

# Robust Management of a Harvested Ecosystem Model

Esther Regnier & Michel De Lara

Paris School of Economics and University Paris 1 Panthéon-Sorbonne  
Ecole des Ponts ParisTech

IIFET 2012

Introduction

The Model

The  
Deterministic  
Viability  
Kernel

The Stochastic  
Viability  
Kernel

Conclusion

## Introduction

## The Model

## The Deterministic Viability Kernel

## The Stochastic Viability Kernel

## Conclusion

### Introduction

### The Model

### The Deterministic Viability Kernel

### The Stochastic Viability Kernel

### Conclusion

# Introduction

The sustainable management of natural resources must deal with several technical issues:

- ▶ **Conflicting objectives**: balancing the risk of resource collapse versus the risk of forgone economic benefits.
- ▶ Taking into account **the complexity of fisheries dynamics**.  
⇒ Calling for moving toward an ecosystemic approach of fisheries management (WSSD, Johannesburg, 2002).
- ▶ Accounting for various sources of **uncertainty**:
  - ▶ Stock estimation status.
  - ▶ Dynamics of ecosystems.
  - ▶ Disturbances: climatic hazard, technical progress, etc.

# Motivation

*Emphasizing the importance of taking into account disturbances likely to affect the dynamics of an ecosystem when designing a management strategy.*

- ▶ A management strategy is the rule governing the practise of a regulatory instrument.  
**Ex:** Setting the yearly harvest as a fixed fraction of the exploited biomass.
- ▶ **Approach:** comparing the set of sustainable initial states (viability kernel) given by a deterministic strategy to that driven by strategies integrating uncertainty.
- ▶ **Case-study:** the hake-anchovy couple in the Peruvian up-welling ecosystem.

# The Viability Theory

- ▶ Seeks the set of states, for which there exist controls, **satisfying the dynamics** of a system, and **constraints**, describing given objectives, at the same time (J. P. Aubin, 1991).
- ▶ Identifies a **decisions sequence** capable of maintaining the system viable. Decisions (controls) are computed by use of a **dynamic programming equation**.
- ▶ All constraints must be satisfied at all dates. The approach can be softened by accepting **constraint violations** with low probability in the **stochastic case**.

Introduction

The Model

The Deterministic Viability Kernel

The Stochastic Viability Kernel

Conclusion

Introduction

The Model

The  
Deterministic  
Viability  
Kernel

The Stochastic  
Viability  
Kernel

Conclusion

# Generic ecosystem model

- ▶ We consider a two-dimensional state model

$$\begin{cases} y(t+1) = y(t)R_y(y(t), z(t))(1 - v(t)) \\ z(t+1) = z(t)R_z(y(t), z(t))(1 - w(t)) \end{cases}$$

- ▶ state vector  $(y, z)$  represents biomasses,
- ▶ control vector  $(v, w)$  is fishing effort of each species, each lying in  $[0, 1]$
- ▶  $R_y$  and  $R_z$  are annual growth factors.
- ▶ catches are  $vyR_y(y, z)$  and  $wzR_z(y)$  (measured in biomass)

Introduction

The Model

The Deterministic Viability Kernel

The Stochastic Viability Kernel

Conclusion

Introduction

The Model

The  
Deterministic  
Viability  
Kernel

The Stochastic  
Viability  
Kernel

Conclusion



# The Viability Kernel

- ▶ The viability kernel is the set of initial states  $y(t_0), z(t_0)$  from which there exists, for  $t = t_0, \dots, T$ , controls  $v(t), w(t)$  producing a trajectory  $y(t), z(t)$  such that *a priori* conflicting requirements

- ▶ **preservation** (minimal biomass thresholds):

$$y(t) \geq y^b, z(t) \geq z^b$$

- ▶ **economic/social requirements** (minimal catch thresholds):

$$\begin{aligned}v(t)y(t)R_y(y(t), z(t)) &\geq Y^b, \\w(t)z(t)R_z(y(t), z(t)) &\geq Z^b\end{aligned}$$

are satisfied for  $t = t_0, \dots, T$ .

# The Viability Kernel

- ▶ If the thresholds  $y^b, z^b, Y^b, Z^b$  are such that the following expressions are satisfied

$$y^b R_y(y^b, z^b) - Y^b \geq y^b \quad \text{and} \quad z^b R_z(y^b, z^b) - Z^b \geq z^b$$

- ▶ the viability kernel is

$$\mathbb{V}(t_0) = \left\{ (y, z) \mid y \geq y^b, z \geq z^b, \right. \\ \left. y R_y(y, z) - Y^b \geq y^b, z R_z(y, z) - Z^b \geq z^b \right\}$$

# The Peruvian hake-anchovy system

- ▶ Fitted by a discrete-time Lotka-Volterra system with density-dependence (IMARPE):

$$y(t+1) = y(t) \overbrace{\left( R - \frac{R}{\kappa} y(t) - \alpha z(t) \right)}^{R_y(y(t), z(t))} (1 - v(t))$$

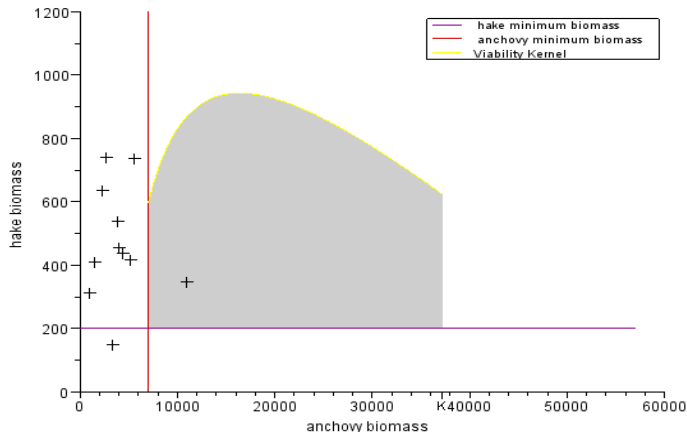
$$z(t+1) = z(t) \underbrace{\left( L + \beta y(t) \right)}_{R_z(y(t), z(t))} (1 - w(t))$$

- ▶ y prey biomass: anchovy
  - ▶ z predator biomass: hake
- 
- ▶ The associated viability kernel

$$\mathbb{V}(t_0) = \left\{ (y, z) \mid y \geq y^b, z^b \leq z \leq \frac{1}{\alpha} \left[ R - \frac{R}{\kappa} y - \frac{y^b + Y^b}{y} \right] \right\}.$$

# The Viability Kernel

The annual objectives and calibration were set by IMARPE (taller internacional sobre la anchoveta peruana), based on data from 1971 to 1981:



**Figure:** Viability Kernel for minimal biomass thresholds  $y^b = 7000$  kt (Anchovy) and  $z^b = 200$  kt (hake), and the minimal catches thresholds  $Y^b = 2000$  kt (Anchovy) and  $Z^b = 5$  kt (hake)

Introduction

The Model

The Deterministic Viability Kernel

The Stochastic Viability Kernel

Conclusion

Introduction

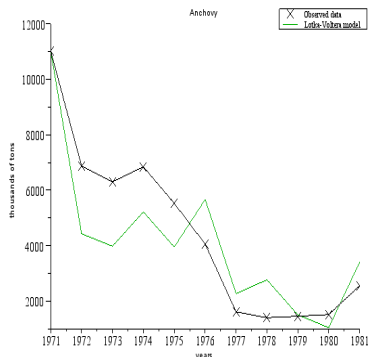
The Model

The  
Deterministic  
Viability  
Kernel

The Stochastic  
Viability  
Kernel

Conclusion

# Accounting for uncertainty



(a) Anchovy



(b) Hake

Figure: Observed and Simulated biomasses over 1971-1981

# Ecosystem model with uncertainty

- ▶ In the stochastic approach the model becomes:

$$y(t+1) = y(t) \overbrace{\left(R - \frac{R}{\kappa}y(t) - \alpha z(t)\right)}^{R_y(y(t), z(t))} (1 - v(t)) + \varepsilon_y(t)$$

$$z(t+1) = z(t) \underbrace{\left(L + \beta y(t)\right)}_{R_z(y(t), z(t))} (1 - w(t)) + \varepsilon_z(t)$$

where  $\varepsilon_y(t)$  and  $\varepsilon_z(t)$  are additive disturbance terms.

- ▶ The targeted preservation and economic objectives are kept equal.

# The uncertainties space $S$

- Defined by taking the difference between observed and simulated biomasses

$$\varepsilon_y(t) = y(t) - \hat{y}(t); \varepsilon_z(t) = z(t) - \hat{z}(t).$$

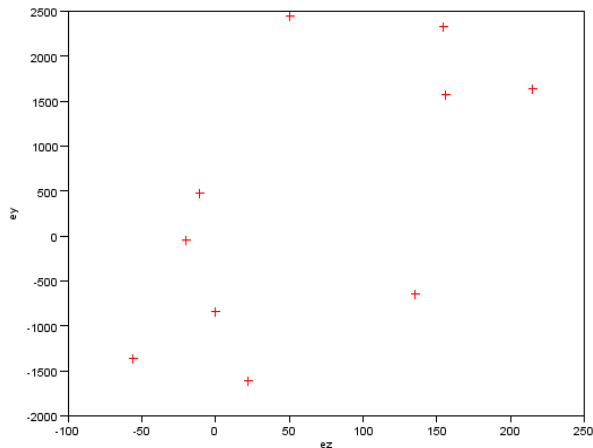


Figure:  $(\varepsilon_y(t), \varepsilon_z(t))$  over 1971-1981



# The Stochastic Viability approach

- ▶  $S = [\varepsilon_y^{min}, \varepsilon_y^{max}] \times [\varepsilon_z^{min}, \varepsilon_z^{max}]$
- ▶ An uncertainty scenario is  $(\varepsilon_y(\cdot), \varepsilon_z(\cdot)) = ((\varepsilon_y(t_0), \varepsilon_z(t_0)), \dots, (\varepsilon_y(T), \varepsilon_z(T)))$
- ▶ The set of uncertainty scenarios is  $\Omega = S^{T-t_0+1}$ .
- ▶  $\Omega$  is equipped with probability distribution.
- ▶ We adopt the uniform distribution law to simulate scenarios over  $S$  (of course results will be conditioned by this choice).

# The Stochastic Viability approach

- ▶ The stochastic viability kernel of **confidence level**  $\beta$  is the set of initial states  $y(t_0), z(t_0)$  from which there exists, for  $t = t_0, \dots, T$ , controls  $v(t), w(t)$  producing a trajectory  $y(t), z(t)$  such that over all scenarios
- ▶ minimal biomass thresholds:

$$y(t) \geq y^b, z(t) \geq z^b$$

- ▶ minimal catch thresholds:

$$\begin{aligned} v(t)y(t)R_y(y(t), z(t)) &\geq Y^b, \\ w(t)z(t)R_z(y(t), z(t)) &\geq Z^b \end{aligned}$$

are satisfied for  $t = t_0, \dots, T$  with a **probability**  $\geq \beta$ .

# The Stochastic Viability Kernel

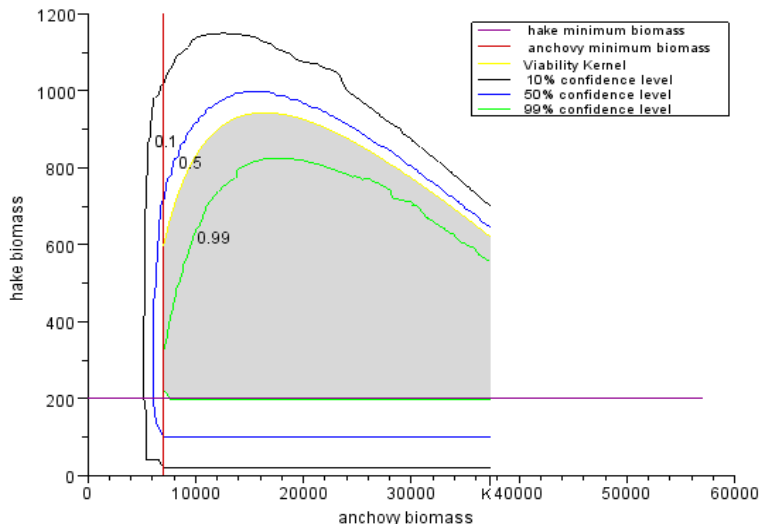


Figure: Viability Probability level curves

Introduction

The Model

The Deterministic Viability Kernel

The Stochastic Viability Kernel

Conclusion

Introduction

The Model

The  
Deterministic  
Viability  
Kernel

The Stochastic  
Viability  
Kernel

Conclusion

# Conclusion

- ▶ There are no **robust viability kernel (100% probability)**
- ▶ The set of initial states included in the deterministic viability kernel are viable with a probability of about 70%
- ▶ We have developed a tool capable of attaching to a potential initial state, a probability of achieving conflicting objectives
- ▶ For a given confidence level, the approach provides a corresponding control sequence