

## AN ABSTRACT OF THE THESIS OF

Chia-Chang Hsu for the degree of Master of Science in Chemical Engineering  
presented on December 1, 1993.

Title: Kinetic Study of  $\text{Si}(\text{NH})_2$  Synthesis via Low Temperature Vapor Phase  
Reaction of  $\text{SiCl}_4$  and  $\text{NH}_3$  in a Fluidized Bed Reactor

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Abstract approved: \_\_\_\_\_  
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$\text{Si}(\text{NH})_2$  synthesis via the vapor phase reaction of  $\text{SiCl}_4$  and  $\text{NH}_3$  was carried out at temperatures in the range of 280-353 K in a fluidized bed of inert  $\text{Si}_3\text{N}_4$  particles. The reaction phenomena were observed through the glass wall of the fluidized bed reactor. It was found that fine  $\text{Si}_3\text{N}_4$  powder with a mean particle size of  $0.5\ \mu\text{m}$  and a density of  $2.9 \times 10^3\ \text{kg/m}^3$  can collect product  $\text{Si}(\text{NH})_2$  more efficiently than large  $\text{Si}_3\text{N}_4$  particles with a mean particle size of  $370\ \mu\text{m}$  and an apparent density of  $2.63 \times 10^3\ \text{kg/m}^3$ . The effects of the concentration of  $\text{SiCl}_4$ , the mass of fluidized particles and the reaction temperature on the reaction rate were studied. A gas-phase reaction rate equation of pseudo-first order with respect to the  $\text{SiCl}_4$  concentration was proposed. A plug flow reactor model with the proposed kinetics equation was developed to describe the reaction of  $\text{SiCl}_4$  and  $\text{NH}_3$  in the fluidized bed reactor. It was found that the reaction time needed to complete the reaction was on the order of seconds and almost a 100% of product  $\text{Si}(\text{NH})_2$  was collected by fluidizing  $\text{Si}_3\text{N}_4$  fine powder. The apparent activation energy was evaluated to be 8.40 kJ/mol in the temperature range of 280-320 K.

Kinetic Study of  $\text{Si}(\text{NH})_2$  Synthesis  
via Low Temperature Vapor Phase Reaction of  $\text{SiCl}_4$  and  $\text{NH}_3$   
in a Fluidized Bed Reactor

by

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A THESIS

Submitted to

Oregon State University

in partial fulfillment of  
the requirements for the  
degree of

Master of Science

Completed December 1, 1993

Commencement June 1994

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## NOMENCLATURES

$A_b$	cross-sectional area of the fluidized bed, $\text{m}^2$
$C_{A0}$	inlet concentration of $\text{SiCl}_4$ vapor, $\text{kmol}/\text{m}^3$
$C_A$	outlet concentration of $\text{SiCl}_4$ vapor, $\text{kmol}/\text{m}^3$
$d_p$	particle size, $\mu\text{m}$
$E$	apparent activation energy, $\text{kJ}/\text{mol}$
$F$	total volumetric flow rate of gases entering the reactor, $\text{m}^3/\text{s}$
$f$	collecting efficiency of product fine powder
$\Delta G_{R,298}^0$	Gibbs free energy, $\text{kJ}/\text{mol}$
$g$	acceleration of gravity, $\text{m}/\text{s}^2$
$H$	bed height, $\text{m}$
$\Delta H_{R,298}^0$	enthalpy, $\text{kJ}/\text{mol}$
$k_A$	apparent rate constant of the pseudo-first order reaction with respect to $\text{SiCl}_4$ , $/\text{s}$
$N_{Cl}$	molar content of chlorine in a sample, mole
$\Delta P$	pressure drop across the bed of solids, $\text{Pa}$
$R_d$	rate of $\text{SiCl}_4$ deposition, $\text{mol}/\text{kg s}$
$r_A$	rate of reaction, $\text{mol}/\text{s}$
$t$	reaction time, $\text{s}$
$u_0$	superficial velocity, $\text{m}/\text{s}$
$u_{mf}$	apparent minimum fluidizing velocity, $\text{m}/\text{s}$
$V$	volume of the bed, $\text{m}^3$
$W_{b0}$	initial mass of the bed, $\text{kg}$
$W_b$	average mass of the bed over the reaction period, $\text{kg}$
$W_C$	cumulative mass, $\text{kg}$
$w$	mass of the sample particles, $\text{kg}$
$X_A$	actual conversion of $\text{SiCl}_4$
$X_A'$	apparent conversion of $\text{SiCl}_4$

### Greek letters

$\epsilon_A$	overall void fraction of the bed
$\rho_s$	density of particles, kg/m <sup>3</sup>
$\tau$	resistance time of gaseous reactants, s

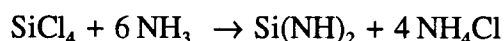


**KINETIC STUDY OF Si(NH)<sub>2</sub> SYNTHESIS  
VIA LOW TEMPERATURE VAPOR PHASE REACTION OF SiCl<sub>4</sub> AND NH<sub>3</sub>  
IN A FLUIDIZED BED REACTOR**

**CHAPTER 1  
INTRODUCTION**

Thermal decomposition of silicon diimide (Si(NH)<sub>2</sub>) is considered to be the most successful approach in the production of high purity  $\alpha$ -form silicon nitride ( $\alpha$ -Si<sub>3</sub>N<sub>4</sub>) [1], which is a high-temperature material for many engineering applications, *e.g.*, gas turbines and aerospace applications. Si(NH)<sub>2</sub>, the precursor of Si<sub>3</sub>N<sub>4</sub> synthesized via low temperature reaction of SiCl<sub>4</sub> with NH<sub>3</sub>, plays an important role in this method [2].

Generally, Si(NH)<sub>2</sub> can be synthesized from SiCl<sub>4</sub> and NH<sub>3</sub> in gas phase, liquid phase, or gas-liquid interphase as



Whenever liquid phase is involved, either in a liquid-liquid system or in a gas-liquid system, high purity Si(NH)<sub>2</sub> powder can be obtained by washing out the by-product, NH<sub>4</sub>Cl, with liquid NH<sub>3</sub>, and then high quality  $\alpha$ -Si<sub>3</sub>N<sub>4</sub> can be produced by calcining Si(NH)<sub>2</sub> at a temperature over 1273 K. The heat of vaporization of a liquid is utilized to control the reaction temperature, which is the major reason why a liquid is used in the system. However, these Si<sub>3</sub>N<sub>4</sub> production processes are not economically attractive

due to the high operation cost associated with the  $\text{NH}_3$  washing procedures. To reduce the production cost, gas phase reaction, in which solid products precipitate from the gaseous reactants and no solvent washing is required, has been considered as an alternative.

Nevertheless, the gas phase reaction also has major disadvantages. It has been reported that several problems are encountered in carrying out the gas phase reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$ . A high chlorine content in the primary  $\text{Si}(\text{NH})_2$  product may subsequently affect the quality of final product  $\alpha\text{-Si}_3\text{N}_4$  and that  $\text{SiCl}_4$  and  $\text{NH}_3$  vapors can react instantaneously at the outlets of reactant supply lines, thus forcing the reaction to be terminated in a short period of time because of the plugging problem.

Wang [3] found that the content of chlorine as an impurity in the final product,  $\text{Si}_3\text{N}_4$ , can be significantly reduced by controlling the reaction temperature and the following heat treatments for the precursor,  $\text{Si}(\text{NH})_2$ . The plugging problem also can be solved by specially designing a feeding system [4]. These technologies to overcome the disadvantages of the gas phase reaction are employed in the present study.

From a view point of reaction engineering, a fluidized bed reactor is ideal for producing solids and for rapid gas phase reactions with large heat released, both of which are typical characteristics of the gas phase reaction of  $\text{SiCl}_4$  and  $\text{NH}_3$ . Because both the products,  $\text{Si}(\text{NH})_2$  and  $\text{NH}_4\text{Cl}$ , are solids precipitating from the gaseous reactants, inert particles being fluidized may collect all the products. Thus, in a fluidized bed, the inert particles are allowed to expose their surface for solid-product collection and the heat of reaction can be simply removed by the fluidizing gas. The

products collected by the inert particles can be heated to remove  $\text{NH}_4\text{Cl}$  at 773 K and thermally decomposed into  $\text{Si}_3\text{N}_4$  at 1273 K. If  $\text{Si}_3\text{N}_4$  particles are used as inert, a fluidized bed reactor is able to prepare  $\text{Si}_3\text{N}_4$  particles coated with  $\text{Si}(\text{NH})_2$  by carrying out this gas phase reaction. These composite particles can then be calcined into pure  $\text{Si}_3\text{N}_4$  via the thermal decomposition in other fluidized beds operated at higher temperatures. With recycling some of these  $\text{Si}_3\text{N}_4$  particles, a continuous fluidized-bed process can be developed to manufacture high quality  $\text{Si}_3\text{N}_4$  powder.

The study presented in this thesis primarily focuses on the synthesis of  $\text{Si}(\text{NH})_2$  via the gas phase reaction of  $\text{SiCl}_4$  and  $\text{NH}_3$  in a fluidized bed reactor with  $\text{Si}_3\text{N}_4$  particles as inert fluidizing media. The objectives of this research are:

1. To design a fluidized bed reactor which can be operated for a period of time long enough for collecting data,
2. To choose a right size of inert  $\text{Si}_3\text{N}_4$  particles for collecting most of the products,
3. To inspect the fluidization phenomena,
4. To develop a model to describe the kinetics of  $\text{Si}(\text{NH})_2$  formation.

The results of this study will provide very useful information in developing an economical process for producing  $\text{Si}_3\text{N}_4$ .

There are five chapters in the thesis. Chapter 2 describes a literature review on the relevant work about the reaction chemistry, fluidization phenomena and the applications of fluidized beds to chemical vapor deposition (CVD) reactions where solid products precipitate from gaseous reactants. Also included are the comparison of different  $\text{Si}(\text{NH})_2$  synthesis-routes and calcine processes. Chapter 3 presents a detailed description of equipment design, experimental procedures and chemical analysis. The

experimental results are analyzed and discussed in Chapter 4. A kinetic model to describe the reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  in a fluidized bed is proposed and tested in this chapter. Finally, Chapter 5 summarizes the results of this work and recommendations for future work.

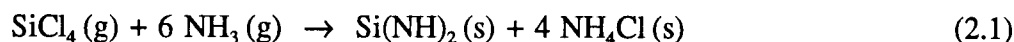
## CHAPTER 2

### LITERATURE REVIEW

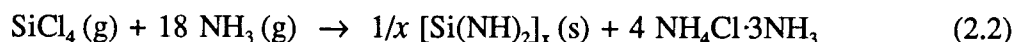
#### 2.1 Reaction Chemistry and Synthesis-Routes of Si(NH)<sub>2</sub>

##### 2.1.1 Reaction chemistry

The reaction of SiCl<sub>4</sub> with NH<sub>3</sub> at the room temperature was investigated for the first time by Billy *et al.* in 1959 [5]. They obtained fine-grained, roentgen-amorphous white powder which was the most typical compound of Si(NH)<sub>2</sub>. The reaction was proposed to be represented by



or



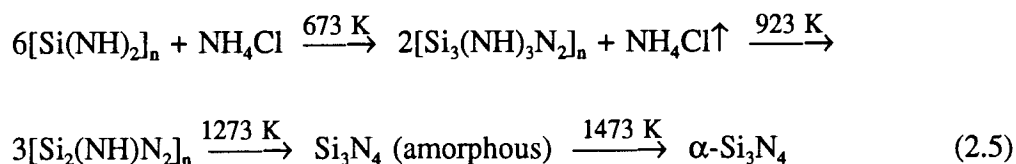
$$\Delta H^\circ_{\text{R},298} = -675.1 \text{ kJ/mol} \quad (2.3)$$

$$\Delta G^\circ_{\text{R},298} = -384.1 \text{ kJ/mol} \quad (2.4)$$

where the products in reaction (2.2) are polymeric silicon diimide and ammonia chloride triammoniate. The enthalpy ( $\Delta H^\circ_{\text{R},298}$ ) and Gibbs free energy ( $\Delta G^\circ_{\text{R},298}$ ) for this reaction were estimated by Crosbie [6]. In general, this reaction proceeds rapidly and completely with a large exothermic heat of reaction. It is suggested that ammonia should be supplied in excess of the stoichiometric ratio in either reaction (2.1) or (2.2) to achieve high conversion of SiCl<sub>4</sub> [4].

Si(NH)<sub>2</sub> obtained from the reaction described above can then be used to synthesize Si<sub>3</sub>N<sub>4</sub>. Synthesizing Si<sub>3</sub>N<sub>4</sub> via the thermal decomposition of Si(NH)<sub>2</sub>

involves several reactions. First, the products from reaction (2.1) or (2.2) are heated to a temperature above 673 K in a stream of  $\text{NH}_3$  gas for more than 2 hours to eliminate  $\text{NH}_4\text{Cl}$  via sublimation. During the sublimation of  $\text{NH}_4\text{Cl}$ , the diimide intermediates,  $[\text{Si}_3(\text{NH})_3\text{N}_2]_n$ , are formed [7]. These intermediate products are then calcined to form amorphous  $\text{Si}_3\text{N}_4$  at 1273 K. Finally, the  $\alpha\text{-Si}_3\text{N}_4$  is obtained by crystallizing the amorphous  $\text{Si}_3\text{N}_4$  at temperatures above 1473 K [8, 9]. A series of reactions summarizing the process of thermal decomposition of  $\text{Si}(\text{NH})_2$  are shown below:



This research mainly focuses on the kinetics of  $\text{Si}(\text{NH})_2$  synthesis, as described by reaction (2.1) or (2.2). The thermal decomposition of  $\text{Si}(\text{NH})_2$  to form  $\text{Si}_3\text{N}_4$ , as described by reaction (2.5) is not included in this work.

### 2.1.2 Routes of synthesis

$\text{Si}(\text{NH})_2$  has been prepared by researchers via three different routes: liquid-liquid, gas-liquid and gas-gas reactions.

#### Liquid-liquid reaction:

The problems often encountered in the  $\text{Si}(\text{NH})_2$  synthesis are the difficulty in removing heat generated by the extremely rapid exothermic reaction, the tendency that

product  $\text{Si}(\text{NH})_2$  plugs  $\text{SiCl}_4$  supply lines, and the difficulty in separating  $\text{Si}(\text{NH})_2$  from by-product  $\text{NH}_4\text{Cl}$ . Yamada *et al.* [1, 2] developed a liquid-liquid interfacial reaction method to solve these problems. In this method,  $\text{NH}_3$  reacts with  $\text{SiCl}_4$  at the interface between a liquid  $\text{NH}_3$  layer and an organic solvent layer which dissolves  $\text{SiCl}_4$ . The products precipitate as a solid mixture at the interface of these immiscible liquids. The reaction temperature may be controlled by the evaporation of  $\text{NH}_3$ . The mixture of reaction products needs to be washed out with an excess amount of liquid  $\text{NH}_3$  to remove by-product  $\text{NH}_4\text{Cl}$ . After the washing,  $\text{Si}(\text{NH})_2$  is processed through heat treatments to form highly pure  $\alpha\text{-Si}_3\text{N}_4$  which has been regarded as  $\text{Si}_3\text{N}_4$  of highest quality. However, this  $\text{Si}(\text{NH})_2$  synthesis route is not very economic because many operating steps are involved and organic solvent as well as a large quantity of liquid  $\text{NH}_3$  are required.

#### Gas-liquid reaction:

The synthesis-route through gas-liquid reactions was first investigated by Billy [5] in 1959 and tested by Ford Motor Company in 1988 [10, 11].  $\text{SiCl}_4$  vapor generated by bubbling nitrogen carrier gas through liquid  $\text{SiCl}_4$  is directed into a liquid  $\text{NH}_3$  vessel for reaction. Heat generated by the reaction is removed by the evaporation of  $\text{NH}_3$  under operating conditions at 5 atm and 273 K. Again,  $\text{NH}_4\text{Cl}$  must be removed from product  $\text{Si}(\text{NH})_2$  using 240 K liquid  $\text{NH}_3$ . Although  $\alpha\text{-Si}_3\text{N}_4$  is finally obtained by calcining  $\text{Si}(\text{NH})_2$ , it has been reported that the quality of  $\text{Si}_3\text{N}_4$  is lower than that produced by the liquid-liquid reaction.

Instead of using liquid  $\text{NH}_3$  and vapor  $\text{SiCl}_4$ , Mazdiasni *et al.* [9] and Mitomo *et al.* [12] used vapor  $\text{NH}_3$  and liquid  $\text{SiCl}_4$  to synthesize  $\text{Si}(\text{NH})_2$ . The reaction is carried out by bubbling  $\text{NH}_3$  gas through liquid *n*-hexane which contains dissolved  $\text{SiCl}_4$  at 273 K. A white powder-mixture of  $\text{Si}(\text{NH})_2$  and  $\text{NH}_4\text{Cl}$  precipitates in *n*-hexane and then is isolated from the hexane solvent by distillation under a reduced pressure at 300 K. Following the sequence represented by equation (2.5), the isolated  $\text{Si}(\text{NH})_2$  is then calcined and crystallized into  $\alpha\text{-Si}_3\text{N}_4$  at temperatures higher than 1473 K.

#### Gas-phase reaction:

To avoid the operation for liquid-solid separation and to simplify the process, gas-phase routes for the synthesis of silicon diimide have been considered. Kasai *et al.* [8] prepared  $\alpha\text{-Si}_3\text{N}_4$  via the thermal decomposition of  $\text{Si}(\text{NH})_2$  synthesized by the gas-phase reaction.

Vapor  $\text{SiCl}_4$ , generated by bubbling  $\text{N}_2$  through liquid  $\text{SiCl}_4$ , and  $\text{NH}_3$  gas are introduced into a tubular reactor, through separate feed lines, operated at the room temperature. Upon the interaction of these vapors, a white powder-mixture containing  $\text{Si}(\text{NH})_2$  and  $\text{NH}_4\text{Cl}$  is produced via a CVD mechanism.  $\text{NH}_4\text{Cl}$  may be removed by heating the powder mixture at 673 K for 2 hours. The isolated  $\text{Si}(\text{NH})_2$  is then calcined to form highly pure  $\alpha\text{-Si}_3\text{N}_4$  in the presence of  $\text{NH}_3$  at 1823 K for 1 hour.

Wang [3] has claimed that the content of chlorine in the final product  $\text{Si}_3\text{N}_4$  prepared by this method can be reduced to a level below 100 ppm by carrying out the gas-phase reaction at a temperature in the range of 298-473 K. He also found that



impurity chlorine can not be reduced appreciably regardless of the following heat treatments when the reaction temperature is higher than 473 K. The present research aims to make full use of the advantage of the gas-phase reaction route carried out at low temperatures.

## 2.2 Reaction Kinetics and Mechanism of the Deposition Process

### 2.2.1 Reaction kinetics

Studies on the kinetics of the reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  have focused on the deposition of  $\text{Si}_3\text{N}_4$  thin films on silicon substrates at high temperatures (973-1473 K), instead of the kinetics for  $\text{Si}(\text{NH})_2$  synthesis at low temperatures. Grieco *et al.* [13] determined the rate of  $\text{Si}_3\text{N}_4$  film deposition by measuring the increase in film thickness during the reaction. From a log-log plot of the deposition rate against the partial pressure of  $\text{SiCl}_4$ , they found a kinetics of 0.8th order with respect to the partial pressure of  $\text{SiCl}_4$ . The activation energy of the reaction at high temperatures in the range of 973-1473 K was determined to be  $62.7 \pm 6.3$  kJ/mol. Nevertheless, the kinetic study on the reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  to produce  $\text{Si}(\text{NH})_2$  at low temperatures around the room temperature has not been reported in literature yet. This thesis presents the results of the kinetic study on the  $\text{Si}(\text{NH})_2$  synthesis.

### 2.2.2 Mechanism of the deposition process

There are two different of mechanisms proposed for the deposition of  $\text{Si}_3\text{N}_4$  via the reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  at high temperatures [14]. One is the heterogeneous reaction of the Langmuir-Hinscheloow type. The reaction has been believed to occur in an adsorbed layer on substrates, and the rate is usually determined by the degrees of coverage of the surface of a growing film with adsorbed  $\text{SiCl}_4$  and  $\text{NH}_3$  molecules. This mechanism is valid for the reactions under low pressures. The deposition of a  $\text{Si}_3\text{N}_4$  thin film on Si substrates is a typical example. Another is the homogeneous reaction in gas phase, precipitating solid products. The reactants interact with each other in gas phase and then the dust-like products fall down to stick on the reactor surface. This mechanism is suggested to proceed under the conditions around the atmospheric pressure with high reactant concentrations. The production of  $\text{Si}_3\text{N}_4$  powder via CVD reactions is a representative example.

Wang [3] conducted the CVD reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  in a 0.915 m long tubular reactor at one atmosphere. At 300 K, he found that the majority of product (75%) was carried out of the reactor by the gas flow and collected by a trap connected to the reactor, and the rest of the product (25%) deposited on the reactor wall down stream. It is suggested that light, fluffy, white powder, obtained both in the reactor tube and the trap, was produced via the homogeneous gas-phase reaction followed by the solid precipitation.

## 2.3 The Characteristics of Fluidizing Fine Particles

### 2.3.1 Particle classification

Geldart *et al.* [15] determined the characteristics of gas-solid fluidization on the basis of the size and density of particles. Geldart D particles, which have a large size and a high density, are spoutable and difficult to be fluidized. Usually, either large exploding bubbles form or severe channeling occurs in a fluidized bed of these particles. Particles with a size ( $d_p$ ) between 40 and 500  $\mu\text{m}$  and a density ( $\rho_s$ ) between  $1.4 \times 10^3$  and  $4.0 \times 10^3 \text{ kg/m}^3$  are classified as Geldart B, which can be fluidized smoothly. Bubbles are generated and rise faster than the interstitial gas velocities in a fluidized bed of these particles [16]. Geldart A particles, which have a size less than 40  $\mu\text{m}$  and a density less than  $1.4 \times 10^3 \text{ kg/m}^3$ , are easily fluidized at low gas velocities. Bubbling and entrainment sometimes occur in fluidizing these particles. Geldart C particles, which have a size less than 30  $\mu\text{m}$ , are extremely difficult to fluidize, because the inter-particle forces are too strong to be overcome by the hydrodynamic forces exerting on the particles. When an ordinary fluidization technique is applied, the whole bed rises as a plug in a small bed in diameter. The rising velocity of bubbles cannot be determined easily, and the entrainment of fines is also significant once these Geldart C particles are fluidized.

### 2.3.2 Fluidizing $\text{Si}_3\text{N}_4$ powder

Some studies have demonstrated that fine particles, classified as Geldart C, can be fluidized if the particles grow in size by self-agglomeration [17, 18]. It has been reported that ultrafine  $\text{Si}_3\text{N}_4$  powder ( $d_p = 0.13\text{-}0.50\ \mu\text{m}$ ,  $\rho_s = 2.91 \times 10^3\ \text{kg/m}^3$ ) can be fluidized [19, 20]. Self-agglomeration takes place when the van der Waals force among adjacent particles and the shearing force, generated by bubble movement, are in dynamic equilibrium. Once sub-micron fines aggregate to form big clusters, it becomes possible to fluidize the fines which behave like group A particles.

Even fines are fluidized in the form of big agglomerates, the entrainment of fines is also significant in the fluidization. Liu & Kimura [20] have reported that, in the fluidization of a mixture of large particles and fines, entrained fines come mainly from two parts: (1) elutriable freely moving fines, which may be continuously and steadily generated from agglomerates of fines, and (2) fines attached to the large particles, being generated due to attrition. In the current case, the elutriable fines may also include product fines produced by the reaction between  $\text{SiCl}_4$  and  $\text{NH}_3$ .

## 2.4 CVD Reactions in Fluidized Beds

The fluidization has been applied to many CVD systems, such as the growth of seed particles, modification of powder surface, introduction of specific function to solids, and formation of fine particles by coagulation [21]. Two successful examples of fluidizing  $\text{Si}_3\text{N}_4$  fine powder are described below.

In the application to modifying powder surface, Morooka *et al.* [4] developed a CVD process to produce composite particles in a fluidized bed. TiN particles, generated by the ammonolysis reaction of  $\text{TiCl}_4$ , were deposited on the surface of fluidized  $\text{Si}_3\text{N}_4$  fines. The composite particles with an average size of 50  $\mu\text{m}$  were obtained in the form of agglomerates.

The production of  $\text{Si}_3\text{N}_4$  powder by the reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  in a fluidized bed was first developed by Marosi [22]. They fluidized amorphous  $\text{Si}_3\text{N}_4$  powder smaller than 4  $\mu\text{m}$  in diameter as seed particles for the reaction. In order to eliminate  $\text{NH}_4\text{Cl}$  from the fluidized bed, the reaction was conducted at temperatures over 773 K. With a cyclone for collecting entrained fine particles, this bed could be continuously operated for 21 hours. Final product having an average particle size of approximately 20  $\mu\text{m}$  and containing 58.8% Si and 39% N was obtained.

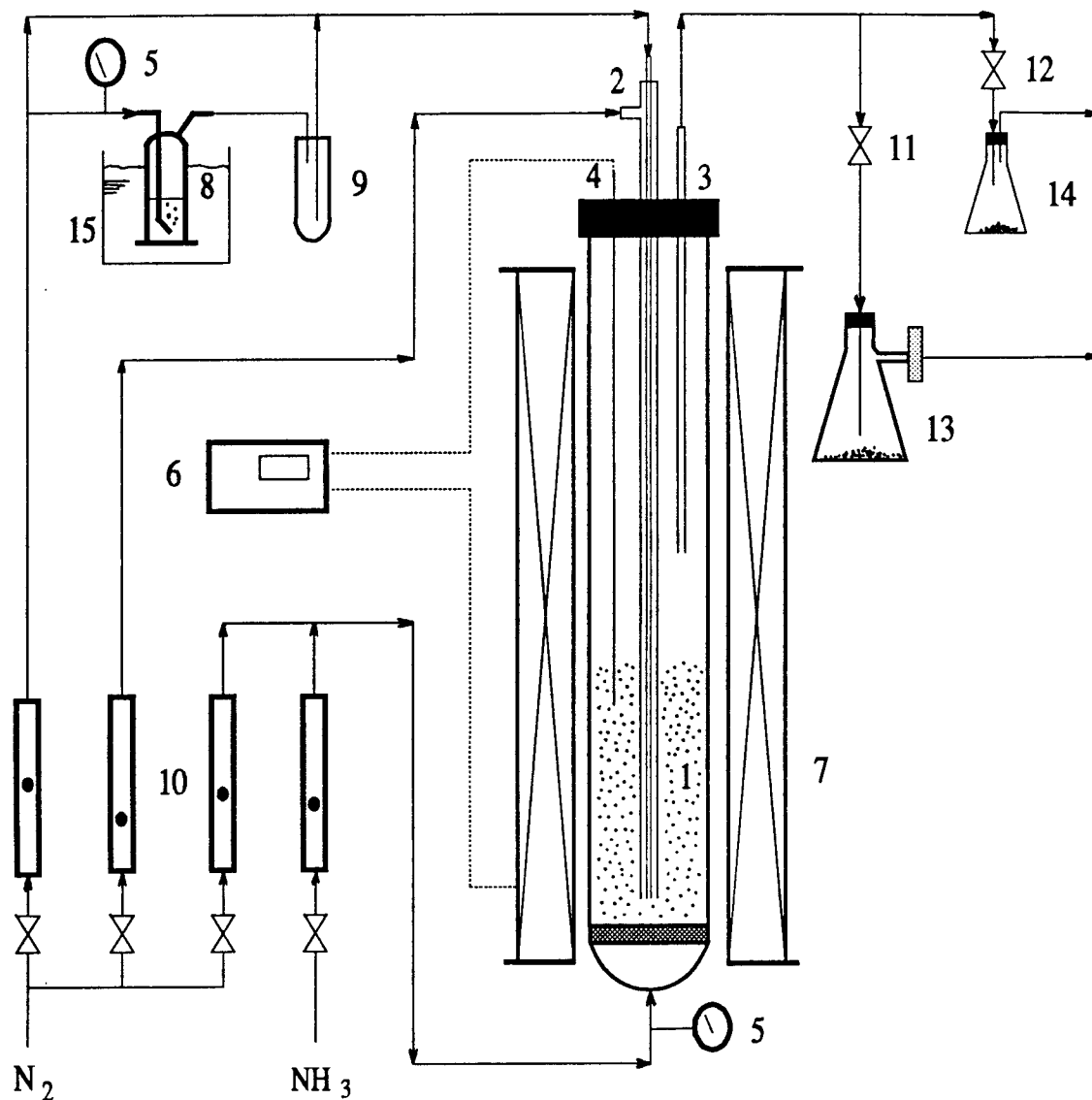
The study described in this thesis focuses mainly on the kinetics of the gas phase reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  at temperatures around the room temperature in a fluidized bed reactor. A fluidized bed reaction system was designed and constructed for this study. Two kinds of  $\text{Si}_3\text{N}_4$  particles, one in Geldart B ( $\rho_s = 2.63 \times 10^3 \text{ kg/m}^3$ ,  $d_p = 370 \text{ }\mu\text{m}$ ) and the other in Geldart C ( $\rho_s = 2.90 \times 10^3 \text{ kg/m}^3$ ,  $d_p = 0.50 \text{ }\mu\text{m}$ ), were fluidized to investigate the capability of collecting solid products.  $\text{NH}_3$  was supplied in excess of the stoichiometric ratio to convert most of  $\text{SiCl}_4$  [3, 22]. The objective of this study is also to develop a kinetic model for the reaction between  $\text{NH}_3$  and  $\text{SiCl}_4$  vapors at low temperatures (280-353 K). The literature review described above provided sufficient background information for conducting the study.

## CHAPTER 3

### EXPERIMENTAL EQUIPMENT AND PROCEDURES

Figure 3.1 shows the schematic diagram of the reaction system used in this study. The system consists of an  $\text{NH}_3$  gas supply, a  $\text{SiCl}_4$  vapor supply, a fluidized bed reactor for the  $\text{NH}_3$ - $\text{SiCl}_4$  reaction, and a sampler to collect product  $\text{Si}(\text{NH})_2$  powder.

$\text{Si}_3\text{N}_4$  particles which served as inert particles for the collection of product  $\text{Si}(\text{NH})_2$  were charged into the reactor. Through the distributor at the bottom of the reactor,  $\text{NH}_3$  gas diluted with oxygen-free  $\text{N}_2$  was fed to fluidize the inert particles.  $\text{SiCl}_4$  vapor, generated by bubbling oxygen-free  $\text{N}_2$  through a reservoir of liquid  $\text{SiCl}_4$ , was fed through concentric tubes into the fluidized bed for reaction. The separate feeding lines for the reactants were designed to prevent solid products from plugging the  $\text{NH}_3$  gas distributor. The reaction temperature in the fluidized bed was controlled by a furnace with a temperature controller or by an ice bath, depending upon the temperature to be set. The outlet of the fluidized bed reactor was divided into two streams: one connected to a flask with a filter to trap very fine particles being blown out of the reactor by the nitrogen carrier gas, and the other connected to a flask to periodically sample products from the reactor for analysis. By opening the sampling valve, closing the vent valve, and inserting the sampling tube to the top of the dense zone of fluidized bed, product powder could be sampled together with inert particles easily when needed. The details of this reaction system, as well as chemicals and experimental procedures used in this study, are described in the following sections.



1. Fluidized bed reactor
2.  $SiCl_4$  supply pipe
3. Sampling tube
4. Thermocouple
5. Pressure gauges
6. Temperature controller
7. Furnace/ ice bath
8.  $SiCl_4$  reservoir/ bubbler

9. Trap
10. Flowmeter
11. Vent valve
12. Sampling valve
13. Trap flask
14. Sampling flask
15. Ice-water bath

Figure 3.1 Schematic diagram of equipment.

### 3.1 Reaction System Set-up

#### 3.1.1 Fluidized bed reactor

The fluidized bed reactor consists of two major parts, (1) a reactor column with an  $\text{NH}_3/\text{N}_2$  gas distributor and an  $\text{NH}_3/\text{N}_2$  gas intake adaptor, and (2) a stopper assembly to seal the upper end of the reactor column and also to permit the  $\text{SiCl}_4/\text{N}_2$  gas entrance, the thermocouple insertion, the  $\text{N}_2$  carrier gas release, and the product sample collection. The reactor column is made of a glass tube of 4.2 cm i.d. and 55 cm long. The  $\text{NH}_3$  gas distributor, welded onto the lower portion of the reactor column, is a 2.5 mm-thick sintered glass disc with pores of an average size of 2.0  $\mu\text{m}$ . The  $\text{NH}_3/\text{N}_2$  gas intake adaptor is a glass ball-socket joint welded at the bottom of the reactor column to be connected to the  $\text{NH}_3/\text{N}_2$  source line. The fluidized bed reactor is corrosion-resistant against the reactants and allows measurements of bed height by direct observation through the glass wall.

The upper stopper is made of Teflon. Through the stopper, a  $\text{SiCl}_4/\text{N}_2$  supply pipe, made of two concentric stainless steel tubes, is connected to the  $\text{SiCl}_4$  vapor supplying source.  $\text{N}_2$  and  $\text{SiCl}_4/\text{N}_2$  mixture gas are fed into the reactor through the annulus and the inner tube of the concentric tube-assembly, respectively. The outlets of the concentric tubes are placed 1.0 cm above the  $\text{NH}_3$  gas distributor. This concentric tube-assembly was designed to prevent solid products from depositing at the outlet of the  $\text{SiCl}_4/\text{N}_2$  feeding line.

A k-type thermocouple to measure the reaction temperature and a stainless steel tube to sample product powder are also inserted through the upper stopper. The



thermocouple probe is located 10 cm above the  $\text{NH}_3$  gas distributor. The sampling tube made of a 0.64 cm i.d. stainless steel tube is held using a Swagelok stainless steel male connector with an O-ring seal. The hole of the male connector is designed to allow the sampling tube to slide up and down within the column during sampling operations.

### 3.1.2 $\text{SiCl}_4$ reservoir with trap

$\text{SiCl}_4$  vapor to be supplied to the fluidized bed reactor was generated by bubbling nitrogen gas at a constant flow rate through a liquid  $\text{SiCl}_4$  in a reservoir. The  $\text{SiCl}_4$  reservoir is made of glass with a sintered glass sparger for nitrogen bubbling. An ice/water bath maintains the temperature of liquid  $\text{SiCl}_4$  at 273 K. Because the saturated vapor pressure of  $\text{SiCl}_4$  at 273 K is known to be 10.3 kPa, assuming that the nitrogen gas is saturated with  $\text{SiCl}_4$  vapor allows one to determine the molar flow rate of  $\text{SiCl}_4$  fed into the fluidized bed. A trap installed in the stream between the bubbler and the  $\text{SiCl}_4$  supply pipe prevents product powder from returning into the bubbler.

### 3.1.3 Controller, furnace and ice bath

A PID controller (model number CN 9000A, purchased from Omega Engineering, Inc.) connected with a thermocouple was used to display the reaction temperature and to adjust the power to be supplied to the furnace (model number M-2724, Hevi-duty Electric Co., Milwaukee, Wisconsin) with heating elements made of a

nickel and chromium alloy. The maximum achievable temperature of the furnace is 1273 K and the maximum available electrical power is 2 kW.

A column, made of a PVC tube of 10 cm i.d. and 50 cm long with a closed bottom, was used as an ice/water bath to keep the fluidized bed reactor at 280 K. The  $\text{NH}_3/\text{N}_2$  intake adaptor was connected with the  $\text{NH}_3/\text{N}_2$  gas supply source through a hole drilled on the bottom of the ice/water bath, which was sealed with a rubber stopper.

### 3.1.4 Sampling flask and trap flasks

A Pyrex 500 ml filtering flask was connected to the sampling tube for sampling product powder from the top of the fluidized bed. A couple of Pyrex 1000 ml filtering flasks with tubulation were used alternatively for collecting carryover fines. The side arm of each flask was connected to a filter in order to trap all the powder. The product powder collected in the sampling flask and the carryover fines collected by the trap flasks with filters were weighed and then chemically analyzed.

## 3.2 Chemicals

There were two kinds of  $\text{Si}_3\text{N}_4$  powder employed as inert particles in the reaction.  $\text{Si}_3\text{N}_4$  fine powder with a mean particle size ( $d_p$ ) of 0.5  $\mu\text{m}$  and a density ( $\rho_s$ ) of  $2.90 \times 10^3 \text{ kg/m}^3$ , classified as Geldart C particles, and large particles with  $d_p = 330 \mu\text{m}$  and  $\rho_s = 2.63 \times 10^3 \text{ kg/m}^3$ , classified as Geldart B particles, were both offered by Shin Etsu Chemical Company, Ltd. Liquid  $\text{SiCl}_4$  (99%) used as one of the reactants,

solid  $\text{AgNO}_3$  (99%) and  $\text{K}_2\text{CrO}_4$  (98%) used for chemical analysis were all of analytical grade, purchased from Aldrich Chemical Company, Inc.  $\text{N}_2$  gas (standard-grade) and  $\text{NH}_3$  gas (99.9%) were supplied from a local dealer. Distilled water was provided by the Department of Chemistry, Oregon State University.

### 3.3 Experimental Procedures

#### 3.3.1 Preliminary experiments

In order to make sure that particles are well-fluidized in the reactor, measuring the apparent minimum fluidizing velocities ( $u_{mf}$ ) is always required even when some suggested values are available in literature [19, 20]. Generally,  $u_{mf}$  can be determined by plotting the pressure drop ( $\Delta P$ ) across the bed of solids versus superficial gas velocity ( $u_0$ ) [24]. The pressure gauge installed on the  $\text{NH}_3/\text{N}_2$  source line, as shown in Figure 3.1, was used to measure the total pressure drop through the  $\text{NH}_3$  gas distributor and across the bed.  $\Delta P$  was then evaluated as the difference between the total pressure drop across the fluidized bed with solids and it across the empty bed. Total pressure drops were measured at velocities  $u_0$  as they were increased (aeration) from zero to 0.34 m/s and then at velocities  $u_0$  as they were decreased (deaeration) back to zero. The total pressures were recorded after the fluidization was maintained at each gas velocity for 5 minutes. Both  $\text{Si}_3\text{N}_4$  fine powder and large particles described in the previous section were investigated.

### 3.3.2 Experimental procedures

A pre-weighed amount of inert  $\text{Si}_3\text{N}_4$  particles were first fluidized by nitrogen at a velocity of 1.5 times  $u_{mf}$ . Meanwhile,  $\text{N}_2$  gas to bubble through liquid  $\text{SiCl}_4$ , at a volumetric flow rate of  $8.3 \times 10^{-7} \text{ m}^3/\text{sec}$ , by-passed the  $\text{SiCl}_4$  reservoir and flowed into the bed through the inner tube of the  $\text{SiCl}_4$  supply pipe.  $\text{N}_2$  gas at a constant flow rate of  $3.3 \times 10^{-6} \text{ m}^3/\text{s}$  was also directed through the annulus of the  $\text{SiCl}_4$  supply pipe into the reactor. At the beginning of each run, the inert particles were fluidized with no reactants supplied for 45 minutes. This preparation step assured the inert powder, in particular, to be agglomerated to a fluidizable size and the fluidized bed to be stabilized. To start the reaction,  $\text{NH}_3$  gas, at a flow rate of  $2.5 \times 10^{-6} \text{ m}^3/\text{s}$ , was added to the fluidizing  $\text{N}_2$  gas. At the same time, the  $\text{N}_2$  gas by-passing liquid  $\text{SiCl}_4$  was switched to pass through the  $\text{SiCl}_4$  reservoir to carry  $\text{SiCl}_4$  vapor into the reactor. The total gas flow rate was set at  $1.05 \times 10^{-4} \text{ m}^3/\text{s}$  for the fine  $\text{Si}_3\text{N}_4$  powder and  $3.08 \times 10^{-4} \text{ m}^3/\text{s}$  for the large  $\text{Si}_3\text{N}_4$  particles. A sample of approximate one gram of solids was taken from the bed every 20 minutes for chemical analysis. The trap flasks for collecting carryover were replaced alternatively every 15 minutes. The increase in the total mass of each trap flask was measured to determine the entrainment from the fluidized bed. The reaction was carried out for 100 minutes.

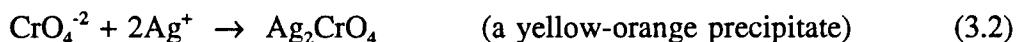
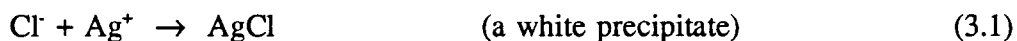
The preliminary experiments for testing the influence of the size of inert particles on the efficiency of collecting solid products were conducted using the fine and large inert  $\text{Si}_3\text{N}_4$  particles. Based on the experimental results, the fine inert  $\text{Si}_3\text{N}_4$  powder which gave a higher efficiency was chosen to study the reaction kinetics.

The concentration of  $\text{SiCl}_4$  was varied from  $9.60 \times 10^{-6} \text{ kmol/m}^3$  to  $4.99 \times 10^{-5} \text{ kmol/m}^3$  to see the influence of the  $\text{SiCl}_4$  concentration on the rate of  $\text{Si}(\text{NH})_2$  deposition onto the inert particles. The initial bed mass of the inert particles was changed in the range of 0.080-0.180 kg to test the reaction kinetics of  $\text{Si}(\text{NH})_2$  synthesis in a fluidized bed reactor. The reaction temperature was set in the range of 280-353 K in order to investigate the temperature dependence of the reaction rate.

### 3.3.3 Chemical analysis

According to reaction (2.1) or (2.2), chloride ion is the only chemical component in product mixtures which can be quantified easily and precisely by a simple chemical analysis. The amount of desired product,  $\text{Si}(\text{NH})_2$ , can be evaluated by dividing the amount of chloride ion by 4, assuming that one mole of  $\text{Si}(\text{NH})_2$  is always associated with four moles of  $\text{NH}_4\text{Cl}$  according to the stoichiometry.

The chlorine contents of samples were determined by the Mohr's titration method [23]. The method uses a  $\text{AgNO}_3$  solution as a titrator and  $\text{K}_2\text{CrO}_4$  as an indicator. There are two kinds of precipitates formed during the titration.



Since  $\text{AgCl}$  is less soluble than  $\text{Ag}_2\text{CrO}_4$ , the latter can not show up until chloride ions have been consumed completely by silver ions. Therefore, the end point is marked by the first formation of the yellow-orange precipitate of  $\text{Ag}_2\text{CrO}_4$ .

After measuring sample mass, each sample was dissolved in  $\text{Cl}^-$ -free distilled water for 5 hours. A few drops of the indicator were added to the solution. The

solution with chloride ions was then titrated by an aqueous 0.01 N  $\text{AgNO}_3$  solution until sharp the yellow precipitate was observed under yellow light. A blank test on the indicator was also carried out when the 0.01 N silver nitrate solution was used.

## CHAPTER 4

### RESULTS AND DISCUSSION

#### 4.1 The Measurement of Minimum Fluidizing Velocities

Figures 4.1 and 4.2 show the diagrams of the pressure drop across the fluidized bed varying with the velocity of fluidizing gas for large and fine  $\text{Si}_3\text{N}_4$  particles, respectively. Here, the pressure drop is normalized by dividing the measured data by the gravitational force exerting on the bed-solids per unit cross-sectional area,  $\Delta P/(W_{b0} g/A_b)$ . These diagrams can be used to determine the minimum fluidizing velocities ( $u_{mf}$ ) for particles [20, 24]. Figure 4.1 shows that the normalized pressure drops for deaeration are around unity while particles are being fluidized and then slip back to the origin when the fluidizing velocity is decreased. Also, the normalized pressure drops in aeration and deaeration do not deviate from unity in the fluidizing region. This result indicates that there is no entrainment in the large Geldart B  $\text{Si}_3\text{N}_4$  particles. The minimum fluidizing velocity  $u_{mf}$  for the large can easily be determined to be 0.135 m/s.

Unlike the pressure drop data shown in Figure 4.1, the pressure drop in deaeration in Figure 4.2 shows a small negative deviation from unity in the fluidizing region. The decreased pressure drop is attributed to the particle entrainment after a bed was fluidized for a certain period of time. Here, the pressure drop data in the deaeration operation were used as the bases to determine the minimum fluidizing velocity. Although there was still uncertainty,  $u_{mf} = 0.045$  m/s was employed in this

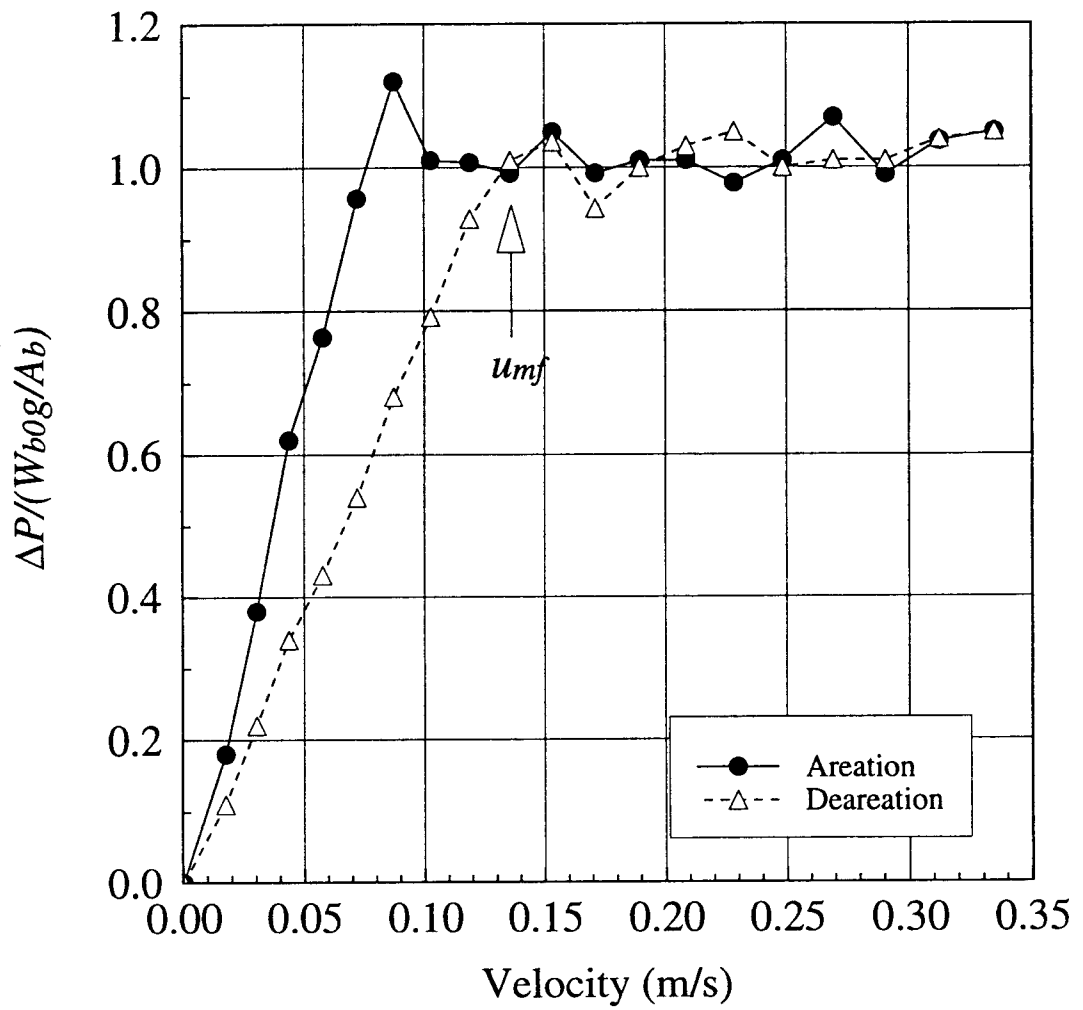


Figure 4.1 Normalized pressure drop across a fluidized bed containing 113.6 g of  $\text{Si}_3\text{N}_4$  large particles.



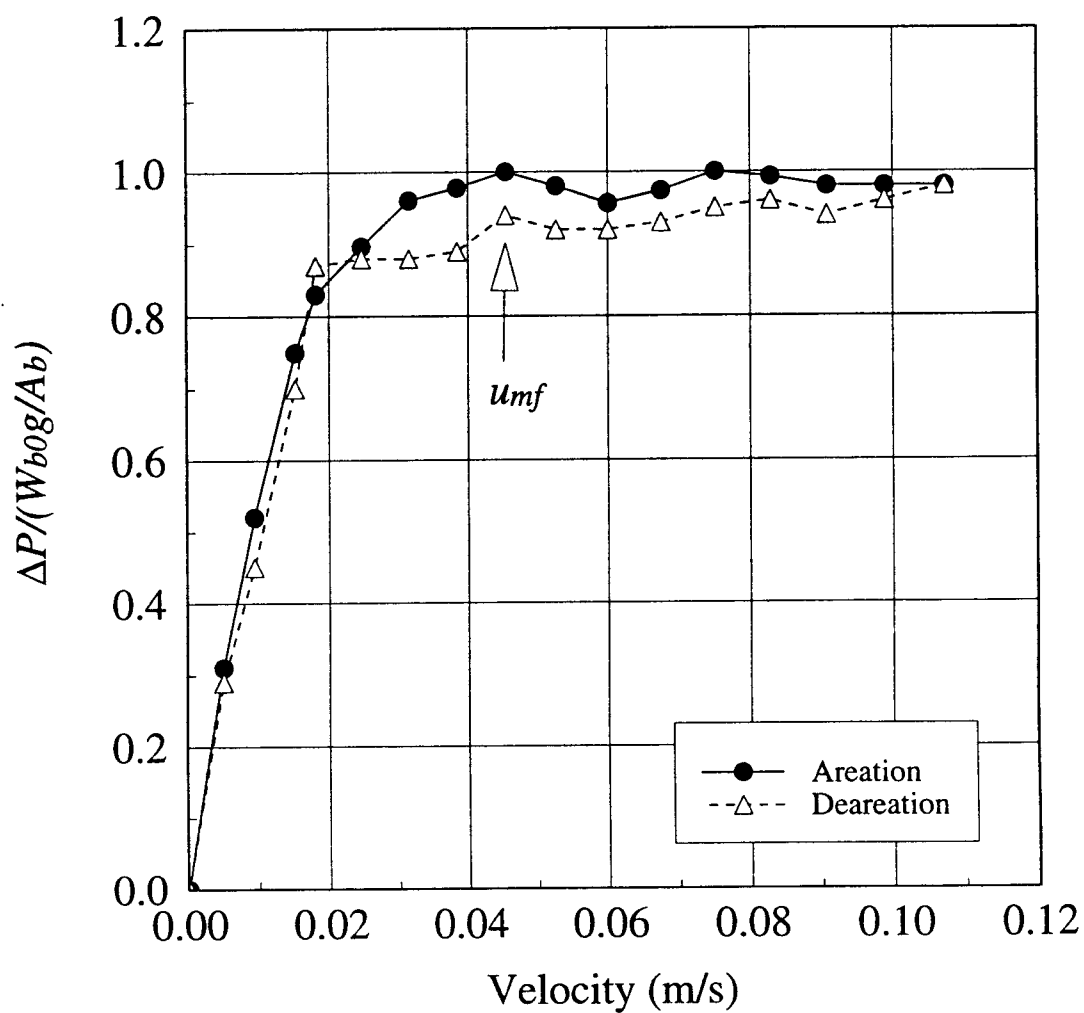


Figure 4.2 Normalized pressure drop across a fluidized bed containing 105.4 g of  $\text{Si}_3\text{N}_4$  fine powders.

case. In the following kinetic study, the superficial gas velocity,  $u_0$  was set at 1.5 times  $u_{mf}$  for smooth fluidization.

## 4.2 Observed Results

Because the furnace was removed during the kinetic study at the room temperature, the fluidizing phenomena were easily observed through the glass wall of the fluidized bed. The product was also taken out of the fluidized bed for examination after the reaction was terminated. These direct inspections provided better understanding of fluidization of the gas phase reaction of  $\text{SiCl}_4$  and  $\text{NH}_3$ . The observed results are described below.

### 4.2.1 Reaction in a fluidized bed with large particles

The large  $\text{Si}_3\text{N}_4$  particles, classified in Geldart B, were first tested as inert particles based on the findings that they are easy-to-fluidize without forming agglomerates and without entrainment. When two reactants were introduced into the fluidized bed at 300 K, with the gas velocity,  $u_0$ , set at 0.20 m/s ( $=1.5 \times u_{mf}$ ), smoke-like white powder formed in the trap flask, not in the bed. The smoke-like powder seemed to be the product blown out of the fluidized bed and caught by the trap flask. This phenomenon suggested that the residence time of the reactants in the bed was not long enough for the product to be generated within the fluidized bed. Even with an increased bed height and a reduced gas velocity, smoke still formed in the trap flask.

Thus, it was concluded that fluidizing the large  $\text{Si}_3\text{N}_4$  inert particles was not suitable for the collection of product powder in this study.

#### 4.2.2 Reaction in a fluidized bed with fine powder

Because the fine powder has a lower minimum fluidization velocity, it is expected that the reactants have a longer residence time in the bed. Hence in preliminary experiments, the fine powder was tested with the gas velocity  $u_0$  set at 0.0675 m/s. The observed results are described below.

The  $\text{Si}_3\text{N}_4$  fine powder appeared to be sticky at the beginning of fluidization. A small portion of fine particles attached to the column wall after fluidization for approximately 20 minutes. However, the attached particles in the splash zone began to fall down after carrying out the reaction for 40 minutes. This indicates that the inter-particle forces changed due to the reaction product coating inert particles, leading to less sticky particles. Particles hardly adhered on the column wall and no white smoke rose within the column or formed in the trap flask during the reaction, indicating that most of the product was collected within the dense zone and the reaction in the freeboard zone was minor.

Compared to the large particles, fluidizing the  $\text{Si}_3\text{N}_4$  fine powder made it easier to collect the product powder. Therefore, all the reaction experiments were carried out by using the  $\text{Si}_3\text{N}_4$  fine powder.

### 4.2.3 Product distribution

After each experiment, the whole bed of particles were poured out for visual inspection. The mixture of inert and product powders behaved like loose sand. There was no change observed in the light tan color of particles although most of the product was collected by the  $\text{Si}_3\text{N}_4$  fine powder. Only a few white clusters were found in the product mixture. It seemed that part of product coagulated to form these small clusters rather than to attach to the inert particles. This occurred especially when the inert particles were not well mixed due to channeling. However, the chemical analysis of product samples showed that 70-95 % of  $\text{SiCl}_4$  vapor was converted to the product powder in the fluidized bed reactor, assuming completely mixed inert and product powders in this reactor.

The solid products were not only collected by the inert particles but also self-coagulated and deposited on surfaces within the fluidized bed. A lump of white deposit was usually found at the outlet of the  $\text{SiCl}_4$  supply pipe and caused the plugging problem. Sometimes, twig-like white product was obtained when stable channels formed in the bed. All of these deposits seemed to have formed due to the locally high concentration of reactants. Therefore, the plugging on the  $\text{SiCl}_4$  supply pipe had to be cleared off by tapping the tee on the stopper, and the stable channels to be broken by vibrating the fluidized bed just in time. The chlorine content in these coagulates was 2 to 4 times higher than that in the average product mixture. However, the total amount of chlorine in these white coagulates was less than 4% of the total chlorine collected in the bed.

### 4.3 Entrainment of Fine Powder

Entrainment and elutriation play important roles in the fluidization of very fine powder. In this kinetic study, it was observed that the inert particles and product fines were continuously elutriated from the dense region and blown out of the reactor, thus the mass of the fluidized bed decreased during the fluidization. The reaction was terminated before the loss of particles caused experimental errors. Therefore, the entrainment of particles was investigated to know when to stop experiments.

Figure 4.3 compares the cumulative mass ( $W_c$ ) of entrained particles with and without the reaction. All these carryover particles were collected by a couple of trap flasks replaced every other 15 minutes. The cumulative mass  $W_c$  with no reaction increased at a constant rate. The constant attrition became more stabilized after fluidizing particles for 45 minutes. In order to predict the bed mass during the fluidization, the reaction was carried out in the constant attrition region. Thus, the reaction was initiated after fluidizing inert powder for 45 minutes. After the reaction was initiated, the entrainment with reaction became higher than that without reaction and increased linearly with reaction time. The attrition rate was evaluated by the slope of each straight line, which is  $2.1 \times 10^{-4}$  kg/min for the case with reaction and  $1.0 \times 10^{-4}$  kg/min for that with no reaction. After fluidizing for 145 minutes, the loss of bed mass for the case with no reaction was 7.7% of the initial bed mass ( $W_{b0}$ ) and that with reaction was 14%.

The results of this experiment suggest that the bed mass at any time during the reaction can be determined from the particle attrition rate. Since all the entrained

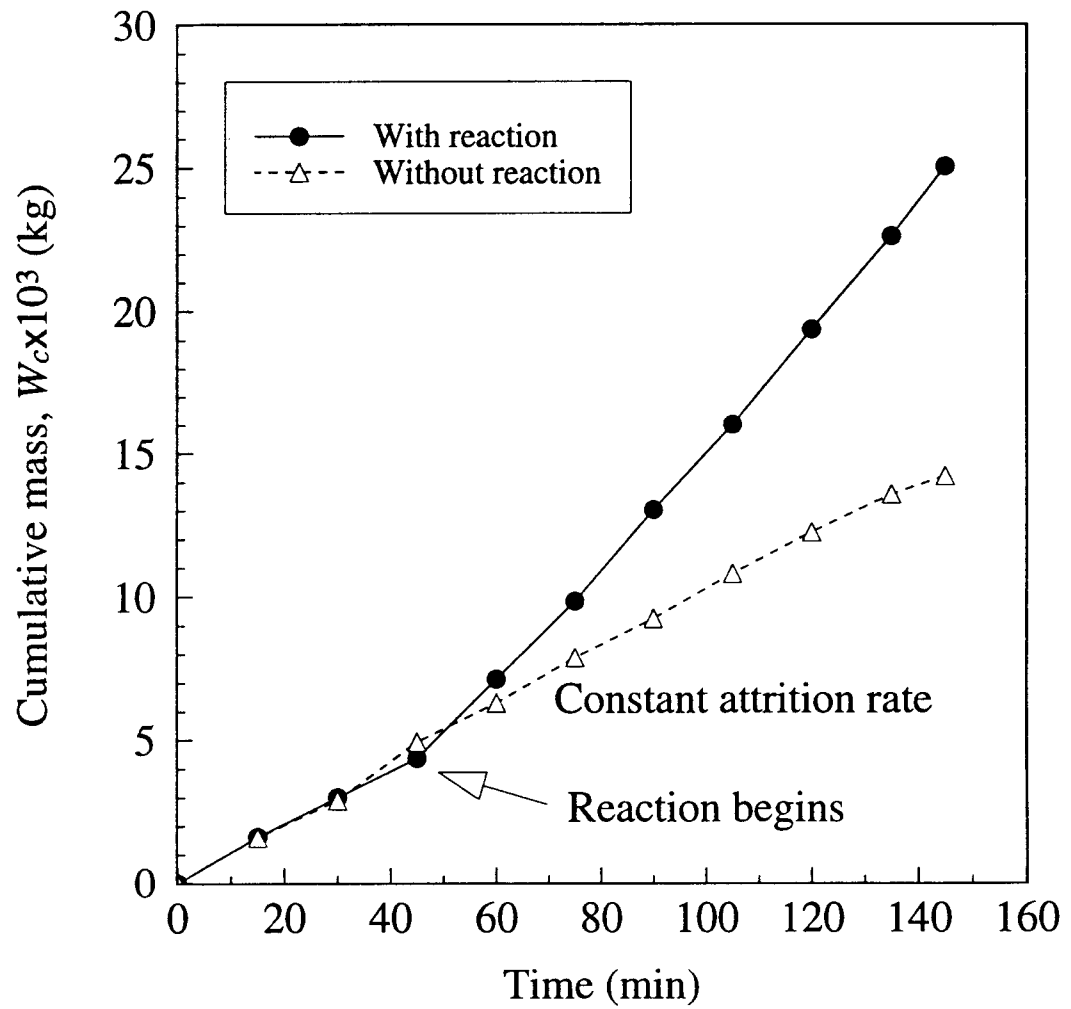


Figure 4.3 The accumulation of carryover fines versus time with  $W_{b0} = 182.5$  g and  $u_0 = 0.0675$  m/s.

particles were collected in the trap flasks at a constant attrition rate, the bed mass at any time during the reaction was expected to be the initial mass  $W_{b0}$  minus the mass of particles collected in the flask.

The effect of the reaction temperature on the entrainment of fines is shown in Figure 4.4. All the experiments were conducted using the same concentration of reactants ( $\text{SiCl}_4$ :  $3.88 \times 10^{-6}$  kmol/m<sup>3</sup>,  $\text{NH}_3$ :  $1.87 \times 10^{-3}$  kmol/m<sup>3</sup>). In each experiment, the reaction was started after the bed was fluidized for 45 minutes and then continued for 100 minutes. Figure 4.4 shows that the particle attrition rate in each run is essentially constant over the period of reaction. The higher the reaction temperature, the more the attrition. Figure 4.4 also shows that a higher attrition rate results from higher bed mass. The entrainment becomes more significant because increasing the bed mass shortens the freeboard zone. The total loss of bed mass after the fluidization with reaction is in range of 15-23% of the initial bed mass  $W_{b0}$ .

#### 4.4 Analysis of Reaction Kinetics

##### 4.4.1 Model description

The chlorine content in samples shows that the product mixture of  $\text{Si}(\text{NH})_2$  and  $\text{NH}_4\text{Cl}$  is collected by the  $\text{Si}_3\text{N}_4$  fine powder in the fluidized bed. The solid products generated in the void space in the fluidized bed are considered to have deposited on the surface of the fluidized inert powder before being blown out. Since a little amount of powder having a high chlorine content was found on the filter paper, the collection of product generated in the bed may not be 100%. Also, previous research [4] help us

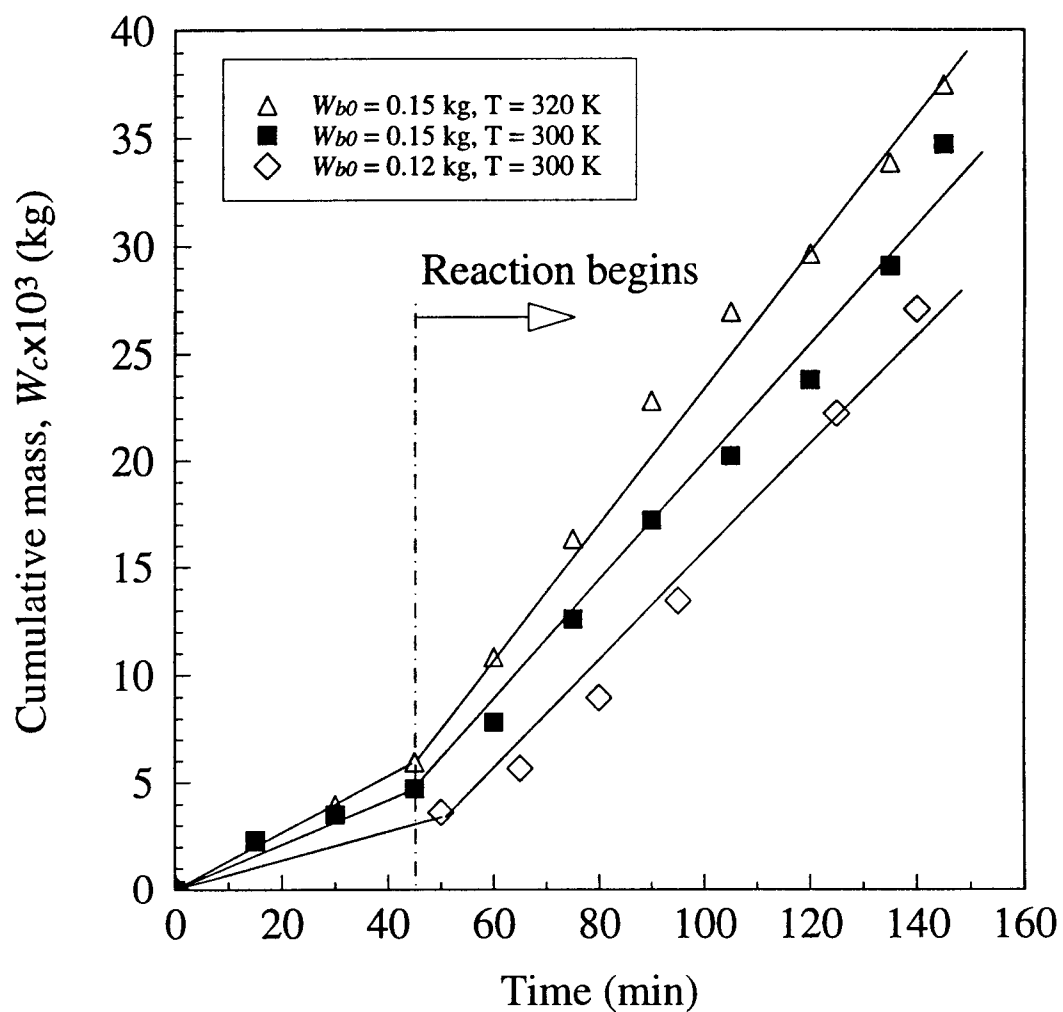


Figure 4.4 The temperature effect and bed weight dependence of cumulative  $\text{Si}_3\text{N}_4$  fine powder.



to realize how fast the reaction is, and what may proceed inside the fluidized bed. Based on the experimental observation and the information obtained from the literature, a kinetic model to describe the reaction in the fluidized bed has been developed. The basic assumptions used in the present kinetic study are described below.

1. The reaction is carried out in the gas phase of the fluidized bed operated at the atmospheric pressure. The contribution of the heterogeneous surface reaction is negligible in comparison to the homogeneous gas phase reaction [3, 14].
2. Plug flow can represent the gas flow in the fluidized bed and the fluidized bed reactor can be considered as a tubular reactor.
3. Most of the solid products formed in the gas phase attach to the surface of fluidized particles. However, some of product particles that are not captured by the inert particles are entrained by the carrier gas. The efficiency  $f$  of collection is defined as

$$f = \frac{\text{moles of product remaining within the fluidized bed reactor}}{\text{moles of product generated in the void of the fluidized bed}} \quad (4.1)$$

4. Fine particles are well mixed in the fluidized bed. The temperature and the concentration of product deposits are of uniform distribution throughout the fluidized bed.
5. The voidage of the bed,  $\epsilon_A$ , is not affected by the system temperature [24]. It can be considered as a constant in the range of 280-353 K.

6. The stoichiometric ratio of  $\text{Si}(\text{NH})_2$  to  $\text{NH}_4\text{Cl}$  is always 1 to 4, no matter what mechanism the reaction at low temperatures follows.
7. Since  $\text{NH}_3$  vapor is supplied in significant excess compared to  $\text{SiCl}_4$  vapor, a pseudo-first order irreversible reaction with respect to  $\text{SiCl}_4$  is assumed to be the reaction kinetics.
8. solid product attach instantaneously to the surface of inert particles after being formed in the gas phase reaction. The rate determined step in this case is the gas-phase reaction, not the product deposition.
9. The bed mass decreases with time due to the entrainment. However, since the decrease in bed mass is maintained small, at most 25% of the initial mass and 17% as average, the bed mass during the reaction is considered as a constant  $W_b$ , evaluated by taking an average of the bed mass before and after the reaction.

#### 4.4.2 Model

Considering that only the gas phase reaction occurs between  $\text{SiCl}_4$  and  $\text{NH}_4$  in a fluidized bed, the conversion of  $\text{SiCl}_4$  is defined as:

$$X_A = \frac{\text{moles of SiCl}_4 \text{ consumed}}{\text{moles of SiCl}_4 \text{ fed into the reactor}} = \frac{C_{A0} - C_A}{C_{A0}} \quad (4.2)$$

where  $C_{A0}$  and  $C_A$  are the inlet and outlet concentrations of  $\text{SiCl}_4$ , respectively. Based on assumptions 3, which considers the efficiency  $f$  of collection and on assumption 6, which assumes stoichiometric mixture of the products, the mass balance for  $\text{SiCl}_4$  in the fluidized bed gives:

$$C_{A0} X'_A F = \frac{1}{4} R_d W_b \quad (4.3)$$

and

$$X'_A = f X_A \quad (4.4)$$

Where  $W_b$  is the average mass of bed over the reaction period,  $F$  is the total volumetric flow rate of gases entering the reactor,  $X'_A$  is the apparent conversion, and  $R_d$  is the molar rate of  $\text{NH}_4\text{Cl}$  deposition per unit mass of mixture particles. The factor of  $1/4$  is needed in equation (4.3) because one mole of  $\text{SiCl}_4$  generates four moles of  $\text{NH}_4\text{Cl}$ . The rate of  $\text{NH}_4\text{Cl}$  deposition,  $R_d$ , may be expressed in terms of measurable quantities as:

$$R_d = \frac{1}{w} \frac{dN_{Cl}}{dt} \quad (4.5)$$

where  $w$  is the mass of sample solids taken from the fluidized bed each time for analysis,  $N_{Cl}$  is the molar content of chlorine in the sample and  $t$  is the reaction time.

Combining Eqs.(4.3) and (4.5) gives  $X'_A$  as

$$X'_A = \frac{W_b}{4 C_{A0} F} \left( \frac{1}{w} \frac{dN_{Cl}}{dt} \right) \quad (4.6)$$

According to assumptions 1 and 2, the performance equation of plug flow reactor is expressed by:

$$C_{A0} F dX_A = (-r_A) \epsilon_A dV \quad (4.7)$$

where  $V$  is the bed volume, and  $\epsilon_A$  is the bed voidage which can be determined from

an observed bed height  $H$  by the following equation:

$$\epsilon_A = 1 - \frac{W_b}{\rho_s V} = 1 - \frac{W_b}{\rho_s A_b H} \quad (4.8)$$

where  $A_b$  is the cross sectional area of the bed.

Based on the assumption that the reaction follows a pseudo-first order kinetics with respect to  $\text{SiCl}_4$ , the rate of homogeneous reaction,  $-r_A$ , per unit void volume can be expressed as

$$-r_A = k_A C_A = k_A C_{A0} (1 - X_A) \quad (4.9)$$

where  $k_A$  is the apparent rate constant. Substituting equation (4.9) and (4.4) into equation (4.7), and integrating the resultant equation yields

$$\ln \left( 1 - \frac{X'_A}{f} \right) = - \frac{k_A \epsilon_A V}{F} = - k_A \tau \quad \text{with} \quad \tau = \frac{\epsilon_A V}{F} \quad (4.10)$$

where  $\tau$  is the resistance time of gaseous reactants. Because the value of  $f$  is not known, the model can be tested by plotting  $1 - X'_A$  against  $\tau$  in a semi-log coordinate system and comparing with curves calculated with a number of estimated values of  $f$ . If the data fall on one of the curves for different values of  $f$ , then the suggested kinetics may describe the reaction system with a value of that curve.

#### 4.4.3 Data analysis

In order to verify the model using experimental data, the experimental procedures and conditions were specifically designed. Firstly, a mixture of solid

products and inert particles were sampled and analyzed every 20 minutes to determine the amount of chlorine collected per unit mass of particles in the bed. The data were used to evaluate  $R_d$  by equation (4.5). Equation (4.3), derived from a mass balance of  $\text{SiCl}_4$ , was tested with respect to the constancy of  $f$  by varying  $C_{A0}$ . Thus,  $X'_A$  was determined from the slope of a linear plot of  $C_{A0}$  versus  $R_d$ .  $\epsilon_A$  was estimated from the measurement of the bed height  $H$ , by changing the mass of bed, according to equation (4.8). The performance equation was also examined in terms of the influence of  $V$  on  $X'_A$ , equation (4.10), and then to find  $f$  and  $k_A$ . Finally, the temperature effect on the rate of reaction was investigated.

Figure 4.5 shows the change in the content of chlorine in mixtures of solids at 300 K. Each experiment used the same initial amount of inert particles and an identical gas flow rate  $F$ .  $C_{A0}$  was varied in the range of  $9.56 \times 10^{-6}$ – $4.99 \times 10^{-5}$  kmol/m<sup>3</sup>, while the concentration of  $\text{NH}_3$  was kept at  $1.87 \times 10^{-3}$  kmol/m<sup>3</sup>. The figure shows that in all the cases moles of chlorine per unit mass of solid ( $N_{Cl}/w$ ) is proportional to the reaction time. The slope of each straight line represents the rate of deposition,  $R_d$ , as defined in equation (4.5).

Figure 4.6 shows the  $R_d$  values, determined from Figure 4.5, plotted against the inlet concentration  $C_{A0}$ . Since  $W_b$  and  $F$  are constant, a straight line passing through the origin indicates that equation (4.3) is valid and the collection efficiency is independent of  $C_{A0}$ . The slope of the line, which is determined to be 0.15, gives  $X'_A$  as 0.955, using  $F = 1.05 \times 10^{-4}$  m<sup>3</sup>/s and  $W_b = 0.1585$  kg.

Measured results of  $V$  and  $\epsilon_A$  are shown in Figure 4.7. In these experiments, the fluidization was carried out at 300 K with  $\text{Si}_3\text{N}_4$  fine powder kept in the range of

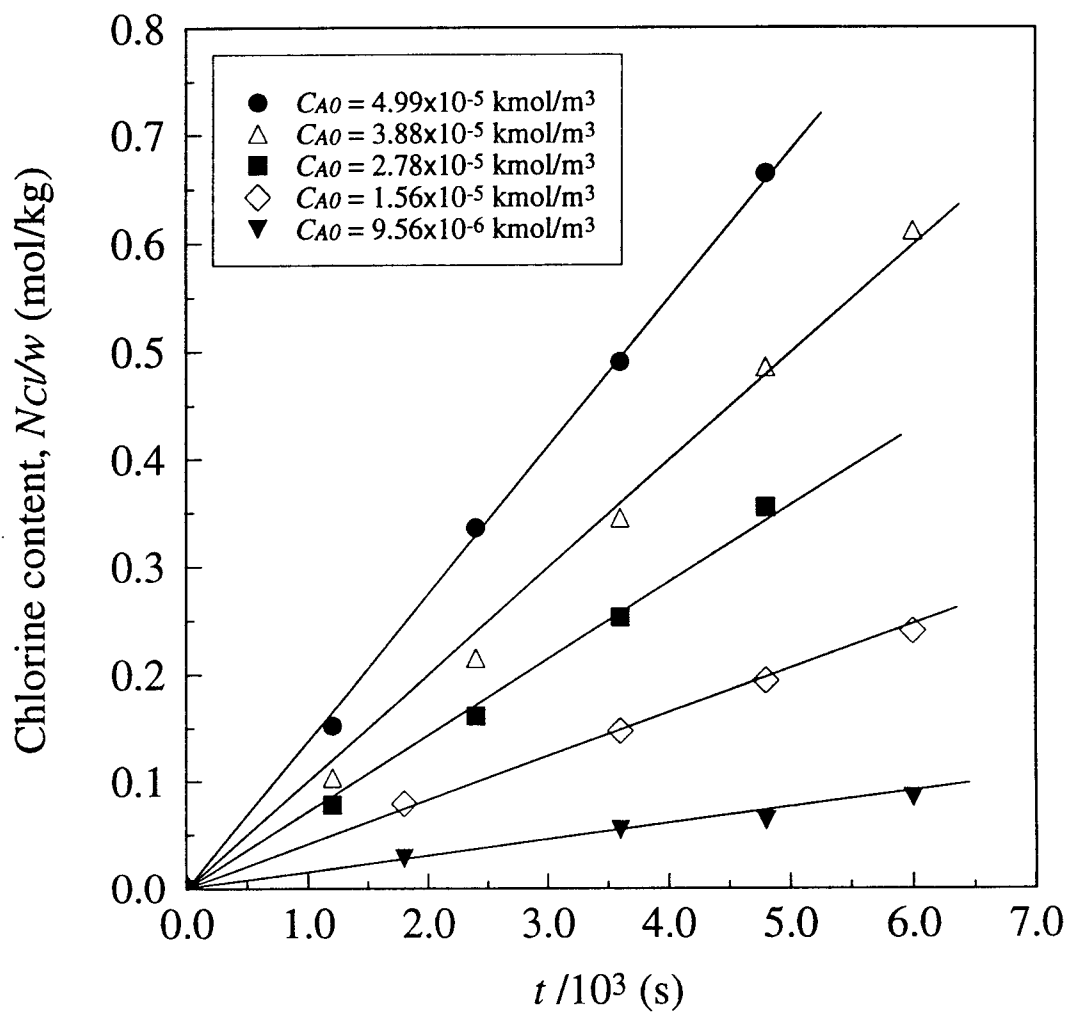


Figure 4.5 Time dependence of chlorine content of sample solids with  $W_b = 0.1585 \text{ kg}$ .

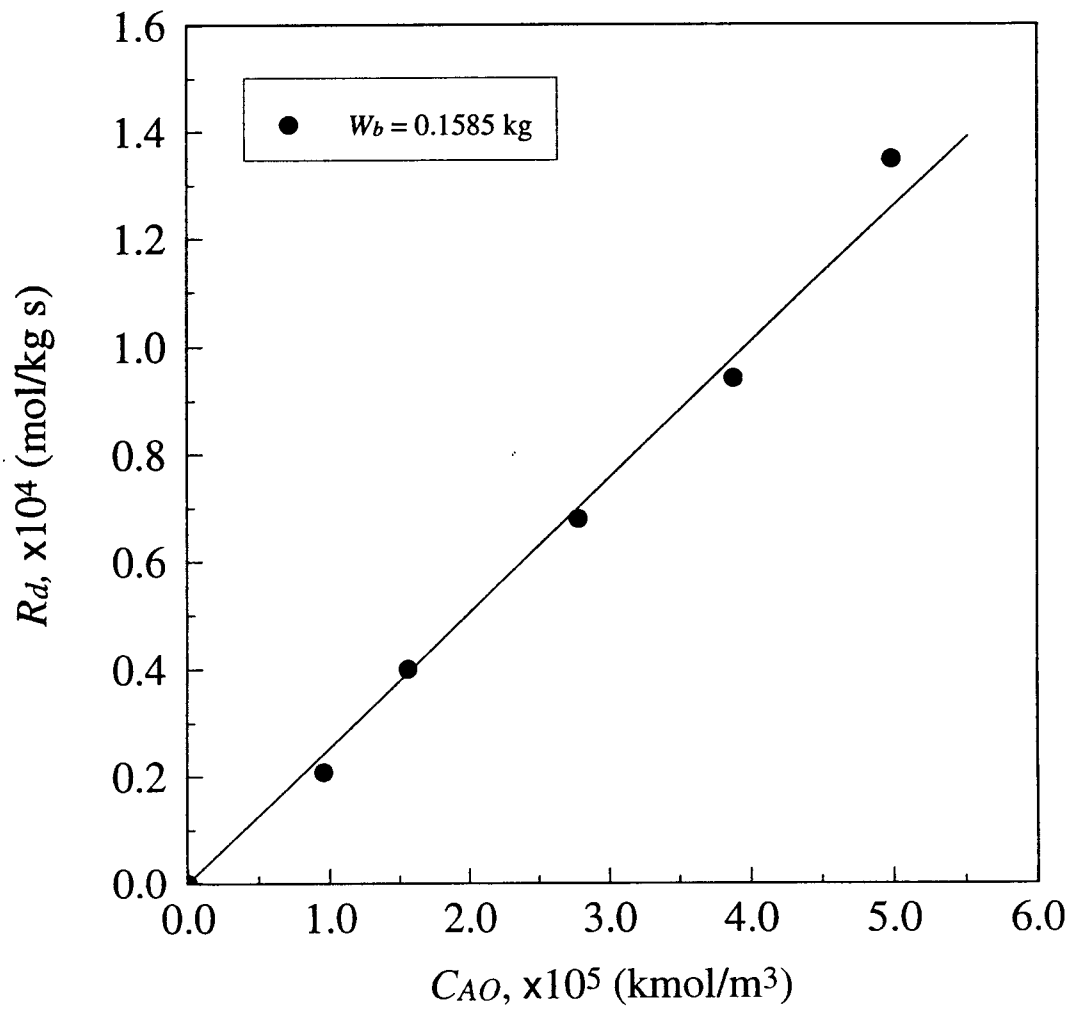


Figure 4.6 Deposition rate versus initial concentration of  $\text{SiCl}_4$ .

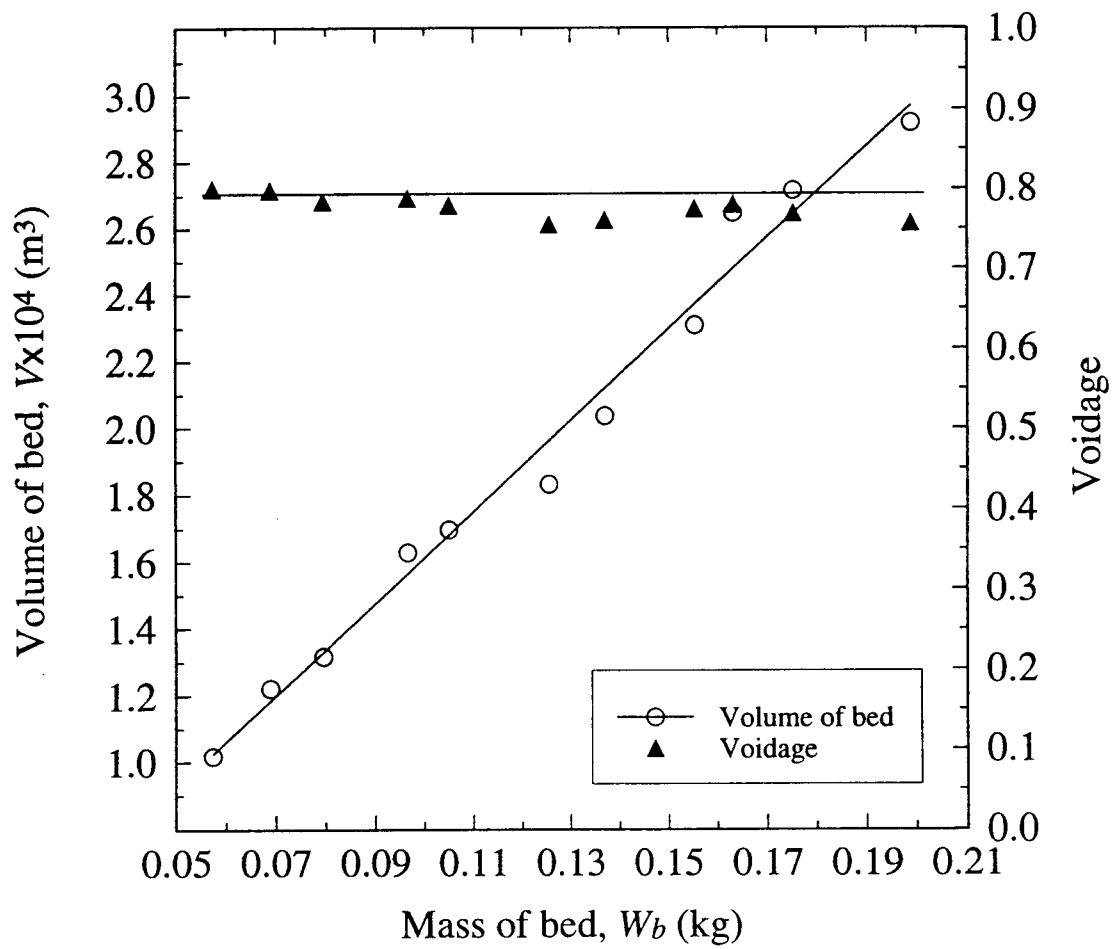


Figure 4.7 Measurements of volume of bed and voidage.



0.058-0.195 kg. The average bed height was measured by the height of the gas-solid mixture, defined as the distance from the gas distributor to the average level of splash zone (*i.e.* the fluctuating bed surface). The actual volume of the fluidized bed was calculated by subtracting the immersed volume of the  $\text{SiCl}_4$  supply pipe from the measured bed volume (the bed height multiplied by the cross sectional area of the column).  $\epsilon_A$  was then evaluated by equation (4.8). Since the ratio  $W_b/V$  was essentially constant,  $\epsilon_A$  did not vary with  $W_b$  or  $V$ . The average  $\epsilon_A$  was calculated to be 0.8 at  $u_0 = 0.0675$  m/s.

Figure 4.8 illustrates the dependence of product deposition on the bed mass. In these experiments,  $W_b$  was changed from 0.1595 kg to 0.0676 kg. A minimum of 0.0676 kg was constrained by the failure of fluidization due to the formation of stable channels resulting from the short bed height less than 0.07 m. It is very interesting that  $R_d$ , the slope of straight line, decreases with  $W_b$ . Since the bed voidage  $\epsilon_A$  is constant, as shown in Figure 4.7,  $V$  can be expressed as a function of  $W_b$  by rearranging equation (4.8). With the expression for  $V$ , equation (4.10) can then be written as

$$X'_A = f \left[ 1 - \exp \left( - \frac{k_A \epsilon_A W_b}{\rho_s F (1 - \epsilon_A)} \right) \right] \quad (4.11)$$

Substituting equation (4.11) into equation (4.3) and solving the resultant equation for  $R_d$  yields a new expression of equation (4.3) in terms of  $W_b$ .

$$R_d = \frac{4 C_{A0} F f}{W_b} \left[ 1 - \exp \left( - \frac{k_A \epsilon_A W_b}{\rho_s F (1 - \epsilon_A)} \right) \right] \quad (4.12)$$

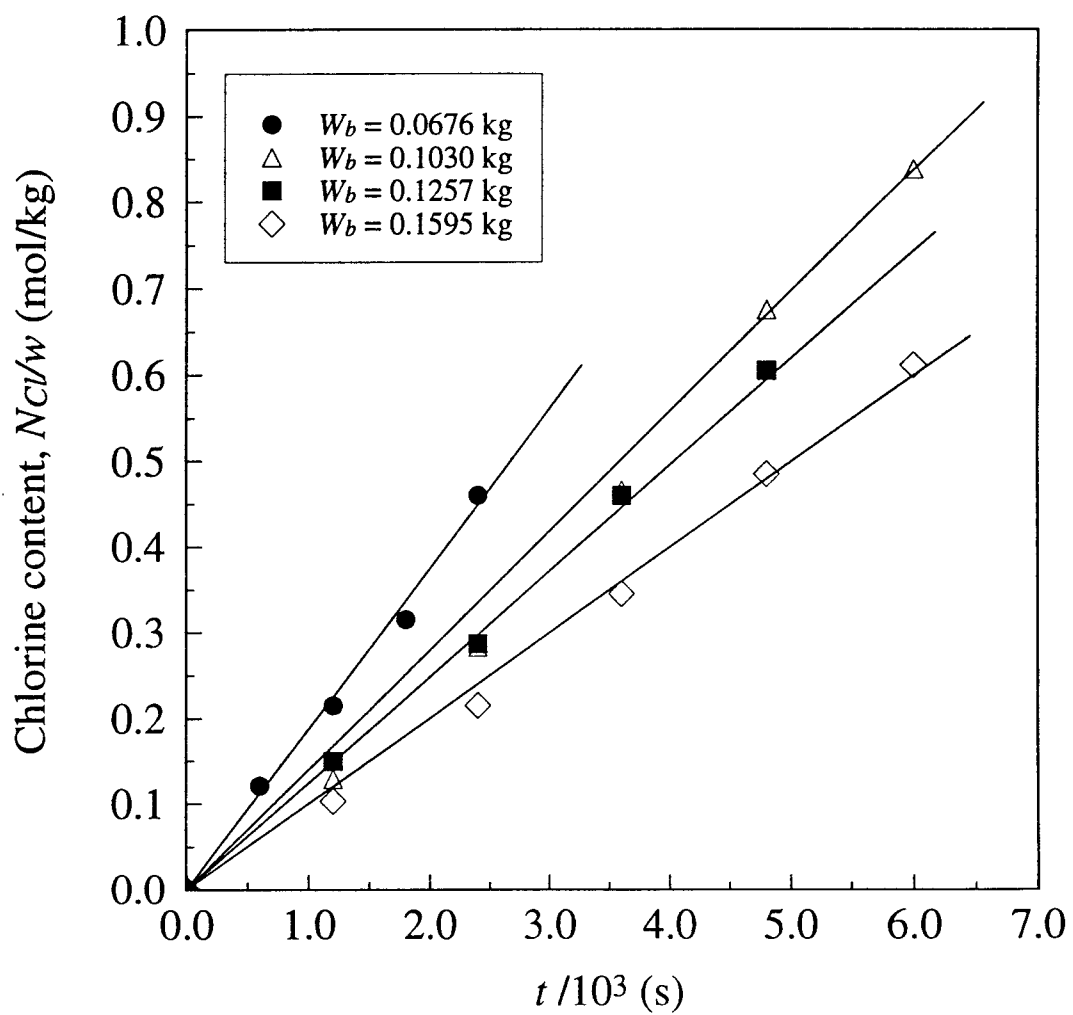


Figure 4.8 Bed weight dependence of product deposits.

According to the equation shown above,  $R_d$  decreases with the increase in  $W_b$  when the other variables, including  $f$ , in particular, are constant.

The proposed first order kinetics may be verified by plotting logarithm of  $1-X'_A$  against  $\tau$  as suggested by equation (4.10). The values of  $X'_A$  were determined by equation (4.6);  $\tau$  for each corresponding  $X'_A$  was calculated by equation (4.10) using  $\epsilon_A = 0.8$ . To find a set of  $k_A$  and  $f$  values that would best fit the  $(1-X'_A)$  and  $\tau$  data, a FORTRAN program to execute trial and error procedures was employed (see Appendix ). Figure 4.9 displays the experimental data obtained at 300 K and the curve of  $1-X'_A$  versus  $\tau$  fitted with various  $f$  values. A value of  $k_A = 1.55$  /s and a value of  $f = 0.99$  give the best fit. Figure 4.10 shows a similar plot of  $1-X'_A$  versus  $\tau$  at 280 K. A value of  $f = 0.98$  gives the best fit. Both values of  $f$  are very close to 1.0, which indicates that the efficiency of product collection is very high and is not affected by the reaction temperature. All the product powder formed in this fluidized bed is collected by the inert particles. Based on these tests, the value of  $f$  was assumed to be 1.00 in the following kinetic study.

The experiments to find the temperature dependence of the reaction were carried out in the range of temperature of 280-353 K. Figure 4.11 shows the plot of data obtained at 280, 300, and 320 K. Data obtained at 353 K were not included, because  $X'_A$  was found to be nearly 1.00. The rate of reaction at this temperature was so fast that  $\text{SiCl}_4$  was totally converted within a short region close to the bottom of the bed. The value of  $k_A$  evaluated in Figure 4.11 from the slope of each line with  $f = 1.00$  may be plotted against the reciprocal of the reaction temperature to determine the activation energy for the pseudo-first order reaction. The Arrhenius plot shown in

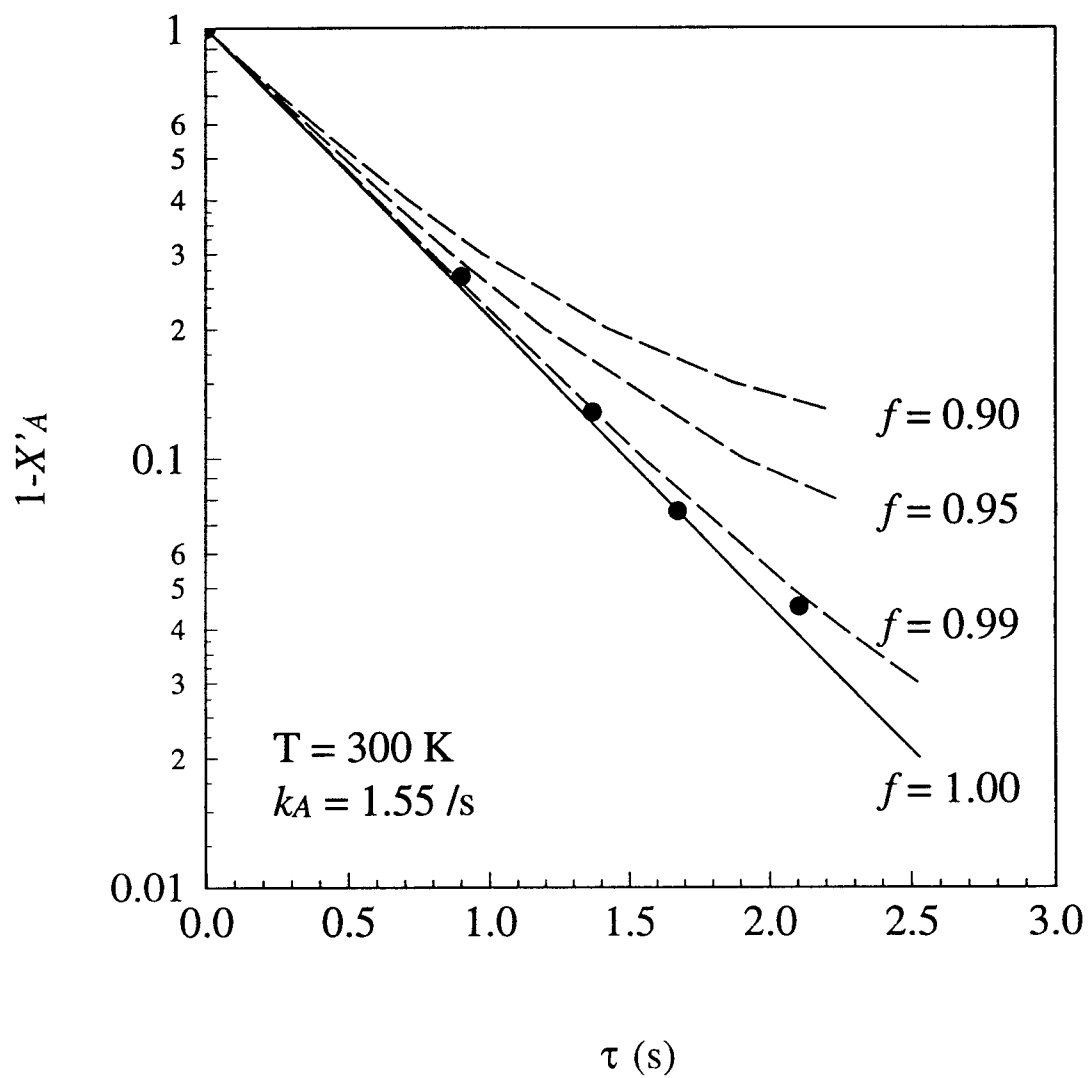


Figure 4.9 Test of plug flow model with pseudo-first order rate of reaction at 300 K, with the collection efficiency  $f$  varied.

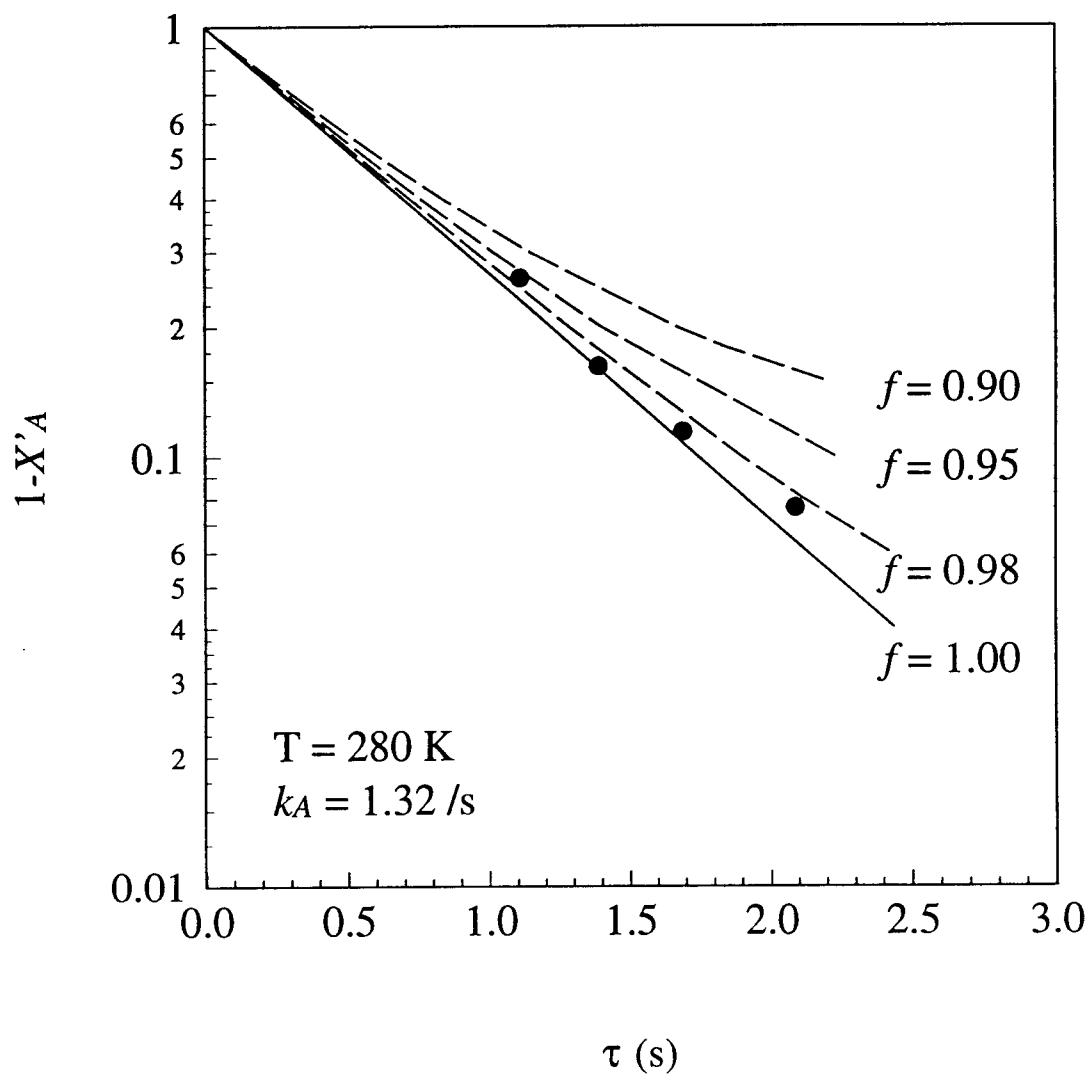


Figure 4.10 Test of plug flow model with pseudo-first order rate of reaction at 280 K, with the collection efficiency  $f$  varied.

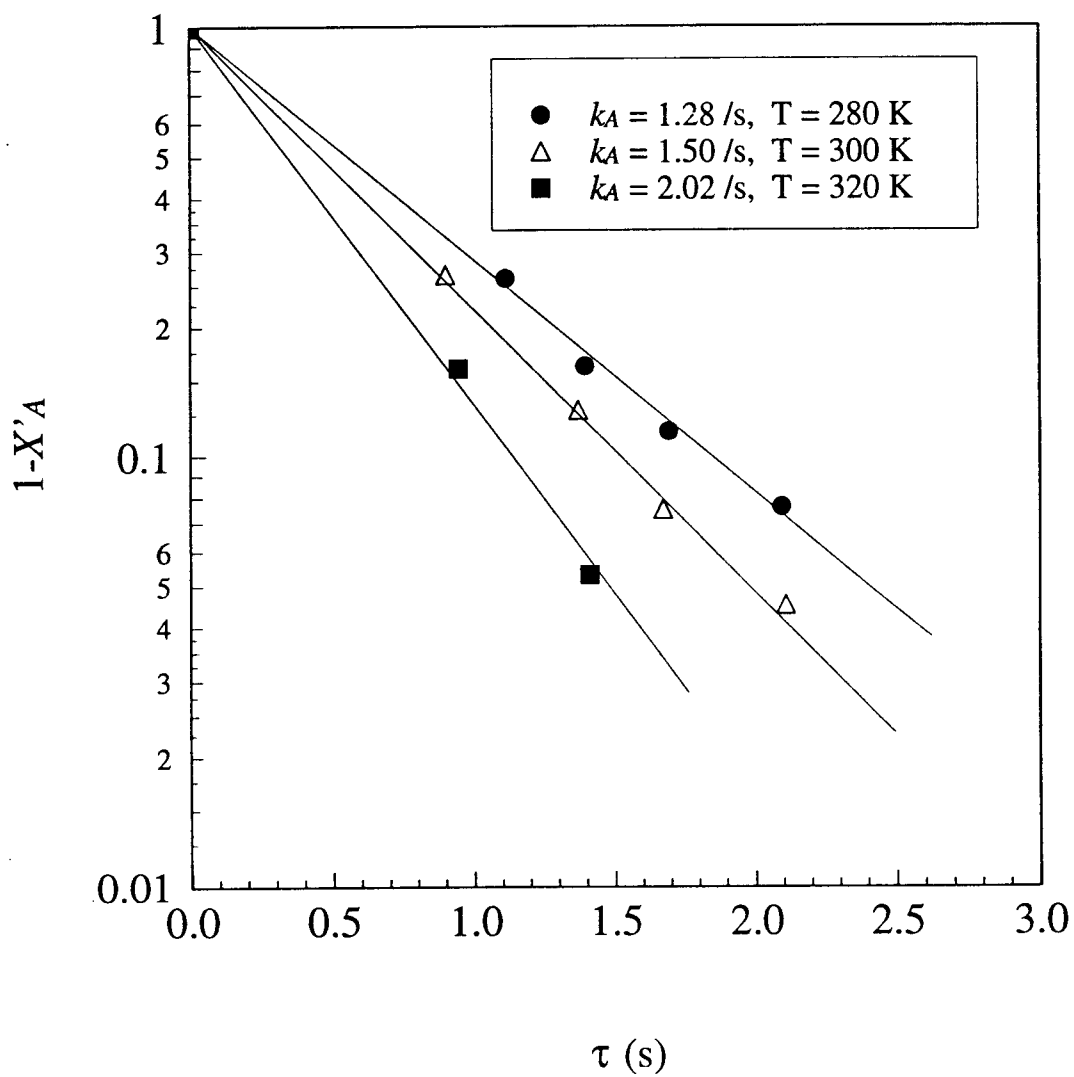


Figure 4.11 Test of plug model with pseudo-first order rate of reaction, with the collection efficiency  $f = 1$ .

Figure 4.12 gives the apparent activation energy of 8.40 kJ/mol, which is much smaller than the activation energy 62.7 kJ/mol reported in the literature [13].

However, the reaction mechanism at the room temperature may be different from that at high temperatures. This is considered to be the major reason for the large difference of the activation energies.

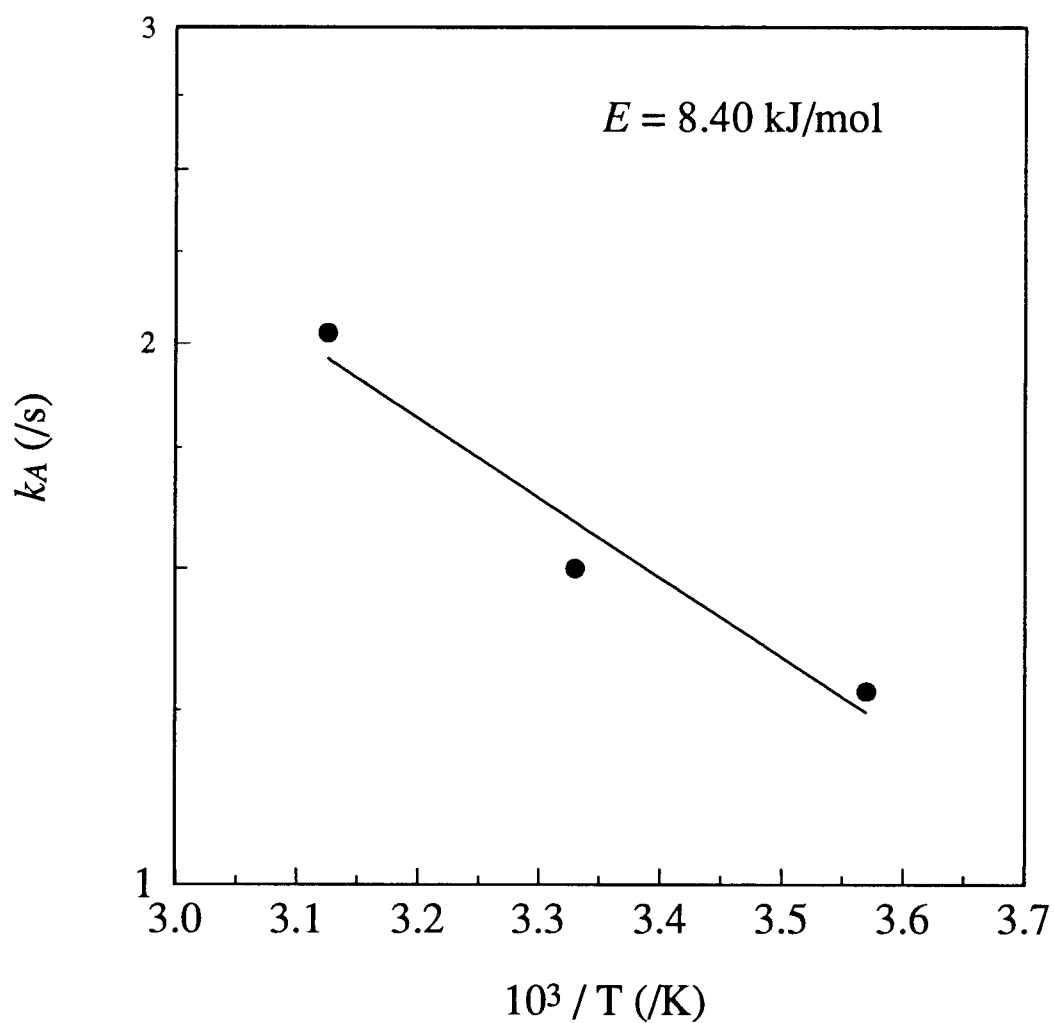


Figure 4.12 Arrhenius plot of the apparent rate constant  $k_A$  of the pseudo-first order reaction in a fluidized bed reactor.



## CHAPTER 5

### CONCLUSIONS AND RECOMMENDATIONS

#### 5.1 Conclusions

The synthesis of  $\text{Si}(\text{NH})_2$  via the vapor phase reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  at temperatures close to the room temperature in a fluidized bed was investigated.  $\text{Si}_3\text{N}_4$  particles having different average sizes were tested to collect product powder, a mixture of  $\text{Si}(\text{NH})_2$  and  $\text{NH}_4\text{Cl}$ . The entrainment of fine powder was measured under the conditions with and without the reaction at different temperatures. A model was proposed to describe the reaction forming the solid products. Experiments for studying the reaction kinetics were carried out to test the model and evaluate the rate constant. The results of this study may be summarized as below.

1. Fine  $\text{Si}_3\text{N}_4$  powder ( $d_p = 0.5 \mu\text{m}$ ) is suitable for collecting the product efficiently.
2. The attrition rate increases with the increase in the reaction temperature as well as with the increase in the molar flow rate of  $\text{SiCl}_4$ .
3. Product powder formed in the void of bed is almost completely (more than 98%) collected by the fine inert particles.
4. A plug flow reactor with a pseudo-first order rate equation with respect to  $\text{SiCl}_4$  can represent the reaction in the fluidized bed reactor.
5. Apparent activation energy is 8.40 kJ/mol in the range of temperature of 280-320 K.

## 5.2 Recommendations for Future Work

In order to complete the development of  $\text{Si}_3\text{N}_4$  synthesis via the gas-phase reaction of  $\text{SiCl}_4$  with  $\text{NH}_3$  at low temperatures around the room temperature in a fluidized bed, some recommendations for future work are given as below:

1. Modify the experimental apparatus to keep all the particles in the bed. A cyclone may be added to collect the entrained powder and feed back to the bed to maintain the amount of fluidized particles constant.
2. Investigate the effects of feeding locations and flow rates of  $\text{SiCl}_4$  vapor to reduce the deposit at the outlet opening of the supply pipe.
3. Perform reaction (2.5) to synthesize  $\text{Si}_3\text{N}_4$  by thermal decomposition of  $\text{Si}(\text{NH})_2$ , step by step in a fluidized bed to test the feasibility of a continuous process.

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## APPENDIX

## LIST OF FORTRAN PROGRAM

## Variable Listing

Program Symbol	Definition
AvCK	Algebra average of $k_A$ values
CK	$k_A$ values which are calculated by equation (4.9)
ER	Absolute error with respect to AvCK
f	f factor in equation (4.9)
I	Index of the experimental data sets
N, Nn	Number of experimental data sets
Tau	$\tau$
XA	$X_A$

## Program Listing

Program kvalue

C

C..... The purpose of this program is to find a set of ( $k_A$ , f) which can best  
 C fit the experimental data (Tau, XA). The method we used is a trial and  
 C error procedure with absolute error criteria. f is varied from 1.00 to  
 C 0.9 to seek a best  $k_A$  value which has smallest absolute error.....

Double Precision CK,F,XA,Tau,AvCK,ER,Nn

Dimension CK(4),Tau(20),XA(20)

Open (UNIT=2,FILE='HSU.DAT',STATUS='UNKNOWN')

C

C..... Data input portion.....

Write (\*,\*) ' Number of data points: '

```

      Read (*,*) N
      Do 10 I = 1, N
      Write (*,5) I
      Read (*,*) Tau(I)
      Write (*,6) I
      Read (*,*) XA(I)
10  Write (2,7) I, Tau(I), I, XA(I)
      Write (2,8)

C
C..... kA value evaluation.....
      F = 1.0
      Nn = N
      40  AvCk = 0.0
      DO 20 I= 1, N

C
C..... The model equation solving for kA.....
           CK(I)= -DLOG (1-XA(I)/F) / Tau(I)
           Write (2,99) I, CK(I)
      20      AvCk = AvCk + CK(I)/ Nn
      ER = 0.0
      DO 50 I=1, N

C
C..... Absolute error evaluation.....
      50      ER = ER + ABS(((AvCk-CK(I))/AvCk*100000)/1000)

C
C..... Result output portion.....
           WRITE(2,999) F,AvCk,ER
           F=F-0.002
           IF(F.GT.0.8) GO TO 40

C
C..... Input data formate.....

```

```

5  Format (' Tau(',I2,')=')
6  Format (' XA(',I2,')=')
7  Format (10X,' Tau(',I2,')= ',F5.3,' XA(',I2,')= ',F5.3)
8  Format (5X,60('='))

```

C

C..... Output data formate.....

```

99  Format (5X,'kA(',I2,')= ',F8.3)
999 Format (5X,'F= ',F6.4,8X,'Av kA=',E10.5,2X,'Error = ',F9.4,'%'/5X
    +      ,60('='))
    STOP
    END

```

### Output Data Listing

```

Tau( 1)=1.110 XA( 1)= .740
Tau( 2)=1.390 XA( 2)= .838
Tau( 3)=1.690 XA( 3)= .886
Tau( 4)=2.090 XA( 4)= .924

```

```

=====
kA( 1)=  1.214
kA( 2)=  1.309
kA( 3)=  1.285
kA( 4)=  1.233
F= 1.0000      Av kA=.12603E+01 Error =  11.7284%

```

```

-----
kA( 1)=  1.219
kA( 2)=  1.317
kA( 3)=  1.294
kA( 4)=  1.245
F= .9980      Av kA=.12687E+01 Error =  11.6370%

```

-----  
 kA( 1)= 1.224  
 kA( 2)= 1.325  
 kA( 3)= 1.304  
 kA( 4)= 1.257  
 F= .9960      Av kA=.12773E+01   Error = 11.5372%

-----  
 kA( 1)= 1.229  
 kA( 2)= 1.332  
 kA( 3)= 1.313  
 kA( 4)= 1.269  
 F= .9940      Av kA=.12861E+01   Error = 11.4284%

-----  
 kA( 1)= 1.234  
 kA( 2)= 1.340  
 kA( 3)= 1.323  
 kA( 4)= 1.282  
 F= .9920      Av kA=.12951E+01   Error = 11.3098%

-----  
 kA( 1)= 1.240  
 kA( 2)= 1.348  
 kA( 3)= 1.333  
 kA( 4)= 1.296  
 F= .9900      Av kA=.13042E+01   Error = 11.1804%

-----  
 kA( 1)= 1.245  
 kA( 2)= 1.356  
 kA( 3)= 1.344  
 kA( 4)= 1.309  
 F= .9880      Av kA=.13136E+01   Error = 11.0394%

-----



kA( 1)= 1.251

kA( 2)= 1.364

kA( 3)= 1.354

kA( 4)= 1.324

F= .9860      Av kA=.13232E+01   Error = 10.9561%

---

kA( 1)= 1.256

kA( 2)= 1.373

kA( 3)= 1.365

kA( 4)= 1.338

F= .9840      Av kA=.13331E+01   Error = 11.5212%

---

kA( 1)= 1.262

kA( 2)= 1.381

kA( 3)= 1.376

kA( 4)= 1.354

F= .9820      Av kA=.13431E+01   Error = 12.1034%

---

kA( 1)= 1.267

kA( 2)= 1.390

kA( 3)= 1.387

kA( 4)= 1.369

F= .9800      Av kA=.13535E+01   Error = 12.7034%

---

kA( 1)= 1.273

kA( 2)= 1.398

kA( 3)= 1.399

kA( 4)= 1.386

F= .9780      Av kA=.13641E+01   Error = 13.3224%