, 3), Carson and Mann (4, 5), Peters (9), Sessions (10), and Falk (7).

## SKYLINE ANALYSIS PROGRAM WITH DRAG

A computer program has been written in Basic and placed on the HP 9830 to solve this problem. This computer program is actually two separate computer programs. The first program is for entering and storing the profile data and the yarder specifications. The profile data is stored on the auxiliary cassette and the yarder specifications are stored on the main cassette along with the computer programs. Once the yarder specifications and profile data are stored on the cassette, they do not have to be reentered and when an analysis is done they can be used over and over.

The second program is for analyzing the profiles determining the allowable loads, mainline tensions, and skyline or haulback tensions. This program uses the yarder specifications and profile data previously stored on the cassettes.

## Profile Input Program

This computer program consists of a mainline memory subprogram, plus ten subprograms on the special function keys 0 through 9. Figure 9 shows the special function key overlay for both programs. The descriptions above the special function keys refer to the profile input program. The descriptions below the special function keys refer to the skyline analysis program.


Figure 9. Special Function Key Overlay.

For example, special function key $f_{0}$ is for entering data from the digitizer in the profile input program and for entering a new profile from tape in the skyline analysis program.

The mainline memory subprogram is for initializing the program and loading the special function key subprograms from tape. Special function keys $f_{0}$ through $f_{4}$ are for entering profile data from a contour map using the digitizer. Special function key $f_{5}$ is for reversing a profile. Special function key $f_{6}$ is for storing a profile once it is entered. Special function keys $f_{7}$ and $f_{8}$ are for entering profile data by $X, Y$ coordinates and slope distance, percent slope data respectively. Special function key $f_{g}$ is for entering and storing the yarder specifications that are used in the skyline analysis program with drag. The profile inputs and computer programs used for these special function key programs are essentially the same as the ones used on the Skyline Analysis Program (Sessions, 1978).


LIUE FND STAPATHG SKGLINE LOAD FRAL'TEIEURIGID LIPK FESUNFTIOND
TAFDEF EFECS -THURDEFEIFD MOBILE YRFDER

| FLLOMAELE | LINE |
| :---: | :---: |
| LOAD | WEIGHT |
| 34500 | 1.85 |
| 19600 | 1.04 |
| 6 | 0.06 |
| 6 | 0.60 |


| EKTLIPE | 34500 | 1. 85 |
| :---: | :---: | :---: |
| MAITALTAE | 19600 | 1. 64 |
| HFidlemide | $\underline{\square}$ | 6. 60 |
| BLACKLINE | $\underline{\square}$ | 日. 60 |

HEACSFRF: HT $=45$
FROFTLE 14
EAEEIAGE HT= TEILEFHE HT= 4G
HEADGFAR T. P. $=1 \quad 1 \quad$ TAILEFAF T. F. $=9$
IDH 'TAFD LIM= DUIT 'TAFD LIH= 1
LENGTH OF CHOKEF= $s$ LEMGTH OF LOIS= $s=$
MIH LOD TG GFOUND CLEAFANGE $=2$
TEFEAIN FOINT STEF SIZE= 1
LIVE SKTLINE FATLOADE

| TEFEHIN | HOES | MA\% LOM | EKTLITAE | NAFINLIME | CAPEIAGE | LOIS TO GROUMD |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FOIMT | QIET | LOHD | TEHSIDN | TENSION | CLEFFARHE | FHGLE |
| 2. ${ }^{\text {a }}$ | 207 | 15141 | 34500 | 1002e | 8.67 | 3. 56 |
| 3. 8 | Ses | 1323 | 34500 | 8554 | 5. 5.1 | 3. 58 |
| 4. 6 | 581 | 1269 | 34560 | 5095 | E. 8 e | 3.58 |
| 5. 9 | 746 | 13284 | 34500 | 8445 | 11. 68 | 3. 56 |
| E 0 | 847 | 24975 | 34560 | 14792 | 9. 29 | E. 59 |
| F. $\square^{\text {a }}$ | 997 | 4737 | 24509 | 1:188 | 9. 68 | 2. 58 |
| 8. 5 | 122 | 51.80 | 34500 | P1E4 | 9.94 | 3. 55 |

ETFADING EFTLIAE FF'TLGADS EHEED DR F EKTLINE LENGTH OF 1S4E. 4E FT.

Figure 10. Typical Printout.

However, the programs were all slightly modified to simplify the input and storing of the profiles. Appendix 1 contains a users guide for using this program. Appendix 2 contains a copy of the program statements for this program.

## Skyline Analysis Program with Log Drag

Figure 10 shows a typical printout of the output for this program. The yarder specifications and profile data are all entered from tape which was stored in the profile input program. The carriage weight, tailspar height, headspar terrain point number, tailspar terrain point number, inner yarding limit, outer yarding limit, length of the choker, length of the log, minimum log to ground clearance, and terrain point step size, were all entered in this program. The terrain point, span, maximum log load, skyline tension, mainline tension, carriage clearance, log to ground angle, and required rigging length are all output by this program.

In this program, the mainline memory subprogram initializes the program and loads the special function key programs from the cassette tape. Referring again to Figure 9, the descriptions below the special function key apply to the skyline analysis program with log drag. Special function key $f_{5}$ enters the program inputs, analyzes the data, and prints the outputs. Once the first profile has been analyzed, special function keys $f_{0}$ through $f_{4}$ and $f_{6}$ through $f_{8}$ are used to change the inputs specified by the user which are then analyzed using special function key $f_{5}$. For example, after the first profile has been run using special function key $f_{5}$, special function keys $f_{0}$ and $f_{6}$ could be used to change the profile data and the carriage weight before analyizing the data using special function key $f_{5}$ again. The yarder data, $\log$ and choker data, log clearance
and terrain point step size would all remain the same and would not have to be input again. If all new data is required for the next analysis after the first profile is run, then special function key $f_{7}$ would be used before using special function key $f_{5}$ again. Special function key $f_{g}$ just gives another listing of the profile. The profile is also listed in the profile input program. The computer programs were set up in this way to require the least amount of input.

Appendix 1 contains a users guide for using this program and Appendix 3 contains a copy of the program statements for this program.

## EFFECTS OF THE PARAMETERS USED IN COMPUTING

THE ALLOWABLE LOADS AND LINE TENSIONS

Appendix 4 contains sample profiles and computer runs to demonstrate the effects of the various parameters. Figures 17 and 28 in Appendix 4 show the basic profiles and inputs. The parameters were varied from this basic data one at a time, to show the effects of the parameters. The following is a discussion of these computer outputs, and the effects of the various parameters.

## Choker Angle

The smaller the choker angle (A in Figure 1), the higher the horizontal component of the force at the carriage from the choker will be $\left(\mathrm{H}_{4}\right.$ in Figures 5 and 6) and the lower the vertical component of the force at the carriage from the choker ( $V_{4}$ in Figures 5 and 6). As the horizontal component of the force increases and the vertical component of the force decreases in the choker, this causes an increase in the mainline tension and a decrease in the skyline tensions. If the skyline is limiting the allowable load, then the allowable load would increase as the choker angle decreases. However, if the mainline is limiting the allowable load, then the allowable load would decrease as the choker angle decreases. Most of the parameters discussed in the following sections affect the line tensions in this manner, by changing the choker angle and horizontal and vertical components of the force at the carriage, shifting the effects of
load from one line to the other.

## Length of Log

Figures 18 and 19 show the effects of the length of the log. For this example the skyline is limiting, and a longer log causes a higher mainline tension and a higher maximum log load, a longer log causes an increase in the horizontal component of the force at the carriage, a decrease in the vertical component of the force at the carriage, and a smaller choker angle. This causes a transfer of the force from the skyline to the mainline, which allows a higher log load, if the skyline is limiting. If the mainline were limiting, a longer log would decrease the allowable load.

## Log to Ground Clearance

Figures 17,20 and 21 show the effect of the $\log$ to ground clearance (C in Figure 1). Again in this example, the skyline is always limiting and the higher the $\log$ to ground clearance, the lower the maximum log load, and the lower the mainline tensions. Higher $\log$ to ground clearances cause a higher vertical component of the force at the carriage, and a larger choker angle. This causes a transfer of some of the load from the mainline to the skyline and decreases the allowable load if the skyline is limiting.

## Length of Choker

Figures 17 and 22 show the effects of the length of the choker. A longer choker causes a shortening of skyline in order to maintain the
minimum $\log$ to ground clearance. In the example this caused a decrease in the maximum log load and a decrease in the mainline tensions. For a given log weight, the horizontal component and vertical component of the force in the choker at the carriage remain the same and the choker angle remains the same. For a given log weight the shorter the skyline, and less the deflection, the higher the tension in the skyline. So if the skyline is limiting, the shorter the choker length the higher the load that can be carried.

## Point of Choker Attachment

In the computer program, the choker is assumed to be attached 2 feet from the end of the log. This value can easily be changed in the computer program or could easily be made an input. To change the point of choker attachment in the computer program, the value of $D_{3}$ needs to be changed in statement number 30 . The point of choker attachment was changed from 2 feet to 14 feet from the end of the $\log$ in the computer program and the results of the output are shown in Figure 23. Comparing Figure 17 ( $\mathrm{D}_{3}=2$ ) and Figure $23\left(D_{3}=14\right)$, placing the choker closer to the center of the log caused a decrease in maximum load and decreased the mainline tension. The negative mainline tension at terrain point 8 , indicates the mainline would be slack at this point and the $\log$ would slide down the hill without the assistance of the mainline. Placing the choker closer to the center of the $\log$ causes the vertical component of the force at the carriage to increase, the horizontal component of the force in the choker at the carriage to decrease, and the choker angle to increase. If the skyline is limiting, then choking the $\log$ closer to the center causes a
decrease in the maximum $\log$ load. If the mainline is limiting then choking the $\log$ closer to the center would increase the maximum log load.

## Center of Gravity of the Log

In the computer program, the center of gravity of the $\log$ is assumed to be located a distance of half the log length from the end of the log $\left(C_{8}=0.5\right)$. This value can be easily changed in the computer program by changing the value of $C_{8}$ in program line number 85 or this value could easily be made on input. Figures 24 and 25 show an example of the effect of having the center of gravity of the $\log 0.3$ and 0.7 of the length of the $\log$ from the end of the log. In this example, having the center of gravity closer to the end of the $\log \left(C_{8}=0.3\right)$ increased the mainline tension and caused the mainline to be limiting in some cases. Also, the maximum $\log$ load increased because the skyline was limiting with $\mathrm{C}_{8}=0.7$. Having the center of gravity closer to the end of the $\log \left(C_{8}=0.3\right)$ caused more of the load to be taken by the mainline and less to be taken by the skyline. The closer the center of gravity of a $\log$ is to the end of the $\log$, the higher the horizontal component of the force in the choker, the lower the vertical component of the force in the choker, and the smaller the choker angle. If the skyline is limiting, a higher load can be carried for a $\log$, with its center of gravity closer to the end of the log. If the mainline is limiting a higher $\log$ load can be carried with a $\log$ that has its center of gravity farther from the end of the log.

## Coefficient of Friction

Values of the coefficient of friction reported in the literature have generally varied from a value of 0.5 to a value of 1.0 with a value of 0.6
for the coefficient of friction being the most commonly used value in most engineering calculations. The computer program assumes a value of $\mathrm{U}=0.6$, however, this value is very easy to change and could be made an input. Figures 17, 26 and 27 show the effect of the coefficient of friction. The coefficient of friction was 0.6 for output shown in Figure 17, 0.4 for the output shown in Figure 26 and 0.8 for the output shown in Figure 27. For the examples shown in Figures 26 and 27 , changing of the coefficient of friction from 0.4 to 0.8 did not significantly change the maximum $\log$ loads, but did cause the mainline tensions to increase. For a log with a given one end suspension, increasing the coefficient of friction causes the choker angle to decrease and causes the tension in the choker to increase. When the skyline is limiting, the increase in load from a decreased choker angle is offset by an increase in the choker tension. When the mainline is limiting, increasing the coefficient of friction would cause an increase in the mainline tension and a decreased log load.

## Terrain Point Step Size

Figures 11 and 12 show the effect of the terrain point step size. As shown in Figure 11 for a terrain point step size of 2 every second terrain point is analyzed with the carriage directly above the terrain point and for a terrain point step size of one every terrain point is analyzed. Similarly, for a terrain point step size of 3 every third terrain point would be analyzed and for a terrain point step size of 4 every fourth terrain point would be analyzed. Figure 12 shows that for a terrain point step size of $: 5(1 / 2)$ two points are analyzed between terrain
points, one with the carriage directly above the terrain point and one with the end of the $\log$ on the next terrain point. For a terrain point step size of $.33(1 / 3)$ three points are analyzed between terrain points as shown in Figure 12. Similarly for a terrain point step size of . 25 (1/4) four points between terrain points would be analyzed and for a terrain point step size of $.20(1 / 5)$ five points between terrain point would be analyzed. The advantage in analyzing more terrain points is that the critical point for the payload is more likely found. Also, for a standing skyline analyzing more terrain points assures that the minimum line length is more accurately found.

## Type of Carriage for a Running Skyline

Figures $28,29,30$, and 31 show the effect of the different types of carriages. In these examples the mainline is always limiting. The MSP carriage gave the highest log loads, the over/under wound carriage with $R_{5}=R_{6}=1.5$ the second highest loads, the over/under wound carriage with $R_{5}=R_{6}=2.0$ the third highest log loads, and the single mainline type carriages giving the lowest loads.* However, the single mainline carriage gave a higher load on a few of the terrain points with flatter or downhill slopes. For the downhill and the flatter uphill slopes, more of the log load is transferred to the haulback with a single mainline carriage, since the choker tension is not transferred directly to the mainline through a sheave or series of drums in the carriage. The MSP and over/under wound carriages are generally more efficient, since the slackpulling line carries a portion of the load. The smaller the ratios of the mainline drum
*See the section on carriage types for an explanation of $R_{5}$ and $R_{6}$.

TERRFIN PGINT STEF 5!ZE $=2$


TERRAIN PGINT STEP SIZE =1


Figure ll.- Effect of Terrain Point

TERRAIN PDINT 5TEP 5IZE $=.5$


Figure 12.- Effect of Terrain Point Step Size.
diameter to the dropline and slackpulling line drum diameter ( $R_{5}$ and $R_{6}$ ), the more efficient is the over/under wound carriage and the more load the slackpulling line will carry.

## COMPARISON WITH SKYLINE ANALYSIS PROGRAM

Figure 13 shows an example of the output from the Skyline Analysis Program on the HP 9830. The value input for the loaded carriage clearance to insure a specified amount of one end suspension is generally a guess. A value of 9 was used in this example because it was the average carriage clearance found using the Skyline Analysis Program with Drag (Figure 14). In the standing skyline output, the carriage clearance can greatly vary and it is generally a guess whether to use the dragging load or the flying load for the actual loads. The value for the dragging loads was determined by multiplying the flying log loads by 1.5. The Skyline Analysis Program does not determine or limit the mainline tensions. To accurately determine the mainline tension for a dragging log, the horizontal component of the force from the choker has to be used in the analysis. Figure 14 shows the output for this same profile using the Skyline Analysis Program with Drag. For the live skyline analysis, which would have a dragging load, the Skyline Analysis Program with Drag gave a lower payload for the first few terrain points since the mainline was limiting and the Skyline Analysis Program on the HP 9830 does not even check the mainline tensions. For the rest of the terrain points, the Skyline Analysis Program with Drag gave higher payloads. The negative mainline tension for terrain point 13 indicates the mainline is slack and the $\log$ would be sliding down the hill. For the standing skyline payloads, the two programs give similar results, since the load is flying for most of the terrain points.

This example demonstrates that for a dragging log, using the fully



FLLOWAELE EKTLINE TEMEIGN= E4GBG

| EKTLINE UT= | 350 | MAINLINE WT= | 2. 34 |
| :---: | :---: | :---: | :---: |
| HEACSFFR HT= | 11.6 | THILSFHF HT= | 2 |
| HEADGFAF: T. F. $=$ | 1 | THILSFAR T.F. $=$ | 16 |
| INW 'TAFD LIM $=$ | 1 | OUIT SAFD LIM= | 16 |

## GFREIFGE WT= <br> 4606

LOAOED GFERIAISE ELEARAROE= ヨ
TEREFIN FGINT LOU LOAD ©FL' LOME LOAD GDFFGY. LINE LENGTH

| 2 | E2313 | 94977 | 4275 |
| :---: | :---: | :---: | :---: |
| 3 | 51845 | 7748 | 4291 |
| 4 | 35984 | 56976 | 4290 |
| 5 | 2951 | 4436 | 4300 |
| $\theta$ | 2856 | $42>5$ | 4215 |
| 7 | 26110 | 39165 | 4295 |
| E | 2779 | 4169 | 4243 |
| 9 | 25562 | 2ses | $4 \leq 59$ |
| 19 | 1506 | 295 | 42917 |
| 11 | 1156 | 17254 | 4295 |
| 12 | 11193 | 16796 | 4280 |
| 13 | 10945 | 2896 | 4315 |
| 1.4 | 1367 | 2019 | 4273 |
| 15 | 1059 | 15809 | 4237 |

```
NEW SFFF LOLHTION = E
MEM THRDER SFEE = = 
FEDO RIGGIMG LENIGTH= =
STROLDING GFTLINE FLOT= Z
```



| STATION | LOES LOHO <FL') | LOİ LOHO ©0FFG\% | ELEAFPRHE |
| :---: | :---: | :---: | :---: |
| 414 | 12594 | 20291 | 129 |
| 689 | 631 | 9496 |  |
| 1242 | Ese | 4951 | 295 |
| 1056 | 1672 | 2509 | 217 |
| 21 | 811 | 1217 | 196 |
| 2485 | 567 | 85 | 167 |
| 2095 | 104E | 156 | 143 |
| 12 | 2769 | 415 | 180 |
| ¢e? | 7921 | 11882 | 32 |

Ficure 13. Outbut from the Skvline Analvsis Proaram.

| ＇THFDEF：EFEES－EFAIIT EU－19 |  |  |
| :---: | :---: | :---: |
|  | FLLCMFELE | LIPE |
|  | LIAPD | WEIGHT |
| 玉ドTL INE | 548016 | 3．50 |
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| HFIILEFIC\％ | 易 | E．E10 |
| SLAITHLIPE | 5 | 6． 60 |

HEFDEFHF HT＝110


LIVE GKTLINE F＇T＇LOARCS

| TEEEPAIM | HORE | MF\％LOS | Er゙TIINE | MAIPLIRE | CARRIFGE | LOUS TO GELUND |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FOINT | DIST | LOAD | TENSION | TEPSIOR | Elefrifrice | FNGLE |
| 2． 9 | 13 | 47845 | 2865： | 4360 | 12． 46 | 3． 53 |
| 3 B | 225 | 56191 | 2955s | 4 S 40 | E． 78 | 3． 58 |
| 4．${ }^{\text {a }}$ | 397 | 57316 | 52696 | 4350 | 9.8 | 3.53 |
| 5.6 | 544 | 58642 | E4060 | 4361 | 9．7E | 3.58 |
| E． $0^{\circ}$ | $67 \%$ | 61595 | $6 \pm 46$ | 4 SE | 9． 78 | 3.58 |
| T．${ }^{\text {d }}$ | E4E | 4 Sc 0 | E4090 | 21294 | 11． 26 | 3.59 |
| 8． | 954 | 62959 | E460 | 413 C | E． 39 | 3.59 |
|  | 116e | G298 | 646016 | 52.21 | 96 | 3． 58 |
| 16． | 1576 | 356 | E4060 | 18085 | e． 43 | 2.58 |
| 11．${ }^{\text {a }}$ | 2122 | 25169 | E460 0 | 12474 | E． 6 | 2． 59 |
| 12． 0 | 2110 | 19742 | 64010 | 10204 | 8． 86 | 3.59 |
| 12．${ }^{\text {a }}$ | Sest | EST | 64609 | －690e | 7． 84 | 2．5e |
| 14． 0 | 3493 | 29145 | 64060 | 7121 | 9.95 | 2．5e |
| 15．0 | Sex | 21901 | E4060 | 6575 | 9.93 | 358 |

ETFNDTHG EKTLINE FATLOADS EAGED DN F EKTLIAE LENGTH OF 42SE 13 FT

| $\begin{aligned} & \text { TEEFEIN } \\ & \text { FOIPNT } \end{aligned}$ | $\begin{aligned} & \text { HORE } \\ & \text { DIET } \end{aligned}$ | infe LOM LOAD | Sk＇rla IPE <br> TENSIOR | MFIRULINE TENEION | EAREIFISE CLEASHRHE | LOIG TO GROUNAD ANHLE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2． 0 | 135 | 34174 | E4060 | 19016 | Fe．17 | 49.11 |
| 3． 0 | 2 s | 2こヶ93 | 64860 | 11767 | 1898 | 65． 61 |
| 4． 9 | 397 | 12955 | E4Ege | 7 TET | 126.36 | 61． 54 |
| 5. | 544 | 18210 | E4096 | 525 | 159.64 | 58．${ }^{\text {c }}$ |
| E． 6 | 676 | 5081 | E4604 | 4475 | 20.55 | Es． 01 |
| F．e | 848 | 5992 | E4060 | 375 | 235 5E | 52． 85 |
| 8． 0 | 954 | 565 | E460 $0^{4}$ | 259 | 2es 26 | 69.89 |
| 9.8 | 11EE | 5614 | 64060 |  | 14．ES | Ere 60 |
| 16． 6 | 1596 | 1811 | E4060 | 336 | 224． 14 | E1． 81 |
| 11． 9 | 2132 | 6 E | E4060 | 46 C | 198． 16 | 85． 2 |
| 12．${ }^{12}$ | 3110 | 1586 | E4609 | 54.5 | 1365 | 72． 5 |
| 13． | 251 | 2981 | E4E60 | 50.5 | 192． 08 | 121． 22 |
| 14． 0 | 3493 | 4156 | 64600 | Eces | 161． 94 | 109．62 |
| 15． 0 | Sess | 21565 | E460 | 6580 | 938 | 3.14 |

FEDUIEED EIGGIN LENISTH＝4593 92
Figure 14．Output from the Skyline Analysis Program with Drag．
suspended payload or using the fully suspended payload and the "rule of thumb" that a 1.5 times greater load can be dragged than flown, can result in payloads which differ by over 50 percent.

## ASSUMPTIONS AND LIMITATIONS

1. The $\log$ diameter was neglected in the analysis. For a $\log$ which is reasonably long as compared to its width, with its choker located near the end, and the center of gravity near the center of the $\log$, the amount of error will be small in neglecting the log diameter. Peters (9) developed equations similar to Carson's (2) which consider the effects of the diameter. These equations could be used, only they are a little more complex and would require an additional input to the program for ${ }^{\circ}$ log diameter.
2. The cable segments were all analyzed using a rigid link analysis as an approximation to the more accurate catenary-type analysis. The error involved in using a rigid link analysis is generally small for taut cables. Since the skyline systems are analyzed using the maximum log weight, the skyline in the standing skyline and live skyline analysis is generally taut. When yarding uphill, a dragging log tends to increase the mainline tensions, so the mainline will usually be reasonably taut for a dragging log. In the running skyline analysis, all of the cables help provide lift, so all of the cables will generally be taut. The biggest possible source of error in the skyline analysis using the rigid link assumption, would be in the mainline for a fully suspended load in the standing skyline analysis or in the slackpulling line in the running skyline analysis. The cables could be analyzed using the catenary relationships or just the mainline and slackpulling line could be analyzed, using the catenary relationships to help
minimize this error. However, the catenary equations require an iterative type solution, which requires more time to compute, especially on the HP 9830, which is slower than some of the newer desk top computers. Also, an error statement could be added to the program to indicate when the rigid link assumption is in error.
3. If a haulback line is used with a standing or live skyline and has tension in it during the inhaul, it could greatly change the payloads. Mechanical slackpulling carriages and over/under wound type carriages are sometimes used in live and standing skylines. The option to use a haulback line, a mechanical slackpulling carriage and over/under wound type carriage could also be added to the program for a standing and live skyline.
4. In some situations, the tension in a line can become negative to obtain static equilibrium. When the log slides down the hill, the mainline tension becomes negative. In these situations where there is a negative tension in the lines, the loads computed will be in error. A haulback line could be added to the analysis when the mainline tension becomes negative.
5. The effects of line stretch are neglected in the analysis. This will cause some error in the standing skyline analysis.
6. The horizontal distance from the carriage to the end of the log must be less than the distance between terrain points, for a terrain point to be analyzed.
7. The maximum allowable tensions are assumed to occur at the headspar. For downhill yarding, whenever the tailspar elevation is higher than the headspar elevation, the skyline and mainline tensions may be
greater at the tailspar and the carriage than the values input for the maximum allowable tensions. For downhill yarding, an analysis procedure which uses a fully suspended load should be used.

## CONCLUSIONS

The method described in this paper provides a means to determine the load carrying capacity of skylines when partial suspension of the logs is used. As shown in the example problems, the load carrying capacity of a skyline system can vary from the result obtained using log drag by over $50 \%$ when $\log$ drag is neglected. A correction factor of 1.5 has been used in the past to determine the increase in payload for a dragging log. This correction factor only applies to the skyline and does not consider the mainline tensions. Also, this factor varies with the ground slope, length of the $\log , \log$ to ground clearance, choker length, point of choker attachment, center of gravity of the 10 g and coefficient of friction. If the mainline tensions are to be considered in skyline analysis with a dragging $\log$, a factor has to be used to determine both the decrease in the vertical component of the force and the increase in the horizontal component of the force in the choker at the carriage. The best method of determining these factors is to use a log drag analysis. This paper describes one such method.

Often when determining the load carrying capacity of a skyline system, several of the parameters such as length of log, length of choker, point of choker attachment, center of gravity of the 1 og , and coefficient of friction are unknown. However, realistic estimates can usually be determined and the effect of different values for these parameters can be determined to arrive at a realistic load carrying capacity for a given skyline operating over a particular terrain.

The computer program presented is as easy to use as the Skyline Analysis Program, which does not consider log drag. If this type of analysis is considered to be too sophisticated, or it is felt that realistic estimates of the parameters cannot be found, then this type of analysis can be used as a comparison to demonstrate the difference in payloads which can occur from using a flying payload and a correction factor of 1.5 , or a flying payload for a dragging log.

APPENDIX

## SKYLINE ANALYSIS PROGRAM WITH LOG DRAG USERS GUIDE*

This program inputs profile data, inputs cable system geometry, determines skyline payloads, mainline tensions, and skyline tensions including the effects of a dragging $\log$ and the $\log$ and ground geometry.

## ASSUMPTIONS AND LIMITATIONS

1. The effects of line stretch are neglected.
2. The maximum allowable tensions are assumed to occur at the headspar. For downhill yarding, the skyline and mainline tensions may be greater at the tailspar and the carriage than the values input for the maximum allowable tensions.
3. The horizontal distance from the carriage to the end of the log must be less than the distance between terrain points, for a terrain point to be analyzed.
4. The program assumes the choker is attached 2 feet from the end of the $\log$ and the center of gravity of the $\log$ is located in the center of of the log.
5. The loaded cables are assumed to be rigid links. This error is generally small for taut cables. If low tensions occur an error check such as Carson's (1) HP 67 error in rigid link program should be used.

[^0]6. The minimum $\log$ to ground distance used in the program is the distance perpendicular to the ground to the top of the front end of the $\log$.
7. The choker length used in the program is the distance from the carriage to the top of the log.
8. When a negative tension occurs the payload is in error.

GENERAL OPERATING NOTES

1. All data is input in response to visual prompters. If more than one piece of data is requested, the pieces of data must be separated by a comma.
2. All data is entered into the program by pressing EXECUTE. Always check the display before pressing EXECUTE; because what you see is what you get.
3. All spar locations are referenced by Terrain Point Numbers and fractions are acceptable.
4. Loads are calculated only at those points the user defines when responding to the prompter "TERRAIN POINT STEP SIZE." For example, if the user inputs "1", the payload is calculated at each terrain point between supports. For "2", every other point is calculated, for "3", every third point, and so forth.
5. Terrain data from the digitizer is entered using the method developed by Carson in PNW-31. Special Function Keys $0-4$ correspond to those functions in PNW-31. Several applicable pages from PNW-31 are attached.
6. When analysis of any profile has been completed, a new profile can be generated by pressing a Special Function Key.
7. If the user makes an input error at any time, the system will recover if the Special Function Key corresponding to the particular operation is repressed and the data re-entered as requested by the display.
8. The analysis program assumes the yarder is on the left.
9. Visual prompters requiring a "yes" or "no" answer require use of " 1 " or "0".

The Skyline Analysis Program with Drag actually consists of two separate computer programs.

The first program enters and stores profile data and yarder specifications. The profile data is stored on the auxiliary cassette, and the yarder specifications are stored on the main cassette along with the computer programs. Once the yarder specifications and profile data are stored on the cassettes they can be entered from the cassettes, and the data does not have to be re-entered when used more than once.

The second program is for analyzing the profiles, determining the allowable loads, mainline tensions, and the skyline or haulback tensions. This program uses the yarder specifications and profile data previously stored on the cassettes.

Figure A shows a copy of the special function key overlay for both of the programs. The descriptions above the special function keys refer to the profile input program. The descriptions below the special function keys refer to the skyline analysis program. For example, special function key $f_{0}$ is for entering data from the digitizer in the profile input program and for entering a new profile from cassette tape in the Skyline Analysis Program with Drag.


Figure A.- Special Function Key Overlay.

In the profile input program, special function keys $f_{0}$ through $f_{4}$ are for entering profile data from a contour map using the digitizer. Special function key $f_{5}$ is for reversing a profile. Special function key $f_{6}$ is for storing a profile once it has been entered. Special function keys $f_{7}$ and $f_{8}$ are for entering profile data by $X, Y$ coordinates and slope distance, percent slope data respectively. Special function key $f_{9}$ is for entering and storing yarder specifications. These profile inputs and computer programs are essentially the same as the ones used in the Skyline Analysis Program (Sessions, 1978). However, the programs were all slightly modified to simplify the input and storing of the profiles.

In the Skyline Analysis Program with Drag special function key $f_{5}$ enters the program inputs, analyzes the data, and prints the outputs. Once the first profile has been analyzed, special function keys $f_{0}$ through $f_{4}$ and $f_{6}$ through $f_{8}$ are used to change the inputs specified by the user. Once the inputs have been changed, special function key $f_{5}$ is used to analyze the data. For example, after the first profile has been run using special function key $f_{5}$, special function keys $f_{0}$ and $f_{5}$ could be used to change the profile data and the carriage weight before analyzing the data using special function key $f_{5}$ again. The yarder data, log and choker data, tailspar height, log clearance and terrain. point step size would all remain the same and would not have to be input again. If all new data is required for the next analysis after the first profile is run, then special function key $f_{7}$ would be used before using special function key $f_{5}$ again. Special function key $f_{9}$ gives a listing of the profile data.

The following example problem demonstrates the use of this program. When entering a different profile the same general procedure should be followed.

## Example

User Instructions
The following example demonstrates the use of the program.

1. Place plotter paper on the plotter, switch it "on" and engage the "chart hold" key.
2. Set the plotting limits.
3. Place the program cassette into the cassette transport on the calculator. Be absolutely certain that the front of the cassette, which is labelled, faces outward.
4. Place the data tape into the peripheral unit, switch that unit "on".
5. Press the REWIND button for that unit.
6. If terrain data is to be entered from a map, then switch on the digitizer and tape map on digitizer surface.
7. Switch the calculator and the printer "on". Press the REWIND key on the calculator.
8. Press the SCRATCH A and EXECUTE keys.
9. Press LOAD and EXECUTE keys.
10. Press RUN and EXECUTE keys.
11. All user inputs are entered by typing the input on the keyboard and pressing the EXECUTE key.
12. Continue with the procedure outlined in the following table by responding to the visual prompters with the numerical entries indicated in the middle column. The descriptions should be read for an understanding of the process.


Figure B.-Contour map.

Input Explanation for the Example Problem

| VISUAL PROMPTER ON DISPLAY | KEYBOARD RESPONSE | DESCRIPTION |
| :---: | :---: | :---: |
| GO TO SPECIAL FUNCTION KEYS | $\mathrm{f}_{0}$ | Selects digitizer input of the profile. |
| MAP SCALE (FT/INCH)? | 200 | Enters scale of the map being used. |
| CONTOUR INTERVAL (FT)? | 40 | Enters contour interval of the map being used. |
| HORIZONTAL GRAPH LIMITS (FT)? | 2000 | Enters scale value for $X$-axis on plotter. |
| PROFILE NUMBER? | 1 | Enters number of profile to be plotted. The profile number must be between 1 and 100. |
| DIGITIZE FIRST POINT AFTER BEEP. |  | (DIGITIZER RESPONSE): Set origin and digitize first point on the profile. |
| SELECT A SLOPE AND PROCEED. | $\mathrm{f}_{3}$ | Executes program on function key $f_{3}$ which anticipates downhill profile. <br> (DIGITIZER RESPONSE): Digitize all downhill points (2 through 15). |
|  | STOP |  |
|  | $\mathrm{f}_{2}$ | Executes program on function key $\mathrm{f}_{2}$ which anticipates level profile. <br> (DIGITIZER RESPONSE): Digitize level section (points 16 and 17). |
|  | STOP |  |
|  | $\mathrm{f}_{4}$ | Executes program on function key $f_{4}$ which anticipates fractional contour interval. |


| VISUAL PROMPTER ON DISPLAY | KEYBOARD RESPONSE | DESCRIPTION |
| :---: | :---: | :---: |
| FRACTION (+FOR UPHILL; -FOR DOWN)? | +. 5 | (DIGITIZER RESPONSE): Digitize next contour (point 19). |
|  | STOP |  |
|  | $\mathrm{f}_{1}$ | Executes program on function key $\mathrm{f}_{1}$ which anticipates uphill profile. <br> (DIGITIZER RESPONSE): Digitize remaining uphill points (points 20 and 24). |
|  | STOP |  |
|  | $\mathrm{f}_{6}$ | Stores the profile in the auxiliary cassette. The profile is stored in the file corresponding to the profile number. |
|  | $\mathrm{f}_{9}$ | Executes program to enter and store the yarder specifications. |
| YARDER NAME? | $\begin{aligned} & \text { SKAGIT } \\ & \text { BU-739 } \end{aligned}$ | Enter the yarder name. |
| ALLOWABLE SKYLINE TENSION (LBS) : | 53300 | Enters the allowable skyline tension. |
| ALLOWABLE MAINLINE TENSION (LBS)? | 34500 | Enters the allowable mainline tension. |
| ALLOWABLE HAULBACK TENSION (LBS)? | 0 | Enters the allowable haulback tension. |
| ALLOWABLE SLACKLINE TENSION (LBS)? | 0 | Enters the allowable slackline tension. |
| SKYLINE WT (LBS/FT)? | 2.89 | Enters the skyline weight per foot. |
| MAINLINE WT (LBS/FT)? | 1.85 | Enters the mainline weight per foot. |
| HAULBACK WT (LBS/FT)? | 0 | Enters the haulback weight per foot. |
| SLACKLINE WT (LBS/FT)? | 0 | Enters the slackline weight per foot. |
| HEADSPAR HT (FT) ? | 100 | Enters the headspar height. |
| STORE YARDER IN FILE \# (4-20)? | 4 | Stores the yarder specifications in file 4. |


| VISUAL PROMPTER ON DISPLAY | KEYBOARD | DESCRIPTION |
| :--- | :--- | :--- |
|  | RESPONSE |  |

Special function keys $f_{0}$ through $f_{9}$ should be used until all of the profiles and yarder specifications that are to be analyzed are entered. The next few steps enter the Skyline Analysis Program with Drag which analyzes the profiles and yarder specifications stored on the cassette tapes.

|  | SCRATCH A | Erases all program lines and data from the calculator memory. |
| :---: | :---: | :---: |
|  | LOAD 2 | Loads program from tape. |
|  | RUN | Initializes the program. |
| GO TO SPECIAL FUNCTION KEY $\mathrm{f}_{5}$ | $\mathrm{f}_{5}$ | Executes the program to analyze the data. |
| LIVE-1, STAND-2, BOTH-3, RUN-4 SKY? | 2 | Selects type of skyline (3 selects both a live and standing skyline for analysis). |
| LOAD YARDER DATA FROM FILE \#? | 4 | Loads yarder data from file 4. |
| PROFILE NUMBER? | 1 | Loads the profile data from file 1. |
| WANT PROFILE PLOTTED? | 1 | Executes plotting of profile. |
| CARRIAGE WT (LB)? | 1000 | Enters the carriage weight. |
| TAILSPAR HT? | 50 | Enters the tailspar ht. |
| HEADSPAR T.P. \#, TAILSPAR T.P. \# | 1, 24 | Enters the terrain point numbers for the location of the headspar and tailspar. |
| WANT DATA PLOTTED? | 1 | Executes plotting of the data. |
| INNER YARD LIM, OUTER YARD LIM? | 1, 24 | Enters the yarding limits between which the payloads are calculated. |
| LENGTH OF CHOKER (FT) ? | 12 | Enters the length of the choker from the carriage to the top of the log. |
| LENGTH OF LOG (FT)? | 32 | Enters the length of the $\log$. |


| VISUAL PROMPTER ON DISPLAY | KEYBOARD <br> RESPONSE | DESCRIPTION |
| :--- | :--- | :--- |
| MIN LOG TO GROUND CLEARANCE? | 5 | Enters the minimum clearance between <br> the top of the front end of the 10 g <br> and the ground. |
| TERRAIN POINT STEP SIZE? | 1 |  |

The program then analyzes and prints out the data. If only a portion of the data is to be changed for the next analysis, special function keys $f_{0}$ through $f_{4}, f_{6}$ and $f_{7}$ can be used to change the desired information. For example, if we wanted to change the tailspar height and the carriage weight, the following steps would be used.

|  | $\mathrm{f}_{2}$ | Selects changing of the tailspar. |
| :---: | :---: | :---: |
| TAILSPAR HT? | 30 | Enters new tailspar height. |
| HEADSPAR T.P. \#, TAILSPAR T.P.\# | 1, 24 | Enters new spar locations. |
|  | $\mathrm{f}_{6}$ | Selects changing of carriage weight. |
| CARRIAGE WT? | 600 | Enters new carriage weight. |
|  | $\mathrm{f}_{5}$ | Executes analysis of the data. |
| LIVE-1, STANDING-2, BOTH-3, RUN-4 SKY? | 2 | Enters type of skyline. |
| WANT PROFILE PLOTTED? | 1 | Executes plotting of profile. |
| WANT DATA PLOTTED? | 1 | Executes plotting of data. |

Figures C, D, E, and F show the outputs for this example problem.

| MAF SCALE $=20$ COWTOUR INTEFWH |  | FEF: INOH FEET |  |
| :---: | :---: | :---: | :---: |
| FROFILE NHMEER: FGINT | $\frac{1}{\operatorname{SFFN}}$ | ELEW OIFF FROM | PTI |
| 1 | $\square$ | $\square$ |  |
|  |  |  | DOLHPHILL SLOFE |
| $\Sigma$ | 158 | -46 |  |
| 3 | 224 | -80 |  |
| 4 | 346 | $-120$ |  |
| 5 | 416 | -160 |  |
| $E$ | 496 | -260 |  |
| 7 | 578 | -249 |  |
| 8 | 654 | -280 | - |
| 9 | 692 | -329 |  |
| 16 | 726 | - 380 |  |
| 11 | 775 | -463 |  |
| 12 | 824 | -449 |  |
| 13 | E56 | -489 |  |
| 14 | 9 Ec | -520 |  |
| 15 | 10.5 | -560 |  |
|  |  |  | LEVEL ELOPE |
| 16 | 1167 | -5684 |  |
| 17 | 1241 | -569 |  |
|  |  |  | FFACTIUNAL IRGFEMENT $=-20$ |
| 13 | 1325 | -560 |  |
|  |  |  | FFAETICMAL INEEEMENT $=2 \mathrm{E}$ |
| 19 | 1397 | -560 |  |
|  |  |  | UFHILL SLOFE |
| 2 E | 1485 | -520 |  |
| 21 | 1517 | -4E0 |  |
| 22 | 1549 | -449 |  |
| 23 | 1575 | -489 |  |
| 24 | 1607 | -360 |  |

EKTLINE
MFINLINE
HFHILEFHEK
SLACKLIAE

| FLLGMFELE |
| :---: |
| 55000 |
| 34560 |
| 0 |
| 8 |

LIME WEIGHT
2. 89

1. 85
E. 60
Q. 60

HEAOSFAE HT $=100$

T＇HREDER SFECS．－EKAGIT EU－TEG

|  | HLLOHAELE LOAD | LIME WEIGHT |
| :---: | :---: | :---: |
| EKTLINE | 5 Sc | 2． 89 |
| MAINLINE | 34506 | 1． 5 |
| HRULLEEACK | 0 | 日． 60 |
| SLFICKLINE | $\underline{\square}$ | 6． 6.10 |

HEADSPAR HT $=160$

| Profile 1 |  |  |
| :---: | :---: | :---: |
| CAFPRIFEE HT＝ | 1600 | TAILSFFF：HT＝ |
| HEADSFHE T．P．$=$ | 1 | THILSFAR T．F．$=$ |
| Irdd CrARD LIM＝ | 1 | DUIT T＇AFSO LIM＝ |
| LETGTH OF CHOKER＝ | 12 | LENGTH OF LiGu＝ |
| MIM LOIS TO GREDUND | CLE |  |
| TEFRRAIM FOINT STEF | F＇SIZ |  |



| TEFPRIN FOIHT | $\begin{aligned} & \mathrm{HOFE} \\ & \text { OIST } \end{aligned}$ | MAN LOIG LOAD | EK＇LITNE TENSION | MAIRLINE TENEION | CAFPIFIE CLEARANEE | LOG TG GROURN FRGLE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2． 0 | 158 | 45977 | 53.606 | 20543 | 16． 20 | 12． 39 |
| 2． 5 | 224 | 20967 | $5 E 56$ | 18265 | 27．5s | 22． 59 |
| 4．${ }^{\text {a }}$ | 346 | 24981 | 53560 | 14216 | 2S． 02 | 23．15 |
| 5．$\square^{\text {a }}$ | 416 | 17990 | 5356 | 8615 | 56． 58 | 43.99 |
| E． 6 | 496 | 14612 | 5350 | 5279 | 56.58 | 64． 64 |
| 7． 9 | 578 | 13760 | 5936 | 477 | 65． 59 |  |
| E． | E54 | 12216 | 53200 | 4424 | 83． 7 | 43.51 |
| 9． 9 | 69 | 12 ET 7 | 5500 | 427 E | 113.28 | 4 C .36 |
| 16． 9 | 72 F | 12もア6 | 53200 | 4161 | 144.13 | 51.34 |
| 11．${ }^{\text {a }}$ | FTE |  | 53506 | 4 Ca | 171． 21 | 50.19 |
| 12．${ }^{\text {a }}$ | 8 c 4 | 12649 | 53509 | SES1 | 199.2 | 36． 83 |
| 13． 0 | 85 | $126 \leq 1$ | 5326 | 3063 | 231． 44 | 60.95 |
| 14． 8 | 9こ5 | 12695 |  | 3649 | 2548 | 72.3 |
| 15． 9 | 165 | 13174 | 5 ESW | 5429 | 268． 25 | 96． 80 |
| 16．${ }^{\text {a }}$ | 1167 | 14121 | 5586 | 5296 | 247.76 | 96． 80 |
| 17．${ }^{\text {a }}$ | 1241 | 15145 | 5360 | 365 | EsE． $\mathrm{E}_{1}$ | 76． 61 |
| 130 | 135 | 16959 | 5356 | 2769 | 244.96 | 105.52 |
| 19．9 | 1397 | 1956 | 5356 | 24.5 | 217． 95 | 114．44 |
| 2 2． 9 | 148 | 2456 | 53560 | －2455 | 174.94 | 141． 34 |
| 21． | 1517 | Eser | 53360 | － 760 | 134． 6 | 141． 34 |
| 22． 9 | 1549 | 5］es4 | 53560 | －6878 | 97.15 | 146.93 |
| 2 E | 1575 | 4 A 43 | $5 \times 64$ | $-13496$ | 61.5 | 141． 29 |

Figure D．－Output for the example problem．


Figure E.- Output for the example problem.

ETANDING EKTLINE LOAD RNFLTEIEGEIGID LIAK ASEUAFTION

| TAFDEE SFECS．－SKHIIT EUM－ |  |  |
| :---: | :---: | :---: |
|  | FLLOURELE <br> LDAD |  |
| SkiL If | 5300 | 2． 6 |
|  | 34506 | 1． 85 |
| HAILEACK | E | E． 6.9 |
| GLFICELINE | 0 | ©． 0.0 |

HEADSFAF $H T=106$

| FROFILE 1 |  |  |
| :---: | :---: | :---: |
| CAFERIAGE MT＝ | 660 | TAILSF＇HR HT＝ |
| HEADSF＇RF：T．F．＝ | 1 | TAILSF＇HF：T．Fi，$=$ |
| INN TAFED LIM＝ | 1 | BUIT＇THRD LIM＝ |
| LENTTH OF CHOKEE： | 12 | LEPMETH OF Linio |

MIN LOG TG GROURD GLEARFRGE $=5$
TEFRAIA FOINT STEF EIZE＝ 1


| TERFAIN FOIPNT | $\begin{aligned} & H O R Z \\ & D I \cong T \end{aligned}$ | $\mathrm{MH} \% \mathrm{LOT}$ LUAD | EK＇TLIME <br> TENETIDN | MAINLINE TENSION | EAFRIATE GLEAFIFRE | LOIS TO GEOUND FRGLE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2． 5 | 158 | 44573 | 53360 | 36145 | 1E． 20 | 12．39 |
| 3.4 | 224 | 30004 | 5350 | 1835 | 라． $\mathrm{g}^{2}$ | 31． 50 |
| 4． 5 | 346 | 25501 | 5 Sc 0 | 1480 | 21． 5 | 20.48 |
| 5． 9 | 416 | 18T0s | 5 Sc 0 | 9835 | 54．13 | 43.63 |
| 6 | 496 | 14521 | 5350 | 5977 | 47． 26 | E4．E05 |
| 7．9 | 59 | 13596 | 5350 | 4792 | 61． 35 | 62.27 |
| 9． 6 | 654 | 13159 | 5 5 510 | 4.54 | 7e． 6 E | 43． 51 |
| 9.6 | 692 | 12965 | $5 \mathrm{SE0}$ | 4315 | 107． 76 | 4星 36 |
| 16． $0^{10}$ | 7 SE | 12 E 7 | 5950 | 4264 | 133． 19 | 51． 34 |
| 11． 9 | アTE | 12682 | 53500 | 4060 | 164． 61 | 519 |
| 12． 0 | 824 | 12006 | $5 \mathrm{5c} 0$ | 3941 | 192． 53 | 58． 88 |
| 12．${ }^{\text {a }}$ | 556 | 12563 | 53506 | 2ecs | 293 Es | 60.98 |
| 14．${ }^{\text {a }}$ | 929 | 12645 | 53500 | 3729 | 246.25 | 72． 39 |
| 15．9 | 1095 | 13113 | 53569 | 3596 | 25s． 92 | 90． 90 |
| 18．0 | 1167 | 14645 | 53506 | 3 364 | 295． 9 | 96． 0.0 |
| 17． 9 | $1 玉 41$ | 15649 | 5336 | －224 | 29317 | 76.61 |
| 19． 9 | 1225 | 16S6 | 5356 | $299 \%$ | 230． 85 | 165．5 52 |
| 19．6 | 1397 | 19 ec | $5 \leq 56$ | 26.47 | 262.76 | 114． 44 |
| 26． 9 | 1485 | $24 E 43$ | 5296 | 2094 | 157． 3 | 141． 3 |
| 21． 9 | 1517 | 28143 | 5 SE 5 | －3こ11 | 117． E | 141． 34 |
| 22． | 1543 | SE495 | 5 SE | －E1E日 | 79． 8 | 146.96 |
| 23． 9 | 1575 | 46446 | 5350 | －12449 | 43． 11 | 141.29 |
|  |  |  |  |  |  |  |

Figure F．－Output for the example Problem．

APPENDIX

## PROFILE INPUT PROGRAM

There is one main program and ten subprograms in the profile input program. The following is a listing of these programs:

## MAIN PROGRAM




```
EG FFIIMT
```



```
*& FFITIT
EQ LIND KEET I
70 [1=6
BQ OISF "GO TG SFEEIFL FIHNOTIONKE'\Xi";
#0 ETOF
1EG ET|E
```

```
SED G
    OL=E THEN EM
    \XiF "NE|& MFF SFECE";
IFIIT DI
OL=E THEN 1EIE
SF" "MFF EGFLE &FT,IPNHO":
|FIIT H
EF "LIDNTGILP IPTEFMFL &FT`";
|FUIT E
FFINT
#FINT "NAP SEFLE = "H" FEET FEE: IPNH"
#FIINT "GINTGLFE INTEFP"HL = "L" FEET"
FFOINT
OL=1
OISF" "FFOGFILE R|MEEFOE-GG%";
IPNFUT PNE
[I\XiF "HBFZ GFHFH LINIT&FT:";
ITFPIT F
```



```
FEH
OFFEET E. 1%%E. E. EF:%%G
FLOT 0.E, -ق
FLLGT E. E. 1
LFEEL &&, 2,1.7.0.7,11?
EFLGT G.:
LFEEL i;: E.1.7.E,TM13PE
FLOT Q.E.1
LHEEL &:, 1, 1. P. E, F,11%
EFLOT B, -こ
LAEEL ध%:1.1.F.E.F.11%"1"
GFLGT E, ב
\Xi1=EQ=E = N1=0
```



```
FEINT
```



```
LIEF "QIGITIEE FIF゙ST FGIVT HFTEF: EEEF"" .
HFIT EENG
WFITE &G,:%
ETTTEF: &.:%%1.'1
RM=$|+1
FFIRT N1, E.E 
U[N1]=5
4[41]=56004
DISF "SELECT H ELEFE FPD FFOMEEED":
ETGF
ErdC
```


## PROGRAM ON $f_{1} K E Y$

```
E F1=1
T FRINT THE4G"BFHILL SLOFE"
OLITE (G):%
G ENTEF <9.*2R2.''%
\12=N1+1
晾 <=%-%1
'日 'т'`'%'2-r'1
```



```
S1=51+5
EME E:=E: + H1:+C
10 E=E1-E5
|g |[N1]=51
<30 U[ N1]=$[1]+E
L4g FRINT N1.E1,E
L5M FLOT S1, E. 2
LEG LAEEL &*, 1, 1. T. E. T,11)
1TG EFLOT -1:-2
LEG LAEEL &%,1,1.7, 6,7,11)N1
19G GFLOT 1.3
2001%1=82
21日 'r1='r'%
220 10T0 20
236 END
```

PROGRAM ON $f_{2} K E Y$

```
10 F1=0
2@ FPINT TFE:4G"LE'MEL SLGPE"
SE HFITE &G,*%
40 ENTEF: 69, +%)2.'r'
```



```
60 %=2-%1
TG 'T='r'E-'T'1
```



```
90 S1=51+5
1601 E 1=E1+F1:+C
1.1E E=E.1-E0
120 |[N1]=51
136 U[N1]=V[1]+E
140 FRINT N1. E1.E
1501 FLOT S1.E,2
1E0 LAEEL (*, 1, 1. 7, 6, 7,11)
1TG CFLGT -1.-2
1EE LFEEL {+, 1.1.7.6.7.11\N1
190 EFLGT 1.3
200 81=%2
210 'r'1='r'2
20日 BiOTG 36
205 EN[
```

```
10 H1=-1
2G FFINT THEAG"DGHNHILL ELOFE"
S@ WFITE G%:* 
4 0 ~ E M T E F ~ \& G ~ * \% M E , 4 2
56 N N = N 1 + 1
60 %=%2->1
T0
O0=51,0%4+%+4:+4%:H
90 E = =1+5
1010 E1=E1+F1:+E:
11E E=E1-EG
125 U[ MN1]=51
125 U[N1]=4[1]+E
140 FPINT R1: E1.E
15G FLOT E1, E:2
1EG LHEEL &%,1.1. ;, E, 7,11)
1FG EFLIT -1.-E
13G LHEEL &*,1.1.7.G.7.11)N1
1GE GFLIT 1. 2
2040 % =92
210 Ч1=な2
2Eg GINTG SG
2EG ERO
```

PROGRAM ON $\mathrm{I}_{4} \mathrm{KEY}$


```
EG IMFUIT F1
30 E:1=F1:NL
4E FF:INT THE4G"FREHETIGNHL IPNFEMENT="EI
EG WFITE &F, t%
6G ENTEF: &. +%XO, 'TE
FE NM=N1+1
EG %=%-41
90 'T'='T'2-'T'1
```



```
110 31=51+5
120 E1=E1+H1:+C
1ZE E=E1-EG
140 |[[M1]=51
150 }\because[||]=\because[1]+
1ES FFINT NL,E1.E
1FE FLDT E1, E Z
1ES LHEEL &+1.1. . . F, 11)
150 EFLOT -1.-2
EEG LHESL &%,1.1. F.E.F.11\N1
219 EFLOT 1: 
z-6 O1=%2
```



```
24日 B1OTD 50
ES END
```


## PROGRAM ON $\mathrm{f}_{5} \mathrm{KEY}$

```
10 FINEO G
20 FOE I=1 TG N1
304 E[I]=u[I]
40 [1] [=4[I]
50 NEKT I
60 U[1]=0
70%[1] ]=W[N1]
G0 FOR I=2 TO N1
96 U1=6[N1+2-I ]-G[N1+1-T]
106 41=N[N1+2-I]-0[N1+1-I]
1.1[ U[[1]=1[[ I-1]+U1
120 v[1]=v[I-1]-4
13Q NE%T I
146 DIEF "FFOFILE NUMEER(E-99)";
150 INFIT NS
160 FOR I=\N1+1) TO 50
176 U[I]=[0
189 ध[I]=0
190 NEKT I
2GU FOR I=1 TO 50,
21E [[I,1]=U[!] ]
2こ日 2[I.2]=V[I]
25日 RENT I
24G STORE DHTA #S.NS. 2
ESM ENO
```

PROGRAM ON I6 KEY
16 FOR $I=C N+1$ ）TG 5
$20 \mathrm{H}[\mathrm{I}]=0$
36 6［ I $]=0$
46 NE K I
$5 \mathrm{FOF} I=1$ TG 50

7日 2［I，2］＝w［I］
BG NEKT I
G6 STGFE DHTA \＃5．NS， 2 16G ERD

## PROGRAM ON $f_{7}$ KEY

```
10 DIGF "FFOFILE NHEER(Q-GG)":
20 INFUT NE
3G FRINT
4E FFINA "FFOOFILE",NE
SG PRINT
GQ DISF "HORZ GEFFH LIMITCFT)";
TG INFUT NG
```



```
90 FEM
1G0 OFFSET E. 1%%G, 0. 65%%G
119 FLOT E, 日, -2
120 FLOT 0, 0, 1
120 LAEEL (%,2,1.7, 8,7,11)
14G EFLGT E,2
150 LFEEL <%,2.1.7.0,7,11)NS
1EQ PLOT G.E.1
170 LFBEL &*, 1.1. 7. ©.7.11)
18G EFLRT E, -2
130 LFBEL (*, 1.1.7.6,711)"1"
204 EFLOT Q,3
216 FFIINT "TEFRAIN"
22G FFINT " FOINT * CINED ' EDORD"
2SE PFIINT
24g 0IGF "INITIFL ETATION, INITIFL ELEV";
25E INFUT F1. HE
260 N1=1
2TG PRINT N1, F1, FE
28Q IEN1J=F1
296 4[N1]=F2
S0日 DISF "ENTER %'т";
31日 INFUT <, 'T
Seg N1=N1+1
350 U[H1]=%
34g v[N+]=''
356 HG=%-F1
305 4'9=ヶーH2
30 FRINT M1.%'t
305 LAEEL (*, 1, 1. 7, 6, 7,11)
Sg FLGT HO, %G, 2
40日 EPLOT -1,-2
419 LFEEL &*, 1, 1. 7, 6, %,11,M1
420 CFLOT 1, ב
430 GOTO 306
44ETIF
450 END
```

```
19 LIGF "FROFILE NOMEERCQ-G%`":
20 INFIIT NE
30 FFEIHT
40 FEINT "FFODFILE", NE
5 6 ~ F F I N T
EQ DISF "HORZ GEAFH LIMIT&FT";
TO IPPUIT %O
80 SCALE 0, 1. 2+%G, 0, 1. 2*%0
09 PEM
106 OFFSET E. 1*%G.6. ESN%G
110 FLOT E. E. -2
120 PLOT E. 6.1
130 LHEEL (%,2.1.7.6,7,11)
146 CFLOT G. 2
156 LAEEL <%,2,1.7.8.7,11)NE
1 0 0 ~ P L O T ~ E . ~ G . 1 ~
170 LAEEL (*: 1, 1. 7, 6. 7,11)
1BQ CFLOT 日, -2
190 LFEEL (%,1:1. F, 0, 7,11)"1"
20G EFLOT G. S
21G PRINT "TEFREAIN"
2SG FRIMT " FOINT & GODRD G GODRE ELOFE DIST * SLOFE"
20 PFEINT
246 DIEP "INITIAL STATION, INITIFL ELEW";
25G INFUIT F1, HE
250 M1=1
2T0 FRINT N1, F1. FE
200 U[N1]=F1
290 v[ &1]=R2
20日 'r'1=H2
310 %1=F1
300 DEG
3SG DISP "SLOFE DISTFNDE. PEFGENT SLOFE ";
240 IPFIIT E.P
S50 N1=N1+1
3E日 F1=HESCP),160
37日 A=ATM(F%1)
30日 &=Ew60SG%
S90 'T=5+EIN(G)
400 IF FDG THEN 420
410 Y=-%
42E %1=%1+%
43日 'r'1='1'4'r
440 |[ N1]=%1
456 リ[N1]='4
4E日 FRINT NL,%1, YL.S.F
47E HG=%1-H1
40日 !G='1-R2
496 LAEEL &*, 1, 1. 7. 1. 7.11)
SGE FLIT HE, W9,Z
S10 EFLOT -1, -2
```



```
50 CFLOT 1, E
546 GOTO SSG
550 ETGF
560 ENDD
```


## PROGRARI ON f $f_{9}$ KEY

```
10 STARNDHFD
20 DIEF "'TARDEF NAME";
30 INFUIT %:$
4 9 ~ F R I N T ~
50 FFINT ''$
60 DISF "ALLOWHELE SKYLINE TENEION(LEES";
TO INFUIT T1
EG OISF "FLLOWAELE MAINLINE TENEIOWGLES`";
90 INFUTT TZ
100 OISF "FLLOWAELE HAULEAEK TENEIONGLE'E";
110 INFIIT TZ
120 DISP "FLLOWHELLE ELFCKLIRE TENEION LEE";
13日 INFFIT TE
149 OIGP "EKTLINE HT &LESGFT)":
15G INFUTT WI
1EQ DIEP "MAIMLINE HT &LESFFT`";
170 INFUT WS
1BG DISP "HFIILEACK HT &LEE,FFT)";
190 INFUT W2
2GQ DIGP "GLFCKLINE MT &LESGFT)";
21日 INFIUT WE
22G FF:INT
2S日 FK:INT " FLLOWHELE LINE"
24G FRI&T " LOAD WEIGHT"
250 WFITE &15, 2G0%T1, H1, TE,WS
```



```
2TG HRITE 《15, 2GOT2, ME, TE, W口
```



```
290 DISF "HEADSFRF HT &FT)";
304 INFUTT HE
316 FEINT
SEQ FRINT "HEADGFHF: HT="HG
3SG DIEF "ETURE TAFOER IN FILE#(4-2G)";
346 INFUTT N
35日 STORE DHTA M
364 END
```


## A P P ENDIX

## SKYLINE ANALYSIS PROGRAM WITH LOG DRAG

There is one main program and ten subprograms in the Skyline Analysis Program with log drag. The following is a listing of these programs:

## MAIN PROGKAM




```
30 FRINT
```



```
54 FRINT
GS LOFD KE'T S
70 11=6
GE DIEF "GO TO EFEGIAL FINOTION KE'T FE";
50 STOF
1E0 EPN
```


## PROGRAM ON $f_{0} K E Y$

```
10 FI%ED E
2G DIEF "FFOFILE NUMEER";
30 IAFUST FI
4G LOHD DHTA #5, F.L.Z
50 FOF: I=1 TO 56
6日 <[I]=2[I.1]
7G Y[I]=Z[I, Z]
8G NE:T I
90 N1=1
10n FOE I=2 TO 5,4
116 IF X[[I]=6 THEN 146
120 N1=I
1SG NE:T I
140 I1=2
1SG DIEF "IO TG SFECIRL FUNOTION KE'T FS"
1EG END
```

PROGRAM ON $f_{1} K E Y$

19 DIEF "LORD 'TARDEF DATA FFOM FILE\#":
29 IPFUT FI
SG LORD DATA FI
4ब DISF "GO TO EFEGIFL FINETIGN KE't FS"
56 Eld

PROGRAM ON $\mathrm{f}_{2} \mathrm{KEY}$
10 DISF "TAILSFAR HT":
20 INFYIT $\mathrm{HT}^{7}$
3 IISF "HEADSFAF T. F. \#. TAILSFAF: T. F. \#":
$4 \mathrm{~S}^{1}$ IPFUT S1. S2
56 DIGF "GUT TO SFECIFL FUNLTION KE'T FS"
ES ERID

G DISF＂LENGTH GF LGHEFT：＂；
E INPUT LZ
E［ISE＂LEPGTH OF EHDKEFEFT）＂；
6 IPAFIIT LI
0 OIEF＂GQ TQ EFEEIAL FUNETIDR KE＇T FE＂
E ENO

PROGRAM ON $f_{4} K E Y$
－DISP＂LCG TO GEGUND CLEAPRPNE＂；
SG IAFITT C
：DISP＂TEREIAR FGINT STEF EIZE＂；
HE IPAPUT SE
G DISP＂GQ TG GFECIAL FLNNTION EE＇T FE＂
㴙 END

PROGRAM ON $\mathrm{I}_{5}$ KEY

```
1酉 GARIDHFD
2G OEG
玉O 0-=こ
40 F=ES=6
56 RT=%
EC 144=9604040
7G U=互昌
B6 F4=1
BC E:B=6 S
GG FFIMT
10日 FRITHT
```



```
1工G IPAFUIT F:
```




```
156 EOTG 2gQ
```



```
1P日 G070 2-6
```



```
AGE GOTG 2-G
```



```
210 F4=?
2ge IF IM#0 THEN 2ed
2OG [ISF "LEIFD 'HFEDE: DHTH FFODH FILE#":
E4E IPFFIIT FI
FEG LDHE OHTA FI
Z回 FFIHT
ZTQ FCITMT "'T'HFDEF: SFER'S. -"'r'$
ZEG FRIMT " FLLQMAE:LE LINE"
2G日 FF:INT " LENE
|EITHT"
```




```
:ZG HF:ITE (15, STOTO. HE, TE, HM
```



```
4G FRINT "HEFDEFFF: HT="HE
SG IF I\##G THEN SEO
GB DIGF "PROFILE NUMEEF";
TG INFUTT F"1
SG FEINT
GG WFITE &1E, 4EGOF1
HEG FOWMAT "FFOFILE".FES
#10 IF I1#日 THEN 5ces
FGG LOHD DATA #5,FH.Z
FSG FOE I=1 TO 5G
44@ %[[I]=2[I:1]
450 T[[I]=Z[I, こ]
46@ NE%T I
470 N1=1
4E0 FOR I=天 TO 50
490 IF X[I ]=0, THEN 520
#ano N1=I
#10 NEMT I
SEQ DISP "UFNT FROFILE FLQTTED";
EEG IMFUT FS
```



```
55日 G1=G9='[1]
SGQ FGF: I=E TO N1
50E IF T'LIMIN THEN 5GQ
50% E1='r[ I]
Sge IF P[CI]CGE THEN EIE
EGG [G=t[I]
G1G NEMT I
G09 G3=FES(%[M1]-M[1])
ES G4=1. 2$03
640 B5=1. 2*40-61+156)
ES IF (8*G4,10,5)<05 THEN E00
6% B5=54%6,10.5
Grg GGTO EOG
ESQ G4=55%10. 5%%
E06 65=$[1]-64-13%)%
T00 6T=61-65-62+61-156),2
P1G EOFLE GE,GE+G4, G7:GF+GS
#g FLol <[1], '[1].1
TSG LHEEL &*, 2,1,7, 5, T,11)
T4E EFLOT Q.2
F5G LFEEL <*, 2, 1. 7, 5, 7,11)F1
GEG FLOT X[1]. Y[1].1
TFG LAEEL (+, 1, 1. 7, E, 7,11)
TE CFLOT -G. 3, -2
FG0 LFEEL (*, 1.1.7.6.7M1)"1"
```



```
BLG FOR I=E TO N1
E<G FLOT X[I ]. 'r[ I ]. 2
BGG EFLOT -1:-2
E46 LAEEL (*,1,1.7, 6, 7,11)I
BEG FLGT %[I ].'T[I ]. 1
```

```
8GG NEMT I
8TG IF II#E THEN 920
gEO DIEF "CHERIHIGE RT &LE`":
EOQ INFUIT W5
9010 dIEF "THILSFFR HT":
G1E INFUT HP
92E WFITE &15, 9300WE HF
93Q FGRMAT "CHERIHGE MT=", 2%FF. 日, E%,"THILSFHF HT=". 2%.FE.E
946 IF II=1 THEN 970
SEG DISP "HEFDSFPFR T.F.#. TAILSFRE T. F. #":
GEQ IPPUTT S1.S2
GTQ PFINT "HEADSFAF:T.F. = "GI:" THILSPAF:T.F. = "SE
GEG DISP "UFNT DHTA FLGTTED";
990 INFUT FS
```






```
1049 '1 = 'r 2+H5
1050 'T2=T4+H7
1060 L=x4-*3
1070 H=ヶ1-'r2
1086 IF FS=0 THEN 1146
1090 FLOT KE, 'r'3,1
110M FLOT %1, '1, 2
1110 FLOT S2. Y'2, z
1120 FLGT X4, 'r'4.2
1130 FLGT %1.''1.1
1140 IF II=1 THEN 1176
1150 OISF "INHER YAFD LIM OUITER THFD LIM":
1160 INFUIT SS. S4
117E FRINT "INN TAFEO LIM= "SS;" OHIT YAFD LIM= "S4
1180 IF I1#G THER 1こ3G
1190 DISF "LENGTH OF CHOKEFEFT)";
19GQ INFUIT LY
1210 OIGF "LENGTH OF LONGFT)";
1200 INFUT LZ
1220 &FITE <15, 124G)L1.LS
1240 FOFMHT "LENGTH OF GHOWEF=".F4. G. G%, "LENGTH OF LOG=",FES
1256 LZ=LS-0E
12G6 ES=L2,《Lz-CE%LZ)
1270 IF IN#G THEN 130日
12ES OISF "LOG TG GROUNO CLEFF:HWE":
12GO INFUIT C
1200 FRINT "MIN LOGG TO GROHNO GLEFF:FNEE="G
1:10 IF 11#G THEN 1340
122G [ISF "TEFERHIN FUINT STEF EIZE";
13SQ IPFUT SE
1346 FRINT "TEFERIN FOIPNT STEF SIZE="ES
1250 FI%ED 2
12EE IF R##4 THEN 15Eg
13TE OISF "MEF-1. OHL WOUND-2 S.ML. -E GAF.";
12ES IMFUT LE
1390 FS=T3
1400 [0T0 G2 OF 1410.1460. 1516
```

```
1410 FRINT "MSF T'TFE EARRIAGE"
\(1420 \quad 4=46+43\)
\(1430 \quad T=T E+T 3\)
\(1446 \mathrm{FS}=\mathrm{FE}=1\)
1450 BOTO 1596
```



```
1479 . \(4=4842\)
\(1480 \mathrm{~T}=\mathrm{TE}+\mathrm{T} \mathrm{S}\)
\(1490 \mathrm{RE}=\mathrm{F}=1.5\)
1560 GOTO 1596
1516 FFINT "SIMGLE MAINLINE T'TFE ERFRIFGE"
\(1506 \quad 4=43\)
15玉6 T=TE
1546 F:5=0
1556 F6=96060n6
156 IF Fi\# THEN 1590
15196 PRINT
15G0 FRINT "LIVE EKTLINE FATLOADS"
```




```
1610 IF WE\#\%4 THEN 162.
1E20 \% \(6=\% 6-16\)
1ES日 IF \%EATS THEN 16SQ
1E46 :5=\%
1650 IF \(55=1\) THEN 1690
\(1600 \quad 5=1\)
16T0 ST=INT(1, 55 )-1
1esa GuTa 1F16
1696 EG=INT SES
\(176 \mathrm{ET}=\mathrm{E} .1\)
1719 IF ECLE THEN 175
\(1726 \mathrm{E} 1=2 \mathrm{E} 0\)
\(175 \mathrm{~L} 4=\mathrm{C}-\mathrm{DS}\)
1746 BTO 1776
1759 L4=L
```



```
1.770 IF \(\mathrm{E}=2\) THEN 1790
1760 GQSUE T 2 O
1790 FOR \(I=I N T G S \%\) TG INTCS4+6. \(99 \%\) STEF EE
1864 SEM[I]
\(1516 \mathrm{E}=\mathrm{B} 1\)
```



```
18 S IF E+PGO THEN 1856
1846 E=96-F
```



```
\(1860 \mathrm{O}=4+\mathrm{COS}(\mathrm{F})+\mathrm{SIN}(\mathrm{F}) \mathrm{O}+\mathrm{K}\)
```





```
1960 IF \(\times 3 \times[1+1]\) THEN 2256
\(1916[1=\% 7-\%\)
\(19 \mathrm{E}[\mathrm{E}=\mathrm{E}[\mathrm{I}+1]-\mathrm{D} 1\)
```




```
\(1956 \mathrm{DE}=\mathrm{L}+0.0 \mathrm{CP}+\mathrm{E})\)
```

```
1760 0=个[ I ]-01+[5
```






```
2015 114=115
```







```
#076 0=$E-x1
ERE:004 'r'='1'1-'%
26%04 144=39606010
```



```
E11g F=F+1
2HEG [M[F]=[0
21玉采 F[F]=F
E149 S[F ]=E`
2156 ![[F]=r'`
```



```
2176 [0SUB z2%G
21E@ EMTO 2Ege
2196 lySuE 2%00
```




```
20% IF U4415 THEN ここ40
2EE4 114=115
Z4G PEST XZ
2E5 NE:TT I
2get if F=1 OF F:=4 THEN ESGS
EPE IF F## THEN ES1E
ETS IF FS=6 THEN E玉1G
2`@ FLOT MQ 'T'E. こ'
2%G FLDT $1, 't'1.1
ETMN NE=E
215 FFIMT
```



```
zESG GDEuE SF2G
```



```
FSG FDF I=1 TD F
ここGG 0=[![]
ETG F=F[ I ]
```



```
2\Xi#G Tr=%[I]
```



```
Z41日 R=E:*1-Z:0,0%)
```





```
245% 'T: B='T'1-'T'
```




```
Z4%1F CLI+LOSE1 THEN ES40
E4g E=F星-F
```



```
2515 CE=1
250 H=90
2534 G0TO 26EG
2540 05=0
2556 K-C1+SIN(90+P)(CL+LE)
2S60 E:=ATM(K7,EDE(1-K7+KT)
```




```
250日 GE=1+(UWSIN(F)-COSQF)+NE
2064 IF HESCCE-C5)< E0, THEN 2050
2010 05=06
2020 F=90-FTH(C7406)
```



```
2E40 BOTO CEES
2650 F=90-RTNCOTMCE%
2es0 GOGuE 2seg
2070 gngue 201g
EGSG RE%T I
2090 IF FS=0 THEN こTEG
2TGU FLOT ME. YE, 2
2710 PEN
2T20 15=INT(S1+1)
2ア3日 IE=INT(Se)
```



```
2750 FOF I=I5 TO (I6-1)
```



```
2TTG HENT I
2760 LS=F44+LS+E**H6+H7)
2r9g FRINT "FEQUIFED FIGGING LENGGTH="LE
28006 I1=1
2818 END
2020 K1='%O
2E日 K゙\Xi=(''-H), (L-D)
284日 F1=H1*S0RCD*D+'*'r')
```




```
20TG M=1+K2+NK2
2BE0 N=-K2+FE
```






```
250 M2=(06-C7+K1) (K1+K2)
2946 MS=k1`2-+こ`
23501 M4=1+K1-2
```







```
20101 44=6,4
SEOE IF WECG THEN 2120
```



```
2046 144=143
3054 TB=TS
```

```
    606 44=E50+014
    9701H4=1:7+1.44
```





```
    11E BGTO SEGE
    1ELTP=T1
    12g H4=C:7+6.04
    144-M=K1-a+1
    2Fg. N=-F1:+K1
```




```
S1800H3=HO+H4-H1
```



```
Z2E10 F:CTUFW
3`10 END
ここご心 K゙=ない品
```






```
ZTE M=1+K゙E*kO
ごGM N=-K゚こ+FO
```







```
K48 M2=4:+K1-彐-K2``+S
25EM M4=1+K1こ
```







```
<400 IF EO=` THEP S4GM
```



```
3430 IF AES&F4)<1G4 THEN S4GE
E446 E4=T
```



```
2480 E==E4
34E FS=F4
348& BOTG SこE日
3495 .14=47
SENG IF 4BC0 THEH SERO
EEN IF WFOE FidD WT<MB THEN SEDG
```



```
TET TB=TE
E54504=6:+6,44
SESE H4=1:7+644
```






```
SEg0 TF=Tこ
```

| 3610 | $W 4=56+2.14$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3629 | $\mathrm{H} 4=\mathrm{C} 7+6.14$ |  |  |  |  |  |  |
| 3630 | $M=k 12+1$ |  |  |  |  |  |  |
| 3646 | $\mathrm{N}=-\mathrm{R} 1 \times+\mathrm{k} 1$ |  |  |  |  |  |  |
| 3650 |  |  |  |  |  |  |  |
| 3506 |  | 3 m |  |  |  |  |  |
| 9570 | $\mathrm{HS}=2+\mathrm{HE} 2+\mathrm{H} 4-\mathrm{HI}$ |  |  |  |  |  |  |
| 3680 | TG＝HEAESCHS）＊CSERC | H3＊K1－FS | $2{ }^{-2+H 5 ゙ こ}$ |  |  |  |  |
| 3694 |  | $2+\mathrm{H}_{4}$ こ） | （1＋R6）＋WE |  |  |  |  |
| 2760 | FEETUFN |  |  |  |  |  |  |
| 3716 | ENO |  |  |  |  |  |  |
| 3726 | FF：INT |  |  |  |  |  |  |
| 8756 | IF R＝4 THEN 3PE日 |  |  |  |  |  |  |
| 3740 | FFEINT＂TEFERAIN HORZ | MAN LEM | GK＇L INE | MAINLINE | CAFRIAGE | Luİ | TO GFOLI |
| $<750$ | GOTO ST7G |  |  |  |  |  |  |
| 3700 | FFINT＂TEFERAIN HOEZ | Mrs：Linj | HRULEEACK | MAINLINE | CAFRIEGE | LOG | TO DROU |
| S77日 | FRINT＂FOINT DIST | LOHD | TENSION | TENSICH | CLEARANCE |  | FRNGLE＂ |
| 5780 | FRINT |  |  |  |  |  |  |
| 3790 | FEETURN |  |  |  |  |  |  |
| 360 | END |  |  |  |  |  |  |
| S816 | WRITE（15，3960） 09. | 14．T7．TS | C1． E |  |  |  |  |
| Sese | FORWHT F5．1， $2 \times$ FS． 9. | （\％FT．E． 2 | ¢ FT．日． $3 \times$ |  | ，5x，FP． 2 |  |  |
|  | IF P5＝9 THEN 3929 |  |  |  |  |  |  |
| 3840 | FLOT XE，TS， 2 |  |  |  |  |  |  |
| 3856 | IF NE\＃S THEN S916 |  |  |  |  |  |  |
| 356 |  | IN（A）． 2 |  |  |  |  |  |
| S6P6 | IFLOT－DS＊OUS（F＋E），D | SWINCF＋ | ． 2 |  |  |  |  |
| 3886 | 1 PLOT LS：COS（F＋E），－L | WSINCF＋E | ， 2 |  |  |  |  |
| 3890 |  |  |  |  |  |  |  |
| 3900 | $\mathrm{NE}=6$ |  |  |  |  | ． |  |
| 3916 | $N E=N E+1$ |  |  |  |  |  |  |
| 3920 | FEETIFN |  |  |  |  |  |  |
| 3930 | END |  |  |  |  |  |  |

## PROGRAM ON £ KEY

19 DIEF＂CAFEIAGE WT．＂：
20 IPFUIT 45
36［ISF＂GO TO EFEGIFL FUND：TION KE＇T FS＂
46 END

PROGRAM ON $f_{7} K E Y$

16 I1＝6
EG DIEP＂GO TG GFELIFL FUHETION KE＇T FE＂
S 9 ERUD

# PROGRAM ON $f_{8} K E Y$ 

10 D1EP "INNER TARD LIM, DUTER TARD LIM";
29 IPFIIT 53,54
SG DISF "EO TO GFECIFL FUNUTION KE't FS"
46 END

PROGRAM ON $f_{9}$ KEY

```
10 FINEO E
EQ FRINT
3E FEINT "FPOFILE"FI
4G FRINT "T. F.# X EOMRD 't EOURO";
5 G ~ F R I N T ,
EQ FOF I=1 TO N1
FG FEINT I, M[I],'TCI]
ES NEMT I
96 FRINT
IEG END
```

A P PENDIX 4




HEADGFHF HT= 45
FFOFILE 14

| EAFEIAILE WT= | 664 | TAILSFAR HT= |
| :---: | :---: | :---: |
| HEFDEFFR T. F. $=$ | 1 | THILSFAF: T. F. $=$ |
| ITA ${ }^{\text {T'HRE }}$ LIM= | 1 | OUT 't'HFD LIM= |


|  | C |
| :---: | :---: |

MIN LOG TG GFOURD CLEAFRRCE $=2$
TEPEAIA FQINT GTEF SIZE= 1
LIVE EKT'LINE FA'tLDADE

| TEERAIN FIINT | $\begin{aligned} & \text { HORE } \\ & D I E T \end{aligned}$ | MAM LDTg LIAD | GTRINE <br> TENEION | MAINLINE TENEIG | EAFPIFIE CLEFPRNEE | LOIS TIG GEOMRD FHGLE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. $E^{4}$ | E6T | 15141 | 34500 | 1605E | 8. 67 | 3. 58 |
| 3. 0 | Ses | 1323 | 34504 | 8554 | 3. 51 | 3. 58 |
| 4. 6 | 581 | 12609 | 34560 | 865 | \% 8t | 2. 58 |
| 5. | T4E | 13984 | 34560 | 8448 | 11. E8 | 3. 59 |
| E. $\square^{\text {a }}$ | 847 | 24973 | 24560 | 14759 | 9. 20 | 3.58 |
| 7. $\square^{\text {a }}$ | 997 | 4735 | 2456 | 18089 | 9. WE | 3.59 |
| E E | 122 | 51290 | 34500 | 7184 | 9.94 | 35 |

ETAHDIMG EFTLINE FHTLOADE EHEED DM A EF'TLIAE LENGTH DF 1S4E 4E FT

| TEPFAIA | HOEZ | MAX LOS | ExTLIME | MFITRIME | CAFRIPISE | LOTj TG TEO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FOINT | DIST | 1080 | TENSI的 | TEMEICH | ELEFFRTCE | Frigle |
| 2.0 | 2617 | 1469 | 24560 | Fez | 8.67 | 5. 4 |
| 3. 9 | 2se | F900 | 34569 | 4434 | 21.29 | 2E. 71 |
| 4. 8 | 581 | 486 | 24060 | 2149 | S5. 78 | 57.18 |
| C.E | T4E | 4215 | 24564 | 1756 | 64. 69 | 51. 43 |
| 6.0 | 847 | 42 e | 24560 | 1795 | 115 | Ez. 81 |
| 7. 5 | 96 | 4611 | 34506 | 1729 | 154. 48 | 96. Ex |
| 8.9 | 122 | 8168 | 34560 | 1852 | 81. 67 | 164. 57 |

FEQUTFED FIGIITG LENGTH=1FES 15

Figure 17. Basic Output.



| , | fll Durele | LINE HE IIGHT |
| :---: | :---: | :---: |
| ErtLIte | 34500 | 1. 85 |
| MFINLINE | 19600 | 1. 14 |
| HFULLEACEK | 6 | Q. 6.4 |
| SLFCELIME | $\square$ | Q. 6.4 |

HEADEFFF: HT=4

| FFOFILE 14 |  |  |  |
| :---: | :---: | :---: | :---: |
| CPFEIFIGE HT= | 661 | TAILSFPF: HT= | 46 |
| HEADSFHE T.F. $=$ | 1 | THILSFAF: T. F. $=$ | 9 |
| INH TAFEC LIH= | 1 | OUIT 'TAFD LIM= | 9 |
| LENGTH DF EHOKEE= | E | LEPISTH OF LIIS= | 16 |
| WIN LOE TG GFOUND | CLEF |  |  |
| TEREAIN FOINT ETEP | SI |  |  |

LIWE GGTLINE FA'tOADE

| TEFEHIN | HOEZ | Mre Log | Erit Ime | MFINL IAE | EAREIAIE | LOG TG Tifoumg |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FGIUT | DIET | LOAR | TENEION | TENEIOH | CLEARHNEE | Fivele |
| 2 B | 207 | 13472 | 24500 | 8492 | E. 48 | 7. 16 |
| 2. $0^{1}$ | 386 | 11920 | 24564 | 7248 | E. 41 | 7. 16 |
| 4.6 | 581 | 1.1420 | 24560 | 6EF9 | E. 54 | 7. 15 |
| 5. $\square^{1}$ | P4E | 12627 | 34569 | 7412 | 9.56 | 7. 13 |
| E. 0 | 847 | 22609 | 34560 | 1292 | E. 68 | 7. 15 |
| 7.9 | 997 | 4069 | 24500 | $14 E 45$ | 9. 18 | 7. 18 |
| E. 0 | 122 | 45762 | 34560 | 5594 | 9.94 | 7. 18 |


 FOIN DIET LOAD TENEIOH TENEION GLEAFPROE FHGLE

| 2. 0 | 207 | 13162 | 34500 | 8210 | E. 46 | 9. 08 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. $0^{4}$ | Tes | 5901 | 3456 | 2609 | 21. 05 | 60. 76 |
| 4. 9 | 581 | 4615 | 2450 | 1691 | 5 5. 59 | E4. 19 |
| 5.0 | 745 | 4340 | 34509 | 1743 | 64.40 | 5.1 .45 |
|  | 847 | 4345 | 34504 | 1714 | 115. 26 | 62 01 |
| 7. 9 | 937 | 468 | 24506 | 1720 | 154.22 | 96.80 |
| 8 E | 132 | 8 cos | 24500 | 180 | 81. 51 | 104. 57 |

FEGUIFED FITGING LENITH= 17ES IE

Figure 18. Output for a Log Length of 16 Feet.

'TAFDEF EFEES - THURDEREIFD MOEILE TAFDEE


HEFOSFHE HT=45

| FROFILE 14 |  |  |  |
| :---: | :---: | :---: | :---: |
| CAFPIFCE HT= | 660 | TAILSFAF HT= | 46 |
| HEADSFAR T. F. $=$ | 1 | THILSFAR T. F. $=$ | 9 |
| INA T'AFE LIM= | 1 | CUIT 't'HED LTM= | 9 |
| LEPGTH DF CHOUEF:= | 8 | LENGTH OF LOİ= | 48 |

MIA LOG TO GEOURD CLEAFAHEE $=2$
TEFRAIP FGINT ETEF 三IZE= 1
LIVE EKTLINE FATLOADE

| TEERAIN | HOES | HA\% Lins | EKTLINE | MAINALIAE | GAREIAIE | LOG TO GEOUHE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FOIPT | CIET | LOAD | TENSION | TENSIOR | CLEAFARUE | FNigle |
| 2. $\square^{\text {a }}$ | 207 | 15650 | 34569 | 10550 | 3. 16 | 2. 29 |
| E. ${ }^{\text {a }}$ | 2es | 13887 | 34560 | 9625 | E. 84 | 2. 39 |
| 4. 0 | 51 | 12934 | 3450 | E45 | 9.44 | 2.3 |
| 5. 9 | T4E | 13 S 4 | 24560 | 876 | 13.72 | 2. 3 |
| 50 | 847 | 2505 | 34500 | 15674 | 9. 34 | 2. ${ }^{\text {c }}$ |
| F.E | 97 | 5069 | 34506 | 19478 | 9. 80 | 2. 39 |
| E 0 | 122 | 52 56 | 34560 | 7754 | 9.84 | 2.29 |



| -TEFEFIN FOINT | $\begin{aligned} & \text { HORE } \\ & \text { DIST } \end{aligned}$ | HAS: LOT LOHD | STRINE <br> TENEION | MAINLINE TENEIOH | CHEEIARE CLERFRNGE | LOG TG GEOURA FNGLE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. 8 | 297 | 1514 | 34560 | 16079 | 9. 10 | 4. 22 |
| 3.8 | Ses | 8600 | 345010 | 516 | 21. 82 | 1E. 1 |
| 4. 0 | 51 | 5747 | 34560 | 3060 | $3 \mathrm{E}-5$ | 55. 12 |
| 5.8 | 745 | 4262 | 34560 | 1721 | E5. 27 | 51.49 |
| E $\square^{\text {a }}$ | 847 | 4 CE | 34569 | 1694 | 116. 15 $^{5}$ | 52.01 |
| F. ${ }^{\text {c }}$ | G9\% | 4555 | 54500 | 176 | 155.91 | 90. 69 |
| E. 9 | 122 | 8685 | 34500 | 1856 | Ex. 61 | 104.57 |

Figure 19. Output for a Log Length of 48 Feet.


| 'TPEDEF SFEES | -THIDNEEEIED FLLOUAEELE | MOEILE TMPDEF: LIPE |
| :---: | :---: | :---: |
|  | LOAD | WEICHT |
| SC'TL INE | 34569 | 1. 85 |
| MSINL THE | 19604 | 1. 14 |
| HFIULEFICK | Q | 6. 204 |
| SLFCKIM INE | 6 | E. 8.4 |
| HEADSF'HF: $\mathrm{HT}=$ |  |  |


| Frufile 14 |  |  |  |
| :---: | :---: | :---: | :---: |
| CAREIAIE UT= | 606 | TRILSFRE HT= | 46 |
| HEADSFAE T. F. $=$ | 1 | THILSFAF: T. F. $=$ | 9 |
| INN 'TAFD LIM= | 1 | OUT 'TAFD LIM= | 9 |
| LENGTH OF CHOEEF: | E | LEMISTH DF LOG= | E |

MIN LOG TO GFOURD GLEAFRNGE= 10
TEFRHIN FQINT ETEP EIZE= 1
LIWE EGTLIHE FF'tLORDE

| TEFEAIN | HOEZ | MAX | GK'TL I PE | MAINLINE | EAERIAGE | LOE TO CROUPAD |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FOINT | OIST | LOHD | TEHSIDH | TENSION | CLEFPRHEE | FldGle |
| 2. 6 | 207 | 9597 | 34560 | 5860 | 17. 52 | 13. 21 |
| 2. $\square^{\text {a }}$ | 386 | 985 | -4560 | 545 | 17. 27 | 18. 21 |
| 4. E | 581 | 9271 | 34560 | 585 | 17. 85 | 13. 21 |
| 5. 6 | 748 | 16453 | 34560 | 5601 | 21. 25 | 13. 21 |
| 6. 6 | 847 | 19579 | 34560 | 1606 | 13. 26 | 18. 21 |
| 7. 0 | 997 | 28098 | 24560 | 1365s | 18.8 | 18. 21 |
| 8. ${ }^{\text {a }}$ | 1229 | 44416 | 5456 | E408 | 17.63 | 18. 21 |

STANTING SKYITAE FA'TLOADE EAGED ON A EKTLINE LENGTH OF 154E. 47 FT



| 2. 0 | 29 | 9431 | 34560 | 554 |
| :---: | :---: | :---: | :---: | :---: |
| 3. 0 | 2es | 4993 | 34500 | 2455 |
| 4. 9 | 581 | 3468 | 34500 | 1512 |
| 5.6 | ア46 | 3227 | 3456 | 1425 |
| E. 0 | 84 | Eser | 3456 | 1435 |
| 7. 9 | 9 F | 345 | 34.501 | 1481 |
| E. 0 | 122 | 845 | 3456 | 176 |


| 17.59 | 19. 94 |
| :---: | :---: |
| 2. 14 | 49.50 |
| 47.51 | 6.4. 19 |
| 76.64 | 5.1. 49 |
| 127. 28 | 62. 61 |
| 185 | 96. 60 |
| Es. 65 | 104. 56 |

FEGUIFED EIGGING LENGTH= 1FES IE

Figure 20. Output for a 10 Foot Minimum Log to Ground Clearance.


```
HEDEF SFECE -THINDEFEIFD MOEILE TAROEF
                FLLOUGELE LINE
            LGAD WEIGHT
                        24560 1.85
                19000 1.84
                g B. 60
ELFOKIINE G G 00
TEFOSFHE:HT=45
\begin{tabular}{|c|c|c|}
\hline FROFILE 14 & & \\
\hline CAEFIFIGE MT= & 609 & THILSFAR HT= \\
\hline HEFDSFAE T. F. \(=\) & 1 & TAILSPAR T. F. \(=\) \\
\hline INA YRED LIM= & 1 & EUT 'TAFO LIM= \\
\hline LEMGTH OF EHOEEE= & E & LENIITH OF LOGI= \\
\hline
\end{tabular}
MIN LOG TO GFOHND ELEAEFNEE= ZQ
TEFRHIN FOINT STEF SIZE= 1
```

LIVE EF'TLINE FF'tLOADS



| TEFERTA | HOEZ | MA\% L0IF | EFTLIME | MAINLIPE | CAFEIFIEE | LOG TO GEOURO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FGINT | QIST | LOFP | TEHETOU | TEHEID. | CLEFEPRUE | Fingle |
| 2. 0 | 2 E | 2465 | 34586 | 1126 | 36.60 | 55.98 |
| 3. | 365 | 125 | 24500 | 794 | 57.51 | ET. E8 |
| 4. 9 | 581 | 850 | 34569 | 729 | 7 F | 64.19 |
| E. | T4E | 681 | 24509 | 794 | 194. 28 | S1. 49 |
| 6 | 847 | 658 | 34560 | 8 Ec | 155 日e | 62.01 |
| F. 0 | 997 | 751 | 24560 | 962 | 191.59 | 90. 96 |
| E. | 1222 | 2345 | 34560 | 123 | 16톤 28 | 104.57 |

Figure 21. Output for a 30 Foot Minimum Log to Ground Clearance.




| TEFEHIN FOTMT | $\begin{aligned} & \text { HBEZ } \\ & O I S T \end{aligned}$ | $\mathrm{MA} \mathrm{\%} \mathrm{LOH}$ LOHD | Ert'LINE <br> TEPEION | MAINLINE TENEIOM | CAFEIFIGE GLEAFHNHE | Loti | TIG GROURD FBHLE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. 4 | 207 | 16939 | 34560 | ETV | 19.85 |  | 5.45 |
| 2. 0 | 26 | 55.54 | 34509 | 154 | 25.61 |  | 27. 21 |
| 4. 0 | 51 | E37 | 24560 | 1844 | 5 E 5 |  | 55. Ex |
| 5. $\square^{4}$ | ア46 | 2959 | 24560 | 155 | 7 Pa |  | ㄷ.1. 49 |
| 50 | 847 | 2 ET | 34560 | 12E1 | 136.3 |  | 52. 91 |
| P. | 997 | 2154 | 34564 | 1417 | 168. 41 |  | 90. 60 |
| 9. 6 | 1322 | 5996 | 34500 | 1727 | 96.5 |  | 164. 57 |

Figure 22. Output for a 24 Foot Choker Length.

ARCER GPECE THUMDEREIFD MOEILE YHROER

|  | LOAD | WEITHT |
| :---: | :---: | :---: |
| ETLME | 34509 | 1. 85 |
| FIML IME | 19609 | 1. 14 |
| Fulleffek | $\square$ | 6. 6.1 |
| LACOIPEE | $\square$ | 6. 06 |

EADSFHF: $H T=45$
FOFILE 14

| HEFIFIGE WT= | 060 | THILSFAR HT= |
| :---: | :---: | :---: |
| IEAOSPRE T. F = | 1 | THILSFAR T.F. $=$ |
| IRN THEO L IM= | 1 | DUIT T'HED LIM= |
| -ESTIH DF EHOEEE= | 日 | LENGTH OF LOIG= |

MIN LOG TO BEOUNO ELEAPRPNE= 2
TEFEAIA FGINT STEF SIZE= 1

LIVE EK'tLIPE FA'tLOADE

| TEFPGIM | HOFZ | MH\% LOG | ErTLINE | MAIPLIME | GAREIFIE | LIIE TG GFOURO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FOIPT | DIET | LOAD | TENEION | TENSICN | CLEAPHRIE | Fidile |
| 2. 9 | 297 | 8179 | 34589 | STV | 9.57 | 3. 58 |
| 2 E | 285 | T24 | 34569 | 2217 | 9.46 | 2.58 |
| 4. ${ }^{\text {a }}$ | 591 | 7479 | 34560 | 3691 | 9.71 | 3.58 |
| 5. 0 | T4E | 9564 | 34509 | 208 | 11. 20 | ․ 58 |
| E. 0 | 84 | 15622 | 34560 | 4827 | 9.31 | 2. 58 |
| F. Q | 957 | 21615 | 24509 | 4525 | 9. 08 | 2. 56 |
| E. ${ }^{\text {a }}$ | 1222 | 24915 | 24509 | -17E3 | 3. 4 | 3. 58 |



| TEFERHIN FIINT | $\begin{aligned} & \text { HEFZ } \\ & \text { OIST } \end{aligned}$ | MAM Ling LOAD | ETGINE TENETOH | MAINLIPE TEMEION | GAREIFGE CLEARHNGE | LOIG TO gROUND Frigle |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.0 | 267 | 815 | 34509 | 375 | 9. 57 | 5. 41 |
| 2 0 | 3E6 | 51481 | 34560 | 222 | 22.30 | 51.75 |
| 4. 5 | 581 | 4475 | 34500 | 1885 | 2e. 98 | E4. 19 |
| 50 | T4E | $4 \mathrm{EV4}$ | 24560 | 1795 | E5. 90 | 51. 49 |
| E. 0 | 847 | 4212 | 24508 | 1689 | 11E. ET | ce. 91 |
| P. ${ }^{\text {a }}$ | 997 | 4494 | 24500 | 189 | 155. 59 | 96. Eu |
| ed 0 | 1222 | 730 | 3456 | 185 | 82.8 | 194.57 |
| PEQUIFED EIGGIHG LENGTH= 17ES 1E |  |  |  |  |  |  |

Figure 23. Output for $D_{3}=15$.


$\mathrm{EADOF} \mathrm{FF}: H T=4.5$
GOFILF 14
AFEIFIEE $H T=$ THILSFRF HT= 46
EADGFHF T.F. $=1 \quad$ TFILSFRF T. F. $=9$
UH 'T'AFD LIM= DUT T'FFO LIM= $1 \quad 9$
EHGTH OF CHOGEF= $\because$ LEMGTH OF LOIG=. 32
IN 1 OU TO GFOUHD CLEAFANGE $=2$
EEFAIA FGIHT STEF EIZE= 1
IWE EK'TLINE F'F'TGADE

| $\begin{aligned} & \text { EFEIN } \\ & \text { GOIPT } \end{aligned}$ | $\begin{aligned} & \text { HERE } \\ & \text { DIST } \end{aligned}$ | MAR LOM LOAD | EKTLINE <br> TENEION | MAINLINE TERETOR | DAERIFGE CLEAFTHEE | LOIS | TO GROUNO Fiblile |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. 8 | 207 | 2546 | 22096 | 1960 | E. 80 |  | 3. 56 |
| 2.8 | SE | 2STE | 34560 | 17719 | E.E1 |  | 2. 58 |
| 4. 8 | 581 | 19937 | 34560 | 15093 | 7. 85 |  | 3.5 |
| C. $\mathrm{E}_{1}$ | F4E | 16937 | 34506 | 1312 | 16. 16 |  | 2. 56 |
| E. | 847 | 26494 | 25561 | 19680 | 7. 41 |  | 2.5 |
| 7. $\square^{\text {a }}$ | 997 | 41298 | 12E45 | 19606 | 7.15 |  | 卫. 58 |
| 8.6 | 1229 | 89344 | 27215 | 19600 | 9.85 |  | 3.5 |



| EFEFHIP | HOES | MF\% LDG | Ertline | MAIRLINE | EAREIFISE | LOIS | Oupde |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FGITM | DIET | LOAD | TENSIOR | TESEIOR | CLEFPAMSE |  | Fidice |
| 2. 0 | 267 | 2589 | 34429 | 19650 | E. 80 |  | 5. 28 |
| 3.8 | 286 | 10750 | 345610 | E8E | 19.61 |  | 24.47 |
| 4. 9 | 581 | 565 | 34590 | Erel | E3. 20 |  | 51.19 |
| E. $0_{0}$ | T4E | 4542 | 24506 | 1896 | EE. 13 |  | 51. 49 |
| 6 | 847 | 455 | 34560 | 17ES | 113.92 |  | E2. 01 |
| 7. $\mathrm{B}^{\text {a }}$ | 997 | 485 | 74569 | 1776 | 152.17 |  | 96. 69 |
| E. 0 | 1322 | 8594 | 34560 | 1895 | 8 Ec 20 |  | 164.5 |
|  |  |  |  |  |  |  |  |

Figure 24. Output for $C_{8}=0.3$.

## LIWE AND STANDING EK'LINE LOAO FNAL'EIEGEIGID LINK FEEUAFTIONO



HEADSFAR HT $=45$

| FFOFILE 14 |  |  |
| :---: | :---: | :---: |
| CAEEIFIGE $4 \mathrm{~T}=$ | 664 | TAILSFHR HT= |
| HEFROFAR T. F. $=$ | 1 | TAILSPAF: T. P. $=$ |
| INA T'RED LIN= | 1 | DIT T'FED LIM= |
| LEFAGTH OF CHOKEF= | 3 | LENGTH OF LOG= |

MId LOIS TG GFEDRD CLEAEARGE= 2
TEFFAIN FGIdT ETEF EIZE= 1

LIGE EKTLIAE FH'tLOADE


 FOTHT DIET LOAD TENEIGH TENEION ELEGEANEE FNGLE

| 2. ${ }^{\text {a }}$ | 297 | 10923 | 24.569 | EESE | 19.69 | 5.44 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 3se | Eser | 3456 | 3697 | 23.92 | 28. 68 |
| 4. $\square^{4}$ | 581 | 4435 | 34.409 | 1846 | $37.6 E$ | 62.95 |
| 5. 0 | 745 | 4141 | 34500 | 1688 | 66.59 | 5.1. 49 |
| E. $0^{\text {a }}$ | 847 | 4145 | 34508 | 1654 | 117. 2 | E2. 6 |
| 7. 4 | 997 | 4426 | 2450 | 1682 | 156. 23 | 90. 610 |
| E. 6 | 1222 | 7897 | 24500 | 185 | E2. 78 | 104. 57 |

FEDUTEE FIGIIUG LENGTH=1765. 16

Figure 25. Output for $C_{8}=0.7$.



Figure 26. Output for $\mathrm{U}=0.4$.



## LIVE EK'LINE FHTLGHDE





| 2. $1^{1}$ | 207 | 1493 | 24560 | 1691 | E. 34 | 5.37 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. | 286 | 7 BCO | 34560 | 4695 | 29.83 | 26. 17 |
| 4. 9 | 581 | 4912 | 3450 | 2916 | 5. S4 | 55.95 |
| 5.9 | 746 | 485 | 3456 | 1747 | 64.34 | 51.49 |
| E. ${ }^{\text {c }}$ | 847 | 4363 | 34560 | 1718 | 115. 94 | 62. 61 |
| F. ${ }^{\text {P }}$ | 997 | 465 | 34506 | 1795 | 154. 6 | 96. 60 |
| E E | 1222 | 893 | 34569 | 164 | E1. 42 | 164.57 |

FEDUIFED FIGGIMG LEPGTH=1?ES 1E

Figure 27. Output for $U=0.8$.

## 

|  |  |  |
| :---: | :---: | :---: |
|  | flotimable | LIME |
|  | LOAD | WEIEHT |
| EKTLINE | E | 6. 6.9 |
| MAIPALINE | 19606 | 1. 14 |
| HFDILEAHEK | 19660 | 1. 94 |
| SLACKL INE | 19606 | 1. 94 |
| HEADSFFF: HT= 50 |  |  |


| PFIOFILE 14 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| CARE1FIEE UT= | 684 | TAILSFPR | $H T=$ | 46 |
| HEADSFAR T. F. $=$ | 1 | THILSF'RR | T. P. $=$ | 9 |
| IRHW THEC LIM= | 1 | CUIT 'T'FED | LIM= | 9 |
| LEPdith of Chikee= | 8 | LEMISTH OF | LOIS $=$ | 2 |
|  | CLEA | ' |  |  |
| TEFPRIN FOIHT STEP | SI |  |  |  |
| MSF T'tFE GAREIAIEE |  |  |  |  |


| TERFAIN Fildet | HOEZ DIET | MAN: LOIT LOAC | HAULEACK TEMETUH | AEINLIME TENETIDN | CAREIAGE ELEAFFHICE | LOM TG GREURAD FHILE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. 0 | 2 Cl | 1593 | 1608 | 19609 | 8. 67 | 2. 56 |
| 3. 0 | Ses | 14658 | 17911 | 19600 | E. 51 | 356 |
| 4. 9 | 581 | 1298 | 13961 | 19609 | 8. Eb | 2. 53 |
| 5. 9 | 746 | 12769 | 17E12 | 19606 | 11. 83 | E. 56 |
| E. 0 | 847 | 17793 | 13197 | 19604 | 9.20 | Z. 58 |
| $7 . \mathrm{B}$ | 997 | 27964 | 11275 | 19606 | 9.6 | 3.58 |
| 8.0 | 1222 | 2ser | 13814 | 19684 | 9.94 | 3.56 |

FEGUIFED FTIGIAG LENGTH=37E. 31

Figure 28. Output for MSP Type Carriage.



Figure 29. Output for Over/Under Wound Carriage with $R_{5}=R_{6}=1.5$.


Figure 30. Output for Over/Under Wound Carriage with $R_{5}=R_{6}=2.0$.


|  | fllowable LOAD | LINE WEIGHT |
| :---: | :---: | :---: |
| GKTLINE | 6 | E. 610 |
| MFINLINE | 19660 | 1. 94 |
| HFILLEHCK | 19660 | 1. 14 |
| ELFEKLINE | 19600 | 1. 14 |

HEADOFHF: $\mathrm{HT}=5 \mathrm{E}$

| PEOFILE 14 |  |  |
| :---: | :---: | :---: |
| CAFFIPISE WT= | 6 ELT | TAILSFPF: HT= |
| HEPDEFAF: T. F. = | 1 | TAILSFAF: T. F. $=$ |
| INA 'tafe Lim= | 1 | OUIT T'AFD LIM $=$ |
| LEAGTH DF CHOEEE= | E | LEPGTH OF LOIG= |

MIN LOM TO GFOUND ELEFFAHAE $=\Xi$
TEFEFIN FGINT STEF SIZE= 1
EIPGLE PAIALINE T'tFE CAERIFGE

| TEFEPIN | HGEz | Max Log | HAIJLEFHLK | MHINLINE | CAREIASE | LOIS | TO GEO |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| FOIPN | DIET | LOAD | TENSIOd | TENETON | CLEAFPFHEE |  | Frigle |
| 2. 1 | 207 | 10729 | 12391 | 196010 | 3. 67 |  | 3.58 |
| 2. | 3 E | 9964 | 13 Sc | 19680. | 5. 51 |  | 3.55 |
| 4. 4 | 581 | 9624 | 1356: | 19680 | 8 |  | 3.58 |
| 5. 5 | 746 | 10685 | 13598 | 19600 | 11. E8 |  | 3.58 |
| E. $E$ | 847 | 14P62 | 11680 | 19860 | 9. 20 |  | 3. 58 |
| 7. E | 997 | 2545 | 16080 | 196010 | 9.6 |  | 5. 53 |
| 8. | 1229 | 41827 | 14096 | 19600 | 9.94 |  | 3. 5 |



Figure 31. Output for a Single Mainline Type Carriage.

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[^0]:    *Portions of the users guide were copied from the Skyline Analysis Program (SAP) documentation (Sessions, 1978).

