


AN ABSTRACT OF THE THESIS OF

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Title: AN INVESTIGATION OF THE METABORATE MONOMER AND  
TRIMER IONS IN ALKALI HALIDE CRYSTALS

Abstract approved:

  
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The infrared spectra of the metaborate monomer and trimer ions in NaCl, KCl, and KBr were studied. These spectra contain bands due to the trimer in solid solution, in a second phase of the appropriate potassium or sodium salt, and perhaps on adjacent lattice sites. Furthermore, complex equilibria exist between the trimer in these three forms and the monomer. These equilibria depend upon the lattice, the boron concentration, and the thermal history of the crystal. The presence of the second phase and its relationship to the infrared bands was confirmed with light scattering experiments.

A model for the trimer in solid solution is proposed in which the planar trimer,  $(\text{BO}_2^-)_3$ , replaces three next nearest neighbor halide ions that form an equilateral triangle. Moreover, the trimer is most soluble in KCl consistent with the argument that the solubility should be greater when the fixed distances between the three negative

charges on the trimer more closely approach the anion-anion distance in the lattice. In contrast, the solubility of the monomer increases as the size of the lattice increases from NaCl to KBr.

A normal coordinate analysis which employs a general valence force field predicts eigenvalues which are in fair agreement with the assigned values of the fundamentals, even though most of the force constants were either borrowed from related compounds or estimated.

Values for the absorption coefficients of the monomer ( $\omega_3$ ) in KCl and KBr, and the trimer ( $\omega_6$  and  $\omega_7$ ) in KCl were determined.

An Investigation of the Metaborate Monomer and  
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by

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To Pamela

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# AN INVESTIGATION OF THE METABORATE MONOMER AND TRIMER IONS IN ALKALI HALIDE CRYSTALS

## I. GENERAL INTRODUCTION

An investigation of the structure of a polyatomic ion in solid solution has distinct advantages compared to an investigation of the ion in a pure crystal of a salt of the ion. Isolation of these ions in a crystal of a different compound reduces interactions between the ions in solution and between fundamental vibrations of the ion and lattice modes of the crystal. This results in bandwidths which are often comparable to those of a gas. If the symmetry of the site where the ion is located is lower than the symmetry of the ion, then degeneracies may be removed and inactive modes may become weakly active, giving additional information about the structure. However, it is difficult to study the structure of an ion in solid solution by independent means such as Raman scattering, NMR, X-ray diffraction, and others because the concentration of the ion is usually near or below the sensitivity limits of these methods.

The crystal structures of potassium and sodium metaborate have been determined by Zachariassen (45) and Fang (14, 15) respectively to be rhombohedral with space group  $D_{3d}^6$  or  $R\bar{3}c$ . The metaborate ion was found to exist as a planar trimer with  $D_{3h}$  symmetry in which three  $BO_3$  groups share corner oxygen atoms and thus form

a six membered ring as shown in Figure 9. Goubeau and Keller (25) recorded and assigned the Raman spectra of  $B_3O_3(OCH_3)_3$ ,  $B_3O_3[N(CH_3)_2]_3$ ,  $B_3O_3(CH_3)_3$ , and  $B_3O_3Cl_3$  whose hexagonal ring structures are similar to those of potassium and sodium metaborate; see the summary of assignments in Table 1. Later Goubeau and Hummel (24) recorded and assigned the infrared spectra of  $B_3O_3(CH_3)_3$ ,  $B_3O_3(OH)_3$ ,  $B_3O_3(OD)_3$ , and  $(B_3O_6)Na_3$  in either KBr pellets or nujol mulls. They concluded that the infrared spectra of orthorhombic metaboric acid and its sodium salt are very similar to that of trimethylboroxine, just as is the case for the Raman spectra of the esters of orthorhombic metaboric acid and trimethylboroxine. Parsons (33) re-examined the spectra of orthorhombic metaboric acid in nujol mulls and made a new assignment for the metaborate trimer ion,  $(BO_2^-)_3$ . The infrared spectra limited to the rock salt region and assignments of trifluoroboroxine published by Fisher, Lehmann, and Shapiro (17) are in good agreement with those of Parsons. Later Latimer and Devlin (29) extended this work to  $250\text{ cm}^{-1}$  on thin films of trifluoroboroxine, and their data and assignments are in qualitative agreement with Fisher et al. . They also studied and made an assignment of the infrared spectra of trichloroboroxine. Büchler and Marram (5) obtained the spectrum of sodium metaborate which was condensed from the vapor, and most of the experimental lines agree with those of Goubeau and Hummel. The infrared spectra of the

Table 1. Previous assignments for metaborate trimer ion,  $(\text{BO}_2^-)_3$ , and related compounds.

- (a) Goubeau and Keller (25)
- (b) Goubeau and Hummel (24)
- (c) Parsons (33)
- (d) Fisher, Lehmann and Shapiro (17)
- (e) Latimer and Devlin (29)
- (f) Büchler and Marram (5)
- (g) Hisatsune and Suarez, in KBr pellet (28)

- 1 Obscured by strong  $\text{OH}^-$  absorbance
- 2 Activated in solid state infrared
- 3 Estimated

s = strong  
m = medium  
w = weak  
v = very  
b = broad  
sh = shoulder

		Raman(a)	Raman (a)	Raman (b)	IR (b)	Raman (a)	IR (b)	IR (b)	IR (c)	IR (c)	IR (c)
		$B_3O_3Cl_3$	$B_3O_3[N(CH_3)_2]_3$	$B_3O_3(CH_3)_3$	$B_3O_3(CH_3)_3$	$B_3O_3(OCH_3)_3$	$B_3O_3(OH)_3$	$B_3O_3(OD)_3$	$B_3O_3(OH)_3$	$^{10}B_3O_3(OH)_3$	$B_3O_3(OD)_3$
$A_1'$	$\omega_1$	1037	1147	1155		1286			1239	1267	1226
	$\omega_2$	807	804	807		804			<u>1/</u>	<u>1/</u>	805
	$\omega_3$	333	537	539		556			595	600	577
$A_2'$	$\omega_4$								1473	1523	1441
	$\omega_5$								478	482	474
$E'$	$\omega_6$		1355		1384 vs		1375vs, vb	1350vs, vb	1397	1451	1407
	$\omega_7$				1226 s		1150 m	1160w, vb	1342	1385	1358
	$\omega_8$				783 m		735 s, b	718 s, b	1360 939	942	930
	$\omega_9$	390	433	451	450 vs	403	456 s		462	463	456
	$\omega_{10}$	150		232		257	280 m				
$A_2''$	$\omega_{11}$				570 s		591 m		745	761	727 739
	$\omega_{12}$				459 m		476 m				
$E''$	$\omega_{13}$			597		350			650	675	639
	$\omega_{14}$			170		156					



Table 1. Continued.

	IR(d)	IR(d)	IR(d)	IR(d)	IR(e)	IR(e)	IR(e)	IR(e)	IR(b)	IR(f)	IR(g)	IR(g)
	$^{11}\text{B}_3\text{O}_3(\text{CH}_3)_3$	$^{10}\text{B}_3\text{O}_3(\text{CH}_3)_3$	$^{11}\text{B}_3\text{O}_3\text{F}_3$	$^{10}\text{B}_3\text{O}_3\text{F}_3$	$^{11}\text{B}_3\text{O}_3\text{F}_3$	$^{10}\text{B}_3\text{O}_3\text{F}_3$	$^{11}\text{B}_3\text{O}_3\text{Cl}_3$	$^{10}\text{B}_3\text{O}_3\text{Cl}_3$	$\text{B}_3\text{O}_6\text{Na}_3$	$\text{B}_3\text{O}_6\text{Na}_3$	$(^{11}\text{BO}_2^-)_3$	$(^{10}\text{BO}_2^-)_3$
$A_1'$												
$\omega_1$											1138	1210
$\omega_2$					826 <sup>2/</sup>	838 <sup>2/</sup>		815 <sup>2/</sup>			823	837
$\omega_3$											616	633
$A_2'$												
$\omega_4$											690	708
$\omega_5$											455	460
$E'$												
$\omega_6$	1384	1430	1450 s, b	1477	1436	1468	1345	1385	1425vs, b 1450vs, b	1460s, b	1400	1460
$\omega_7$	1227	1260	1381 s, b	1431	1373	1403	1183	1220	1227s, b 1255s, b	1235s, b	1222	1265
$\omega_8$	918	942	966 m	968	964	966	760	765	702 w 720 w	700 w 720 w	950	957
$\omega_9$					462	465	390	392			473	478
$\omega_{10}$					316	319					200 <sup>3/</sup>	205 <sup>3/</sup>
$A_2''$												
$\omega_{11}$	784	786	714 s, b	733	711	731	664	686			728	754
$\omega_{12}$											387	388
$E''$												
$\omega_{13}$											717	717
$\omega_{14}$											280 <sup>3/</sup>	280 <sup>3/</sup>

metaborate trimer ion in pressed disks of alkali halides were observed by Hisatsune and Suarez (28). The trimer ions were prepared directly in the alkali halide matrices by the oxidation of  $\text{BH}_4^-$  with either trapped atmospheric oxygen,  $\text{KClO}_3$ , or  $\text{KClO}_4$ . They concluded that the trimer ion was in solid solution; however, the published fundamentals reproduced in Table 2 do not show a lattice effect in either sodium halides or potassium halides suggesting the trimer ion was in a second phase of  $\text{Na}_3(\text{BO}_2)_3$  or  $\text{K}_3(\text{BO}_2)_3$  respectively.

Table 2. Matrix effects on some  $(\text{BO}_2^-)_3$  fundamentals at 25° C published by Hisatsune and Suarez.

	NaCl	NaBr	NaI	KCl	KBr	KI
$\omega_6$	1466	1465	1462	1440	1440	1439
	1436	1439	1434	1405	1405	1405
$\omega_7$	1264	1264	1260	1250	1249	1250
	1241	1240	1239	1225	1225	1228
$\omega_{11}$	724	721	722	735	734	734
	708	706	708	717	717	717

Single crystals of alkali halides containing metaborate trimer ions in solid solution were grown allowing the present infrared investigation to be conducted. A normal coordinate analysis of the metaborate trimer ion was also carried out using a general valence force field.

## II. EXPERIMENTAL TECHNIQUES AND EQUIPMENT

### Sample Preparations

#### Materials

Reagent grade KCl and NaCl were purified by an ion exchange process originally developed by Fredericks, Rosztochy, and Hatchett (18) for KCl. This was modified later by Fredericks, Schuerman, and Lewis (19) for both KCl and NaCl. Infrared quality KBr and CsI obtained from the Harshaw Company were used without further purification.

The doping materials consisted of  $\text{LaBO}_3$ ,  $\text{KBO}_2$ ,  $\text{NaBO}_2$ ,  $\text{H}_3\text{BO}_3$ , glassy  $\text{B}_2\text{O}_3$ , and crystalline  $\text{B}_2\text{O}_3$ .  $\text{LaBO}_3$  was prepared using a modification of the method of Goldschmidt and Hauptmann (23). A solution of  $\text{H}_3\text{BO}_3$  and chemically pure  $\text{LaCl}_3$  was evaporated to dryness, and the product was heated to red heat for five or ten minutes. An infrared spectrum of a nujol mull of the final product is in good agreement with the spectra of  $\text{LaBO}_3$  published by Steele and Decius (39). Both  $\text{KBO}_2$  and  $\text{NaBO}_2$  were produced by evaporating to dryness a solution of  $\text{H}_3\text{BO}_3$  and the appropriate reagent grade alkali metal hydroxide as suggested by Cole, Scholes, and Ambery (6). In order to prepare crystalline  $\text{B}_2\text{O}_3$ , reagent grade boric acid was held at 150° C for three weeks in a platinum crucible; the temperature was

subsequently increased to 200° C at a rate of 10° C per day, and finally it was held at 500° C for one day. Glassy  $B_2O_3$  was prepared by merely heating reagent grade boric acid until molten in a platinum crucible.

Reagent grade boric acid which consequently contains boron isotopes in natural abundance was employed, while the isotopically enriched forms of boron were obtained from the Oak Ridge National Laboratory. The enriched  $^{11}B$  in the form of boric acid was reported to contain 97.42% of  $^{11}B$ , whereas the enriched  $^{10}B$  was elemental boron and stated to contain 96% of  $^{10}B$ .  $H_3BO_3$  containing enriched  $^{10}B$  was made by the oxidation of elemental  $^{10}B$  with excess concentrated nitric acid. The solution was diluted, activated charcoal was added and then removed by filtration, and finally the solution was evaporated to dryness which resulted in the volatilization of the excess nitric acid.

The preparation of  $K_3(BO_2)_3$  crystals was accomplished as described by Zachariassen (45) by fusing  $K_2CO_3$  and  $H_3BO_3$  in a platinum crucible and rapidly cooling the melt. The product was broken open and the small clear crystals were removed. Crystals of  $Ca(BO_2)_2$  were prepared in the same manner using CaO after the method of Goubeau and Hummel (24). Standard mull techniques were used in obtaining the spectra of  $K_3(BO_2)_3$  and  $Ca(BO_2)_2$ .

## Crystal Growth

The alkali halide crystals were grown by the Stockbarger method in both Vycor and quartz growth tubes. Quartz was occasionally employed because of the isotopic dilution of the enriched boron which occurred when Vycor was used. The Vycor employed in these experiments consisted of 96% silica and 4% boric oxide, alumina, and other impurities; whereas the quartz was relatively pure  $\text{SiO}_2$ . The quartz tubing was type 204 clear fused quartz obtained from the General Electric Company and was reported to contain an average of 0.5 ppm and a maximum of 0.6 ppm of boron. A tapped Marshall metallurgical testing furnace which is Kanthal wound, is 16 inches long, and has an inside diameter of three inches was used for crystal growth. The furnace was shunted and a stainless steel sleeve was placed in the bottom of the furnace to provide a temperature gradient. The furnace was controlled to within  $\pm$  one degree centigrade with a continuous power regulator consisting of a model 407 Wheelco controller and a 620A silicon controlled rectifier. The growth tubes were dropped through the temperature gradient at a speed of 0.4 cm/hr. with a synchronous motor using a chain drive.

The growth tubes filled with either KCl or NaCl were placed on a vacuum system and evacuated at 150° C. An HCl atmosphere was added and removed two or three times both at 150° C and 400° C to

remove most of the water present. The salt was then melted with an HCl atmosphere in order to remove the remaining  $H_2O$ . The HCl was removed and  $Cl_2$  was subsequently added to form covalent chlorides of any heavy metals present which being volatile were then removed by sublimation. Because monovalent ions are more difficult to remove than polyvalent ions by the ion exchange process (19), this step mainly removes monovalent metal ions which form covalent chlorides after being oxidized to higher valence states. Growth tubes containing KBr and CsI were merely evacuated at  $150^\circ C$  and  $400^\circ C$  for 12 hours or more to remove most of the water present. The doping material was then added, and the growth tube was sealed while under a vacuum. The final steps were slightly altered for two KCl crystals. In this case, the doping materials consisting of  $H_3BO_3$  and excess reagent grade KOH were added to the melt. After a short time an HCl atmosphere was added to remove the excess  $OH^-$  with the ensuing water being removed by evacuation before the tube was sealed.

After removal from the growth tube the crystals were cooled to room temperature by merely allowing them to lose heat to the atmosphere. Although most observations were made on crystals with this thermal history, some measurements were made on crystals which had been quenched rapidly to the boiling point of nitrogen or annealed slowly. Single crystals wrapped in platinum foil were held at some temperature near the melting point, e.g.  $605^\circ C$  for KCl, between 1

and 24 hours and then were placed in a copper container filled with liquid nitrogen. A precooled copper weight was placed on top of the crystal to prevent bubbles of gaseous nitrogen from insulating the crystal from the copper. Crystals in an evacuated quartz tube were annealed by lowering the temperature from a temperature near the melting point to approximately 250° C at the rate of about 12° C per hour.

### Measurements

#### Optical

Beckman IR-7 and IR-11 spectrophotometers (3, 4) were used in the near IR, 650-4000  $\text{cm}^{-1}$ , and the far IR, 33-650  $\text{cm}^{-1}$ , respectively; but host absorbance limited range to  $> 450 \text{ cm}^{-1}$  in KCl and to  $> 280 \text{ cm}^{-1}$  in KBr. Both are double beam instruments and are similar electronically. The IR-7 utilizes double prism dispersion for primary separation of the wavelengths and a grating for final dispersion of the light. A 60 x 75 mm, 60°, NaCl foreprism and a 64 x 64 mm replica grating with 75 lines per mm and a 12  $\mu$  blaze were used. The resolution of the IR-7 for the actual scanning conditions was about one  $\text{cm}^{-1}$ . The monochromator in the IR-11 is a filter and grating device which uses a combination of one of four different gratings and one of eight filters. The resolution of the IR-11 for the actual scanning

conditions was  $< 2.5 \text{ cm}^{-1}$ .

Most of the infrared spectra were taken while the samples were cooled to near the boiling point of liquid nitrogen. Both a pyrex cold cell and a commercial liquid helium cold cell with alkali halide windows were used. Soft indium spacers ensured good thermal contact between the crystalline sample and the brass sample holder.

A model 450 Perkin-Elmer spectrophotometer (35) was used in the U. V. and far U. V. regions. It is a double beam instrument employing matched detectors. The monochromator consists of two quartz prisms, and the instrument is capable of resolution better than one  $\text{\AA}$  in the region of interest, 175-250  $\text{m}\mu$ .

Defect scattering of U. V. and visible light in doped KBr and NaCl, thought to be due to a precipitate or second phase, was observed and photographed by means of an ultramicroscope. The ultramicroscope consists of an optical bench with a variable lens (10-40X) and a variable slit, a xenon lamp, and a Tiyoda research microscope. The photographs, including several of a stage micrometer for calibration purposes, were taken with a single lens, reflex camera made by the Honeywell Pentax Company. Quantitative measurements of the defect scattering were made using a recording polarization spectrometer built by Evett and Isenberg (13). The incident light was vertically polarized, and the vertical and horizontal components of the scattered light were measured separately. Defect scattering should



depolarize the light, whereas scattering from surfaces should not.

Therefore, the ratio of the scattered horizontal component to the scattered vertical component  $EB/EE$  is a measure of light scattering by defects which depolarizes the light. Information about the size of the defects was not available from this experiment because the wavelength dependence of the scattered bands was caused by the instrument.

#### Concentration of Boron

The concentration of boron in alkali halide crystals was determined by means of a colorimetric method developed by Hatcher and Wilcox (26). This method uses carminic acid which changes from an absorption at 520  $m\mu$  to one at 585  $m\mu$  in the presence of boron and its effective range is one to ten  $\mu g$  of boron.

### III. EXPERIMENTAL RESULTS AND DISCUSSION

#### Introduction

The initial infrared spectra were obtained from KCl crystals grown in Vycor growth tubes and doped with  $\text{OH}^-$ . Because it was quite evident that the  $\text{OH}^-$  had chemically reacted with the Vycor, the source of the impurity was proposed to be the Vycor tube which contains 4% boric oxide, alumina, and other impurities. The spectra contained intense bands which were attributed to the linear, symmetric metaborate monomer ion (31, 32), indicating that the  $\text{OH}^-$  had reacted with the boric oxide in the Vycor to produce the metaborate monomer. Furthermore, this suggested that the unknown portion of the spectra was due to some impurity which contained boron. In order to substantiate this, KCl and KBr crystals were doped with boron in the form of  $\text{LaBO}_3$ ,  $\text{KBO}_2$ , glassy  $\text{B}_2\text{O}_3$ , crystalline  $\text{B}_2\text{O}_3$ , and boric acid. Spectra similar to the original spectra were obtained when the doping materials were  $\text{LaBO}_3$  and  $\text{KBO}_2$ , and appropriate shifts in the bands for different isotopic ratios of  $^{10}\text{B}$  to  $^{11}\text{B}$  demonstrated that the impurity does contain boron; see Figure 1. The bands were much more intense when  $\text{KBO}_2$  was employed rather than  $\text{LaBO}_3$ , as is expected, because a large amount of electrostatic energy is required to place a trivalent ion such as  $\text{La}^{+3}$  or  $\text{BO}_3^{-3}$  on a monovalent lattice site. In addition, some of the fundamentals were observed to

have at least four isotopic components demonstrating that the impurity contains more than one boron atom. When  $B_2O_3$  and boric acid were used, only weak and extremely broad bands were observed except for the very sharp lines of the metaborate monomer. These broad bands may be due to a small amount of polymer or an amorphous second phase. Thus, the impurity was introduced only when the dopant contained some ionic form of boron and oxygen, and therefore we infer that the impurity is ionic. Boric acid exists in the three forms  $H_3BO_3$ ,  $HBO_2$ , and  $B_2O_3$  and being a very weak acid may be considered a neutral molecule. This inference is by no means conclusive, even though the introduction of a charged impurity substitutionally is energetically more favorable. The impurity may occupy an interstitial position; however, the amount of space available at such a position is small. Consequently, this would impose restrictions on the size and shape of the impurity. A neutral molecule which may be coordinated interstitially to four chloride ions is considered in a following section.

The amount of  $OH^-$  present was small compared to the amount of  $KBO_2$  added or thought present in crystals doped with  $OH^-$ . The concentration of  $OH^-$  was determined from an electronic transition at 204  $m\mu$  in KCl using an absorption coefficient published by Gie and Klein (22). This band at 204  $m\mu$  in KCl and 215  $m\mu$  in KBr was shown to be due to  $OH^-$  by Fritz, Lüty, and Anger (20) and Rolfe (37)

respectively. In one KCl crystal doped with  $\text{OH}^-$ , the concentration of the remaining  $\text{OH}^-$  was 13 ppm, and most of the crystals doped with  $\text{KBO}_2$  contained 2-4 ppm or less. This may be compared with the amount of boron present which was found colorimetrically to be approximately 50-200 ppm depending upon the position of the sample in the crystal. If this electronic transition is nearly the same for free  $\text{OH}^-$  isolated in the lattice and  $\text{OH}^-$  as part of a larger ion also isolated in the lattice, as expected, then it is possible to conclude that the impurities present do not contain hydroxide groups. Moreover, when KCl was doped with  $\text{H}_3\text{BO}_3$  and KOH and subsequently treated with HCl to remove the excess KOH, the same infrared spectra were obtained.

There is evidence from the intensities of the bands that there are three impurities present in addition to the metaborate monomer. These have been designated species A, B, and C. The bands due to A and B are very sharp whereas those due to C are quite broad. Their relative concentrations depend on the host lattice, the concentration of boron, and the thermal history of the crystal. The effect of boron concentration may be conveniently studied in samples taken from different parts of the same crystal, thereby maintaining the same isotopic ratio of boron. This is possible because the solubility of an impurity is usually greater in the liquid phase than in the crystalline phase. Hence the part of the crystal grown last would have a

larger concentration of impurities. A brief discussion of these effects follows, and the appropriate spectra are given in Figures 2, 3, and 4; but a more detailed discussion will be deferred until models for each of these impurities have been considered. The spectra in Figures 1 through 4 correspond to samples near the boiling point of liquid nitrogen except for the portions containing  $\omega_3$  of the metaborate monomer,  $1900-2100 \text{ cm}^{-1}$ , which were observed at room temperature.

Even though the predominant features in spectra of KCl are due to A, the bands which have been assigned to B and C become more intense relative to A as the concentration of impurities increases. The broad bands of C are much weaker than either A or B. In the most concentrated samples available some of the stronger bands of B are comparable to those of A, but in the most dilute samples these same bands are very weak. Conversely, the metaborate monomer ion,  $\text{BO}_2^-$ , is much more concentrated in the more dilute samples. These observations suggest equilibria exist between at least two and perhaps all four impurities. With the NaCl and KBr matrices the sharp and relatively weaker features of A are superimposed on the strong, broad bands of C. Due to the complexity of the spectra it is difficult to determine whether B is present or not. Later in this chapter, species C is proposed to be a precipitate of the sodium or potassium salt of species A. If this is true, it may be concluded that of these three alkali halides KCl is the optimum host lattice for species A. This is

Figure 1. Spectra of boron containing species in KCl at various compositions of isotopic boron taken at  $T \approx 100^\circ \text{K}$ .  $^{11}\text{B}$  is equal to the fraction of  $^{11}\text{B}$  present.

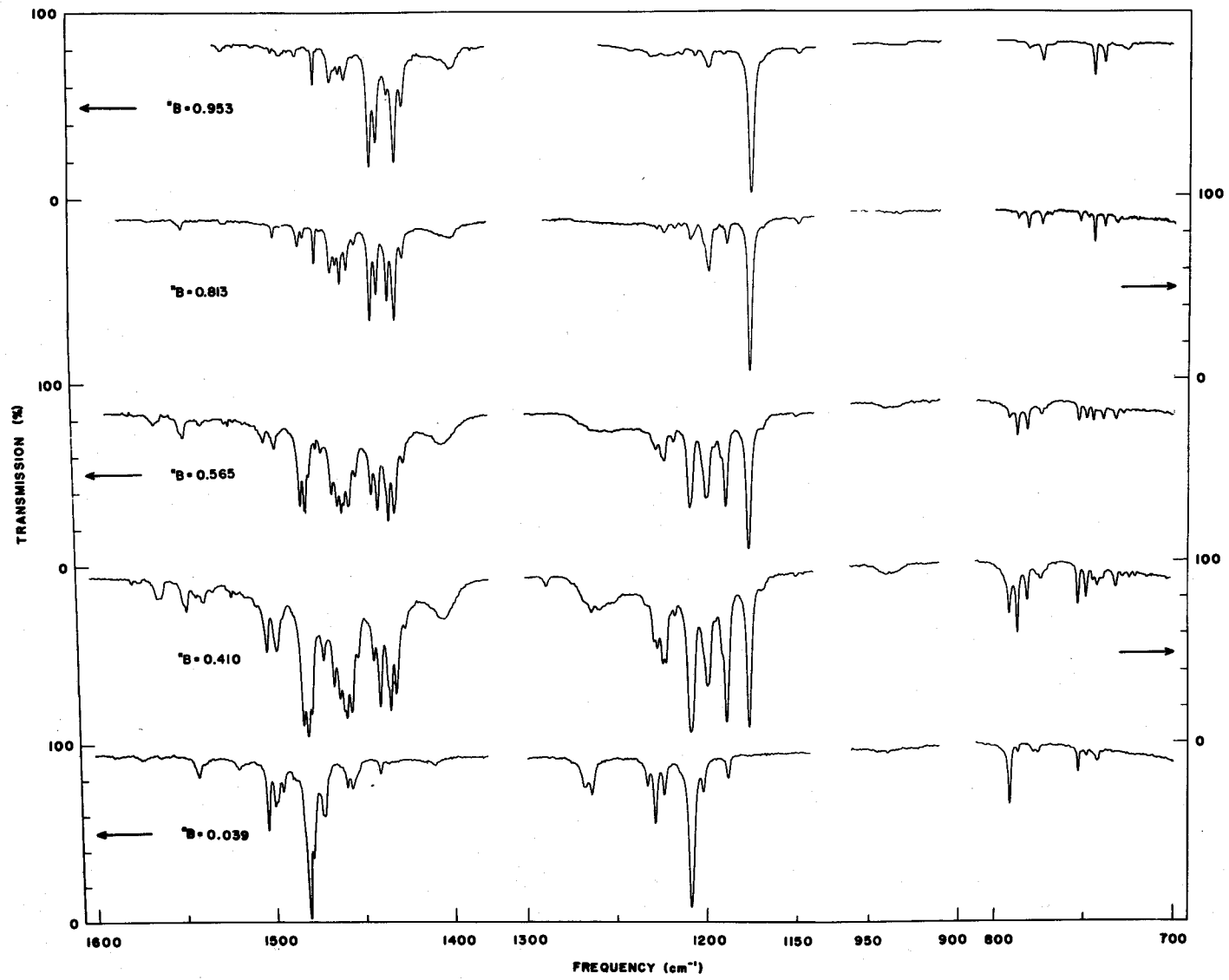


Figure 2. Spectra of boron containing species in NaCl, KCl, and KBr taken at  $T \approx 100^\circ \text{K}$  ( $700\text{-}1600 \text{ cm}^{-1}$ ) and  $T \approx 300^\circ \text{K}$  ( $1930\text{-}2080 \text{ cm}^{-1}$ ) which demonstrate the effect of thermal history upon the equilibria between species.

a. (before quenching), b. (after quenching from  $605^\circ \text{C}$ ), and c. (after annealing) denote the thermal history of a particular crystal.



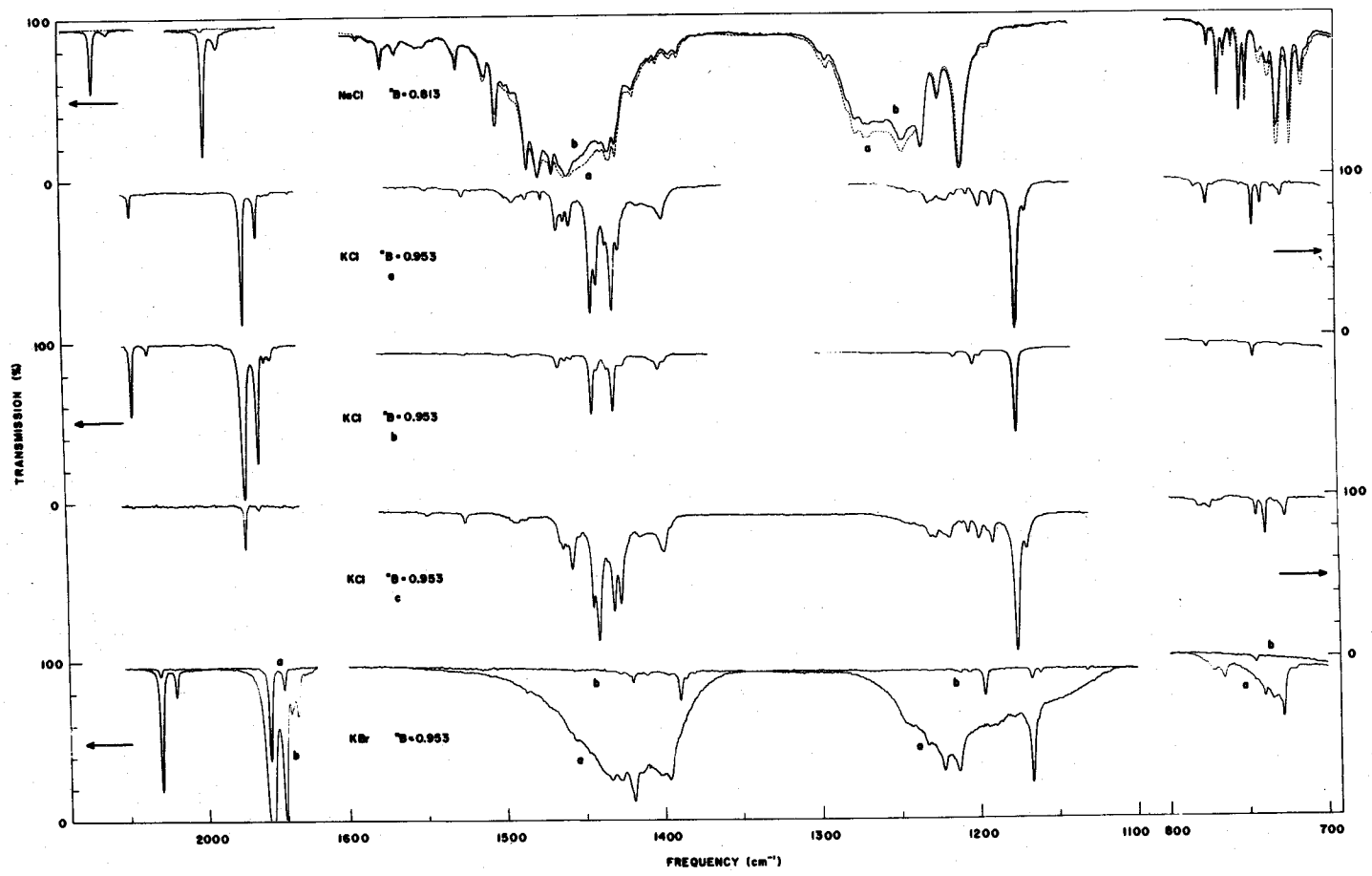


Figure 3. Spectra of boron containing species in a KCl crystal with  $^{11}\text{B} = .083$  taken at  $T \approx 100^\circ\text{K}$  ( $700\text{-}1600\text{ cm}^{-1}$ ) and  $T \approx 300^\circ\text{K}$  ( $1940\text{-}2050\text{ cm}^{-1}$ ) which demonstrate the effect of thermal history and boron concentration upon the equilibria between species. The concentration of boron increases from bottom to top.

a. (before quenching), b. (after quenching from  $605^\circ\text{C}$ ), and c. (after annealing) denote the thermal history of the crystal.

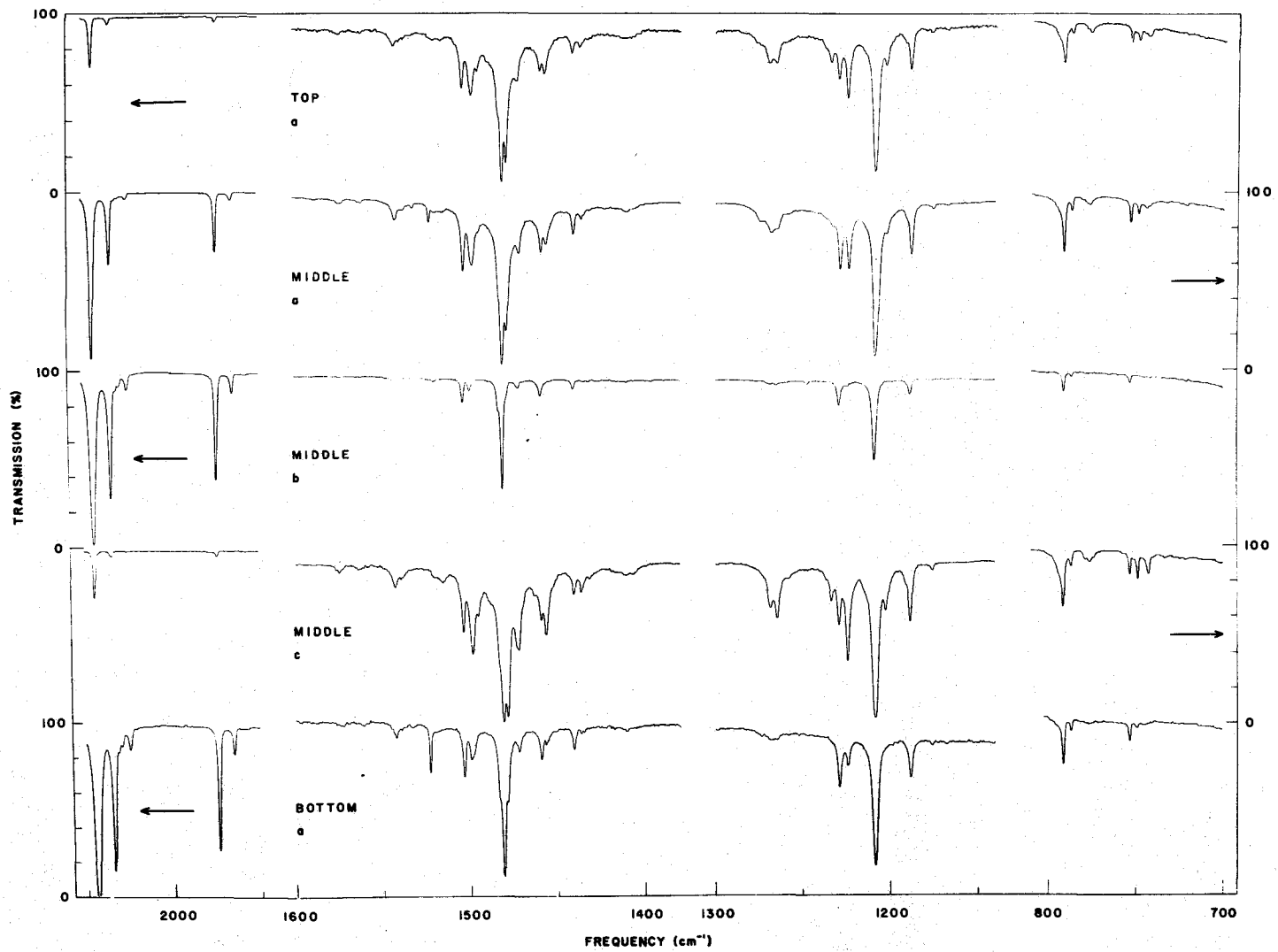


Figure 4. Spectra of boron containing species in KCl taken at  $T \approx 100^\circ \text{K}$  ( $700\text{-}1600 \text{ cm}^{-1}$ ) and  $T \approx 300^\circ \text{K}$  ( $1940\text{-}2050 \text{ cm}^{-1}$ ) which demonstrate the effect of thermal history and boron concentration upon the equilibria between species.

a. (before quenching), b. (after quenching from  $605^\circ \text{C}$ ), and d. (after quenching from  $710^\circ \text{C}$ ) denote the thermal history of a particular crystal.



a natural consequence if A is in solid solution because of spatial and electrostatic reasons which are considered below. If an impurity is in solid solution, the frequencies of the corresponding modes should decrease as the size of lattice is increased. This trend is shown in Tables 3 and 4 for one of the fundamentals of A. Furthermore, the sharpness of the features due to A and B suggest that they are in solid solution. For these reasons it is concluded that A and perhaps B are in solid solution.

Table 3. Interatomic distances in alkali halides.

	Anion-cation distances (42)	Calculated anion- anion distances
NaCl	2.814	3.980
KCl	3.139	4.439
KBr	3.293	4.657
CsI*	3.950	4.561

\*CsCl structure

Table 4.  $\omega_7$  of species A.

	$^{10}\text{B}$	$^{11}\text{B}$
NaCl	1243	1210
KCl	1208	1175
KBr	1199	1166

Weir and Schroeder (41) have studied the infrared absorption spectra of anhydrous, crystalline, inorganic borates. Based on zinc metaborate which contains  $\text{BO}_4$  tetrahedra with B-O distances of

1.48 Å, they conclude only tetrahedrally coordinated boron would display its B-O stretching frequency in the 800-1100  $\text{cm}^{-1}$  region. Because of a lack of stretching frequencies in this region with the exception of a weak doublet at 950  $\text{cm}^{-1}$ , it has been concluded that the impurities being studied in this investigation do not contain  $\text{BO}_4$  tetrahedra.

The fundamental  $\omega_7$  of species A, listed in Table 4, has at least four components whose intensities depend on the isotopic ratio of  $^{10}\text{B}$  to  $^{11}\text{B}$ . Some information can be obtained from this about the number of boron atoms in the molecule and the symmetry of the molecule. From the number of components it may be established that A must contain two or more boron atoms. Several models are considered in the next four sections.

### Proposed Models for A

#### Two Boron Atoms

Three isotopically different molecules which contain  $2^{10}\text{B}$ ,  $^{10}\text{B}+^{11}\text{B}$ , or  $2^{11}\text{B}$  are possible; and the four lines may be accounted for if  $\omega_7$  is a degenerate mode which is split for the molecule containing  $^{10}\text{B}+^{11}\text{B}$ . This is possible if there is either a threefold axis of symmetry or if the molecule has  $V_d$  symmetry. An example of the latter case is the hypothetical molecule shown in Figure 5, although such a molecule

is chemically very unlikely under these circumstances. The distance between the two negatively charged oxygen atoms is about the same as the halide-halide distance in an alkali halide crystal. Thus, this hypothetical model might fit in an alkali halide lattice by replacing two adjacent halide ions. This molecule contains two mutually perpendicular  $\text{BO}_2^-$  groups and can be shown to have three vibrational fundamentals belonging to the E symmetry species which may be split into  $B_1$  and  $B_2$  of the  $C_{2v}$  subgroup.

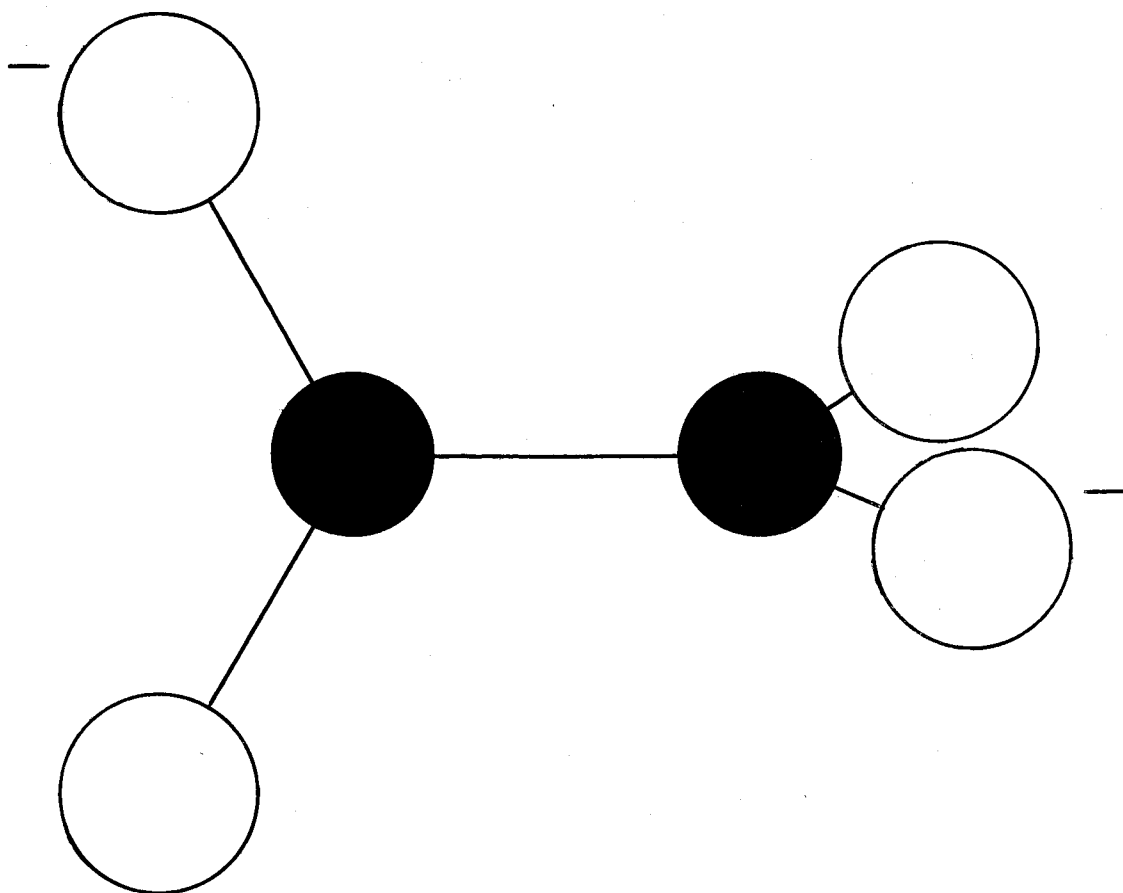


Figure 5. Hypothetical  $(\text{BO}_2^-)_2$  ion which belongs to the  $V_d$  group.



A hypothetical molecule with a threefold axis, although unlikely, is one in which two  $\text{BO}_3$  groups are held together through a boron-boron bond with three oxygen atoms and one boron atom at the corners of a tetrahedron and the remaining boron atom near the center. This structure may be described as two tetrahedra interposed at a corner. The details about the number of components are very similar to those of  $(\text{BO}_2^-)_2$ ; however, these models are not able to predict the experimental intensities of  $\omega_7$  and the other fundamentals of A. This is shown qualitatively for  $\omega_7$  in Table 5.

Table 5. Comparison of experimental intensities of  $\omega_7$  with theoretical concentrations of the models containing two boron atoms.

$^{11}\text{P}^*$	Theoretical				$\omega_7$ in KCl			
	$(^{11}\text{P})^2$	$^{11}\text{P}^{10}\text{P}$	$^{11}\text{P}^{10}\text{P}$	$(^{10}\text{P})^2$	1	2	3	4
.97	.94	.03	.03	.00	vs	vw	w	vw
.80	.64	.16	.16	.04	s	w	m	w
.50	.25	.25	.25	.25	vs	s	s	vs
.04	.00	.04	.04	.92	w	m	w	vs

\*  $^{11}\text{P}$  = probability that a boron atom is  $^{11}\text{B}$ .



Dunicz (12) recently proposed that this molecule has a cage structure in which four nonplanar  $\text{BO}_3$  groups share oxygen atoms. He further proposes that the boron atoms may be coordinated to four external halide ions which are at the corners of a tetrahedron. It is

feasible that such a molecule could exist in an alkali halide lattice at the interstitial position  $(1/4, 1/4, 1/4)$  coordinated to four tetrahedral halide ions. Even though this is a large molecule compared to the amount of space available, it has been considered too.

This molecule has five isotopically different forms whose symmetry and the corresponding infrared active modes are given in Table 6.

Table 6. The isotopic forms of  $B_4O_6$  and their symmetry.

Molecule	Symmetry	Symmetry species (IR active modes)
$4^{11}B$	$T_d$	$F_2$
$3^{11}B+^{10}B$	$C_{3v}$	$A_1+E$
$2^{11}B+2^{10}B$	$C_{2v}$	$A_1+B_1+B_2$
$^{11}B+3^{10}B$	$C_{3v}$	$A_1+E$
$4^{10}B$	$T_d$	$F_2$

Internal symmetry coordinates of the symmetry species  $F_2$

$$S_1 = 1/\sqrt{12}(3r_1 - r_2 - r_3 - r_4)$$

$$S_2 = 1/\sqrt{6}(2r_2 - r_3 - r_4)$$

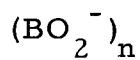
$$S_3 = 1/\sqrt{2}(r_3 - r_4)$$

$r_i$  = change in B(i) - X distance,

where X is a halide ion

Under  $C_{3v}$  symmetry if the boron corresponding to  $r_1$  is

isotopically different, the appropriate internal symmetry coordinates (E) are similar to  $S_2$  and  $S_3$ . Therefore E should occur at nearly the same frequency as  $F_2$ , but  $A_1$  should be shifted a certain amount consistent with the Teller-Redlich product rule. The relative intensities expected and the possible positions are shown schematically in Figure 6 for two cases of splitting under  $C_{2v}$  symmetry. The first case is a zero order splitting in which no splitting is assumed, and the second case corresponds to an equal spacing between all three components. The experimental pattern of  $\omega_7$ , four almost equally spaced components, and especially the concentration dependence cannot be explained by this model.



The infrared spectra of nujol mulls of  $\text{CaB}_2\text{O}_4$  published by Goubeau and Hummel (24) and observed in this investigation are in many respects similar to the one corresponding to species A. The crystal structure was determined by Zachariasen and Ziegler (44, 46, 47) to be orthorhombic and to contain the polymer  $(\text{BO}_2^-)_n$ . This polymer is a nearly planar chain of  $\text{BO}_3$  groups which share one oxygen as shown in Figure 7. The distance between two adjacent negatively charged oxygen atoms is approximately equal to the halide-halide distance in an alkali halide crystal. Therefore this large polymer might possibly fit in the lattice if the negatively charged oxygen

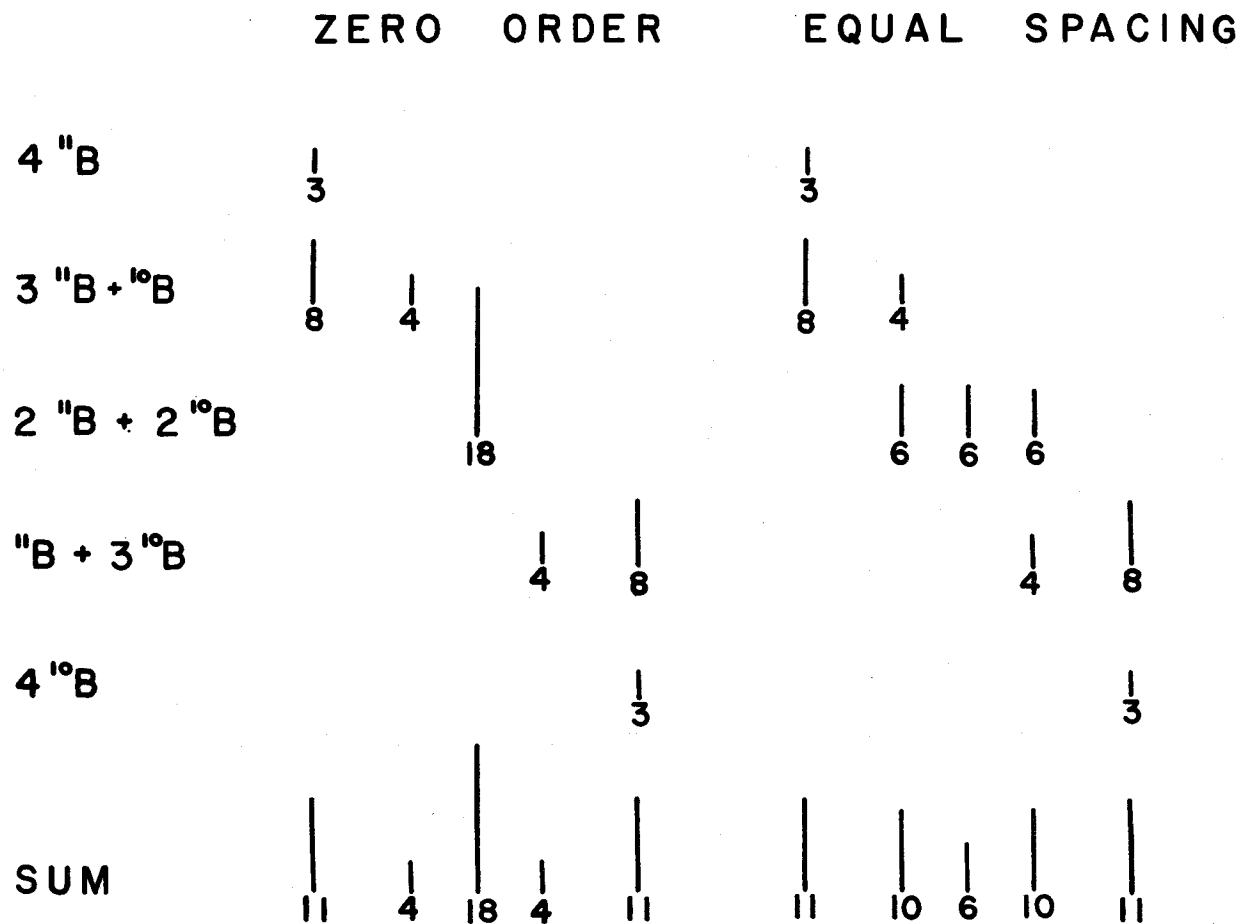


Figure 6. Isotopic components of a triply degenerate mode ( $F_2$ ) of  $\text{B}_4\text{O}_6$  indicating proposed positions of the members of an isotopic component which result from a reduction in the symmetry due to the appropriate isotopic perturbation.  $^{11}\text{P} = 0.5$ .

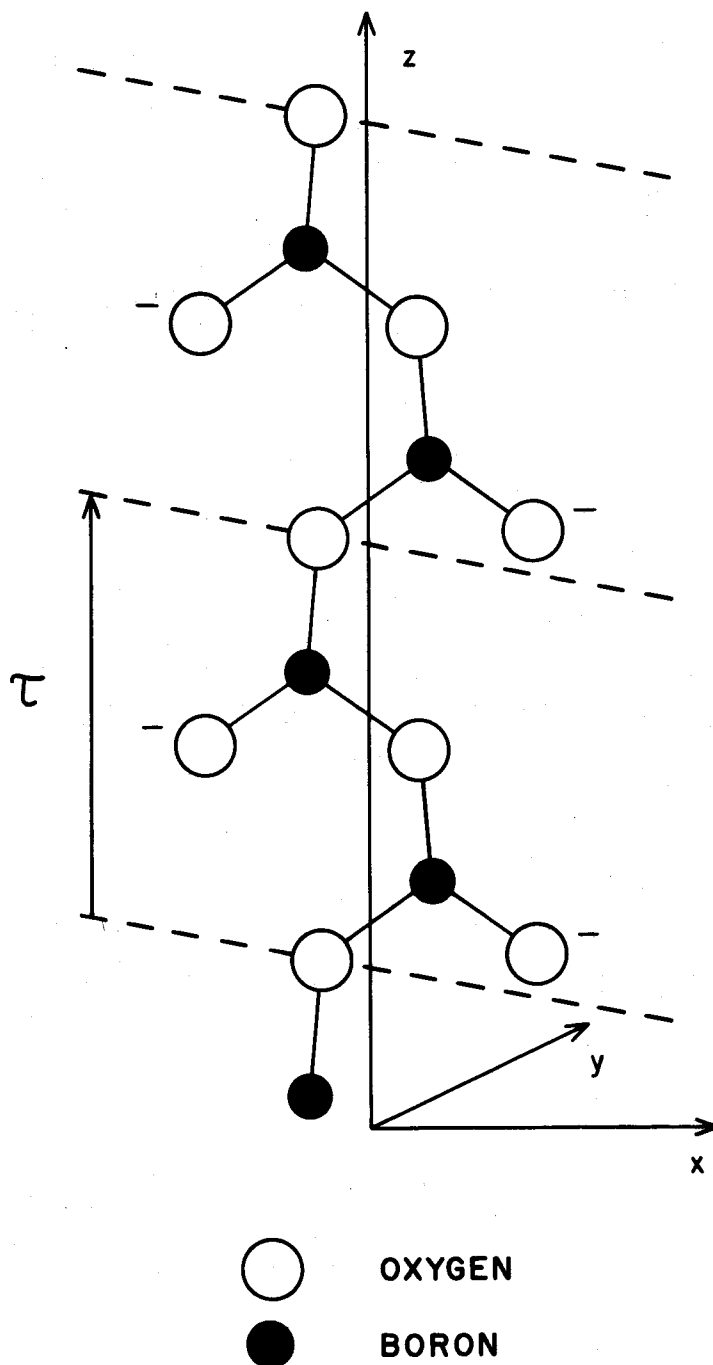


Figure 7. The structure of  $(\text{BO}_2)_n^-$  from calcium metaborate according to Zachariasen (44).  $\tau$  is the primitive translation vector which defines the unit cell in this one dimensional lattice.

atoms replace two parallel rows of halide ions such that  $\tau$  is parallel to a  $\langle 110 \rangle$  direction and a normal to the plane of the molecule is in a  $\langle 111 \rangle$  direction.

The unit cell consists of  $(\text{BO}_2^-)_2$ , and if it is planar the following symmetry operations are present;  $E$ ,  $\sigma_{xz}$ ,  $[C_2; \tau/2]$ , and  $[\sigma_{yz}; \tau/2]$ . Hence  $(\text{BO}_2^-)_n$  belongs to a group which is isomorphic to  $C_{2v}$ . A normal coordinate analysis using several simplifying assumptions such as separation of high and low frequencies, stretching and bending modes respectively, predicts stretching frequencies which agree to some extent with the experimental ones. However, this model will not account for the positions of the isotopic components of the modes which have been ascribed to species A. Decius, Malan, and Thompson (7, 10) have dealt with similar problems involving intermolecular coupling between nitrates and between carbonates which are arranged in a chain in the aragonite structure. Their calculations predict that the frequencies due to isotopically pure chains will be either larger or smaller, depending upon the sign of the coupling constant in the F matrix, than those due to the corresponding sequence of slightly impure chains. However, in this investigation the mixed isotope components are between those of the two pure isotopes. If a chain has a threefold axis of symmetry or belongs to the group  $V_d$ , then the isotopic components of a doubly degenerate mode would possibly fit such a pattern. No such polymer is

known to exist or is physically imaginable.

Trimer of Metaborate,  $(\text{BO}_2^-)_3$

The infrared spectra of  $\text{K}_3(\text{BO}_2)_3$  and  $\text{Na}_3(\text{BO}_2)_3$  (24, 28) in mineral oil mulls and in pressed disks of alkali halides are quite similar to those of species A. The trimer has four different isotopic forms and consequently each fundamental should have at least four components. The doubly degenerate fundamentals are split by the reduction in symmetry from  $D_{3h}$  to  $C_{2v}$  for the molecules containing one nonequivalent boron isotope. The four components of  $\omega_7$  and their intensities may be accounted for if the six components which result from the removal of the degeneracy under  $C_{2v}$  symmetry overlap in the manner shown schematically in Figure 8. A qualitative comparison of experimental intensities and theoretical concentrations is given in Table 7.

Table 7. Comparison of experimental intensities of  $\omega_7$  with theoretical concentration of  $(\text{BO}_2^-)_3$ .

$^{11}\text{P}$	Theoretical				$\omega_7$ in KCl			
	$\binom{11}{\text{P}}^3 +$		$\binom{10}{\text{P}}^3 +$		1	2	3	4
	$3/2 \binom{11}{\text{P}}^2 \binom{10}{\text{P}}$	$3/2 \binom{10}{\text{P}}^2 \binom{11}{\text{P}}$	$3/2 \binom{11}{\text{P}}^2 \binom{10}{\text{P}}$	$3/2 \binom{10}{\text{P}}^2 \binom{11}{\text{P}}$				
.97	.96	.00	.04	.00	vs	vw	w	vw
.80	.72	.04	.18	.05	s	w	m	w
.50	.31	.19	.19	.31	vs	s	s	vs
.04	.00	.06	.00	.94	w	m	w	vs

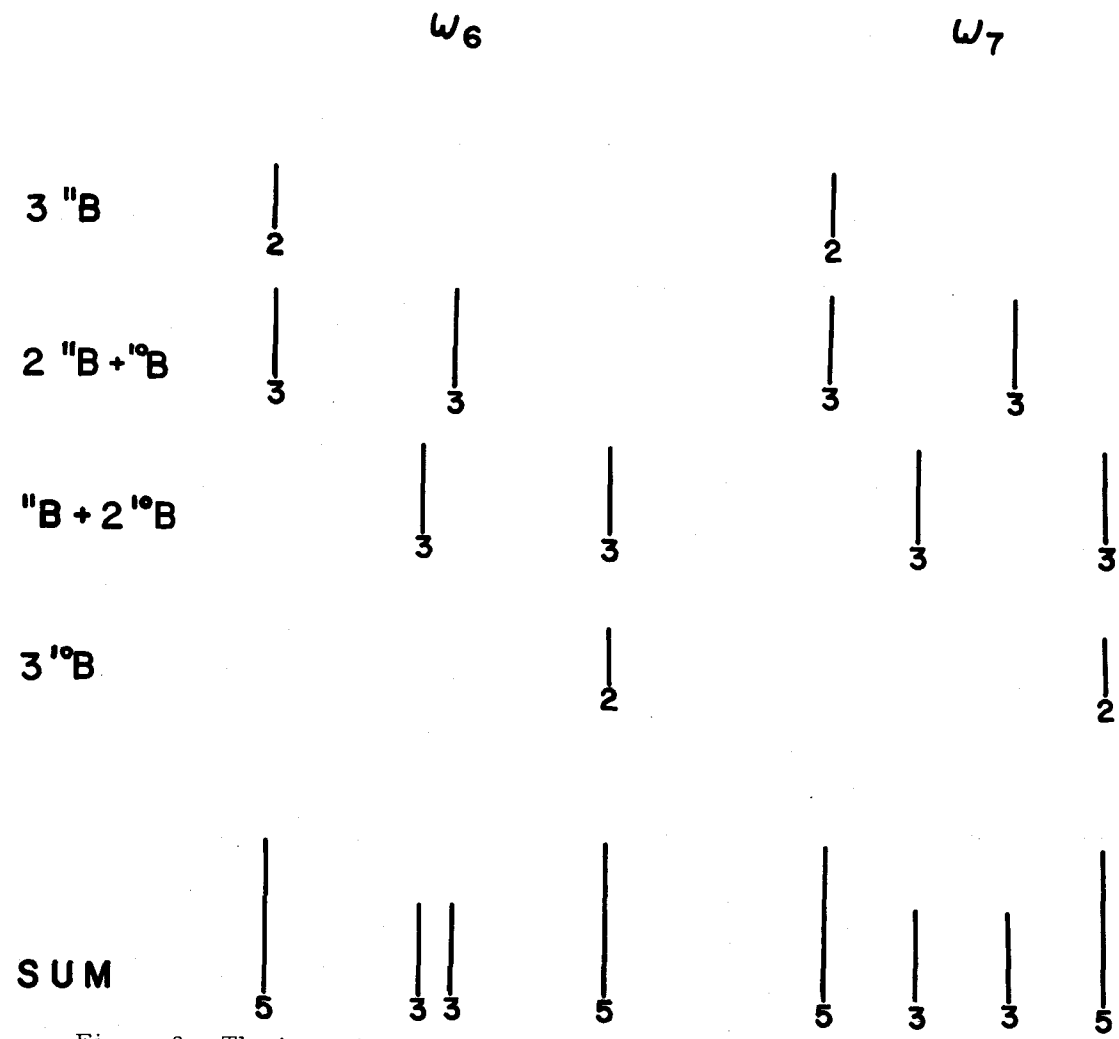


Figure 8. The isotopic components of  $\omega_6$  and  $\omega_7$  of the metaborate trimer when  $^{11}\text{P} = ^{10}\text{P} = 0.5$ .



The trimer ion belongs to the  $D_{3h}$  group, and its planar structure in  $K_3(BO_2)_3$  according to Zachariasen is shown in Figure 9.

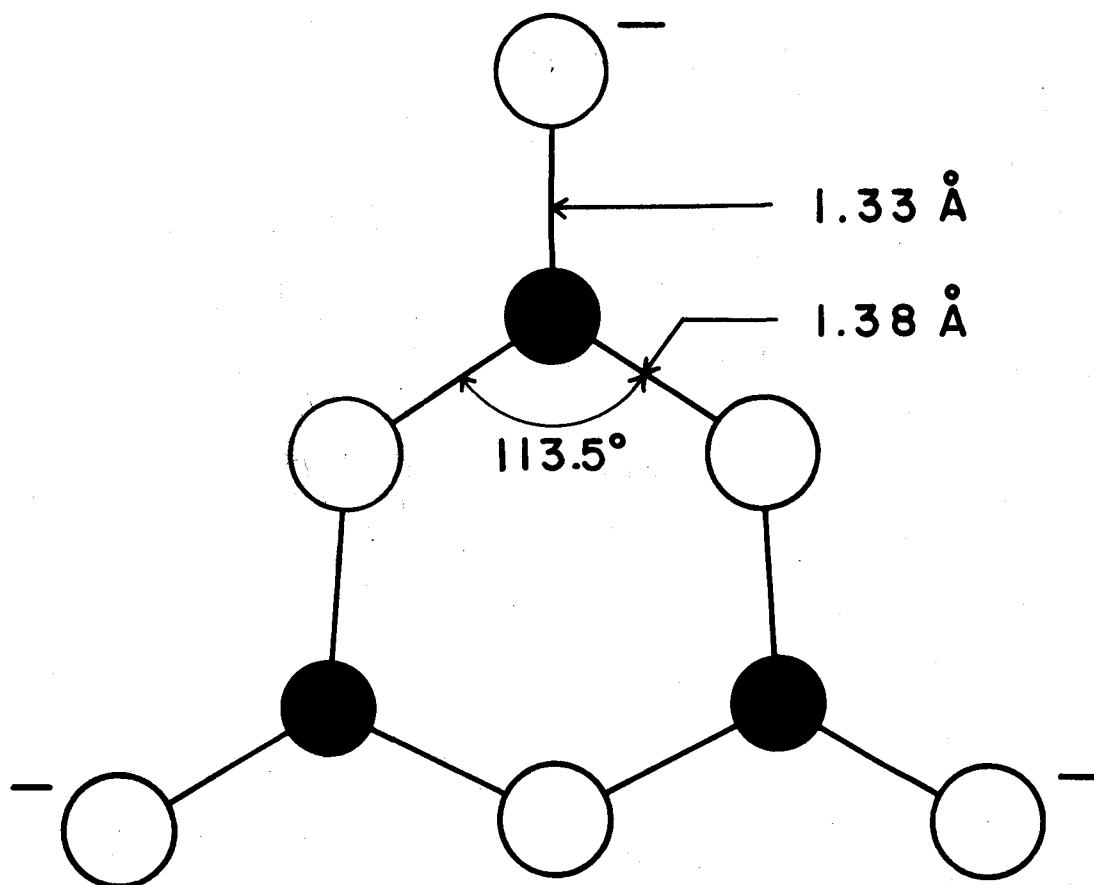


Figure 9. The metaborate trimer in  $K_3(BO_2)_3$  according to Zachariasen (45).

The trimer in the potassium salt has a ring B-O distance of  $1.38 \text{ \AA}$ , an external B-O distance of  $1.33 \text{ \AA}$ , and an interior ring O-B-O angle of  $113.5^\circ$ . Whereas these bond lengths in the sodium salt are reported by Marezio *et al.* (30) to be  $1.433 \text{ \AA}$  and  $1.280 \text{ \AA}$  respectively. It is feasible that the trimer ion fits in an alkali halide

lattice by replacing three next nearest neighbor halide ions which form an equilateral triangle. The plane of the trimer would then be in a (111) plane in the crystal as shown in Figure 10.

Using the dimensions for the trimer in the potassium salt, the  $O^- - O^-$  distance was calculated to be  $4.74 \overset{\circ}{\text{Å}}$ , and the anion-anion distances for NaCl, KCl, KBr, and CsI have been listed in Table 3. Although the impurity fits best in KCl, a consideration of the anion-anion distances suggests that KBr should be the best host. This argument assumes that the three negative charges are on the exterior oxygens which is not altogether true. The ring B-O distance is longer than the exterior B-O<sup>-</sup> distance; hence the exterior B-O<sup>-</sup> bond must have more double bond character. Thus the actual structure of the trimer ion must be somewhere between the two resonance structures shown in Figure 11.

Dingle (11) determined the bond order of  $\pi$  electrons in several boron-oxygen compounds using the standard Hückel-type analysis including the  $\omega$ -technique. Some of these calculated bond orders and published bond lengths are given in Table 8. By interpolation the bond order of the exterior B-O<sup>-</sup> and interior B-O bonds for the potassium salt should be approximately 0.54 and 0.45. Therefore, the oxygen exterior to the ring shares two  $\pi$  electrons with the boron atom approximately half of the time. The negative charge should, on the average, be situated along the exterior B-O bond about 1/4 of the bond

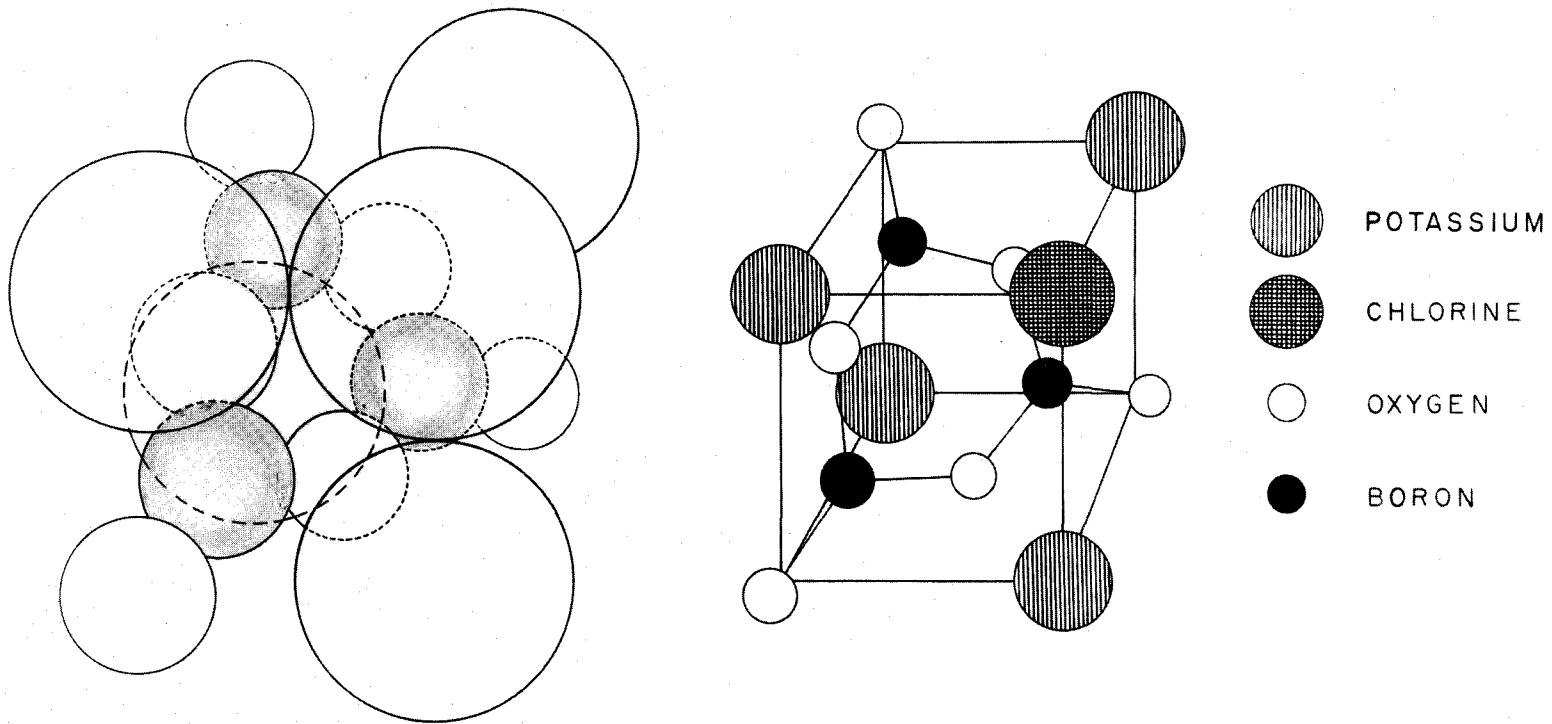


Figure 10. The metaborate trimer,  $(\text{BO}_2^-)_3$ , in solid solution in the KCl lattice.

length from the oxygen atom. Several distances between two negative charges have been calculated and are tabulated in Table 9 assuming specified distances between the boron atom and negative charge. If the distance between the boron atom and the negative charge is 1.00-1.15 Å which is consistent with the bond order calculations, then the electrostatic energy required to introduce the trimer into the lattice would be a minimum for either KCl or NaCl.

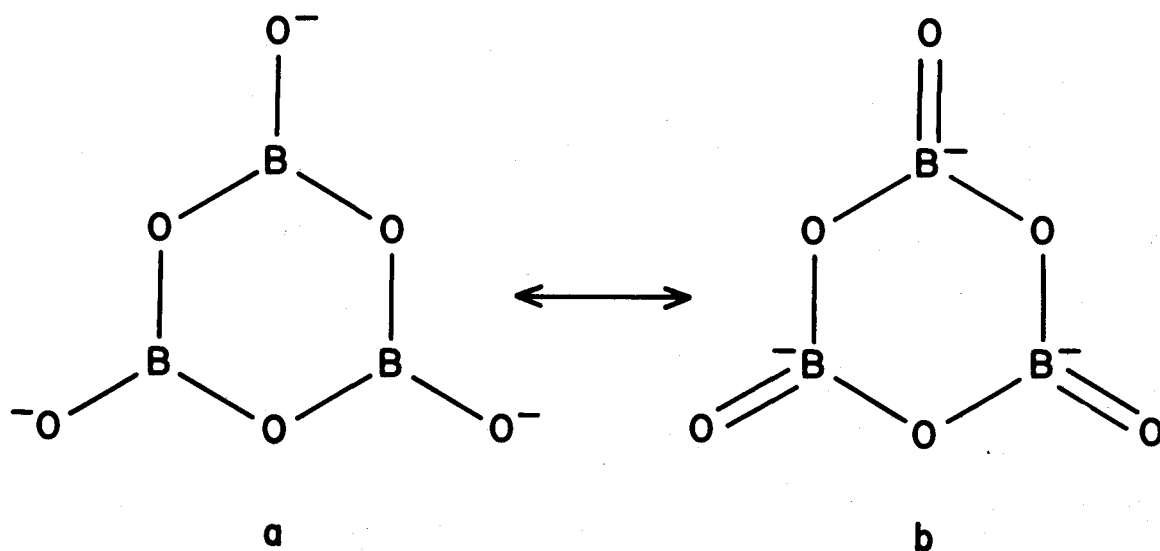


Figure 11. Two resonance structures of the metaborate trimer.

Table 8. Bond order of  $\pi$  electrons in boron-oxygen compounds according to Dingle (11).

Molecule	Bond	Bond length (Angstroms)	References	Bond order	
				Simple theory	$\omega$ -technique
$B_3O_6^{-3}$	BO-B	1.433	30	...	0.372
$BO_3^{-3}$	OB-O	1.35		0.555	0.503
$B_3O_6^{-3}$	B-O <sup>-</sup>	1.28	30	...	0.599

Table 9. Distance between two negative charges in the metaborate trimer.

Distance between boron and negative charge	Distance between two negative charges
1. 00 Å	4. 16 Å
1. 10 Å	4. 34 Å
1. 15 Å	4. 43 Å
1. 33 Å	4. 74 Å

Spatial considerations alone predict that the solubility of the trimer should increase as the size of the lattice and the ratio of anion to cation radii increase. Thus, for spatial reasons KBr should be the best host lattice; however for this model, in light of the electrostatic arguments, it is reasonable to expect KCl to be the best host. In this model the ring of the cyclic trimer fits in an interstitial position with the three ring oxygens and center of the ring situated near  $(1/4, 1/4, 0)$  and  $(1/6, 1/6, 1/6)$  respectively. There are three  $K^+$  ions at  $(1/2, 1/2, 0)$  and one  $K^+$  at  $(0, 0, 0)$  which lie directly above and below the ring. The calculated positions of the atoms of the undistorted trimer assuming that the distance from the boron atom to the special lattice sites  $(1/2, 0, 0)$  is  $1.15 \text{ \AA}$ , are given in Table 10 as well as the distances between these atoms and nearby  $K^+$  ions.

The amount of space available can now be compared with appropriate dimensions of this model which have been approximated with the aid of ionic radii recently published by Fumi and Tosi (21). These

ionic radii in addition to the ionic radius of  $O^-$  calculated from the interatomic distance of  $2.00 \text{ \AA}$  in  $Li_2O$ , are listed in Table 11. To a first approximation the ionic radius of  $O^-$  may be used as the radius of the oxygen in the trimer. However, the oxygen radii which are orientated toward the  $K^+$  ions should be smaller than the ionic radius because of localization of bonding  $\sigma$  and  $\pi$  electrons. The localization of nearly one  $\pi$  electron per B-O bond is expected to cause the greatest decrease in the radii in the directions of interest. If these radii are assumed to be  $0.7 \text{ \AA}$ , the sums of appropriate radii are in good agreement with the distances between the trimer atoms and  $K^+$  ions. The radius of boron is assumed to be the same; there is even less information about the ionic radius of boron while covalently bonded. If the effective radii are larger than  $0.7 \text{ \AA}$ , the corresponding electronic clouds would be compressed or more likely the trimer and lattice would be distorted. Even if it does not occur for this reason, a puckering of the ring is expected due to the expected discrepancy between the distance from the  $K^+$  at  $(0, 0, 0)$  to the center of the ring at  $(1/6, 1/6, 1/6)$ , and the sum of the ionic radius of the  $K^+$  and the half-thickness of the ring at the center. The bonding  $\pi$  electrons which are localized along B-O bonds project above and below the plane of the ring. Hence, the half-thickness of the ring at the center should be less than the radii of the atoms in the ring. In light of this, the half-thickness of the ring is assumed to be  $.1 \text{ \AA}$  less than

the radii of the boron and oxygen atoms resulting in 2.1 Å for the appropriate sum in the most favorable case as compared to 1.8 Å, the distance between (0, 0, 0) and (1/6, 1/6, 1/6).

Table 10. Positions of undistorted trimer atoms in the KCl lattice.

O <sup>-</sup>	(-.012, .524, -.012)
O	(.255, -.010, .255)
B	(.075, .350, .075)
Interatomic distances between trimer and KCl lattice	
d	O <sup>-</sup> O B
K (0, 1/2, 1/2)	3.07 2.87
K (1/2, 0, 1/2)	2.18
K (0, 0, 0)	3.29 2.26 2.30

Table 11. Ionic radii according to Fumi and Tosi (26).

	Ionic radii Å
K <sup>+</sup>	1.54
Cl <sup>-</sup>	1.60
*Li <sup>+</sup>	.86-1.00
O <sup>=</sup>	1.14-1.00

\* Represents the range found in four lithium halides.

Because of the C<sub>3v</sub> symmetry of the three K<sup>+</sup> ions above the ring and the one K<sup>+</sup> below it, any perturbation of the trimer would

lower the symmetry from  $D_{3h}$  to  $C_{3v}$ . A distortion of the lattice in the vicinity of this impurity would be expected to take the form of larger lattice constants while the symmetry of the site occupied by the trimer should be  $C_{3v}$  just as in the unperturbed case. Such a distortion seemed to be present, for it was evident that the single crystals which contained the impurities were strained to a greater extent than pure single crystals grown by the same method.

CsI was doped with  $H_3BO_3$  and most of the HI and  $H_2O$  formed was removed by evacuation. However no infrared absorption bands were observed. This is consistent with the above model because in the CsI lattice, which has the CsCl structure, the anion lattice sites form squares rather than the necessary equilateral triangles.

In light of the foregoing discussion the metaborate trimer ion which replaces three next nearest neighbor halide ions is considered the best model.

#### Proposed Model for C

The impurity which has been called species C is proposed to be the appropriate salt of the trimer ion in a second phase. This is based on the spectrum of  $Na_3(BO_2)_3$  observed by Goubeau and Hummel (24) and on the spectra observed by Hisatsune and Suarez (28). These experimental data are summarized for the sodium salt in Table 12. In the present investigation there is more of this impurity in



NaCl and KBr than in KCl; see Figure 2. The lines assigned to  $K_3(BO_2)_3$  in KCl and KBr, and the data of Hisatsune and Suarez are given in Table 13. Their assignment for KBr, being more complete, has been used rather than the assignment for KCl. Their experimental frequencies for KCl and KBr are the same within experimental error; see Table 2.

Table 12. Some fundamentals of  $Na_3(BO_2)_3$  ( $cm^{-1}$ )

Goubeau and Hummel		Hisatsune and Suarez $T \approx 300^\circ K$		Present work $T \approx 100^\circ K$	
$\omega_6$	1450 vs, vb 1425 vs, vb	$\omega_6$	1466 1436	$\omega_6$	1458 b 1432 b
$\omega_7$	1255 s, b 1227 s, b	$\omega_7$	1264 1241	$\omega_7$	1268 b 1246 b
$\omega_8$	720 w 702 m	$\omega_{11}$	724 708	$\omega_{11}$	720.5 703.4

The crystal structure of potassium and sodium metaborate has been determined by Zachariasen (45) and Fang (14) respectively to be rhombohedral with the space group  $R\bar{3}c$  ( $D_{3d}^6$ ). There are two  $K_3(B_3O_6)$  or  $Na_3(B_3O_6)$  molecules per unit cell, and the  $(BO_2^-)_3$  groups occupy sites having  $D_3$  symmetry. The number of internal modes, their symmetry species, and spectral activity may be obtained by means of correlation diagrams which are given in Figure 12. Because  $A_{2u}$  and  $E_u$  modes are infrared active for the  $D_{3d}$  group;  $\omega_4$ ,  $\omega_5$ ,  $\omega_{13}$ , and  $\omega_{14}$  should become infrared active in the crystal.

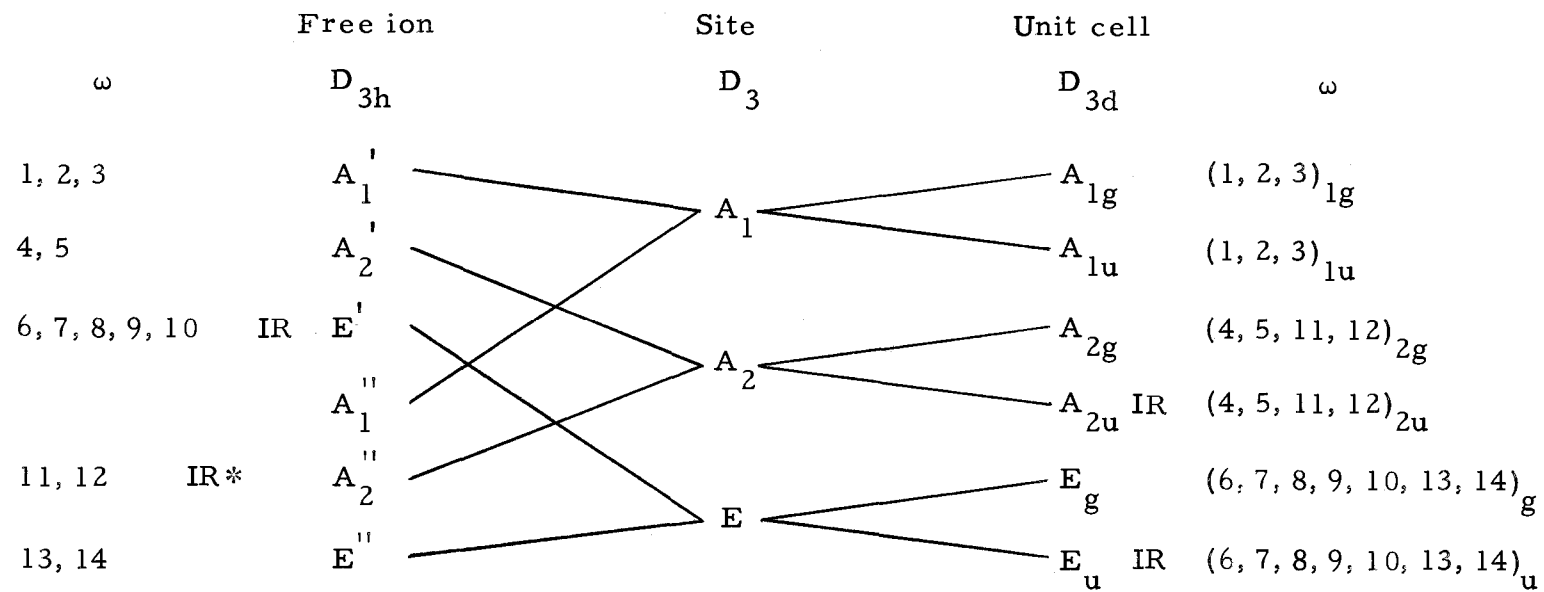
Table 13. Some fundamentals of  $K_3(BO_2)_3$ . ( $cm^{-1}$ )

	Hisatsune and Suarez				Present work in KCl				Present work in KBr	
	$T \approx 300^\circ K$				$T \approx 100^\circ K$				$T \approx 100^\circ K$	
	$B^{nat}$	$B^{syn}$	$^{11}B$	$^{10}B$	$B^{nat}$	$B^{syn}$	$^{11}B$	$^{10}B$	$^{11}B$	$^{10}B$
$\omega_6$	1405 vs	1406 vs	1400 vs	1460 vs	1401 m	1405 m	1399 m	a	1400 vs	1470 vs
$\omega_7$	1225 s	1233 s	1222 vs	1238 s	1225 b, m	1225 b	1220 b		1228 vs	1232 s
	1249 s	1257 vs	1247 s	1265 vs	1245 b, w	1255 b, m		1265 m	1250 s	1260 s
$\omega_{11}$	734 s	736 s	728 s	754 s	726 w	728 vw	726.5vw	743 w	728 s	749 m
		746 s			732 w	732 w	732.6 vw			

a = obscured

$B^{nat}$  = natural abundance

$B^{syn}$  = 50%  $^{11}B$



\* IR denotes infrared activity

Figure 12. Correlation diagrams and spectral activity corresponding to the metaborate trimer as a free ion and in the rhombohedral unit cell of  $K_3(BO_2)_3$  or  $Na_3(BO_2)_3$ .

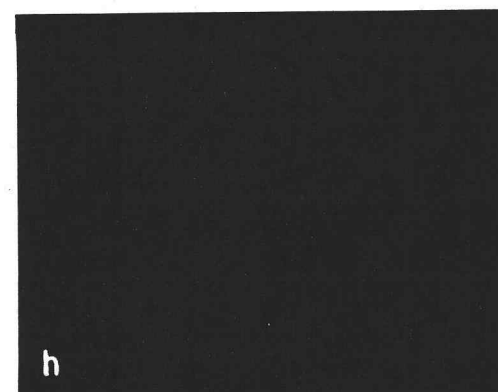
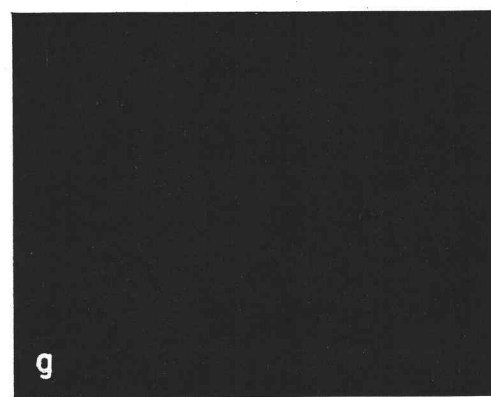
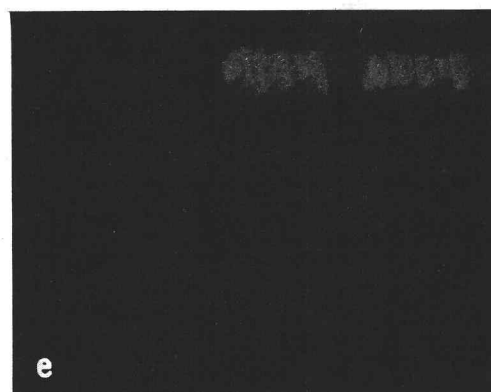
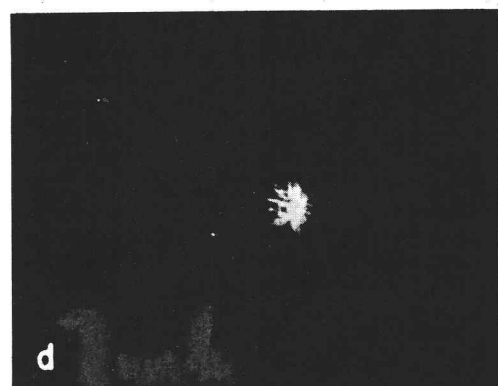
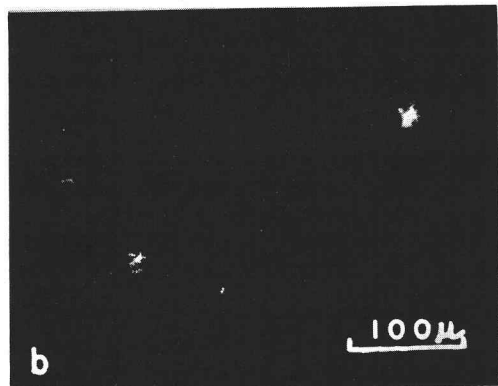
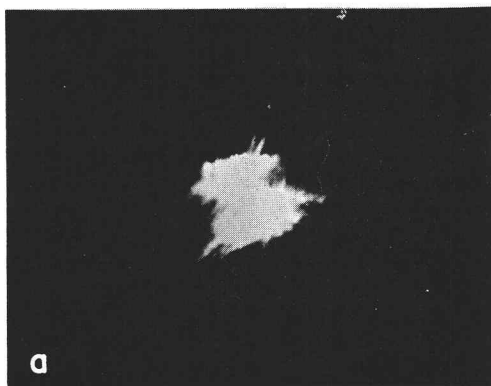
There is a further complication which must be considered. If adjacent trimer ions are isotopically nonequivalent, then a weak interaction would result. There should, therefore, be more components than originally anticipated, and the components due to the trimer with equivalent borons should become weaker when mixtures of boron isotopes are used. This is found to be the case. If adjacent  $C_{2v}$  trimer ions are to be isotopically equivalent, in addition to containing the same number of  $^{10}\text{B}$  and  $^{11}\text{B}$  atoms, the nonequivalent boron atom in one trimer ion must occupy the same position as the corresponding boron atom in the adjacent trimer ion. Therefore a large number of modes are expected which may account for the broad, almost polymer-like bands.

#### Light Scattering Evidence of a Second Phase

The bands observed by Hisatsune and Suarez (28), previously attributed to a second phase, and the good agreement between their observations and those in NaCl and KBr in this investigation suggest that a second phase is present. The width of these bands is also evidence of a second phase. In order to confirm the presence of a second phase, scattering experiments using visible light were performed. Defect scattering was observed in NaCl and KBr doped with  $\text{NaBO}_2$  and  $\text{KBO}_2$  respectively with an ultramicroscope, and photomicrographs were taken and are shown in Figure 13. It appears that one

Figure 13. Light scattering observed by means of an ultramicroscope.

- |               |              |
|---------------|--------------|
| a. doped KBr  | e. pure KBr  |
| b. doped NaCl | f. pure NaCl |
| c. doped KBr  | g. doped KCl |
| d. doped NaCl | h. pure KCl  |



should be able to estimate the size of the defects; however, the microscope was focused in order to maximize the scattered light and therefore the microscope was not, in general, focused on the defects but on the light scattered from the defect. Aside from a few large clusters of defects the size of the scattered light became relatively much smaller when the microscope was focused on an individual scattering center. Bansigir and Schneider (2) conducted direct microscopic studies and measurements of the optical scattering spectrum of relatively pure and doped alkali halide crystals. Using the Mie theory they calculated the radii of their equivalent scattering spheres to be of the order of  $1600 \text{ \AA}$ .

In the present investigation the amount of defect scattering was measured by means of a recording polarization spectrometer (13). The incident light was vertically polarized and designated E, and the vertically and horizontally polarized components, E and B respectively, of the scattered light were measured perpendicular to the incident light. The EB component is a measure of the scattered light which has been depolarized by the defects and by things such as surfaces, whereas the EE component is a measure of light scatter from surface imperfections. Consequently, the ratio EB/EE is related to the amount of light which has been depolarized by defects and therefore to the number and size of the defects. The EB/EE ratio is tabulated in Table 14 for several different crystals which were grown in this

laboratory by the Stockbarger method except for the pure KBr crystal which is a Harshaw crystal. This behavior is typical for Harshaw crystals due to very small bubbles and other defects introduced during the growing process. Therefore, the amount of defect scattering in doped NaCl and KBr is significant, whereas the defect scattering in doped KCl is much smaller.

Table 14. Light scattering in alkali halides.

		EB/EE	Ratio of doped to pure
KCl	pure	. 26	1. 2
KCl	doped	. 32	
NaCl	pure	. 27	1. 8
NaCl	doped	. 49	
*KBr	pure	. 46	1. 0
KBr	doped	. 48	

\* Harshaw crystal

In a recent investigation by Squire and Zamecki (38) the optical birefringence in pure single crystals of KCl and LiF has been studied. The crystals used in their study typically contained some  $10^6$  dislocations per  $\text{cm}^2$  which arise during the growth from the melt.

Unless the temperature gradient across the liquid-to-solid interface is kept very uniform, a stress is generated which is relieved by the formation of dislocations. These dislocations are preferentially oriented in the crystal because the temperature gradient which is not uniform within the furnace has an orientation.

Their results using polarized light demonstrated that a majority of the



defects which produce the optical anisotropy may be linked with the  $\langle 100 \rangle$  direction. Adair, Sharp, and Squire (1) observed that these same crystals have a small paramagnetic, uniaxial anisotropy by means of a delicate torsion pendulum technique and assigned the magnetic centers to a great number of dislocations orientated along the  $\langle 100 \rangle$  direction. In addition, two recent optical studies on alkali halides support the above evidence for dislocations acting as scattering centers. Plint and Watson (36) reported light scattering from charged dislocations in KCl:Pb whose intensity has fourfold symmetry when the crystal is rotated about an axis parallel to the  $\langle 100 \rangle$  direction at 23 rev/sec. The scattered light was observed at  $90^\circ$  to the incident light which was incident upon the (100) plane using a photomultiplier and an amplifier tuned to 92 and 184 cps. The ratio of the signals at the two frequencies gives some information on the shape of the centers. They attributed the scattering centers to charged dislocations which have an effective diameter of  $100 \text{ \AA}$ , have an approximate length of  $10,000 \text{ \AA}$ , and may be orientated in the  $\langle 100 \rangle$  direction. Taurel and Girard-Nottin (40) observed light scattering in single crystals of sodium chloride, and the intensity was found to have fourfold symmetry as the crystal was rotated in a manner similar to that of Plint and Watson. The authors attributed the scattering centers to orientated precipitates which decorate dislocation lines.

Many dislocations are expected in the crystals grown during this

investigation because of the nonuniform temperature gradient across the liquid-to-solid interface. Therefore, it seems reasonable to assign the defects which are responsible for light scattering to precipitates along dislocation lines. It is evident from the photomicrographs that the defects tend to lie along what seem to be crystalline axis, particularly in the larger clusters of defects. When the doped crystals were quenched from near the melting temperature to near the boiling point of liquid nitrogen, the intensities of the broad bands became smaller. The size of this attenuation increased for the series NaCl, KCl, and KBr from a slight attenuation in NaCl to an apparently complete removal of these bands in KBr. Moreover, no scattering centers were observed with the ultramicroscope in the KBr crystal after quenching. This is good evidence that the broad infrared bands and the light scattering are both due to the potassium and sodium salts of the metaborate trimer.

#### Proposed Model for B

The spectral information on species B is quite complex, and has thus far defied a complete interpretation. The infrared bands occur near the fundamental and combination bands of the trimer, and their intensities vary independently of the trimer band intensities as the concentration of boron and as the thermal history are varied. Most of the bands of B as well as the corresponding trimer bands are

listed in Table 15 for the molecules containing  $3^{10}\text{B}$  and  $3^{11}\text{B}$ . The assignment is much less complete for the molecules containing a mixture of boron isotopes due to the much greater complexity.

Species B is favored as the concentration of boron becomes larger and when the crystal is annealed slowly compared to a rapid quench. That both of these conditions favor larger molecules coupled with the proximity of the infrared bands of the trimer and species B suggest that B contains trimer ions which are somehow associated. These trimer ions could share an exterior oxygen or they might merely be on adjacent sites. Interactions between adjacent trimer ions have been discussed in the previous section, and they are theoretically capable of producing the observed perturbations on the vibrational modes of the trimer.

Some of these perturbed modes are more intense than other perturbed modes relative to their adjacent trimer modes. This may be explained using this model as follows. The size of the interaction and consequently the resulting normal coordinate depends upon the unperturbed motion or the original normal coordinate and the orientation of the two trimer ions. The integrated intensity, in turn, is related to the perturbed normal coordinate,  $Q_k$ , according to the expression

$$I_k = \left(\frac{\partial \mu_x}{\partial Q_k}\right)_0^2 + \left(\frac{\partial \mu_y}{\partial Q_k}\right)_0^2 + \left(\frac{\partial \mu_z}{\partial Q_k}\right)_0^2 = \left(\frac{\partial \mu}{\partial Q_k}\right)_0 \cdot \left(\frac{\partial \mu}{\partial Q_k}\right)_0 \quad (3-1)$$

in which  $\mu_x$ ,  $\mu_y$  and  $\mu_z$  are components of the dipole moment. For these reasons species B is tentatively attributed to interaction between trimer ions.

### The Monomer of Metaborate and Boron Isotope Ratios

The metaborate monomer is a symmetrical linear ion which is isoelectronic with carbon dioxide. It was first observed in commercial NaCl by McDonald (31) and later studied in KCl and KBr by Morgan and Staats (32). The latter investigators observed the combination band  $\omega_2 + \omega_3 - \omega_2$  in addition to the fundamentals  $\omega_2$  and  $\omega_3$ . The initial state corresponding to the transition  $\omega_2 + \omega_3 - \omega_2$  is  $\Pi_u$  as shown in Figure 14, and the population of this state is

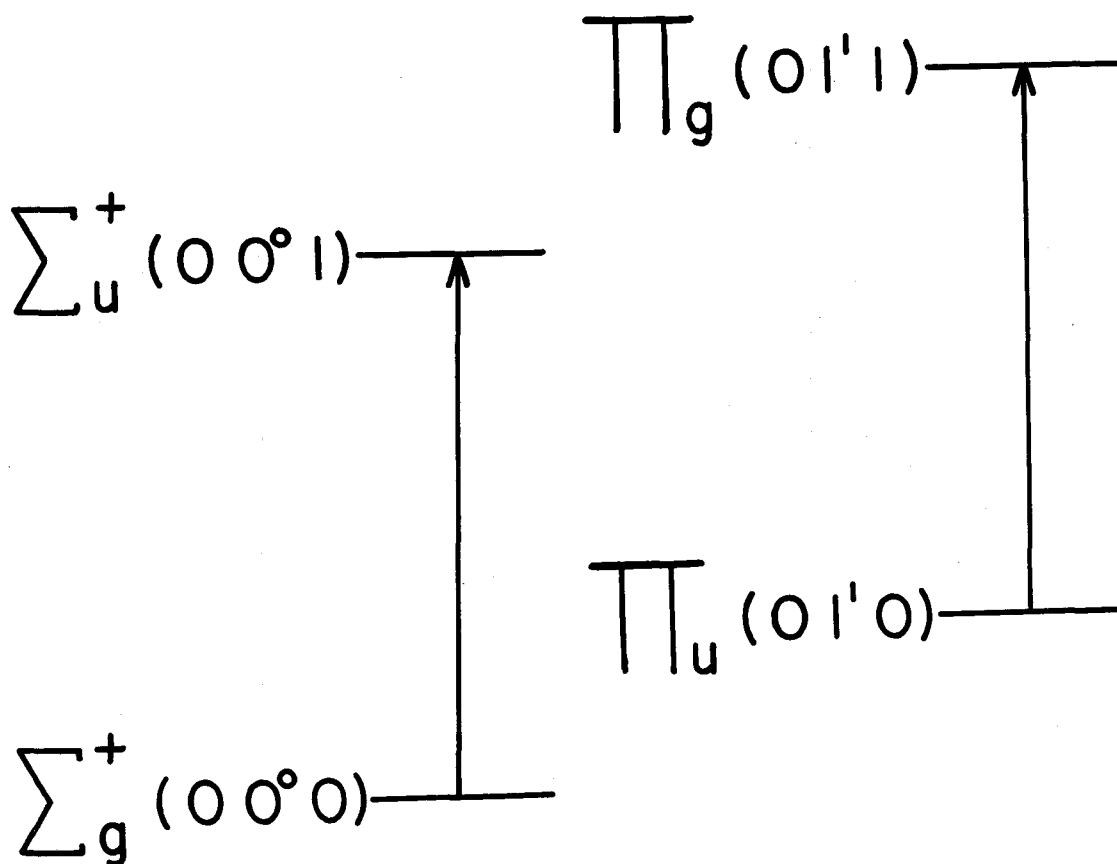
$$\frac{e^{-h\omega_2 c/kT}}{2e} \quad (3-2)$$

times the number in the ground state  $\Sigma_g^+$  (00° 0).

To a first approximation when calculating the number of  $\omega_2 + \omega_3 - \omega_2$  transitions relative to  $\omega_3$ , the same Boltzmann factor can be employed. This is very useful when calculating the relative amounts of isotopic boron in highly enriched boron samples because of the large errors which are normally present when comparing largely different absorbances. At room temperature this Boltzmann factor is about .10 which allows a favorable comparison between  $\omega_2 + \omega_3 - \omega_2$

Table 15. Trimer fundamentals and trimer interaction bands in KCl at  $\approx 100^\circ\text{K}$ . ( $\text{cm}^{-1}$ )

	Trimer				Trimer interaction			
	$3^{11}\text{B}$	$2^{11}\text{B}^+{}^{10}\text{B}$	$11^{10}\text{B}^+{}^{10}\text{B}$	$3^{10}\text{B}$	$3^{11}\text{B}$	$2^{11}\text{B}^+{}^{10}\text{B}$	$11^{10}\text{B}^+{}^{10}\text{B}$	$3^{10}\text{B}$
$\omega_{11}$	773.5	781.1	786.6	791.1	770 w			
$\omega_7$	1175.2	1175.9	1188.3	1208.8	1169 w	1195 sh	1200 sh	1202.5 w
		1198.7	1207.9		1190.6 m			1224.3 m
					1206.2 m			1233.6 mw
$\omega_6$	1430.6	1430.8	1459.4	1481.8	1426.5 m	1452	1457	1472 w
		1460.8	1480.8		1440.0 s			1479 s
					1457.5 m			1495 w
					1463.4 w			1499 w

Figure 14. The fundamental  $\omega_3$  and combination  $\omega_2 + \omega_3 - \omega_2$  of the metaborate monomer.

of the enriched isotope and  $\omega_3$  of the other isotope. Values of .039 and .027 were obtained by this method for  $^{10}\text{B}$  and  $^{11}\text{B}$  in enriched samples, and the respective isotopic contents according to the manufacturer are .040 and .026.

It may easily be shown that

$$\sum_k \frac{I_k}{(\omega_k)^2} \quad (3-3)$$

is an isotopic invariant where  $I$  is the integrated intensity and the sum is carried out over the  $k$  normal modes which belong to the symmetry species of interest; see for example Wilson, Decius and Cross (43). Therefore, the absorption coefficient which is proportional to the integrated intensity is larger for the isotopic component which occurs at a higher frequency. Since  $\omega_3$  is the only fundamental of  $\text{BO}_2^-$  which corresponds to the  $\Sigma_u^+$  symmetry species, the relative isotopic absorption coefficients can be calculated. The reported isotopic compositions have accordingly been corrected, but those used in predicting absorbances of the fundamentals of the trimer were not, because similar but unknown corrections would have to be applied to the experimental absorbances.

This combination band may also be used to determine the temperature of the crystal by means of the temperature dependence of the Boltzmann factor given in Equation 3-2.

### Equilibria Between Impurities

The equilibria that exist between the impurities depend upon the lattice, concentration of boron, and thermal history; and they are discussed in light of the proposed models. As the total concentration of  $\text{NaBO}_2$  becomes larger within the same  $\text{NaCl}$  crystal, the increase in concentration of  $\text{Na}_3(\text{BO}_2)_3$  is greater than that of the trimer in solid solution. Conversely, the concentration of monomer actually decreases as the concentration of boron increases within the same crystal. Upon quenching, the amount of precipitate decreased slightly, the trimer remained unchanged within experimental error, but the accompanying increase in the monomer was apparently greater than anticipated as may be seen in Figure 2. It should be borne in mind that the removal of each trimer ion results in three monomer ions and that the monomer lines are much narrower. Thus, the increase in monomer ions merely appears to be greater than anticipated.

The dependence upon boron concentration is very similar in  $\text{KCl}$  for the monomer, trimer, trimer interaction, and  $\text{K}_3(\text{BO}_3)_3$  and is shown for the first three in Table 16 and in Figures 3 and 4 for typical crystals. The numbers in Table 16 should be considered only as approximate indications of relative changes in each of the three impurities. The boron concentration in one crystal was determined colorimetrically to be four times greater in a sample near the top compared

to near the bottom. In some very dilute samples the trimer interaction bands were almost completely missing.

Table 16. Relative concentrations of the monomer, trimer, and trimer interaction in a KCl crystal.

	Monomer	Trimer	Trimer interaction
Top	1	6	14
Middle	7	2.7	3.4
Bottom	10	1	1

When KCl crystals were quenched, the concentration of monomer increased and those due to the trimer and trimer interaction decreased with the trimer interaction showing the greatest decrease. As in the case of the dilute samples the interaction bands were very weak and negligible compared to those of the monomer and trimer. Two weak bands which had not previously been observed in these crystals were observed and will be discussed later. As expected, annealing the KCl crystals gave results opposite to those observed in the quenching experiments. Relative concentrations of the monomer, trimer, and trimer interaction as determined from the intensities of corresponding modes were then known after three different thermal treatments. Information on the absorption coefficients of the monomer and trimer is available from these data if the absorption coefficient of the interaction bands are the same as those of the unperturbed trimer bands. The amount of trimer present is then related to the



sum of the trimer band and the trimer interaction bands. The total amount of boron or number of  $\text{BO}_2$  groups present is

$$C = 3C_T + C_M \quad (3-4)$$

where  $C_T$  and  $C_M$  are the concentrations of the trimer and monomer respectively. Using Beer's law, Equation 3-4 becomes

$$\frac{A_M}{t} = -3 \frac{a_M}{a_T} \frac{A_T}{t} + \frac{1}{2.3} C a_M \quad (3-5)$$

in which  $A$ ,  $a$ , and  $t$  refer to absorbance, absorption coefficient, and the thickness of the sample respectively. From a plot of  $A_M/t$  versus  $A_T/t$ ,  $a_M$  and  $a_T$  may be determined from the slope and  $A_M/t$  intercept. Although it might be simpler to plot  $A_M$  versus  $A_T$ , the thickness has been included because the samples were repolished after annealing which resulted in a thickness attenuated by  $< 10\%$ . This raises the question of error due to possible inhomogeneity. Since the amount of boron was shown to vary  $< 10\%$  both perpendicular to the growth axis and for a distance of one cm parallel to the axis, the error due to inhomogeneity is known to be small. Such plots which are reproduced in Figure 15 for two crystals doped with enriched  $^{10}\text{B}$  and  $^{11}\text{B}$  gave values for  $a_M$  which were different by 30% while those for  $a_T(\omega_7)$  were within 1% of each other.

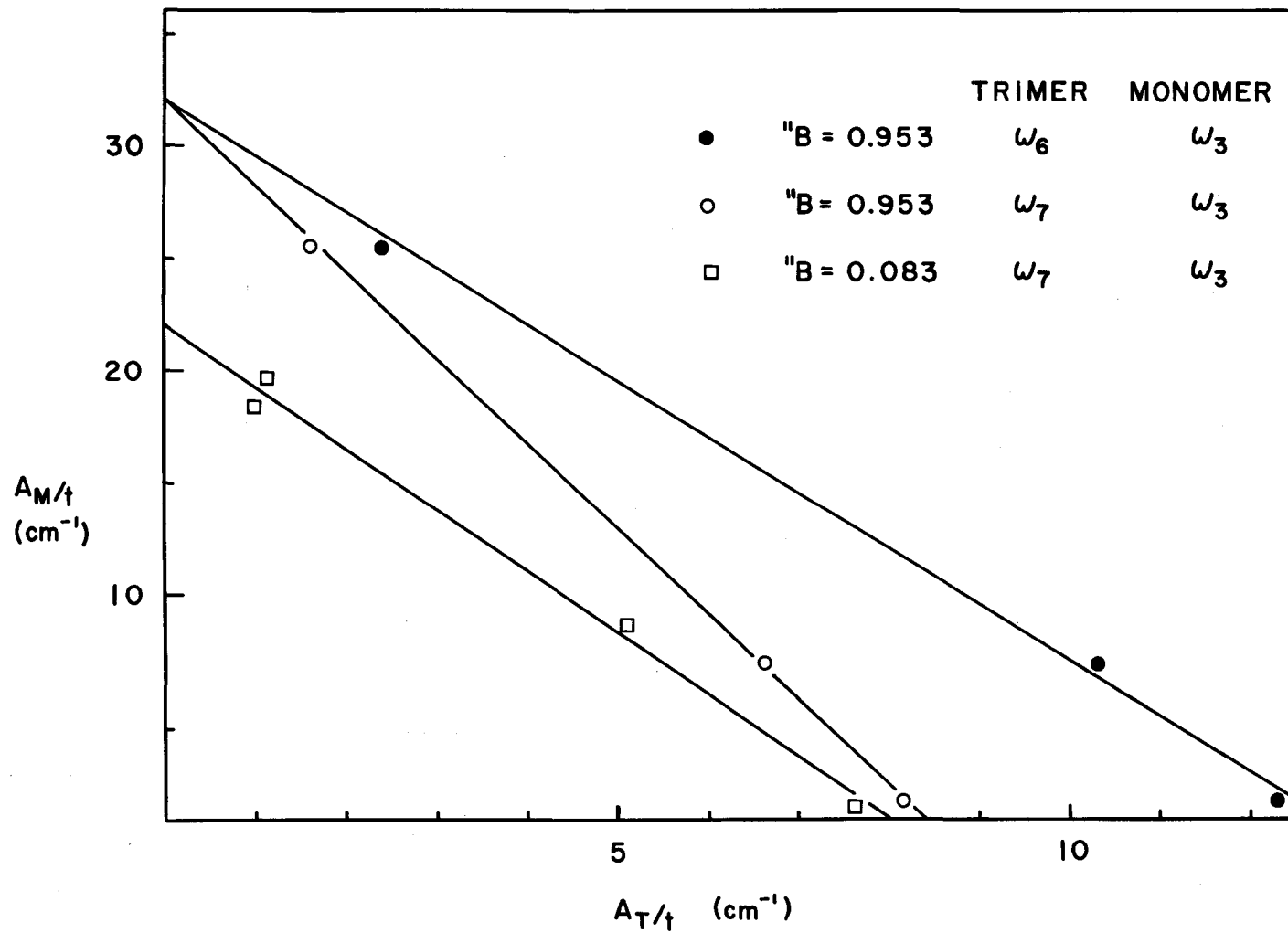


Figure 15.  $A_M/t$  at  $T \approx 300^\circ \text{K}$  versus  $A_T/t$  at  $T \approx 100^\circ \text{K}$  in KCl crystals at various thermal histories.

The assumption that the absorption coefficients of the trimer and the interaction bands are equal may not be valid; or, more likely, significant overlapping may result between these bands including smaller interaction bands which have not been considered, thereby causing the observed uncertainty. However, the observed linearity of these plots is good evidence that the species which has been attributed to the trimer is composed of  $\text{BO}_2^-$  units; although no information is available from these plots on the number of  $\text{BO}_2^-$  units. Average values are listed in Table 17 as well as the value of  $a_M$  found in KBr.

Table 17. Absorption coefficients.

		KCl	KBr
		$(\text{cm}^{-1} \text{ppm}^{-1})^*$	$(\text{cm}^{-1} \text{ppm}^{-1})^*$
$a_M$	$\omega_3$	.9	.71
$a_T$	$\omega_6$	1.2	
$a_T$	$\omega_7$	.8	

\* In molar fraction

The more dilute samples of KBr were found to contain nearly all monomer and only very small amounts of trimer in solid solution and in a second phase, thereby allowing the absorption coefficient of the monomer to be determined. A quenching experiment on a more concentrated KBr sample, as shown in Figure 2, resulted in the complete removal of the precipitated trimer, the reduction of the trimer bands to very weak bands, and a very large increase in metaborate

monomer producing the largest concentration of monomer observed in this laboratory. One very weak and two weak bands were observed in the quenched KBr crystal which may be related to the bands in KCl produced upon quenching. In KBr these bands may have been obscured by the broad second phase bands before quenching. Neglecting these for the moment, this result demonstrates that the broad and sharp features which have been assigned to the trimer in a second phase and in solid solution are due to impurities which contain  $\text{BO}_2^-$  units. If the trimer is made of  $\text{BO}_2^-$  groups, we may conclude that the trimer interaction bands in KCl which are nearly removed by quenching are also due to an impurity which may be constructed with  $\text{BO}_2^-$  groups.

The metaborate monomer was found to be more soluble as the size of the lattice was increased from NaCl to KBr, as is expected for a monovalent ion which fits substitutionally in the lattice. This trend was not observed for the trimer consistent with the argument that the solubility is greater when the fixed distances between the three negative charges on the trimer more closely approach the anion-anion distance in the lattice. From the above results we also know that an equilibrium exists between the monomer and the trimer which may be in solid solution, near another trimer ion, or in a precipitate. This equilibrium favors a larger concentration of monomer as the temperature is increased. The monomer ions being small diffuse through the crystal in a random manner, but the larger trimer ions are not

expected to move as a unit. If the temperature of the crystal is lowered rapidly, the monomer ions lose their ability to move. Because the equilibrium between the monomer and trimer depends upon the probability of having three monomer ions at approximately the same position in the lattice, the concentrations of the various impurities correspond to the equilibrium which existed at the temperature from which the crystal was quenched. When the temperature is lowered slowly the equilibrium would then roughly correspond to the temperature range at which the monomer becomes nearly immobile.

After quenching KCl and KBr crystals, several sharp and weak bands were found which were not observed before. These bands became significantly larger in KCl as the starting temperature of the quench was increased, whereas all the nearby bands became slightly less intense as shown in Figure 4. This behavior suggests that either another impurity is being formed which is favored by higher temperatures or the trimer ion is at a different position in the lattice. These bands are more intense in KBr even though the KBr crystal was quenched from a temperature less than or equal to those used with KCl. The frequencies and intensities in KCl seem to fit a pattern very similar to the one shown in Figure 8 for the trimer of metaborate except all six components are resolved. Furthermore, the frequencies are somewhere between those observed for the trimer ion in solid solution and in a second phase. Therefore, these bands are

very tentatively assigned to metaborate trimer ions in some unknown position.

Table 18. Bands observed upon quenching.  $T \approx 100^\circ \text{K}$ .

KBr	KCl			
$^{11}\text{B}$	$3^{11}\text{B}$	$2^{11}\text{B}+^{10}\text{B}$	$^{11}\text{B}+2^{10}\text{B}$	$3^{10}\text{B}$
1398.8	1402.3			1459
1196.5	1202.2	1204.3	1215.6	1246.4
		1234.2	1244.8	
753				

#### IV. NORMAL COORDINATE ANALYSIS OF THE TRIMER OF METABORATE

##### Symmetry Considerations and Internal Symmetry Coordinates

The trimer of metaborate has a total of nine atoms and therefore  $3N - 6 = 21$  vibrational degrees of freedom which consist of  $2N - 3 = 15$  in-plane and  $N - 3 = 6$  out-of-plane, vibrational degrees of freedom. When all three boron atoms are isotopically equivalent the trimer belongs to the  $D_{3h}$  group, whereas the replacement of one boron atom with an isotopically nonequivalent one lowers the symmetry to  $C_{2v}$ . The irreducible representations are

$$\Gamma = 3A_1' + 2A_2' + 5E' + 2A_2'' + 2E'' \quad (4-1)$$

and

$$\Gamma = 8A_1 + 2A_2 + 4B_1 + 7B_2 \quad (4-2)$$

for  $D_{3h}$  and  $C_{2v}$  respectively. The  $C_{3v}$  symmetry of the proposed site would lower the symmetry to  $C_{3v}$  and  $C_s$  for the trimer belonging to the  $D_{3h}$  and  $C_{2v}$  groups respectively. Correlation diagrams between these groups corresponding to both isotopic and site symmetry perturbations and the activity of the various modes are shown in Figure 16.

In this analysis the trimer was treated as if it consisted of

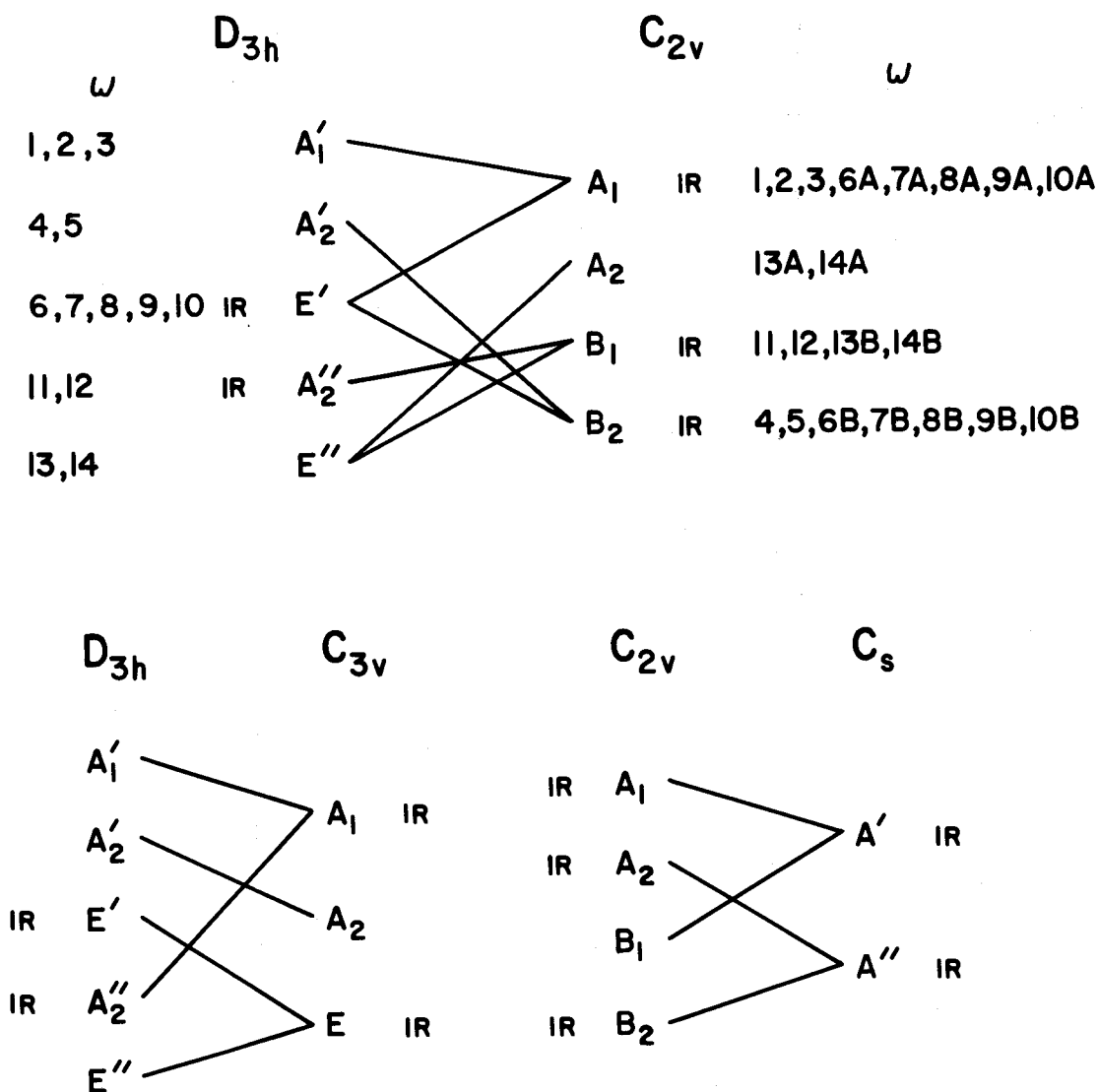


Figure 16. Correlation diagrams and spectral activity corresponding to isotopic and site symmetry perturbations of the metaborate trimer in alkali halides with the NaCl structure.



three symmetrically equivalent  $\text{BO}_3$  groups which were loosely coupled together. For convenience each internal symmetry coordinate was constructed from symmetrically complete sets of equivalent internal coordinates;  $r_i$ ,  $s_j$ ,  $\beta_i$ ,  $\alpha_j$ ,  $z_i$ , and  $Z_i$  which are described and depicted in Figure 17. The irreducible representations for these sets are listed in Table 19, and the internal symmetry coordinates formed from these internal coordinates are given in Appendix I. The second set of  $E'$  and  $E''$  symmetry coordinates are not necessary and have been included merely for completeness.

Table 19. Irreducible representations of  $(\text{BO}_2^-)_3$  for  $D_{3h}$  symmetry.

$\Gamma^{(\gamma)}$	$\eta_{\text{total}}^{(\gamma)}$	$\eta_{\text{vib.}}^{(\gamma)}$	$\eta_r^{(\gamma)}$	$\eta_s^{(\gamma)}$	$\eta_\alpha^{(\gamma)}$	$\eta_\beta^{(\gamma)}$	$\eta_z^{(\gamma)}$	$\eta_Z^{(\gamma)}$
$A_1'$	3	3	1	1	0	1	0	0
$A_2'$	3	2	0	1	1	0	0	0
$E'$	6	5	1	2	1	1	0	0
$A_1''$	0	0	0	0	0	0	0	0
$A_2''$	3	2	0	0	0	0	1	1
$E''$	3	2	0	0	0	0	1	1

#### G and F Matrices

The elements of both matrices were obtained by hand calculation, first for the internal coordinates and then for the internal symmetry coordinates. The F matrices corresponding to the  $D_{3h}$  internal

$r_i$  = change in exterior B-O<sup>-</sup> bond length

$s_j$  = change in interior OB-O bond length

$\alpha_j$  = change in exterior O-B-O<sup>-</sup> angle

$\beta_i$  = change in interior O-B-O angle

$\gamma$  = equilibrium interior B-O-B angle

$z_i$  =  $r \sin \theta$

$Z_i$  =  $-s \cos \gamma \sin \phi$

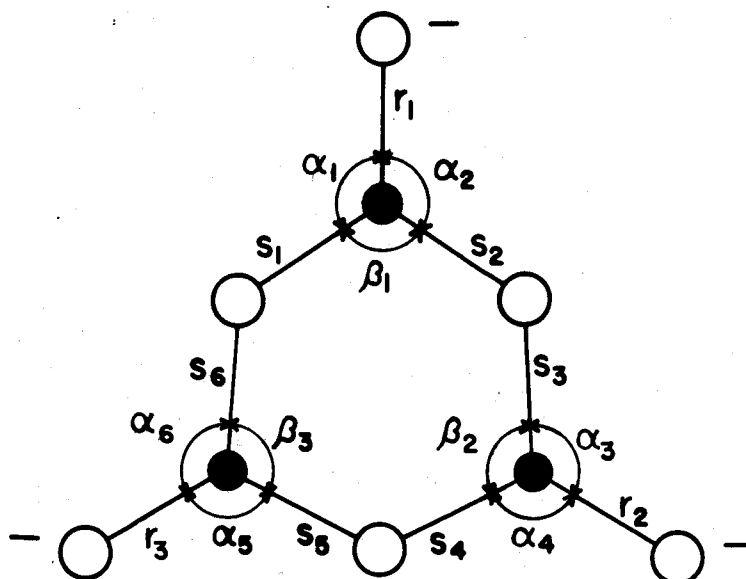
$\theta$  = angle formed by external O<sup>-</sup> and plane of BO<sub>2</sub>

$\phi$  = angle formed by interior ring oxygen and plane of the remainder of ring.

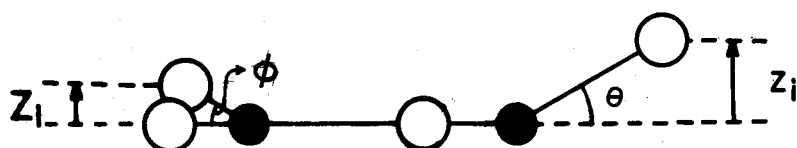
Where + and - numbers denote relative out-of-plane motion of the atoms.

\* No subscript denotes equilibrium value of coordinates

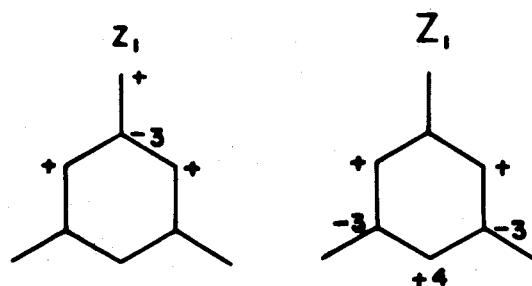
Figure 17. Internal coordinates of the metaborate trimer.



IN - PLANE



SIDE VIEW



TOP VIEW

OUT - OF - PLANE

coordinates and internal symmetry coordinates are given in Table 20 and Appendix II. Because of their complexity the corresponding G matrices, which are similar in form, are not shown. Although the formation of the G matrix was normally straightforward, the equilibrium bond lengths and angles were assumed to be equal to those for the trimer in  $K_3(BO_2)_3$  published by Zachariassen (45) and given in Table 21. A comparison with the corresponding values in  $Na_3(BO_2)_3$  published by Mazerio et al. (30) reveals the order of magnitude of the uncertainty that may be involved in this assumption. Their values of 1.280 and 1.433 Å are the smallest and largest ever observed for the triangular boron-oxygen bond.

In this normal coordinate analysis a generalized valence force field has been employed whose force constants have been tabulated in the F matrix in Table 20. All the terms corresponding to a potential interaction between two internal coordinates which are in different  $BO_3$  groups, with the exception of  $\phi_z'$ , have not been included due to the complexity of the potential function. The force constants

$$\phi_r = 6.96 \quad \text{and} \quad \phi_s = 5.57 \text{ md/\AA} \quad (4-3)$$

corresponding to a change in the exterior  $B-O^-$  and interior  $OB-O$  bond lengths were calculated using the empirical function

$$\phi_{\bar{r}} = 38.5 \bar{r}^{-6} \quad (4-4)$$

Table 20. F matrix for internal coordinates of metaborate trimer.

F	r <sub>1</sub>	r <sub>2</sub>	r <sub>3</sub>	s <sub>1</sub>	s <sub>2</sub>	s <sub>3</sub>	s <sub>4</sub>	s <sub>5</sub>	s <sub>6</sub>	β <sub>1</sub>	β <sub>2</sub>	β <sub>3</sub>	a <sub>1</sub>	a <sub>2</sub>	a <sub>3</sub>	a <sub>4</sub>	a <sub>5</sub>	a <sub>6</sub>
r <sub>1</sub>	φ <sub>r</sub>	0	0	φ <sub>s</sub> '	φ <sub>s</sub> '	0	0	0	0	sφ <sub>rβ</sub>	0	0	√rsφ <sub>rβ</sub> '	√rsφ <sub>rβ</sub> '	0	0	0	0
s <sub>1</sub>				φ <sub>s</sub>	φ <sub>s</sub> '	0	0	0	0	sφ <sub>rβ</sub> '	0	0	√rsφ <sub>rβ</sub> '	√rsφ <sub>rβ</sub> '	0	0	0	0
β <sub>1</sub>										s <sup>2</sup> φ <sub>β</sub>	0	0	s <sup>2</sup> φ <sub>β</sub> '	s <sup>2</sup> φ <sub>β</sub> '	0	0	0	0
a <sub>1</sub>													rsφ <sub>β</sub>	s <sup>2</sup> φ <sub>β</sub> '	0	0	0	0

F	z <sub>1</sub>	z <sub>2</sub>	z <sub>3</sub>	Z <sub>1</sub>	Z <sub>2</sub>	Z <sub>3</sub>
z <sub>1</sub>	s <sup>2</sup> φ <sub>z</sub>	s <sup>2</sup> φ <sub>z</sub> '	s <sup>2</sup> φ <sub>z</sub> '	s <sup>2</sup> φ <sub>zZ</sub>	s <sup>2</sup> φ <sub>zZ</sub> '	s <sup>2</sup> φ <sub>zZ</sub> '
Z <sub>1</sub>				s <sup>2</sup> φ <sub>Z</sub>	s <sup>2</sup> φ <sub>Z</sub> '	s <sup>2</sup> φ <sub>Z</sub> '

according to Decius (8, 9) where  $\bar{r}$  is the equilibrium bond length. Consequently the uncertainty in  $r$  and  $s$  mentioned in the previous paragraph will produce a relative uncertainty in  $\phi_{\bar{r}}$  which is six times larger. The effect of this and other uncertainties upon the predicted eigenvalues will be discussed later in this chapter. There is no information available on the restoring forces which are due to an interaction between internal coordinates in adjacent  $\text{BO}_3$  groups. Because these forces are thought to be small, the corresponding force constants have been set equal to zero. Values for the remaining, in-plane force constants or combinations of them;  $\phi_s'$  (.98 md/Å),  $\phi_\beta - \phi_\beta'$ , and  $\phi_{r\beta} - \phi_{r\beta}'$ ; which are thought to be similar to those for the borate ion, were borrowed from the values observed by Steele and Decius (39). Unfortunately individual values of  $\phi_\beta$ ,  $\phi_{r\beta}$ , and  $\phi_{r\beta}'$  were needed; therefore, several reasonable values have been tried.

Table 21. Bond lengths and angles in the meta-borate trimer.

	$\text{K}_3(\text{BO}_2)_3$	$\text{Na}_3(\text{BO}_2)_3$
$r(\text{B}-\text{O}^-)$	1.33 Å	1.280 ± .016 Å
$s(\text{BO}-\text{B})$	1.38 Å	1.433 ± .009 Å
$\angle \text{O}-\text{B}-\text{O}$	113.5°	

The situation for the out-of-plane blocks of the F matrix is less favorable. There are six force constants only one of which is similar

to the out-of-plane force constant for the borate ion, and there is no available information on the remaining five. Therefore, using the experimental frequencies which have been assigned to the corresponding modes in the present investigation and in that of Hisatsune and Suarez (28), the force constants were obtained by solving the secular equation simultaneously for  $^{10}\text{B}$  and  $^{11}\text{B}$ . The average of the values for the out-of-plane force constant obtained by Steele and Decius (39),  $1.815 \text{ md}\overset{\circ}{\text{A}} (\text{s}^2 \cdot 953 \text{ md}/\overset{\circ}{\text{A}})$ , agrees well with the calculated value of  $1.855 \text{ md}\overset{\circ}{\text{A}}$  given in Table 22. The small value of  $\phi_z'$ , the interaction force constant between two  $z$  coordinates in adjacent  $\text{BO}_3$  groups, is consistent with the assumption that the trimer ion may be described as three  $\text{BO}_3$  groups which are loosely coupled together. There are two values for each force constant because of the quadratic nature of the problem. There are actually four sets of values, but two of these sets lead to answers which are physically unrealistic.

Table 22. Calculated out-of-plane force constants for the metaborate trimer.

	$\overset{\circ}{\text{md}} \cdot \overset{\circ}{\text{A}}$	
	1	2
$\phi_z$	1.855	1.416
$\phi_z'$	.003	.222
$\phi_{zZ}$	.594	.390
$\phi_{zZ}'$	-.691	-.589
$\phi_Z$	.763	.723
$\phi_Z'$	-.178	-.157

Normal Coordinates and Eigenvalues

The normal coordinates (column matrix Q) are related to the internal symmetry coordinates (column matrix S) by the linear transformation

$$S = LQ \quad (4-5)$$

or upon multiplying on the left by  $L^{-1}$

$$Q = L^{-1}S \quad (4-6)$$

Substitution of (4-6) into the kinetic and potential energies of vibration results in the well known secular equation in matrix notation

$$(GF - \Lambda)L = 0 \quad (4-7)$$

as shown in Wilson, Decius, and Cross (43).

In order to solve the secular equation, an unsymmetric eigenvalue program obtained from the University of Wisconsin and adapted to a CDC-3300 computer was used in conjunction with matrix multiplication and matrix inversion subroutines. Furthermore, the elements  $G_{ij}$  for  $C_{2v}$  symmetry were numerically evaluated with the aid of the computer. Solutions of the secular equation for  $D_{3h}$  symmetry, which are given in Appendix III, depend strongly on the assumed values of  $\phi_{\beta}$ ,  $\phi_{r\beta}$ , and  $\phi_{r\beta}'$ . Also when some of the B-O stretching



force constants were altered corresponding to a five percent change in the equilibrium B-O distances, changes of up to 10% in the eigenvalues (15% for  $\omega_4$ ) were observed.

It is evident that this calculation can be used only as a rough prediction of the experimental frequencies and normal coordinates to aid in the assignment and not as a means to refine the force constants. A comparison between one set of predicted frequencies which is in good agreement with the best understood fundamentals and the complete assignment of the observed fundamentals in KCl is made in Table 23.  $\omega_1$  and  $\omega_4$ , which are infrared inactive for  $D_{3h}$  symmetry and weakly active for  $C_{2v}$  symmetry, are predicted to be near  $\omega_6$ , and between  $\omega_6$  and  $\omega_7$  respectively. Furthermore, several possible  $E'$  combinations involving an  $A_1'$  or  $A_2'$  mode occur near  $\omega_6$ , but only one such combination occurs near  $\omega_7$ , consistent with the relatively complex and simple patterns observed near  $\omega_6$  and  $\omega_7$ .

Solution of the secular equation for  $C_{2v}$  symmetry predicts that the eigenvalues for the trimer containing equivalent boron isotopes bracket the eigenvalues of the mixed isotope trimer as is experimentally observed. In addition, the solution for  $C_{2v}$  symmetry yields information on the splitting of modes previously degenerate under  $D_{3h}$  symmetry, which is depicted in Table 24.

The linear transformation  $L^{-1}$  corresponding to the set of eigenvalues given in Table 23, which are in reasonable agreement with the

experimental values observed for the trimer of metaborate and similar compounds, is given in Appendix IV. This allows the normal modes to be described in terms of the internal coordinates and in terms of vibrations of individual atoms. However this description must not be pushed too far.

Table 23. Predicted and experimental, in-plane fundamentals of the metaborate trimer.

	Predicted eigenvalues for $D_{3h}$ symmetry when $\phi_{\beta} = .80$ , $\phi_{r\beta} = -.50$ , and $\phi_{r\beta}^{\circ} = .25$ md/Å ( $\text{cm}^{-1}$ )		Experimental fundamentals in KCl at $T \approx 100^{\circ}$ K ( $\text{cm}^{-1}$ )	
	$11_{\text{B}}$	$10_{\text{B}}$	$11_{\text{B}}$	$10_{\text{B}}$
$\omega_1$	1315	1360	1435*	1484*
$\omega_2$	801	801		
$\omega_3$	548	555	588	604
$\omega_4$	1224	1255	1258	1279
$\omega_5$	756	768		757
$\omega_6$	1367	1411	1430.6	1481.4
$\omega_7$	1147	1177	1175.2	1208.8
$\omega_8$	1012	1025	936.8	938.9
$\omega_9$	427	430	466	472
$\omega_{10}$	372	373	290	295

\* Values for the trimer containing  $2^{11}\text{B} + ^{10}\text{B}$  and  $^{11}\text{B} + 2^{10}\text{B}$ .

Table 24. Predicted isotopic splitting of degenerate modes of the metaborate trimer.

	$\omega_6, \omega_9$ and $\omega_{10}$	$\omega_7$ and $\omega_8$	$\omega_{13}$ and $\omega_{14}$
$3^{10}\text{B}$	E'	E'	E''
$2^{10}\text{B} + ^{11}\text{B}$	$\text{B}_2$ $\text{A}_1$	$\text{A}_1$ $\text{B}_2$	$\text{A}_2$ $\text{B}_1$
$^{10}\text{B} + 2^{11}\text{B}$	$\text{A}_1$ $\text{B}_2$	$\text{B}_2$ $\text{A}_1$	$\text{B}_1$ $\text{A}_2$
$3^{11}\text{B}$	E'	E'	E''

## V. ASSIGNMENTS FOR THE METABORATE TRIMER

Because the experimental spectra are very complex, the following assignments, even though they fit the experimental facts, may not necessarily be entirely correct. This complexity is due in part to the presence of at least four species which are  $\text{BO}_2^-$ ,  $(\text{BO}_2^-)_3$ ,  $\text{K}_3(\text{BO}_2)_3$  or  $\text{Na}_3(\text{BO}_2)_3$ , and possibly  $[(\text{BO}_2^-)_3]_n$ . In addition, the trimer ion which is normally the primary constituent has 14 fundamental vibrations on the basis of  $D_{3h}$  symmetry. Seven are infrared active with five of them being doubly degenerate. When the symmetry is lowered to  $C_{2v}$  by an isotopic perturbation or to  $C_{3v}$  and  $C_s$  by the site symmetry, degeneracies are removed and/or some of the inactive fundamentals become weakly active. This is shown in the correlation diagrams in Figure 16. There are also many possible combinations which, if they belong to the proper symmetry species, may be in Fermi resonance with the fundamentals.

The vibrational modes have been classified according to the type of motion involved, where possible, to aid in the discussion. This classification consists of in-plane, stretching and bending modes ( $A_1'$ ,  $A_2'$ , and  $E'$ ), and out-of-plane, bending modes ( $A_2''$  and  $E''$ ).

### In-Plane Modes

The assignments of the in-plane and out-of-plane modes in KCl, NaCl, and KBr are presented in Table 25. The assignments in NaCl and KBr are less complete because of the presence of very broad

Table 25. Assignment of fundamental modes of  $(\text{BO}_2^-)_3$  in NaCl, KCl, and KBr.  $(\text{cm}^{-1}) T \approx 100^\circ \text{K}$ 

Species and activity			NaCl				KCl				KBr			
			$3^{11}\text{B}$	$2^{11}\text{B}+^{10}\text{B}$	$11_{\text{B}+2}^{10}\text{B}$	$3^{10}\text{B}$	$3^{11}\text{B}$	$2^{11}\text{B}+^{10}\text{B}$	$11_{\text{B}+2}^{10}\text{B}$	$3^{10}\text{B}$	$3^{11}\text{B}$	$2^{11}\text{B}+^{10}\text{B}$	$11_{\text{B}+2}^{10}\text{B}$	$3^{10}\text{B}$
$A_1'$	$A_1$	$\omega_1$		1476.6				1434.7	1483.5					
	IR	$\omega_2$												
		$\omega_3$	611			631	588					604		
$A_2'$	$B_2$	$\omega_4$	1290					1258				1279		
	IR	$\omega_5$				777		732	752.5			757	747	
$E'$	$A_1+B_2$	$\omega_6$	1467.8	1468 $B_2$	1503 $A_1$	1529.3	1430.6	1430.8 $B_2$	1459.4 $A_1$	1481.4	1419.4		1466.8	
IR	IR			1502.7 $A_1$	1527.3 $B_2$			1460.8 $A_1$	1480.8 $B_2$					
		$\omega_7$	1209.5	1210 $A_1$	1223.2 $B_2$	1243.6	1175.2	1175.9 $A_1$	1188.3 $B_2$	1208.8	1166.5	1166.5 $A_1$	1179.1 $B_2$	1199.3
				1234.2 $B_2$	1243 $A_1$			1198.7 $B_2$	1207.9 $A_1$			$B_2$	1199. $A_1$	
		$\omega_8$	955			959	936.8			938.9	936		936	
		$\omega_9$	481				466			472	466		472	
		$\omega_{10}$	300				290			295	290		295	
$A_2''$	$B_1$	$\omega_{11}$					773.5	781.1	786.6	791.1	765		785	
IR	IR	$\omega_{12}$												
$E''$	$A_2+B_1$	$\omega_{13}$	739.6				720.5	$A_2$	720.9 $B_1$	724.1	715.6		718.4	
	$B_1$ ; IR							720.5 $B_1$	$A_2$					
		$\omega_{14}$												

bands which have been assigned to a second phase of the appropriate salts of the trimer ion. Although the assignment of  $\omega_6$  and  $\omega_7$  to the strong lines in the stretching region of the spectrum was straightforward, the assignment of individual lines to isotopic components was somewhat more difficult. Under  $C_{2v}$  symmetry  $E'$  is split into  $A_1$  and  $B_2$  resulting in six possible components. Using the splitting predicted by the normal coordinate analysis given in Table 24, the experimental components and their intensities may be explained with the proposed patterns shown schematically for  $\omega_6$  and  $\omega_7$  in Figure 8. The experimental pattern for  $\omega_7$  is close to the theoretical one except for minor discrepancies in the intensities. These discrepancies are caused by two shoulders at about  $1190$  and  $1200\text{ cm}^{-1}$ , which are due to trimer interaction, and by less overlapping between  $E'$  and  $A_1$  at the high frequency component compared to the low frequency component.

The theoretical pattern for  $\omega_6$  is, however, not sufficient to explain the experimental lines in this region. Rather than the expected singlet which is observed in  $^{10}\text{B}$  enriched crystals, a doublet is present in spectra of  $^{11}\text{B}$  enriched crystals. The singlet in  $^{10}\text{B}$  enriched crystals is about 50% larger than the corresponding component of  $\omega_7$ . Although both members of the doublet are much less intense than the corresponding component of  $\omega_7$ , the sum of the absorbances of the two members of the doublet is about 50% larger than the corresponding component of  $\omega_7$  as in the enriched  $^{10}\text{B}$  case. In KCl and perhaps NaCl and KBr crystals containing enriched  $^{11}\text{B}$ , the two members of the doublet are of nearly equal intensity; however, they seemingly are

not equal in some crystals containing mixtures of boron isotopes. The additional intensity of the lower frequency member in these cases is due to a shoulder which has also caused this band to be shifted to a higher frequency by one wavenumber. This shoulder and many other bands in this region are due to interactions between trimer ions.

The presence of this doublet and its anomalous intensities may be explained by Fermi resonance between  $\omega_6$  and  $2\omega_{13}$ . Since the frequency of  $\omega_{13}$  depends very weakly upon the boron isotope,  $^{11}\text{B}$  rich components of  $2\omega_{13}$  and  $\omega_6$  are much closer than those of  $^{10}\text{B}$  resulting in a stronger Fermi resonance.

The constant  $b$  which is related to the perturbation or repulsion of the two energy levels has been calculated for some of the isotopic components by means of Equation 5-1.

$$\begin{vmatrix} \omega_1^0 - \omega & b/\sqrt{2} \\ b/\sqrt{2} & \omega_2^0 - \omega \end{vmatrix} = 0 \quad (5-1)$$

Because of the nearly equal intensities of the two members of the doublet in KCl and NaCl, the unperturbed energy levels are assumed to be midway between the experimental lines. The same anharmonicities were used in NaCl, KCl, and KBr and have been listed in Table 26 as have the other details of this calculation. This is only an approximate calculation because there are several weak bands nearby assigned to  $E'$  combinations whose presence have been neglected. The combination and overtone bands are listed in Table 27, and arguments for their assignments are given in the next paragraph. Because

$\omega_7 + \omega_{10}$  is closer than  $2\omega_{13}$  to the fundamental  $\omega_6$  for the  $3^{10}\text{B}$  trimer, the approximation is not a good one for  $3^{10}\text{B}$ . A better approximation would be to consider Fermi resonance between  $\omega_6$ ,  $2\omega_{13}$ , and  $\omega_7 + \omega_{10}$ ; however, this would involve solving a  $3 \times 3$  determinant with six unknowns, and if the assignments of the combinations are correct, then the determinant is even larger.

Table 26. Fermi resonance calculation. ( $\text{cm}^{-1}$ )

	KCl			KBr		NaCl
	$3^{11}\text{B}$ E'	$2^{11}\text{B} + ^{10}\text{B}$ $\text{B}_2$	$3^{10}\text{B}$ E'	$3^{11}\text{B}$ E'	$3^{10}\text{B}$ E'	$3^{11}\text{B}$ E'
$2\omega_{13}$	1444.0	1444.6	1441.0	1434	1429.3	1483.3
$2\omega_{13}^0$	1437.3	1438.3	1443.0	1427.6	1431.6	1475.6
$\omega_6^0$	1437.3	1437.3	1479.5	1425.8	1464.5	1475.5
$\omega_6$	1430.6	1431.0	1481.5	1419.4	1466.5	1467.8
Anhar-						
monicity	3.7	4.4	5.2	3.7	5.2	3.7
b	9.5	9.6	12.4	10.2	12.6	11.0
$\omega_{13}^*$				715.6	718.4	739.6

\* Calculated from  $2(\omega_{13}) - 2\omega_{13}^0 = \text{Anharmonicity}$ .

There are many weak bands which occur near the  $E'$  fundamentals  $\omega_6$ ,  $\omega_7$ , and  $\omega_8$  and which may be assigned to combination modes consistent with the trimer model. In general, the further removed a nearby band is from the fundamental  $\omega_6$ , the less intense it is. There is only one band near  $\omega_7$  and one near  $\omega_8$ , and their relative intensities



Table 27. Overtones and combinations of  $(\text{BO}_2^-)_3$  in NaCl, KCl, and KBr. ( $\text{cm}^{-1}$ )  $T \approx 100^\circ \text{K}$

	NaCl		KCl		KBr	
	$11_{\text{B}}$	$10_{\text{B}}$	$11_{\text{B}}$	$10_{\text{B}}$	$11_{\text{B}}$	$10_{\text{B}}$
$2\omega_9$	962 w, b		931 w, b	943 w, b		944 w, b
$\omega_5 + \omega_9$		1264 m, b		1229. 2 m		1218. 8 m
$\omega_8 + \omega_9$	1436. 5 <sup>+</sup>		1401	1410	1402 <sup>+</sup>	
$2\omega_{13}$	1483. 3 s		1444. 0 s	1441. 0 m	1434 <sup>+</sup>	1429. 3 m
$\omega_7 + \omega_{10}$	1509 sh		1465. 4 m	1503. 7 m	1456. 0 <sup>+</sup>	1494. 8 <sup>+</sup>
$\omega_{11} + \omega_{13}$			1497. 7 vw	1519. 5 vw		
$\omega_3 + \omega_8$	1565. 6 w	1589. 8 vw	1524. 8 w	1542. 5 w		
$\omega_4 + \omega_{10}$	1590 vw		1547. 5 vw	1574. 0 vw		
$\omega_{10}; *(\omega_7 + \omega_{10}) - \omega_7$	300		290	295	289	295
$\omega_9; 1/2(2\omega_9)$	481		466	472		472
$\omega_9; (\omega_8 + \omega_9) - \omega_8$	481. 5		464		466	
$\omega_3; (\omega_3 + \omega_8) - \omega_8$	611	631	588	604		
$\omega_5; (\omega_5 + \omega_9) - \omega_9$		777		757		747
$\omega_4; (\omega_4 + \omega_{10}) - \omega_{10}$	1290		1258	1279		

\* Neglecting anharmonicity and Fermi resonance.

<sup>+</sup> Partially obscured by broad bands assigned to the trimer in a second phase.

are consistent with those near  $\omega_6$ . From this it is reasoned that these weak bands are combination bands which belong to the  $E'$  symmetry species and have consequently obtained some of their intensity from the fundamental through Fermi resonance. The forbidden and the weak, allowed fundamentals obtained from these combination bands, given in Table 27, were found to be comparable with infrared and Raman data from  $\text{Na}_3\text{B}_3\text{O}_6$  and related compounds.

A weak doublet near  $950\text{ cm}^{-1}$  has been assigned to  $\omega_8$  and  $2\omega_9$ . The stronger line which has been assigned to  $\omega_8$  does not vary appreciably with a change in boron isotope and must, therefore, be due primarily to a movement of the oxygen atoms. It is worthwhile noting that the normal coordinate analysis for  $D_{3h}$  symmetry predicts a degenerate mode near  $1000\text{ cm}^{-1}$  due primarily to a movement of the oxygen atoms. Although the fundamental  $\omega_9$  was not observed in KCl or NaCl because of the strong lattice absorption, a very weak and very broad band was observed in KBr at about  $470\text{ cm}^{-1}$  at room temperature. This assignment of  $\omega_8$  and  $\omega_9$  agrees with the assignment of Hisatsune and Suarez (28) for the trimer ion and with those of similar molecules which contain the  $(\text{BO}_2^-)_3$  ring (29 and 33). Hisatsune and Suarez also report that  $\omega_9$  is a very weak fundamental.

The remaining  $E'$  mode,  $\omega_{10}$ , was obtained indirectly from the combination  $\omega_7 + \omega_{10}$ . In KBr weak bands were observed at room temperature at  $303$  and  $304.5\text{ cm}^{-1}$  for enriched  $^{11}\text{B}$  and  $^{10}\text{B}$

respectively. These may be  $\omega_{10}$  but this would require an anharmonicity of at least  $10 \text{ cm}^{-1}$ ; the temperature effect is in the opposite direction.

All but two of the five forbidden fundamentals belonging to the  $A_1'$  and  $A_2'$  symmetry species were obtained from combination bands in KCl. These assignments were made with the aid of Raman data for similar compounds (25, 33) which are reproduced in Table 28 for the Raman active  $A_1'$  modes.

Table 28.  $A_1'$  modes of  $B_3O_3X_3$  observed in Raman spectra by Goubeau and Keller (25), and Parsons (33). ( $\text{cm}^{-1}$ )

	$\omega_1$	$\omega_2$	$\omega_3$
$B_3O_3Cl_3$	1037	807	333
$B_3O_3[N(CH_3)_2]_3$	1147	804	537
$B_3O_3(CH_3)_3$	1155	807	539
$B_3O_3(OCH_3)_3$	1286	804	556
		849*	
$B_3O_3(OH)_3$		819	598

\* Unassigned by authors

Latimer and Devlin (29) observed two weak and broad lines at  $826$  and  $896 \text{ cm}^{-1}$  for  $^{11}\text{B}$ , and at  $838$  and  $903 \text{ cm}^{-1}$  for  $^{10}\text{B}$  in the infrared spectra of thin films of  $(\text{BOF})_3$ . They suggest that  $826$  and  $838$  are  $\omega_2$  which has been activated by the lattice. If their activation argument is valid, then  $896$  and  $903 \text{ cm}^{-1}$  might also be  $\omega_2$ .

The predicted normal coordinate corresponding to  $\omega_2$  involves a motion of the ring oxygen atoms, while the boron atoms and exterior oxygen ions do not move appreciably. Just the opposite is true for  $\omega_1$ , whereas the expected motion of the exterior oxygen ions in  $\omega_3$  is about two or three times greater than that of the oxygen and boron atoms in the ring. In light of this, if the mass of the oxygen ion is increased either by substitution of an isotope or an isoelectronic atom such as fluorine, a progressively larger decrease in the frequencies of  $\omega_2$ ,  $\omega_3$ , and  $\omega_1$  is expected with  $\omega_1$  showing the greatest decrease. This pattern is consistent with the frequencies reproduced in Table 28. Although, without Raman data on  $\omega_1$  and  $\omega_3$  of  $(\text{BOF})_3$ , less can be said about the frequencies of these  $A_1'$  modes; it has been assumed, subject to further information, that  $\omega_2$  and  $\omega_3$  are approximately equal to 820 and 600  $\text{cm}^{-1}$  and that  $\omega_1$  is somewhat larger than 1290  $\text{cm}^{-1}$ . Therefore, 588 and 604  $\text{cm}^{-1}$  in KCl, and 611 and 631  $\text{cm}^{-1}$  in NaCl have been assigned to  $\omega_3$ ; whereas 777, 757, and 747  $\text{cm}^{-1}$  were assigned to  $\omega_5$  ( $3^{10}\text{B}$ ) in NaCl, KCl, and KBr. None of the observed combination bands were thought to contain  $\omega_2$  because a very weak Fermi resonance was expected due to large differences in frequency between the fundamentals and possible combinations if  $\omega_2 \simeq 820 \text{ cm}^{-1}$ .  $\omega_4$  rather than  $\omega_1$  has been assigned to 1258 and 1279  $\text{cm}^{-1}$  in KCl primarily on the basis or arguments in the next paragraph as well as the frequency argument above.

Two strong lines at 1434.7 and 1483.5  $\text{cm}^{-1}$  having the proper change in intensity with change in boron isotope have been assigned to the  $2^{11}\text{B} + {}^{10}\text{B}$  and  ${}^{11}\text{B} + 2^{10}\text{B}$  components of  $\omega_1$ . When an isotopic perturbation lowers the symmetry from  $D_{3h}$  to  $C_{2v}$ , the  $A_1'$  and  $A_2'$  modes become  $A_1$  and  $B_2$  modes which are expected to be, at most, weakly active. However if these modes are near any of the fundamentals of the same symmetry species, an interaction should occur. These two lines are very near the  $B_2$  components of  $\omega_6$  and  $2\omega_{13}$  without apparently disrupting the expected pattern. In contrast, both of these lines are symmetrically separated by about  $25 \text{ cm}^{-1}$  from the  $A_1$  components of  $\omega_6$ . Therefore these lines are thought to belong to the  $A_1$  symmetry species and have been assigned to  $\omega_1$ . If the frequency differences between all four components of  $\omega_1$  are assumed to be the same,  $\prod \frac{\omega_i'}{\omega_i}$  is larger than predicted by the product rule. However if an interaction occurs between the  $A_1$  components of  $\omega_6$  and  $\omega_1$  when the symmetry is reduced to  $C_{2v}$ ; there is no theoretical reason to believe an equal spacing between components should exist.

The product rule has been applied to various symmetry species where the assignments are complete, and the results are given in Table 29.  $\omega_6^0$  has been employed in this calculation, whereas experimental values for the other frequencies neglecting anharmonicities and Fermi resonance have been used. In the latter frequencies the Fermi resonance is much weaker, and no information is easily attainable

concerning the magnitude of this resonance.

Table 29. Teller-Redlich product rule for  $(\text{BO}_2^-)_3$  with  $D_{3h}$  symmetry in KCl and KBr.

Symmetry species	Host	$\prod \frac{\omega_k'}{\omega_k}$	
$A_1'$		$\prod \left(\frac{m}{m'}\right)^{1/2}$	= 1.049
$A_2'$		$\prod \left(\frac{m}{m'}\right)^{1/2} \left(\frac{I_Z}{I_Z'}\right)^{1/2}$	= 1.043
$E'$	KCl KBr	1.093 1.088	$\prod \left(\frac{m}{m'}\right) \left(\frac{M}{M'}\right) = 1.087$
$A_2''$		$\prod \left(\frac{m}{m'}\right)^{1/2} \left(\frac{M}{M'}\right)^{1/2}$	= 1.036

where  $m$  = mass of atoms

$M$  = mass of molecules

#### Out-of-Plane Modes

According to the arguments and dimensions given in Chapter III, the trimer in solid solution should be distorted. Since this distortion is due to three potassium ions lying above the plane of the ring and one lying below this plane, any motion perpendicular to the plane of the ring should be much more restricted than a motion in the plane. As there is much more space available to the trimer in a crystal of  $\text{K}_3(\text{BO}_2)_3$ , it is logical that the restoring force for an out-of-plane motion should be larger and the amplitude smaller for the trimer in

an alkali halide compared to  $K_3(BO_2)_3$ .

Four medium intensity bands between 781 and 791  $cm^{-1}$  in KCl have been assigned to  $\omega_{11}$ , one of the two allowed  $A_2''$  fundamentals. As expected, these frequencies are larger than those observed by Büchler and Marram (5), Goubeau and Hummel (24), and Hisatsune and Suarez (28); and the relative intensities of these bands are less than the corresponding bands observed by Hisatsune and Suarez. Furthermore, the bands at 387 and 388  $cm^{-1}$  in a KBr pellet that they describe as medium intensity bands and assign to  $\omega_{12}$  were either not observed or are very weak. This is due partially to the greater thickness of the single crystal and consequently more lattice absorption. In the spectrum of one KBr crystal at room temperature a very weak and broad band at about 370  $cm^{-1}$  was found. If this mode is  $\omega_{12}$ , its amplitude has been severely restricted since KBr is reasonably transparent in this region.

As the amount of space available to the trimer decreases for the series KBr, KCl, and NaCl; an accompanying increase in the frequency of  $\omega_{11}$  is expected. Although this is true for KBr and KCl, several bands were observed in NaCl which do not fit the simple pattern observed in KCl and which occur at frequencies smaller than  $\omega_{11}$  in KCl and KBr. Another anomaly exists in KCl and perhaps in KBr. In addition to the components of  $\omega_{11}$  in KCl two medium intensity bands occur at 752.5 and 744.5  $cm^{-1}$  in samples doped with enriched  $^{10}B$

and  $^{11}\text{B}$  respectively. Although these bands exhibit the same dependence upon boron concentration and thermal history as the trimer and are accompanied by relatively strong "trimer interaction bands," the relative intensity of  $752.5\text{ cm}^{-1}$  is at least three or four times larger than that of  $744.5\text{ cm}^{-1}$ . Nevertheless,  $744.5\text{ cm}^{-1}$  is slightly stronger than  $752.5\text{ cm}^{-1}$  in crystals containing mixtures of boron isotopes. Furthermore, instead of the isotopic components that are expected between these two bands in the latter crystals, there is a band at  $732\text{ cm}^{-1}$  of comparable intensity; see the appropriate spectra after quenching in Figure 4. It is interesting that these spectra would be identical with the two superimposed spectra in the enriched  $^{10}\text{B}$  and  $^{11}\text{B}$  cases, if it were not for the band at  $732\text{ cm}^{-1}$  and a greater than anticipated intensity at  $752.5\text{ cm}^{-1}$ . To explain this anomaly, the band at  $732\text{ cm}^{-1}$  and the majority of absorption at  $752.5\text{ cm}^{-1}$  have been assigned to the  $2\text{ }^{11}\text{B} + \text{}^{10}\text{B}$  and  $\text{}^{11}\text{B} + 2\text{}^{10}\text{B}$  components of  $\omega_5$  which have been made infrared active by the  $\text{C}_{2v}$  isotopic perturbation. This assignment agrees well with the value of  $\omega_5$  for  $3\text{}^{10}\text{B}$  obtained from the combination  $\omega_5 + \omega_9$ . Since the band at  $744.5\text{ cm}^{-1}$  and the remainder of the absorbance at  $752.5\text{ cm}^{-1}$  appear to be simultaneously due to the trimer and a species containing one boron atom, they have tentatively been assigned to a motion due to a coupling between a lattice mode and either a translational or librational mode of the trimer which involves only one boron atom.



One of the strongest pieces of evidence for the trimer model is the agreement between the observed components of  $\omega_{11}$  in KCl and those predicted for a nondegenerate mode. The trimer model predicts that the relative intensities of the four components will be

$$({}^{11}\text{P})^3 : 3({}^{11}\text{P})^2({}^{10}\text{P}) : 3({}^{11}\text{P})({}^{10}\text{P})^2 : ({}^{10}\text{P})^3 \quad (5-2)$$

which, for example, is equivalent to 1:3:3:1 when  ${}^{11}\text{P} = 0.5$ . The experimental components, in general, fit this pattern yet there are minor discrepancies. These discrepancies are due, at least in part, to overlapping between adjacent components, and between individual components and trimer interaction bands. The latter effect is made evident by the relative increase in intensity of a band at about  $770 \text{ cm}^{-1}$  and a shift in the high frequency component to the lower frequency of  $790.4 \text{ cm}^{-1}$  as the intensity of other trimer interaction bands increase. The former effect is greater for the higher frequency components because of a progressive decrease in separation between adjacent components. Quenching which reduces the concentration of trimer ions and therefore interaction between trimer ions, results in less overlapping and closer agreement between the model and experiment. Results of an appropriate quenching experiment are shown in Figure 4 and listed in Table 30. Nevertheless, agreement is still not complete due to residual overlapping and perhaps to a larger than expected intensity in the mixed boron components that

results from an interaction between  $\omega_{11}$  and the  $B_1$  component of  $\omega_{13}$  for  $C_{2v}$  symmetry. The nonuniform separation between components may also be explained by this interaction as shown schematically in Figure 18.

Table 30. Experimental and theoretical absorbances for  $\omega_{11}$  of  $(BO_2^-)_3$  in KCl with  $^{11}P = .547$  at  $T \approx 100^\circ K$ .

$\omega(\text{cm}^{-1})$	Experimental absorbance normalized to one		Theoretical absorbance
	Before quench	After quench	
773.6	.132	.128	$(^{11}P)^3 = .164$
781.4	.319	.362	$3(^{11}P)^2(^{10}P) = .406$
786.9	.371	.378	$3(^{11}P)(^{10}P)^2 = .336$
791.2	.178	.132	$(^{10}P)^3 = .093$

The two out-of-plane  $E''$  fundamentals are infrared inactive under  $D_{3h}$  symmetry, but under  $C_{2v}$  symmetry the degeneracy is removed and the  $B_1$  component becomes weakly infrared active while  $A_2$  remains inactive. If the  $C_{3v}$  site symmetry perturbation is strong enough the inactive out-of-plane modes ( $E'' \rightarrow E$  and  $A_2 \rightarrow A'$ ) should become weakly infrared active. The spectra of KCl samples containing isotopically enriched  $^{11}B$  and  $^{10}B$  contain a weak band at  $720.5 \text{ cm}^{-1}$  and a weak doublet at  $720.9$  and  $724.1 \text{ cm}^{-1}$  respectively. The weak bands at  $724.1$  and  $720.9 \text{ cm}^{-1}$  are proposed to be the weakly active  $E$  ( $3^{10}B$ ) and  $B_1$  ( $^{11}B + 2^{10}B$ ) modes. These two modes apparently overlap in the enriched  $^{11}B$  case as shown in Figure 18. For

samples containing mixtures of boron isotopes the intensity of both bands,  $724.1 \text{ cm}^{-1}$  and a band comprising  $720.5$  and  $720.9 \text{ cm}^{-1}$ , became more intense relative to the active fundamentals of the  $3^{10}\text{B}$  and  $3^{11}\text{B}$  trimer ions with  $720.5 \text{ cm}^{-1}$  showing the largest increase. As the relative number of  $\text{C}_{2v}$  molecules is increased, the intensity of the band containing the  $\text{B}_1$  components should become larger. The increase in intensity of  $724.1 \text{ cm}^{-1}$  may be explained by an increase in the weakly active  $\text{A}'$  mode of the  $^{11}\text{B} + 2^{10}\text{B}$  trimer. Although the size of the anticipated increase in the  $\text{B}_1$  components is larger than what is observed, this discrepancy can be explained by the proposed interaction between  $\omega_{11}$  and  $\omega_{13}$ . Values for  $\omega_{13}$  in KBr and NaCl were obtained from the Fermi resonance calculations summarized in Table 26, and they are consistent with the above assignment of  $\omega_{13}$  in KCl.

Table 31.  $\omega_{11}^0$  and  $\omega_{13}^0$  of  $(\text{BO}_2^-)_3$  in KCl at  $T \approx 100^\circ \text{K}$ . ( $\text{cm}^{-1}$ )

	$\omega_{11}^0$	$\omega_{13}^0$
$3^{11}\text{B}$	773.5	720.5
$2^{11}\text{B} + ^{10}\text{B}$	779.4	720.5 $\text{A}_2$ 722.2 $\text{B}_1$
$^{11}\text{B} + 2^{10}\text{B}$	785.4	722.3 $\text{B}_1$ 724.1 $\text{A}_2$
$3^{10}\text{B}$	791.1	724.1

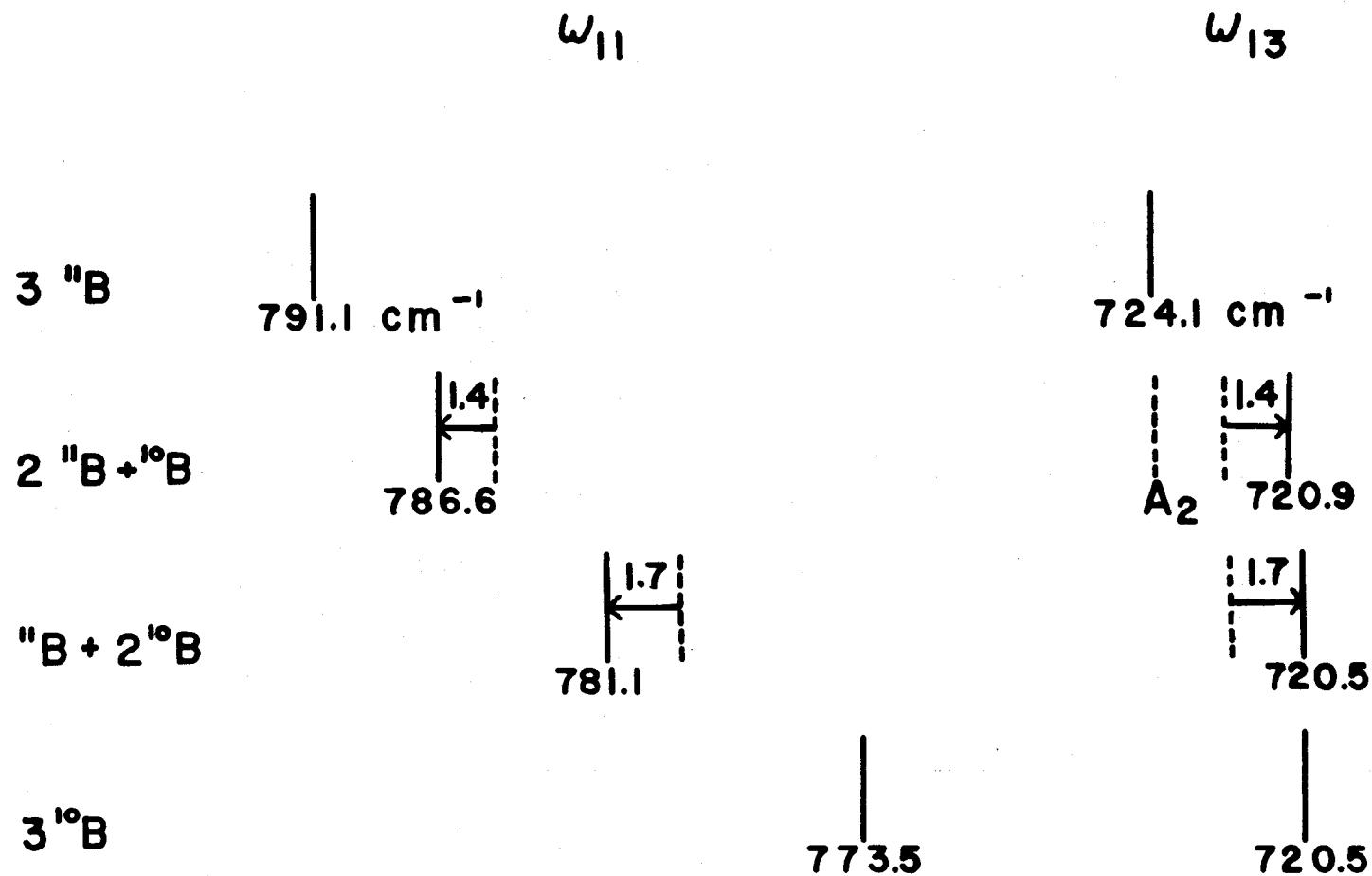


Figure 18. Interaction between  $\omega_{11}(B_1)$  and  $\omega_{13}(A_2+B_1)$  of  $(\text{BO}_2^-)_3$  in KCl at  $T \approx 100^\circ\text{K}$ . ( $\text{cm}^{-1}$ )

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## APPENDICES

## APPENDIX I

Internal Symmetry Coordinates of the Metaborate Trimer  
for D<sub>3h</sub> Symmetry

In-PlaneSymmetry Species

$$A_1' \quad S_1 = 1/\sqrt{3}(r_1 + r_2 + r_3)$$

$$S_2 = 1/\sqrt{3}(K_1^{A_1'} + K_2^{A_1'} + K_3^{A_1'})$$

$$S_3 = 1/\sqrt{3}(\beta_1 + \beta_2 + \beta_3)$$

$$A_2' \quad S_4 = 1/\sqrt{3}(K_1^{B_2'} + K_2^{B_2'} + K_3^{B_2'})$$

$$S_5 = 1/\sqrt{3}(a_1^{B_2'} + a_2^{B_2'} + a_3^{B_2'})$$

$$E' \quad S_6 = 1/\sqrt{6}(2r_1 - r_2 - r_3)$$

$$S_7 = 1/\sqrt{6}(2K_1^{A_1'} - K_2^{A_1'} - K_3^{A_1'})$$

$$S_8 = 1/\sqrt{2}(K_2^{B_2'} - K_3^{B_2'})$$

$$S_9 = 1/\sqrt{6}(2\beta_1 - \beta_2 - \beta_3)$$

$$S_{10} = 1/\sqrt{2}(a_2^{B_2'} - a_3^{B_2'})$$

$$\begin{aligned}
 E' \quad S_{11} &= 1/\sqrt{2}(r_2 - r_3) \\
 S_{12} &= 1/\sqrt{2}(K_2^{A_1} - K_3^{A_1}) \\
 S_{13} &= 1/\sqrt{6}(2K_1^{B_2} - K_2^{B_2} - K_3^{B_2}) \\
 S_{14} &= 1/\sqrt{2}(\beta_2 - \beta_3) \\
 S_{15} &= 1/\sqrt{6}(2\alpha_1^{B_2} - \alpha_2^{B_2} - \alpha_3^{B_2})
 \end{aligned}$$

### Out-of-Plane

#### Symmetry Species

$$\begin{aligned}
 A_2'' \quad S_{16} &= 1/\sqrt{3}(z_1 + z_2 + z_3) \\
 S_{17} &= 1/\sqrt{3}(Z_1 + Z_2 + Z_3) \\
 E'' \quad S_{18} &= 1/\sqrt{6}(2z_1 - z_2 - z_3) \\
 S_{19} &= 1/\sqrt{6}(2Z_1 - Z_2 - Z_3) \\
 E'' \quad S_{20} &= 1/\sqrt{2}(z_2 - z_3) \\
 S_{21} &= 1/\sqrt{2}(Z_2 - Z_3)
 \end{aligned}$$

where

$$\begin{aligned}
 K_1^{A_1} &= 1/\sqrt{2}(s_1 + s_2) & K_1^{B_2} &= 1/\sqrt{2}(s_1 - s_2) \\
 K_2^{A_1} &= 1/\sqrt{2}(s_3 + s_4) & K_2^{B_2} &= 1/\sqrt{2}(s_3 - s_4) \\
 K_3^{A_1} &= 1/\sqrt{2}(s_5 + s_6) & K_3^{B_2} &= 1/\sqrt{2}(s_5 - s_6)
 \end{aligned}$$

$$a_1^{A_1} = 1/\sqrt{2}(a_1 + a_2) \quad a_1^{B_2} = 1/\sqrt{2}(a_1 - a_2)$$

$$a_2^{A_1} = 1/\sqrt{2}(a_3 + a_4) \quad a_2^{B_2} = 1/\sqrt{2}(a_3 - a_4)$$

$$a_3^{A_1} = 1/\sqrt{2}(a_5 + a_6) \quad a_3^{B_2} = 1/\sqrt{2}(a_5 - a_6)$$

Internal Symmetry Coordinates of the Metaborate Trimer  
for C<sub>2v</sub> Symmetry

In-Plane

Symmetry Species

A<sub>1</sub>

$$S_1 = r_1$$

$$S_2 = 1/\sqrt{2}(r_2 + r_3)$$

$$S_3 = K_1^{A_1}$$

$$S_4 = 1/\sqrt{2}(K_2^{A_1} + K_3^{A_1})$$

$$S_5 = 1/\sqrt{2}(K_2^{B_2} - K_3^{B_2})$$

$$S_6 = \beta_1$$

$$S_7 = 1/\sqrt{2}(\beta_2 + \beta_3)$$

$$S_8 = 1/\sqrt{2}(a_2^{B_2} - a_3^{B_2})$$

$$\begin{aligned}
 B_2 \quad S_9 &= 1/\sqrt{2}(r_2 - r_3) \\
 S_{10} &= 1/\sqrt{2}(K_2^{A_1} - K_3^{A_1}) \\
 S_{11} &= K_1^{B_2} \\
 S_{12} &= 1/\sqrt{2}(K_2^{B_2} + K_3^{B_2}) \\
 S_{13} &= 1/\sqrt{2}(\beta_2 - \beta_3) \\
 S_{14} &= a_1^{B_2} \\
 S_{15} &= 1/\sqrt{2}(a_2^{B_2} + a_3^{B_2})
 \end{aligned}$$

### Out-of-Plane

#### Symmetry Species

$$\begin{aligned}
 A_2 \quad S_{16} &= 1/\sqrt{2}(z_2 + z_3) \\
 S_{17} &= 1/\sqrt{2}(Z_2 + Z_3) \\
 B_1 \quad S_{18} &= z_1 \\
 S_{19} &= 1/\sqrt{2}(z_2 + z_3) \\
 S_{20} &= Z_1 \\
 S_{21} &= 1/\sqrt{2}(Z_2 + Z_3)
 \end{aligned}$$

APPENDIX II

F Matrix for the  $D_{3h}$  Internal Symmetry Coordinates of the Metaborate Trimer

F	$S_1$	$S_2$	$S_3$	$S_4$	$S_5$	$S_6$	$S_7$	$S_8$	$S_9$	$S_{10}$
$S_1$	$\phi_r$	$\sqrt{2}\phi_s'$	$s\phi_{r\beta}$							
$S_2$	$\sqrt{2}\phi_s'$	$\phi_s + \phi_s'$	$\sqrt{2}s\phi_{r\beta}$							
$S_3$	$s\phi_{r\beta}$	$\sqrt{2}s\phi_{r\beta}'$	$s^2\phi_\beta$							
$S_4$				$\phi_s - \phi_s'$	$(rs)^{\frac{1}{2}}(\phi_{r\beta}' - \phi_{r\beta})$					
$S_5$				$(rs)^{\frac{1}{2}}(\phi_{r\beta}' - \phi_{r\beta})$	$rs(\phi_\beta - \phi_\beta')$					
$S_6$						$\phi_r$	$\sqrt{2}\phi_s'$	0	$s\phi_{r\beta}$	0
$S_7$						$\sqrt{2}\phi_s'$	$\phi_s + \phi_s'$	0	$\sqrt{2}s\phi_{r\beta}'$	0
$S_8$						0	0	$\phi_s - \phi_s'$	0	$(rs)^{\frac{1}{2}}(\phi_{r\beta}' - \phi_{r\beta})$
$S_9$						$s\phi_{r\beta}$	$\sqrt{2}s\phi_{r\beta}'$	0	$s^2\phi_\beta$	0
$S_{10}$						0	0	$(rs)^{\frac{1}{2}}(\phi_{r\beta}' - \phi_{r\beta})$	0	$rs(\phi_\beta - \phi_\beta')$

F	S <sub>16</sub>	S <sub>17</sub>	S <sub>18</sub>	S <sub>19</sub>
S <sub>16</sub>	$s^2(\phi_z + 2\phi_z')$	$s^2(\phi_{zZ} + 2\phi_{zZ}')$		
S <sub>17</sub>	$s^2(\phi_{zZ} + 2\phi_{zZ}')$	$s^2(\phi_Z + 2\phi_Z')$		
S <sub>18</sub>			$s^2(\phi_z - \phi_z')$	$s^2(\phi_{zZ} - \phi_{zZ}')$
S <sub>19</sub>			$s^2(\phi_{zZ} - \phi_{zZ}')$	$s^2(\phi_Z - \phi_Z')$



## APPENDIX III

Calculated Eigenvalues ( $\text{cm}^{-1}$ ) of Metaborate Trimer with  
 $D_{3h}$  Symmetry Using Various Values for the Force Constants;

		$\phi_{r\beta} = .25$				$\phi_{r\beta}' = 1.00$			
		$^{11}B$				$^{10}B$			
$\phi_{\beta}$		.40	.60	.80	1.00	.40	.60	.80	1.00
$A_1'$		1318	1338	1361	1387	1357	1379	1404	1432
		903	926	950	972	903	927	951	974
		174	295	367	417	177	300	372	423
$A_2'$		1224	1224	1224	1224	1255	1255	1255	1255
		756	756	756	756	768	768	768	768
$E'$		1318	1340	1363	1388	1358	1382	1407	1434
		1111	1114	1117	1120	1151	1154	1156	1158
		985	987	988	990	989	990	992	994
		402	403	403	409	403	403	404	410
		155	269	340	389	158	272	344	393
		$\phi_{r\beta} = -.25$				$\phi_{r\beta}' = .50$			
		$^{11}B$				$^{10}B$			
$\phi_{\beta}$		.40	.60	.80	1.00	.40	.60	.80	1.00
$A_1'$		1292	1308	1327	1349	1333	1351	1372	1396
		798	826	858	891	799	827	858	891
		358	441	495	532	364	448	502	539
$A_2'$		1224	1224	1224	1224	1255	1255	1255	1255
		756	756	756	756	768	768	768	768
$E'$		1304	1330	1357	1385	1345	1373	1402	1432
		1135	1137	1139	1140	1170	1170	1171	1172
		1009	1009	1009	1009	1019	1020	1020	1020
		404	406	413	441	405	407	417	446
		267	336	381	396	270	339	383	397

$\phi_\beta$	$\phi_{r\beta} = -.50$				$\phi_{r\beta} = .25$			
	$^{11}B$				$^{10}B$			
	.40	.60	.80	1.00	.40	.60	.80	1.00
$A_1$	1284	1298	1315	1335	1324	1341	1360	1382
	741	767	801	840	741	767	801	840
	408	494	548	581	415	501	555	588
$A_2$	1224	1224	1224	1224	1255	1255	1255	1255
	756	756	756	756	768	768	768	768
$E$	1311	1338	1367	1396	1351	1381	1411	1443
	1146	1146	1147	1147	1176	1176	1177	1177
	1012	1012	1012	1012	1025	1025	1025	1025
	409	414	427	451	411	416	430	456
	272	333	372	388	275	336	373	388

## APPENDIX IV

 $L^{-1}$  Matrices for the Metaborate Trimer with  $D_{3h}$  Symmetry

These transformations are for the trimer of metaborate when all three boron atoms are  $^{11}\text{B}$  or  $^{10}\text{B}$  with the following assumed values for the force constants:

$$\begin{aligned}\phi_{\beta} &= .80 \text{ md}/\text{\AA}^{\circ} \\ \phi_{r\beta} &= -.50 \text{ md}/\text{\AA}^{\circ} \\ \phi_{r\beta}' &= .25 \text{ md}/\text{\AA}^{\circ}\end{aligned}$$

The first set of out-of-plane force constants in Table 22.

The normal coordinates  $Q$  and internal symmetry coordinates  $S$  which are related by means of the linear transformation  $L^{-1}$  according to Equation (4-6) are the column matrices

$$Q^{\dagger} = (Q_1 Q_2 Q_3 Q_4 Q_5 Q_6 Q_7 Q_8 Q_9 Q_{10} Q_{11} Q_{12} Q_{13} Q_{14}) \quad (6-1)$$

and

$$S^{\dagger} = (S_1 S_2 S_3 S_4 S_5 S_6 S_7 S_8 S_9 S_{10} S_{16} S_{17} S_{18} S_{19}) \quad (6-2)$$

in which  $Q_i$  and  $S_i$  are the observed normal modes and the internal symmetry coordinates for  $D_{3h}$  symmetry described in Appendix I.

$10_B$   
 $L^{-1}$

2.07    -.70    .06

.89    3.38    1.35

3.30    3.06    -2.14

2.10    .08

1.22    2.01

1.51    -1.19    .37    .14    .06

1.33    .77    -1.67    -.15    .25

1.91    2.26    .32    -.03    -.70

2.18    .84    3.80    -2.28    2.43

-.68    3.77    2.51    3.34    2.24

-1.02    .83

4.06    -1.30

2.41    1.75

-1.25    .13

$^{11}\text{B}$

$L^{-1}$

2.17    -.69    .05

.88    3.38    1.35

3.24    3.15    -2.17

2.18    .14

1.10    2.04

1.53    -1.27    .42    .13    .07

1.62    1.02    -1.64    -.17    .17

1.74    2.14    .59    .001    -.74

2.12    .99    3.93    -2.21    2.50

-.74    3.73    2.34    3.43    2.16

-1.09    .86

4.07    -1.29

2.41    1.75

-1.34    .11